

Computer Algebra Independent Integration Tests

Summer 2023 edition

4-Trig-functions/4.3-Tangent/100-4.3.11-e-x-^m-a+b-tan-c+d-xⁿ-
^p

Nasser M. Abbasi

September 5, 2023

Compiled on September 5, 2023 at 11:36am

Contents

1	Introduction	3
2	detailed summary tables of results	21
3	Listing of integrals	43
4	Appendix	461

CHAPTER 1

INTRODUCTION

1.1	Listing of CAS systems tested	4
1.2	Results	5
1.3	Time and leaf size Performance	8
1.4	Performance based on number of rules Rubi used	10
1.5	Performance based on number of steps Rubi used	11
1.6	Solved integrals histogram based on leaf size of result	12
1.7	Solved integrals histogram based on CPU time used	13
1.8	Leaf size vs. CPU time used	14
1.9	list of integrals with no known antiderivative	15
1.10	List of integrals solved by CAS but has no known antiderivative	15
1.11	list of integrals solved by CAS but failed verification	15
1.12	Timing	16
1.13	Verification	16
1.14	Important notes about some of the results	16
1.15	Design of the test system	19

This report gives the result of running the computer algebra independent integration test. The download section in on the main webpage contains links to download the problems in plain text format used for all CAS systems. The number of integrals in this report is [66]. This is test number [100].

1.1 Listing of CAS systems tested

The following are the CAS systems tested:

1. Mathematica 13.3.1 (August 16, 2023) on windows 10.
2. Rubi 4.16.1 (Dec 19, 2018) on Mathematica 13.3 on windows 10
3. Maple 2023.1 (July, 12, 2023) on windows 10.
4. Maxima 5.47 (June 1, 2023) using Lisp SBCL 2.3.0 on Linux via sagemath 10.1 (Aug 20, 2023).
5. FriCAS 1.3.9 (July 8, 2023) based on sbcl 2.3.0 on Linux via sagemath 10.1 (Aug 20, 2023).
6. Giac/Xcas 1.9.0-57 (June 26, 2023) on Linux via sagemath 10.1 (Aug 20, 2023).
7. Sympy 1.12 (May 10, 2023) Using Python 3.11.3 on Linux.
8. Mupad using Matlab 2021a with Symbolic Math Toolbox Version 8.7 on windows 10.

Maxima and Fricas and Giac are called using Sagemath. This was done using Sagemath `integrate` command by changing the name of the algorithm to use the different CAS systems.

Sympy was run directly in Python not via sagemath.

1.2 Results

Important note: A number of problems in this test suite have no antiderivative in closed form. This means the antiderivative of these integrals can not be expressed in terms of elementary, special functions or `Hypergeometric2F1` functions. `RootSum` and `RootOf` are not allowed. If a CAS returns the above integral unevaluated within the time limit, then the result is counted as passed and assigned an A grade.

However, if CAS times out, then it is assigned an F grade even if the integral is not integrable, as this implies CAS could not determine that the integral is not integrable in the time limit.

If a CAS returns an antiderivative to such an integral, it is assigned an A grade automatically and this special result is listed in the introduction section of each individual test report to make it easy to identify as this can be important result to investigate.

The results given in in the table below reflects the above.

System	% solved	% Failed
Rubi	100.00 (66)	0.00 (0)
Mathematica	100.00 (66)	0.00 (0)
Maxima	92.42 (61)	7.58 (5)
Fricas	72.73 (48)	27.27 (18)
Mupad	57.58 (38)	42.42 (28)
Maple	54.55 (36)	45.45 (30)
Giac	54.55 (36)	45.45 (30)
Sympy	53.03 (35)	46.97 (31)

Table 1.1: Percentage solved for each CAS

The table below gives additional break down of the grading of quality of the antiderivatives generated by each CAS. The grading is given using the letters A,B,C and F with A being the best quality. The grading is accomplished by comparing the antiderivative generated with the optimal antiderivatives included in the test suite. The following table describes the meaning of these grades.

grade	description
A	Integral was solved and antiderivative is optimal in quality and leaf size.
B	Integral was solved and antiderivative is optimal in quality but leaf size is larger than twice the optimal antiderivatives leaf size.
C	Integral was solved and antiderivative is non-optimal in quality. This can be due to one or more of the following reasons <ol style="list-style-type: none"> 1. antiderivative contains a hypergeometric function and the optimal antiderivative does not. 2. antiderivative contains a special function and the optimal antiderivative does not. 3. antiderivative contains the imaginary unit and the optimal antiderivative does not.
F	Integral was not solved. Either the integral was returned unevaluated within the time limit, or it timed out, or CAS hanged or crashed or an exception was raised.

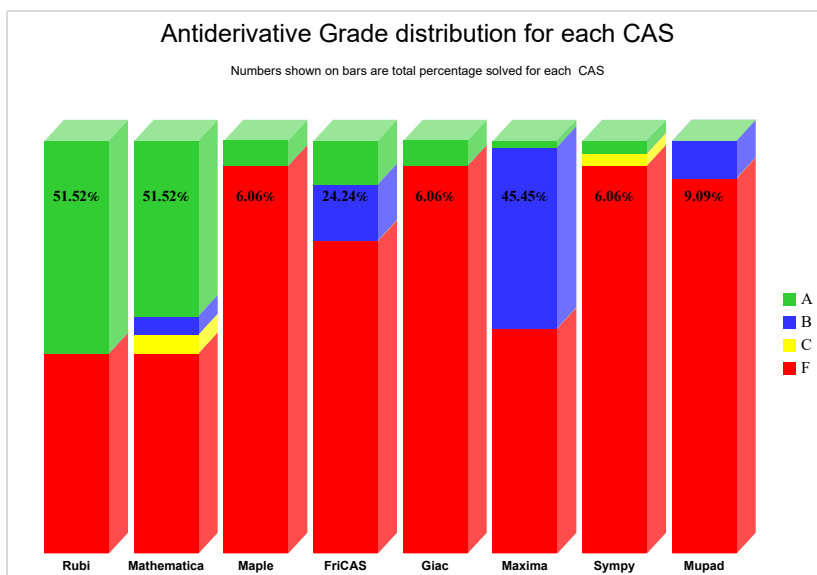
Table 1.2: Description of grading applied to integration result

Grading is implemented for all CAS systems. Based on the above, the following table summarizes the grading for this test suite.

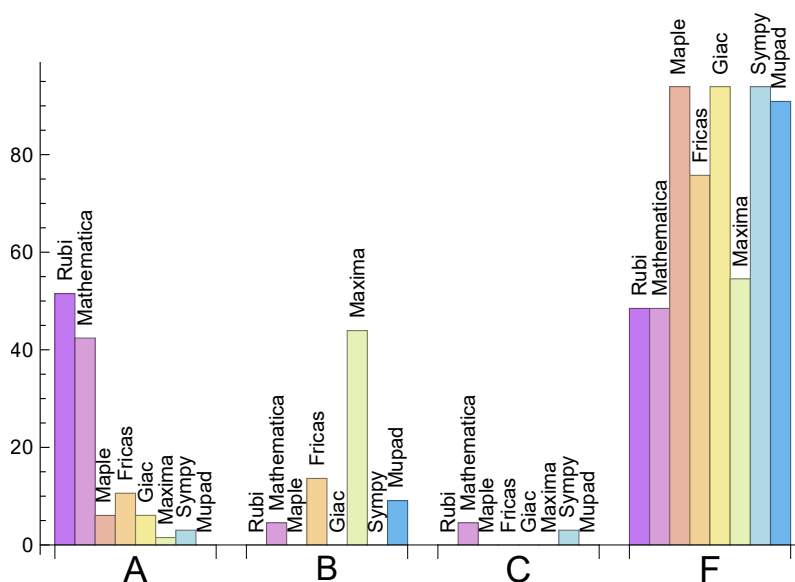
System	% A grade	% B grade	% C grade	% F grade
Rubi	51.515	0.000	0.000	48.485
Mathematica	42.424	4.545	4.545	48.485
Fricas	10.606	13.636	0.000	75.758
Maple	6.061	0.000	0.000	93.939
Giac	6.061	0.000	0.000	93.939
Sympy	3.030	0.000	3.030	93.939
Maxima	1.515	43.939	0.000	54.545
Mupad	0.000	9.091	0.000	90.909

Table 1.3: Antiderivative Grade distribution of each CAS

The following is a Bar chart illustration of the data in the above table.



The figure below compares the grades of the CAS systems.



The following table shows the distribution of the different types of failures for each CAS. There are 3 types failures. The first is when CAS returns the input within the time limit, which means it could not solve it. This is the typical failure and given as **F**.

The second failure is due to time out. CAS could not solve the integral within the 3 minutes time limit which is assigned. This is assigned **F(-1)**.

The third is due to an exception generated, indicated as **F(-2)**. This most likely indicates an interface problem between sagemath and the CAS (applicable only to FriCAS, Maxima and Giac) or it could be an indication of an internal error in the CAS itself. This type of

error requires more investigation to determine the cause.

System	Number failed	Percentage normal failure	Percentage time-out failure	Percentage exception failure
Rubi	0	0.00	0.00	0.00
Mathematica	0	0.00	0.00	0.00
Maxima	5	80.00	0.00	20.00
Fricas	18	100.00	0.00	0.00
Mupad	28	0.00	100.00	0.00
Maple	30	100.00	0.00	0.00
Giac	30	100.00	0.00	0.00
Sympy	31	93.55	6.45	0.00

Table 1.4: Failure statistics for each CAS

1.3 Time and leaf size Performance

The table below summarizes the performance of each CAS system in terms of time used and leaf size of results.

Mean size is the average leaf size produced by the CAS (before any normalization). The Normalized mean is relative to the mean size of the optimal anti-derivative given in the input files.

For example, if CAS has **Normalized mean** of 3, then the mean size of its leaf size is 3 times as large as the mean size of the optimal leaf size.

Median size is value of leaf size where half the values are larger than this and half are smaller (before any normalization). i.e. The Middle value.

Similarly the **Normalized median** is relative to the median leaf size of the optimal.

For example, if a CAS has Normalized median of 1.2, then its median is 1.2 as large as the median leaf size of the optimal.

System	Mean time (sec)
Fricas	0.25
Maple	0.36
Rubi	0.36
Giac	0.58
Maxima	1.17
Sympy	2.02
Mupad	3.93
Mathematica	14.64

Table 1.5: Time performance for each CAS

System	Mean size	Normalized mean	Median size	Normalized median
Maple	21.67	0.95	18.00	0.98
Giac	25.94	1.09	20.00	1.09
Mupad	32.34	1.14	20.00	1.11
Sympy	73.09	1.56	17.00	0.94
Fricas	148.69	1.89	36.00	1.80
Mathematica	187.00	1.14	46.00	1.10
Rubi	187.39	1.00	38.50	1.00
Maxima	1153.36	24.61	497.00	4.87

Table 1.6: Leaf size performance for each CAS

1.4 Performance based on number of rules Rubi used

This section shows how each CAS performed based on the number of rules Rubi needed to solve the same integral. One diagram is given for each CAS.

On the y axis is the percentage solved which Rubi itself needed the number of rules given the x axis. These plots show that as more rules are needed then most CAS system percentage of solving decreases which indicates the integral is becoming more complicated to solve.

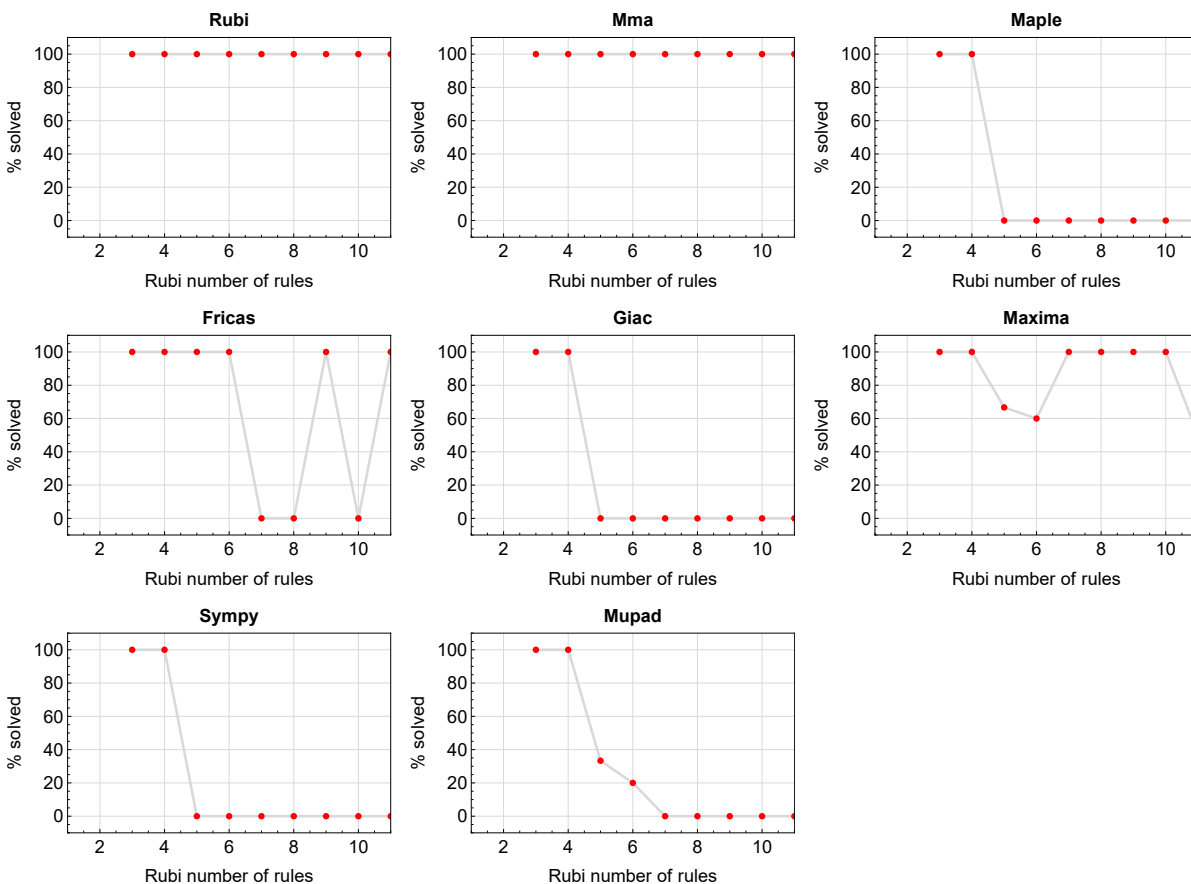


Figure 1.1: Solving statistics per number of Rubi rules used

1.5 Performance based on number of steps Rubi used

This section shows how each CAS performed based on the number of steps Rubi needed to solve the same integral. Note that the number of steps Rubi needed can be much higher than the number of rules, as the same rule could be used more than once.

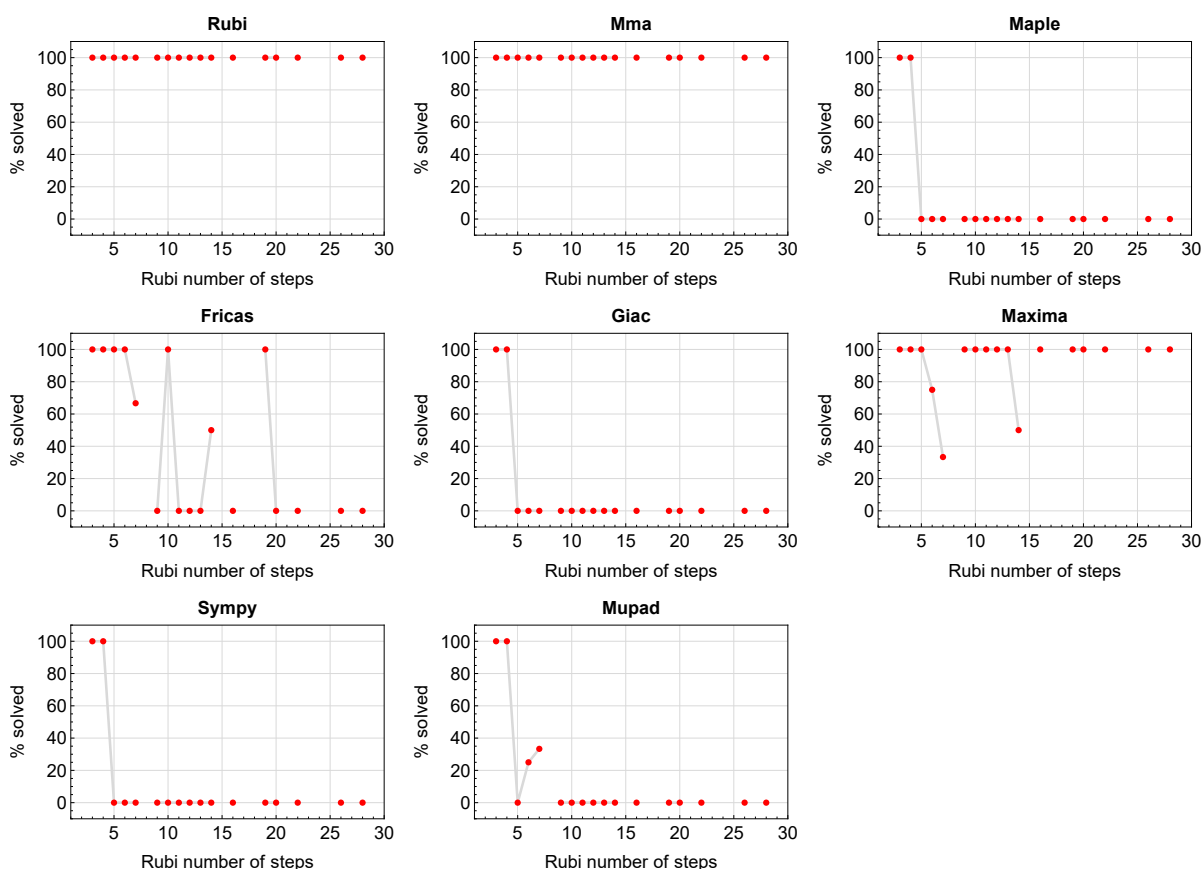


Figure 1.2: Solving statistics per number of Rubi steps used

The above diagram shows that the percentage of solved integrals decreases for most CAS systems as the number of steps increases. As expected, for integrals that required less steps by Rubi, CAS systems had more success which indicates the integral was not as hard to solve. As Rubi needed more steps to solve the integral, the solved percentage decreased for most CAS systems which indicates the integral is becoming harder to solve.

1.6 Solved integrals histogram based on leaf size of result

The following shows the distribution of solved integrals for each CAS system based on leaf size of the antiderivatives produced by each CAS. It shows that most integrals solved produced leaf size less than about 100 to 150. The bin size used is 40.

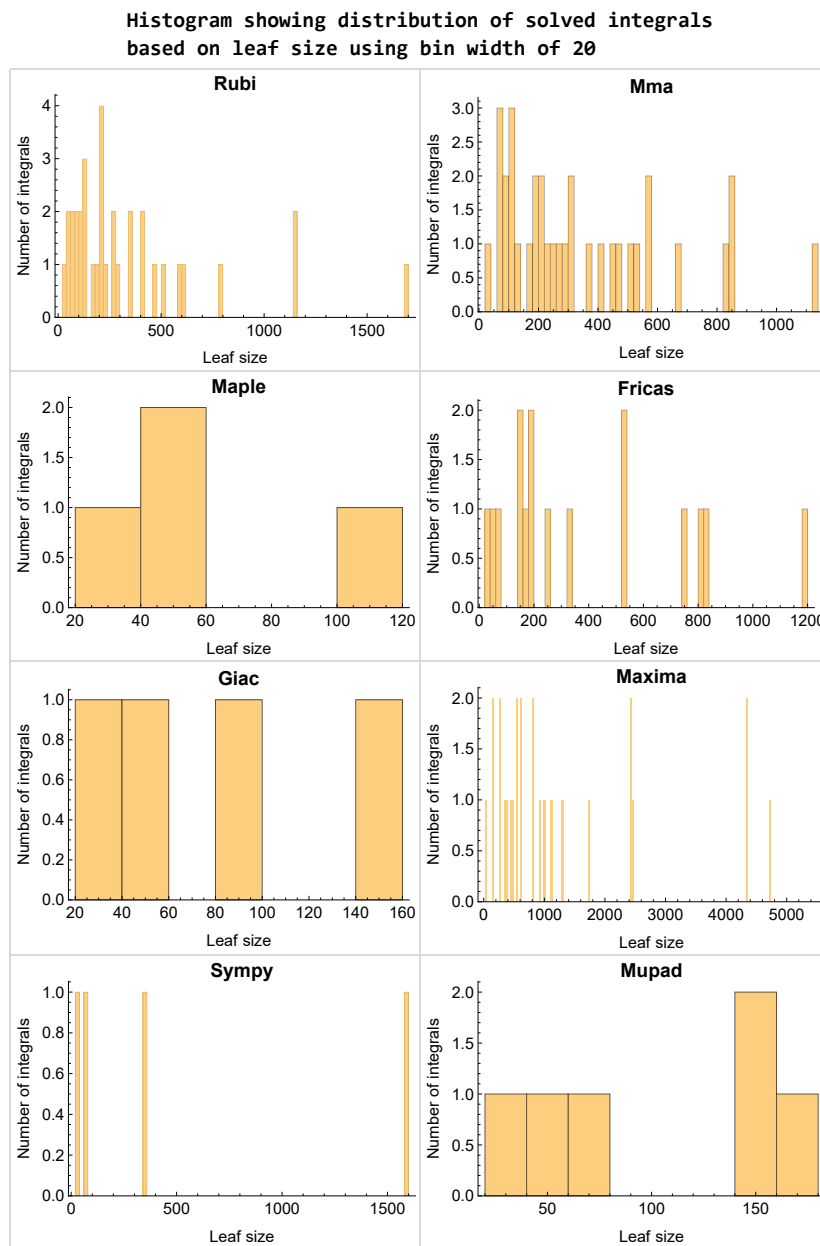


Figure 1.3: Solved integrals based on leaf size distribution

1.7 Solved integrals histogram based on CPU time used

The following shows the distribution of solved integrals for each CAS system based on CPU time used in seconds. The bin size used is 0.1 second.

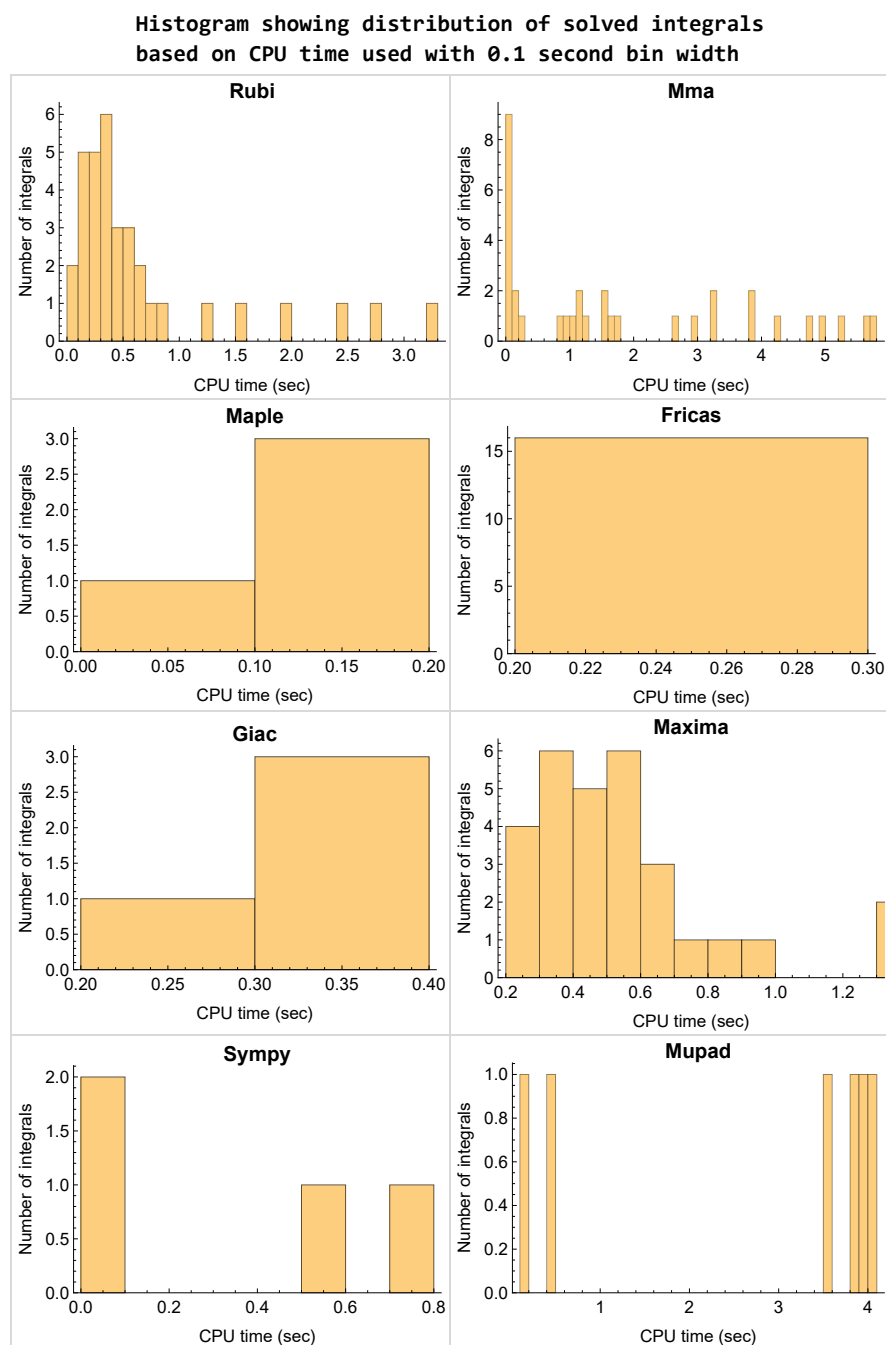


Figure 1.4: Solved integrals histogram based on CPU time used

1.8 Leaf size vs. CPU time used

The following shows the relation between the CPU time used to solve an integral and the leaf size of the antiderivative.

The result for Fracas, Maxima and Giac is shifted more to the right than the other CAS system due to the use of sagemath to call them, which causes an initial slight delay in the timing to start the integration due to overhead of starting a new process each time. This should also be taken into account when looking at the timing of these three CAS systems. Direct calls not using sagemath would result in faster timings, but current implementation uses sagemath as this makes testing much easier to do.

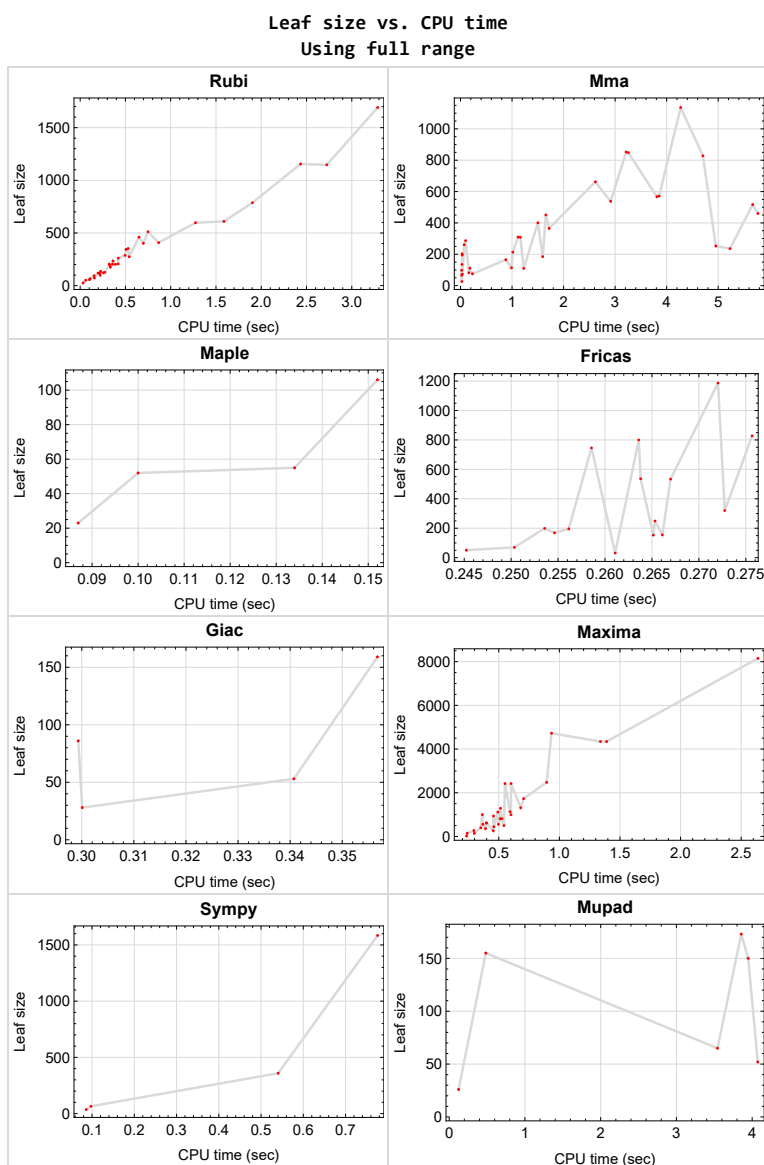


Figure 1.5: Leaf size vs. CPU time. Full range

1.9 list of integrals with no known antiderivative

{2, 4, 5, 6, 8, 10, 11, 12, 14, 16, 17, 18, 20, 22, 23, 24, 29, 30, 34, 35, 40, 41, 45, 46, 50, 51, 55, 56, 60, 61, 65, 66}

1.10 List of integrals solved by CAS but has no known antiderivative

Rubi {}

Mathematica {}

Maple {}

Maxima {}

Fricas {}

Sympy {}

Giac {}

Mupad {}

1.11 list of integrals solved by CAS but failed verification

The following are integrals solved by CAS but the verification phase failed to verify the anti-derivative produced is correct. This does not necessarily mean that the anti-derivative is wrong as additional methods of verification might be needed, or more time is needed (3 minutes time limit was used). These integrals are listed here to make it possible to do further investigation to determine why the result could not be verified.

Rubi {}

Mathematica {}

Maple {}

Maxima Verification phase not currently implemented.

Fricas Verification phase not currently implemented.

Sympy Verification phase not currently implemented.

Giac Verification phase not currently implemented.

Mupad Verification phase not currently implemented.

1.12 Timing

The command `AbsoluteTiming[]` was used in Mathematica to obtain the elapsed time for each integrate call. In Maple, the command `Usage` was used as in the following example

```
cpu_time := Usage(assign ('result_of_int',int(expr,x)),output='realtime')
```

For all other CAS systems, the elapsed time to complete each integral was found by taking the difference between the time after the call completed from the time before the call was made. This was done using Python's `time.time()` call.

All elapsed times shown are in seconds. A time limit of 3 CPU minutes was used for each integral. If the integrate command did not complete within this time limit, the integral was aborted and considered to have failed and assigned an F grade. The time used by failed integrals due to time out was not counted in the final statistics.

1.13 Verification

A verification phase was applied on the result of integration for Rubi and Mathematica.

Future version of this report will implement verification for the other CAS systems. For the integrals whose result was not run through a verification phase, it is assumed that the antiderivative was correct.

Verification phase also had 3 minutes time out. An integral whose result was not verified could still be correct, but further investigation is needed on those integrals. These integrals were marked in the summary table below and also in each integral separate section so they are easy to identify and locate.

1.14 Important notes about some of the results

Important note about Maxima results

Since tests were run in a batch mode, and using an automated script, then any integral where Maxima needed an interactive response from the user to answer a question during the evaluation of the integral will fail.

The exception raised is `ValueError`. Therefore Maxima results is lower than what would result if Maxima was run directly and each question was answered correctly.

The percentage of such failures were not counted for each test file, but for an example, for the `Timofeev` test file, there were about 14 such integrals out of total 705, or about 2 percent. This percentage can be higher or lower depending on the specific input test file.

Such integrals can be identified by looking at the output of the integration in each section for Maxima. The exception message will indicate the cause of error.

Maxima integrate was run using SageMath with the following settings set by default

```
'besselexpand : true'
'display2d : false'
'domain : complex'
'keepfloat : true'
'load(to_poly_solve)'
'load(simplify_sum)'
'load(abs_integrate)' 'load(diag)'
```

SageMath automatic loading of Maxima `abs_integrate` was found to cause some problems. So the following code was added to disable this effect.

```
from sage.interfaces.maxima_lib import maxima_lib
maxima_lib.set('extra_definite_integration_methods', '[]')
maxima_lib.set('extra_integration_methods', '[]')
```

See <https://ask.sagemath.org/question/43088/integrate-results-that-are-different-from-using-maxima/> for reference.

Important note about FriCAS result

There were few integrals which failed due to SageMath interface and not because FriCAS system could not do the integration.

These will fail With error `Exception raised: NotImplementedError`.

The number of such cases seems to be very small. About 1 or 2 percent of all integrals. These can be identified by looking at the exception message given in the result.

Important note about finding leaf size of antiderivative

For Mathematica, Rubi, and Maple, the builtin system function `LeafSize` was used to find the leaf size of each antiderivative.

The other CAS systems (SageMath and Sympy) do not have special builtin function for this purpose at this time. Therefore the leaf size for Fricas and Sympy antiderivative was determined using the following function, thanks to user `slelievre` at https://ask.sagemath.org/question/57123/could-we-have-a-leaf_count-function-in-base-sagemath/

```
def tree_size(expr):
    r"""
    Return the tree size of this expression.
    """
    if expr not in SR:
        # deal with lists, tuples, vectors
        return 1 + sum(tree_size(a) for a in expr)
    expr = SR(expr)
```

```
x, aa = expr.operator(), expr.operands()
if x is None:
    return 1
else:
    return 1 + sum(tree_size(a) for a in aa)
```

For Sympy, which was called directly from Python, the following code was used to obtain the leafsize of its result

```
try:
    # 1.7 is a fudge factor since it is low side from actual leaf count
    leafCount = round(1.7*count_ops(anti))

except Exception as ee:
    leafCount =1
```

Important note about Mupad results

Matlab's symbolic toolbox does not have a leaf count function to measure the size of the antiderivative. Maple was used to determine the leaf size of Mupad output by post processing Mupad result.

Currently no grading of the antiderivative for Mupad is implemented. If it can integrate the problem, it was assigned a B grade automatically as a placeholder. In the future, when grading function is implemented for Mupad, the tests will be rerun again.

The following is an example of using Matlab's symbolic toolbox (Mupad) to solve an integral

```
integrand = evalin(symengine, 'cos(x)*sin(x)')
the_variable = evalin(symengine, 'x')
anti = int(integrand, the_variable)
```

Which gives $\sin(x)^2/2$

1.15 Design of the test system

The following diagram gives a high level view of the current test build system.



High level overview of the CAS independent integration test build system

One record (line) per one integral result. The line is CSV comma separated. This is description of each record

1. integer. the problem number.
2. integer. 0 for failed, 1 for passed, -1 for timeout, -2 for CAS specific exception. (this is not the grade field)
3. integer. Leaf size of result.
4. integer. Leaf size of the optimal antiderivative.
5. number. CPU time used to solve this integral. 0 if failed.
6. string. The integral in Latex format
7. string. The input used in CAS own syntax.
8. string. The result (antiderivative) produced by CAS in Latex format
9. string. The optimal antiderivative in Latex format.
10. integer. 0 or 1. Indicates if problem has known antiderivative or not
11. String. The result (antiderivative) in CAS own syntax.
12. String. The grade of the antiderivative. Can be "A", "B", "C", or "F"
13. String. Small string description of why the grade was given.
14. integer. 1 if result was verified or 0 if not verified. (For mma, rubi and maple only)

The following fields are present only in *Rubi Table file*

15. integer. Number of steps used.
16. integer. Number of rules used.
17. integer. Integrand leaf size.
18. real number. Ratio. Field 16 over field 17
19. String of form "{n,n,...}" which is list of the rules used by Rubi
20. String. The optimal antiderivative in Mathematica syntax

Nasser M. Abbasi
June 27, 2023
Design v1.0

CHAPTER 2

DETAILED SUMMARY TABLES OF RESULTS

2.1	List of integrals sorted by grade for each CAS	22
2.2	Detailed conclusion table per each integral for all CAS systems	25
2.3	Detailed conclusion table specific for Rubi results	39

2.1 List of integrals sorted by grade for each CAS

Rubi	22
Mma	22
Maple	23
Fricas	23
Maxima	23
Giac	24
Mupad	24
Sympy	24

Rubi

A grade { 1, 3, 7, 9, 13, 15, 19, 21, 25, 26, 27, 28, 31, 32, 33, 36, 37, 38, 39, 42, 43, 44, 47, 48, 49, 52, 53, 54, 57, 58, 59, 62, 63, 64 }

B grade { }

C grade { }

F normal fail { }

F(-1) timedout fail { }

F(-2) exception fail { }

Mma

A grade { 1, 3, 7, 13, 25, 26, 27, 28, 31, 32, 36, 37, 38, 39, 42, 43, 47, 48, 49, 52, 53, 54, 57, 58, 59, 62, 63, 64 }

B grade { 19, 33, 44 }

C grade { 9, 15, 21 }

F normal fail { }

F(-1) timedout fail { }

F(-2) exception fail { }

Maple

A grade { 3, 9, 15, 21 }

B grade { }

C grade { }

F normal fail { 1, 7, 13, 19, 25, 26, 27, 28, 31, 32, 33, 36, 37, 38, 39, 42, 43, 44, 47, 48, 49, 52, 53, 54, 57, 58, 59, 62, 63, 64 }

F(-1) timeout fail { }

F(-2) exception fail { }

Fricas

A grade { 3, 7, 9, 15, 21, 33, 54 }

B grade { 1, 13, 19, 28, 39, 44, 49, 59, 64 }

C grade { }

F normal fail { 25, 26, 27, 31, 32, 36, 37, 38, 42, 43, 47, 48, 52, 53, 57, 58, 62, 63 }

F(-1) timeout fail { }

F(-2) exception fail { }

Maxima

A grade { 3 }

B grade { 7, 9, 13, 15, 19, 21, 25, 26, 27, 31, 32, 33, 36, 37, 38, 39, 42, 43, 44, 47, 48, 52, 53, 57, 58, 59, 62, 63, 64 }

C grade { }

F normal fail { 1, 28, 49, 54 }

F(-1) timeout fail { }

F(-2) exception fail { 46 }

Giac

A grade { 3, 9, 15, 21 }

B grade { }

C grade { }

F normal fail { 1, 7, 13, 19, 25, 26, 27, 28, 31, 32, 33, 36, 37, 38, 39, 42, 43, 44, 47, 48, 49, 52, 53, 54, 57, 58, 59, 62, 63, 64 }

F(-1) timeout fail { }

F(-2) exception fail { }

Mupad

A grade { }

B grade { 1, 3, 9, 15, 21, 28 }

C grade { }

F normal fail { }

F(-1) timeout fail { 7, 13, 19, 25, 26, 27, 31, 32, 33, 36, 37, 38, 39, 42, 43, 44, 47, 48, 49, 52, 53, 54, 57, 58, 59, 62, 63, 64 }

F(-2) exception fail { }

Sympy

A grade { 3, 9 }

B grade { }

C grade { 15, 21 }

F normal fail { 1, 7, 13, 19, 25, 26, 27, 28, 31, 32, 33, 36, 37, 38, 39, 42, 43, 44, 47, 48, 49, 52, 53, 54, 58, 59, 62, 63, 64 }

F(-1) timeout fail { 57, 66 }

F(-2) exception fail { }

2.2 Detailed conclusion table per each integral for all CAS systems

Detailed conclusion table per each integral is given by the table below. The elapsed time is in seconds. For failed result it is given as **F(-1)** if the failure was due to timeout. It is given as **F(-2)** if the failure was due to an exception being raised, which could indicate a bug in the system. If the failure was due to integral not being evaluated within the time limit, then it is given as **F**.

In this table, the column **N.S.** means **normalized size** and is defined as $\frac{\text{antiderivative leaf size}}{\text{optimal antiderivative leaf size}}$. To make the table fit the page, the name **Mathematica** was abbreviated to **MMA**.

Problem 1	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	N/A	A	A	F	F	B	F	F	B
verified	N/A	Yes	Yes	N/A	TBD	TBD	TBD	TBD	TBD
size	73	73	73	0	0	155	0	0	155
N.S.	1	1.00	1.00	0.00	0.00	2.12	0.00	0.00	2.12
time (sec)	N/A	0.157	0.036	0.000	0.000	0.266	0.000	0.000	0.484

Problem 2	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	N/A	N/A	N/A	N/A	N/A	N/A	N/A	N/A	N/A
verified	N/A	N/A	N/A	N/A	TBD	TBD	TBD	TBD	TBD
size	16	16	18	16	70	21	15	18	18
N.S.	1	1.00	1.12	1.00	4.38	1.31	0.94	1.12	1.12
time (sec)	N/A	0.024	2.758	0.102	0.303	0.237	0.581	0.372	3.645

Problem 3	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	N/A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	Yes	TBD	TBD	TBD	TBD	TBD
size	26	26	26	23	22	31	36	28	26
N.S.	1	1.00	1.00	0.88	0.85	1.19	1.38	1.08	1.00
time (sec)	N/A	0.033	0.028	0.087	0.234	0.261	0.086	0.300	0.124

Problem 4	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	N/A	N/A	N/A	N/A	N/A	N/A	N/A	N/A	N/A
verified	N/A	N/A	N/A	N/A	TBD	TBD	TBD	TBD	TBD
size	12	12	14	12	64	14	12	14	14
N.S.	1	1.00	1.17	1.00	5.33	1.17	1.00	1.17	1.17
time (sec)	N/A	0.006	1.155	0.135	0.285	0.228	0.236	0.322	4.439

Problem 5	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	N/A	N/A	N/A	N/A	N/A	N/A	N/A	N/A	N/A
verified	N/A	N/A	N/A	N/A	TBD	TBD	TBD	TBD	TBD
size	16	16	18	16	70	18	14	18	18
N.S.	1	1.00	1.12	1.00	4.38	1.12	0.88	1.12	1.12
time (sec)	N/A	0.023	1.697	0.096	0.311	0.243	0.649	0.338	3.756

Problem 6	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	N/A	N/A	N/A	N/A	N/A	N/A	N/A	N/A	N/A
verified	N/A	N/A	N/A	N/A	TBD	TBD	TBD	TBD	TBD
size	16	16	18	16	80	18	15	18	18
N.S.	1	1.00	1.12	1.00	5.00	1.12	0.94	1.12	1.12
time (sec)	N/A	0.021	1.637	0.105	0.342	0.232	0.379	0.366	4.126

Problem 7	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	N/A	A	A	F	B	A	F	F	F(-1)
verified	N/A	Yes	Yes	N/A	TBD	TBD	TBD	TBD	TBD
size	126	126	236	0	398	199	0	0	0
N.S.	1	1.00	1.87	0.00	3.16	1.58	0.00	0.00	0.00
time (sec)	N/A	0.273	5.229	0.000	0.351	0.254	0.000	0.000	0.000

Problem 8	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	N/A	N/A	N/A	N/A	N/A	N/A	N/A	N/A	N/A
verified	N/A	N/A	N/A	N/A	TBD	TBD	TBD	TBD	TBD
size	18	18	20	18	271	42	17	20	20
N.S.	1	1.00	1.11	1.00	15.06	2.33	0.94	1.11	1.11
time (sec)	N/A	0.027	5.441	0.173	0.380	0.242	0.813	0.593	3.610

Problem 9	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	N/A	A	C	A	B	A	A	A	B
verified	N/A	Yes	Yes	Yes	TBD	TBD	TBD	TBD	TBD
size	51	51	75	52	149	51	65	53	52
N.S.	1	1.00	1.47	1.02	2.92	1.00	1.27	1.04	1.02
time (sec)	N/A	0.061	0.232	0.100	0.240	0.245	0.097	0.341	4.074

Problem 10	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	N/A	N/A	N/A	N/A	N/A	N/A	N/A	N/A	N/A
verified	N/A	N/A	N/A	N/A	TBD	TBD	TBD	TBD	TBD
size	14	14	16	14	288	32	14	16	16
N.S.	1	1.00	1.14	1.00	20.57	2.29	1.00	1.14	1.14
time (sec)	N/A	0.006	1.886	0.161	0.351	0.242	0.567	0.503	3.725

Problem 11	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	N/A	N/A	N/A	N/A	N/A	N/A	N/A	N/A	N/A
verified	N/A	N/A	N/A	N/A	TBD	TBD	TBD	TBD	TBD
size	18	18	20	18	314	36	15	20	20
N.S.	1	1.00	1.11	1.00	17.44	2.00	0.83	1.11	1.11
time (sec)	N/A	0.025	11.510	0.174	0.422	0.243	2.145	0.388	5.039

Problem 12	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	N/A	N/A	N/A	N/A	N/A	N/A	N/A	N/A	N/A
verified	N/A	N/A	N/A	N/A	TBD	TBD	TBD	TBD	TBD
size	18	18	20	18	306	36	17	20	20
N.S.	1	1.00	1.11	1.00	17.00	2.00	0.94	1.11	1.11
time (sec)	N/A	0.025	4.974	0.211	0.406	0.235	0.634	0.498	4.418

Problem 13	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	N/A	A	A	F	B	B	F	F	F(-1)
verified	N/A	Yes	Yes	N/A	TBD	TBD	TBD	TBD	TBD
size	122	122	110	0	267	536	0	0	0
N.S.	1	1.00	0.90	0.00	2.19	4.39	0.00	0.00	0.00
time (sec)	N/A	0.257	1.227	0.000	0.295	0.264	0.000	0.000	0.000

Problem 14	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	N/A	N/A	N/A	N/A	N/A	N/A	N/A	N/A	N/A
verified	N/A	N/A	N/A	N/A	TBD	TBD	TBD	TBD	TBD
size	18	18	20	18	196	20	15	20	20
N.S.	1	1.00	1.11	1.00	10.89	1.11	0.83	1.11	1.11
time (sec)	N/A	0.030	3.333	0.138	0.662	0.237	0.362	0.468	4.005

Problem 15	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	N/A	A	C	A	B	A	C	A	B
verified	N/A	Yes	Yes	Yes	TBD	TBD	TBD	TBD	TBD
size	57	57	82	55	143	70	359	86	65
N.S.	1	1.00	1.44	0.96	2.51	1.23	6.30	1.51	1.14
time (sec)	N/A	0.103	0.162	0.134	0.299	0.250	0.541	0.299	3.543

Problem 16	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	N/A	N/A	N/A	N/A	N/A	N/A	N/A	N/A	N/A
verified	N/A	N/A	N/A	N/A	TBD	TBD	TBD	TBD	TBD
size	14	14	16	14	187	16	14	16	16
N.S.	1	1.00	1.14	1.00	13.36	1.14	1.00	1.14	1.14
time (sec)	N/A	0.008	1.414	0.132	0.444	0.236	0.291	0.363	3.557

Problem 17	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	N/A	N/A	N/A	N/A	N/A	N/A	N/A	N/A	N/A
verified	N/A	N/A	N/A	N/A	TBD	TBD	TBD	TBD	TBD
size	18	18	20	18	510	19	15	20	20
N.S.	1	1.00	1.11	1.00	28.33	1.06	0.83	1.11	1.11
time (sec)	N/A	0.032	1.352	0.144	0.550	0.231	0.764	0.339	4.348

Problem 18	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	N/A	N/A	N/A	N/A	N/A	N/A	N/A	N/A	N/A
verified	N/A	N/A	N/A	N/A	TBD	TBD	TBD	TBD	TBD
size	18	18	20	18	534	23	17	20	20
N.S.	1	1.00	1.11	1.00	29.67	1.28	0.94	1.11	1.11
time (sec)	N/A	0.029	2.880	0.133	0.562	0.242	0.635	0.455	4.023

Problem 19	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	N/A	A	B	F	B	B	F	F	F(-1)
verified	N/A	Yes	Yes	N/A	TBD	TBD	TBD	TBD	TBD
size	202	202	460	0	1001	800	0	0	0
N.S.	1	1.00	2.28	0.00	4.96	3.96	0.00	0.00	0.00
time (sec)	N/A	0.389	5.771	0.000	0.364	0.264	0.000	0.000	0.000

Problem 20	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	N/A	N/A	N/A	N/A	N/A	N/A	N/A	N/A	N/A
verified	N/A	N/A	N/A	N/A	TBD	TBD	TBD	TBD	TBD
size	18	18	20	18	764	38	17	20	20
N.S.	1	1.00	1.11	1.00	42.44	2.11	0.94	1.11	1.11
time (sec)	N/A	0.031	8.344	0.168	10.405	0.249	1.073	0.614	4.119

Problem 21	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	N/A	A	C	A	B	A	C	A	B
verified	N/A	Yes	Yes	Yes	TBD	TBD	TBD	TBD	TBD
size	94	94	114	106	556	169	1584	159	173
N.S.	1	1.00	1.21	1.13	5.91	1.80	16.85	1.69	1.84
time (sec)	N/A	0.154	0.989	0.152	0.369	0.255	0.776	0.357	3.856

Problem 22	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	N/A	N/A	N/A	N/A	N/A	N/A	N/A	N/A	N/A
verified	N/A	N/A	N/A	N/A	TBD	TBD	TBD	TBD	TBD
size	14	14	16	14	2550	34	15	16	16
N.S.	1	1.00	1.14	1.00	182.14	2.43	1.07	1.14	1.14
time (sec)	N/A	0.007	6.812	0.178	1.423	0.245	0.610	0.427	4.276

Problem 23	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	N/A	N/A	N/A	N/A	N/A	N/A	N/A	N/A	N/A
verified	N/A	N/A	N/A	N/A	TBD	TBD	TBD	TBD	TBD
size	18	18	20	18	3616	38	17	20	20
N.S.	1	1.00	1.11	1.00	200.89	2.11	0.94	1.11	1.11
time (sec)	N/A	0.025	12.875	0.208	1.315	0.241	1.144	0.452	4.175

Problem 24	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	N/A	N/A	N/A	N/A	N/A	N/A	N/A	N/A	N/A
verified	N/A	N/A	N/A	N/A	TBD	TBD	TBD	TBD	TBD
size	18	18	20	18	2599	44	19	20	20
N.S.	1	1.00	1.11	1.00	144.39	2.44	1.06	1.11	1.11
time (sec)	N/A	0.026	9.759	0.176	1.412	0.246	0.987	0.511	4.380

Problem 25	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	N/A	A	A	F	B	F	F	F	F(-1)
verified	N/A	Yes	Yes	N/A	TBD	TBD	TBD	TBD	TBD
size	261	261	261	0	937	0	0	0	0
N.S.	1	1.00	1.00	0.00	3.59	0.00	0.00	0.00	0.00
time (sec)	N/A	0.421	0.072	0.000	0.456	0.000	0.000	0.000	0.000

Problem 26	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	N/A	A	A	F	B	F	F	F	F(-1)
verified	N/A	Yes	Yes	N/A	TBD	TBD	TBD	TBD	TBD
size	195	195	195	0	618	0	0	0	0
N.S.	1	1.00	1.00	0.00	3.17	0.00	0.00	0.00	0.00
time (sec)	N/A	0.327	0.033	0.000	0.398	0.000	0.000	0.000	0.000

Problem 27	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	N/A	A	A	F	B	F	F	F	F(-1)
verified	N/A	Yes	Yes	N/A	TBD	TBD	TBD	TBD	TBD
size	135	135	135	0	359	0	0	0	0
N.S.	1	1.00	1.00	0.00	2.66	0.00	0.00	0.00	0.00
time (sec)	N/A	0.226	0.029	0.000	0.390	0.000	0.000	0.000	0.000

Problem 28	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	N/A	A	A	F	F	B	F	F	B
verified	N/A	Yes	Yes	N/A	TBD	TBD	TBD	TBD	TBD
size	66	66	66	0	0	153	0	0	150
N.S.	1	1.00	1.00	0.00	0.00	2.32	0.00	0.00	2.27
time (sec)	N/A	0.110	0.024	0.000	0.000	0.265	0.000	0.000	3.947

Problem 29	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	N/A	N/A	N/A	N/A	N/A	N/A	N/A	N/A	N/A
verified	N/A	N/A	N/A	N/A	TBD	TBD	TBD	TBD	TBD
size	18	18	20	16	68	18	15	18	18
N.S.	1	1.00	1.11	0.89	3.78	1.00	0.83	1.00	1.00
time (sec)	N/A	0.022	5.249	0.446	0.526	0.233	1.546	0.478	4.052

Problem 30	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	N/A	N/A	N/A	N/A	N/A	N/A	N/A	N/A	N/A
verified	N/A	N/A	N/A	N/A	TBD	TBD	TBD	TBD	TBD
size	18	18	20	16	72	18	17	18	18
N.S.	1	1.00	1.11	0.89	4.00	1.00	0.94	1.00	1.00
time (sec)	N/A	0.023	12.483	0.368	0.538	0.237	0.784	0.486	4.447

Problem 31	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	N/A	A	A	F	B	F	F	F	F(-1)
verified	N/A	Yes	Yes	N/A	TBD	TBD	TBD	TBD	TBD
size	402	402	567	0	2421	0	0	0	0
N.S.	1	1.00	1.41	0.00	6.02	0.00	0.00	0.00	0.00
time (sec)	N/A	0.698	3.810	0.000	0.601	0.000	0.000	0.000	0.000

Problem 32	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	N/A	A	A	F	B	F	F	F	F(-1)
verified	N/A	Yes	Yes	N/A	TBD	TBD	TBD	TBD	TBD
size	274	274	365	0	1290	0	0	0	0
N.S.	1	1.00	1.33	0.00	4.71	0.00	0.00	0.00	0.00
time (sec)	N/A	0.542	1.719	0.000	0.515	0.000	0.000	0.000	0.000

Problem 33	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	N/A	A	B	F	B	A	F	F	F(-1)
verified	N/A	Yes	Yes	N/A	TBD	TBD	TBD	TBD	TBD
size	119	119	253	0	497	196	0	0	0
N.S.	1	1.00	2.13	0.00	4.18	1.65	0.00	0.00	0.00
time (sec)	N/A	0.215	4.953	0.000	0.543	0.256	0.000	0.000	0.000

Problem 34	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	N/A	N/A	N/A	N/A	N/A	N/A	N/A	N/A	N/A
verified	N/A	N/A	N/A	N/A	TBD	TBD	TBD	TBD	TBD
size	20	20	22	18	298	36	17	20	20
N.S.	1	1.00	1.10	0.90	14.90	1.80	0.85	1.00	1.00
time (sec)	N/A	0.025	130.413	0.967	0.730	0.251	8.719	0.846	4.026

Problem 35	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	N/A	N/A	N/A	N/A	N/A	N/A	N/A	N/A	N/A
verified	N/A	N/A	N/A	N/A	TBD	TBD	TBD	TBD	TBD
size	20	20	22	18	300	36	19	20	20
N.S.	1	1.00	1.10	0.90	15.00	1.80	0.95	1.00	1.00
time (sec)	N/A	0.023	19.325	1.053	0.995	0.247	1.791	0.888	4.843

Problem 36	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	N/A	A	A	F	B	F	F	F	F(-1)
verified	N/A	Yes	Yes	N/A	TBD	TBD	TBD	TBD	TBD
size	460	460	401	0	1133	0	0	0	0
N.S.	1	1.00	0.87	0.00	2.46	0.00	0.00	0.00	0.00
time (sec)	N/A	0.649	1.502	0.000	0.593	0.000	0.000	0.000	0.000

Problem 37	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	N/A	A	A	F	B	F	F	F	F(-1)
verified	N/A	Yes	Yes	N/A	TBD	TBD	TBD	TBD	TBD
size	344	344	308	0	813	0	0	0	0
N.S.	1	1.00	0.90	0.00	2.36	0.00	0.00	0.00	0.00
time (sec)	N/A	0.507	1.160	0.000	0.526	0.000	0.000	0.000	0.000

Problem 38	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	N/A	A	A	F	B	F	F	F	F(-1)
verified	N/A	Yes	Yes	N/A	TBD	TBD	TBD	TBD	TBD
size	234	234	213	0	555	0	0	0	0
N.S.	1	1.00	0.91	0.00	2.37	0.00	0.00	0.00	0.00
time (sec)	N/A	0.362	1.015	0.000	0.497	0.000	0.000	0.000	0.000

Problem 39	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	N/A	A	A	F	B	B	F	F	F(-1)
verified	N/A	Yes	Yes	N/A	TBD	TBD	TBD	TBD	TBD
size	119	119	111	0	264	534	0	0	0
N.S.	1	1.00	0.93	0.00	2.22	4.49	0.00	0.00	0.00
time (sec)	N/A	0.198	0.181	0.000	0.455	0.267	0.000	0.000	0.000

Problem 40	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	N/A	N/A	N/A	N/A	N/A	N/A	N/A	N/A	N/A
verified	N/A	N/A	N/A	N/A	TBD	TBD	TBD	TBD	TBD
size	20	20	22	18	496	19	17	20	20
N.S.	1	1.00	1.10	0.90	24.80	0.95	0.85	1.00	1.00
time (sec)	N/A	0.029	4.452	0.394	1.092	0.247	2.102	0.612	4.065

Problem 41	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	N/A	N/A	N/A	N/A	N/A	N/A	N/A	N/A	N/A
verified	N/A	N/A	N/A	N/A	TBD	TBD	TBD	TBD	TBD
size	20	20	22	18	496	23	19	20	20
N.S.	1	1.00	1.10	0.90	24.80	1.15	0.95	1.00	1.00
time (sec)	N/A	0.028	5.362	0.456	1.268	0.246	2.037	0.681	3.663

Problem 42	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	N/A	A	A	F	B	F	F	F	F(-1)
verified	N/A	Yes	Yes	N/A	TBD	TBD	TBD	TBD	TBD
size	1147	1147	848	0	4345	0	0	0	0
N.S.	1	1.00	0.74	0.00	3.79	0.00	0.00	0.00	0.00
time (sec)	N/A	2.724	3.257	0.000	1.390	0.000	0.000	0.000	0.000

Problem 43	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	N/A	A	A	F	B	F	F	F	F(-1)
verified	N/A	Yes	Yes	N/A	TBD	TBD	TBD	TBD	TBD
size	787	787	662	0	2477	0	0	0	0
N.S.	1	1.00	0.84	0.00	3.15	0.00	0.00	0.00	0.00
time (sec)	N/A	1.902	2.616	0.000	0.895	0.000	0.000	0.000	0.000

Problem 44	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	N/A	A	B	F	B	B	F	F	F(-1)
verified	N/A	Yes	Yes	N/A	TBD	TBD	TBD	TBD	TBD
size	204	204	517	0	994	828	0	0	0
N.S.	1	1.00	2.53	0.00	4.87	4.06	0.00	0.00	0.00
time (sec)	N/A	0.321	5.669	0.000	0.601	0.276	0.000	0.000	0.000

Problem 45	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	N/A	N/A	N/A	N/A	N/A	N/A	N/A	N/A	N/A
verified	N/A	N/A	N/A	N/A	TBD	TBD	TBD	TBD	TBD
size	20	20	22	18	3514	38	19	20	20
N.S.	1	1.00	1.10	0.90	175.70	1.90	0.95	1.00	1.00
time (sec)	N/A	0.025	168.734	0.653	3.513	0.252	3.461	1.117	4.733

Problem 46	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	N/A	N/A	N/A	N/A	F(-2)	N/A	N/A	N/A	N/A
verified	N/A	N/A	N/A	N/A	TBD	TBD	TBD	TBD	TBD
size	20	20	22	18	0	44	20	20	20
N.S.	1	1.00	1.10	0.90	0.00	2.20	1.00	1.00	1.00
time (sec)	N/A	0.025	33.606	0.716	0.000	0.253	3.431	1.111	4.120

Problem 47	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	N/A	A	A	F	B	F	F	F	F(-1)
verified	N/A	Yes	Yes	N/A	TBD	TBD	TBD	TBD	TBD
size	287	287	287	0	1119	0	0	0	0
N.S.	1	1.00	1.00	0.00	3.90	0.00	0.00	0.00	0.00
time (sec)	N/A	0.497	0.098	0.000	0.493	0.000	0.000	0.000	0.000

Problem 48	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	N/A	A	A	F	B	F	F	F	F(-1)
verified	N/A	Yes	Yes	N/A	TBD	TBD	TBD	TBD	TBD
size	203	203	203	0	618	0	0	0	0
N.S.	1	1.00	1.00	0.00	3.04	0.00	0.00	0.00	0.00
time (sec)	N/A	0.357	0.032	0.000	0.399	0.000	0.000	0.000	0.000

Problem 49	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	N/A	A	A	F	F	B	F	F	F(-1)
verified	N/A	Yes	Yes	N/A	TBD	TBD	TBD	TBD	TBD
size	98	98	98	0	0	249	0	0	0
N.S.	1	1.00	1.00	0.00	0.00	2.54	0.00	0.00	0.00
time (sec)	N/A	0.221	0.022	0.000	0.000	0.265	0.000	0.000	0.000

Problem 50	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	N/A	N/A	N/A	N/A	N/A	N/A	N/A	N/A	N/A
verified	N/A	N/A	N/A	N/A	TBD	TBD	TBD	TBD	TBD
size	18	18	20	16	68	18	15	18	18
N.S.	1	1.00	1.11	0.89	3.78	1.00	0.83	1.00	1.00
time (sec)	N/A	0.029	4.948	0.393	0.530	0.229	1.634	0.458	4.104

Problem 51	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	N/A	N/A	N/A	N/A	N/A	N/A	N/A	N/A	N/A
verified	N/A	N/A	N/A	N/A	TBD	TBD	TBD	TBD	TBD
size	18	18	20	16	72	18	17	18	18
N.S.	1	1.00	1.11	0.89	4.00	1.00	0.94	1.00	1.00
time (sec)	N/A	0.028	2.096	0.348	0.531	0.247	1.820	0.459	4.100

Problem 52	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	N/A	A	A	F	B	F	F	F	F(-1)
verified	N/A	Yes	Yes	N/A	TBD	TBD	TBD	TBD	TBD
size	597	597	828	0	4725	0	0	0	0
N.S.	1	1.00	1.39	0.00	7.91	0.00	0.00	0.00	0.00
time (sec)	N/A	1.274	4.704	0.000	0.935	0.000	0.000	0.000	0.000

Problem 53	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	N/A	A	A	F	B	F	F	F	F(-1)
verified	N/A	Yes	Yes	N/A	TBD	TBD	TBD	TBD	TBD
size	408	408	571	0	2421	0	0	0	0
N.S.	1	1.00	1.40	0.00	5.93	0.00	0.00	0.00	0.00
time (sec)	N/A	0.867	3.853	0.000	0.552	0.000	0.000	0.000	0.000

Problem 54	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	N/A	A	A	F	F	A	F	F	F(-1)
verified	N/A	Yes	Yes	N/A	TBD	TBD	TBD	TBD	TBD
size	206	206	185	0	0	320	0	0	0
N.S.	1	1.00	0.90	0.00	0.00	1.55	0.00	0.00	0.00
time (sec)	N/A	0.420	1.595	0.000	0.000	0.273	0.000	0.000	0.000

Problem 55	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	N/A	N/A	N/A	N/A	N/A	N/A	N/A	N/A	N/A
verified	N/A	N/A	N/A	N/A	TBD	TBD	TBD	TBD	TBD
size	20	20	22	18	298	36	17	20	20
N.S.	1	1.00	1.10	0.90	14.90	1.80	0.85	1.00	1.00
time (sec)	N/A	0.025	123.769	0.935	0.717	0.246	8.785	0.876	4.536

Problem 56	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	N/A	N/A	N/A	N/A	N/A	N/A	N/A	N/A	N/A
verified	N/A	N/A	N/A	N/A	TBD	TBD	TBD	TBD	TBD
size	20	20	22	18	299	36	19	20	20
N.S.	1	1.00	1.10	0.90	14.95	1.80	0.95	1.00	1.00
time (sec)	N/A	0.023	19.051	1.214	1.023	0.234	2.600	0.868	4.285

Problem 57	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	N/A	A	A	F	B	F	F(-1)	F	F(-1)
verified	N/A	Yes	Yes	N/A	TBD	TBD	TBD	TBD	TBD
size	511	511	451	0	1315	0	0	0	0
N.S.	1	1.00	0.88	0.00	2.57	0.00	0.00	0.00	0.00
time (sec)	N/A	0.750	1.656	0.000	0.681	0.000	0.000	0.000	0.000

Problem 58	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	N/A	A	A	F	B	F	F	F	F(-1)
verified	N/A	Yes	Yes	N/A	TBD	TBD	TBD	TBD	TBD
size	352	352	310	0	813	0	0	0	0
N.S.	1	1.00	0.88	0.00	2.31	0.00	0.00	0.00	0.00
time (sec)	N/A	0.529	1.117	0.000	0.512	0.000	0.000	0.000	0.000

Problem 59	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	N/A	A	A	F	B	B	F	F	F(-1)
verified	N/A	Yes	Yes	N/A	TBD	TBD	TBD	TBD	TBD
size	176	176	165	0	446	746	0	0	0
N.S.	1	1.00	0.94	0.00	2.53	4.24	0.00	0.00	0.00
time (sec)	N/A	0.333	0.880	0.000	0.460	0.259	0.000	0.000	0.000

Problem 60	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	N/A	N/A	N/A	N/A	N/A	N/A	N/A	N/A	N/A
verified	N/A	N/A	N/A	N/A	TBD	TBD	TBD	TBD	TBD
size	20	20	22	18	496	19	17	20	20
N.S.	1	1.00	1.10	0.90	24.80	0.95	0.85	1.00	1.00
time (sec)	N/A	0.031	4.394	0.431	1.000	0.228	2.146	0.755	3.966

Problem 61	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	N/A	N/A	N/A	N/A	N/A	N/A	N/A	N/A	N/A
verified	N/A	N/A	N/A	N/A	TBD	TBD	TBD	TBD	TBD
size	20	20	22	18	496	23	19	20	20
N.S.	1	1.00	1.10	0.90	24.80	1.15	0.95	1.00	1.00
time (sec)	N/A	0.028	5.260	0.473	1.461	0.227	12.636	0.675	3.959

Problem 62	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	N/A	A	A	F	B	F	F	F	F(-1)
verified	N/A	Yes	Yes	N/A	TBD	TBD	TBD	TBD	TBD
size	1691	1691	1136	0	8152	0	0	0	0
N.S.	1	1.00	0.67	0.00	4.82	0.00	0.00	0.00	0.00
time (sec)	N/A	3.285	4.271	0.000	2.639	0.000	0.000	0.000	0.000

Problem 63	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	N/A	A	A	F	B	F	F	F	F(-1)
verified	N/A	Yes	Yes	N/A	TBD	TBD	TBD	TBD	TBD
size	1155	1155	852	0	4345	0	0	0	0
N.S.	1	1.00	0.74	0.00	3.76	0.00	0.00	0.00	0.00
time (sec)	N/A	2.434	3.215	0.000	1.339	0.000	0.000	0.000	0.000

Problem 64	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	N/A	A	A	F	B	B	F	F	F(-1)
verified	N/A	Yes	Yes	N/A	TBD	TBD	TBD	TBD	TBD
size	610	610	538	0	1732	1187	0	0	0
N.S.	1	1.00	0.88	0.00	2.84	1.95	0.00	0.00	0.00
time (sec)	N/A	1.588	2.913	0.000	0.705	0.272	0.000	0.000	0.000

Problem 65	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	N/A	N/A	N/A	N/A	N/A	N/A	N/A	N/A	N/A
verified	N/A	N/A	N/A	N/A	TBD	TBD	TBD	TBD	TBD
size	20	20	22	18	3514	38	19	20	20
N.S.	1	1.00	1.10	0.90	175.70	1.90	0.95	1.00	1.00
time (sec)	N/A	0.025	165.447	0.636	3.561	0.235	3.810	1.059	4.583

Problem 66	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	N/A	N/A	N/A	N/A	N/A	N/A	F(-1)	N/A	N/A
verified	N/A	N/A	N/A	N/A	TBD	TBD	TBD	TBD	TBD
size	20	20	22	18	2524	44	0	20	20
N.S.	1	1.00	1.10	0.90	126.20	2.20	0.00	1.00	1.00
time (sec)	N/A	0.026	119.963	0.669	15.397	0.244	0.000	1.127	4.287

2.3 Detailed conclusion table specific for Rubi results

The following table is specific to Rubi only. It gives additional statistics for each integral. the column **steps** is the number of steps used by Rubi to obtain the antiderivative. The **rules** column is the number of unique rules used. The **integrand size** column is the leaf size of the integrand. Finally the ratio $\frac{\text{number of rules}}{\text{integrand size}}$ is also given. The larger this ratio is, the harder the integral is to solve. In this test file, problem number [54] had the largest ratio of [.687500000000000000]

Table 2.1: Rubi specific breakdown of results for each integral

#	grade	number of steps used	number of unique rules	normalized antiderivative leaf size	integrand leaf size	$\frac{\text{number of rules}}{\text{integrand leaf size}}$
1	A	7	6	1.00	16	0.375
2	N/A	0	0	1.00	16	0.000
3	A	4	3	1.00	14	0.214
4	N/A	0	0	1.00	12	0.000
5	N/A	0	0	1.00	16	0.000
6	N/A	0	0	1.00	16	0.000
7	A	10	9	1.00	18	0.500
8	N/A	0	0	1.00	18	0.000
9	A	3	3	1.00	16	0.188
10	N/A	0	0	1.00	14	0.000
11	N/A	0	0	1.00	18	0.000
12	N/A	0	0	1.00	18	0.000
13	A	5	5	1.00	18	0.278
14	N/A	0	0	1.00	18	0.000
15	A	3	3	1.00	16	0.188
16	N/A	0	0	1.00	14	0.000
17	N/A	0	0	1.00	18	0.000
18	N/A	0	0	1.00	18	0.000
19	A	6	6	1.00	18	0.333
20	N/A	0	0	1.00	18	0.000
21	A	4	4	1.00	16	0.250
22	N/A	0	0	1.00	14	0.000

Continued on next page

Table 2.1 – continued from previous page

#	grade	number of steps used	number of unique rules	normalized antiderivative leaf size	integrand leaf size	$\frac{\text{number of rules}}{\text{integrand leaf size}}$
23	N/A	0	0	1.00	18	0.000
24	N/A	0	0	1.00	18	0.000
25	A	13	8	1.00	18	0.444
26	A	11	8	1.00	18	0.444
27	A	9	8	1.00	16	0.500
28	A	6	5	1.00	14	0.357
29	N/A	0	0	1.00	18	0.000
30	N/A	0	0	1.00	18	0.000
31	A	20	10	1.00	20	0.500
32	A	16	10	1.00	18	0.556
33	A	10	9	1.00	16	0.562
34	N/A	0	0	1.00	20	0.000
35	N/A	0	0	1.00	20	0.000
36	A	11	7	1.00	20	0.350
37	A	9	7	1.00	20	0.350
38	A	7	7	1.00	18	0.389
39	A	5	5	1.00	16	0.312
40	N/A	0	0	1.00	20	0.000
41	N/A	0	0	1.00	20	0.000
42	A	28	10	1.00	20	0.500
43	A	22	10	1.00	18	0.556
44	A	6	6	1.00	16	0.375
45	N/A	0	0	1.00	20	0.000
46	N/A	0	0	1.00	20	0.000
47	A	14	8	1.00	18	0.444
48	A	11	8	1.00	16	0.500
49	A	7	6	1.00	14	0.429
50	N/A	0	0	1.00	18	0.000
51	N/A	0	0	1.00	18	0.000
52	A	26	10	1.00	20	0.500
53	A	20	10	1.00	18	0.556
54	A	14	11	1.00	16	0.688
55	N/A	0	0	1.00	20	0.000

Continued on next page

Table 2.1 – continued from previous page

#	grade	number of steps used	number of unique rules	normalized antiderivative leaf size	integrand leaf size	$\frac{\text{number of rules}}{\text{integrand leaf size}}$
56	N/A	0	0	1.00	20	0.000
57	A	12	7	1.00	20	0.350
58	A	9	7	1.00	18	0.389
59	A	6	6	1.00	16	0.375
60	N/A	0	0	1.00	20	0.000
61	N/A	0	0	1.00	20	0.000
62	A	37	10	1.00	20	0.500
63	A	28	10	1.00	18	0.556
64	A	19	11	1.00	16	0.688
65	N/A	0	0	1.00	20	0.000
66	N/A	0	0	1.00	20	0.000

CHAPTER 3

LISTING OF INTEGRALS

3.1	$\int x^3(a + b \tan(c + dx^2)) dx$	46
3.2	$\int x^2(a + b \tan(c + dx^2)) dx$	51
3.3	$\int x(a + b \tan(c + dx^2)) dx$	54
3.4	$\int (a + b \tan(c + dx^2)) dx$	58
3.5	$\int \frac{a+b \tan(c+dx^2)}{x} dx$	61
3.6	$\int \frac{a+b \tan(c+dx^2)}{x^2} dx$	64
3.7	$\int x^3(a + b \tan(c + dx^2))^2 dx$	67
3.8	$\int x^2(a + b \tan(c + dx^2))^2 dx$	73
3.9	$\int x(a + b \tan(c + dx^2))^2 dx$	76
3.10	$\int (a + b \tan(c + dx^2))^2 dx$	80
3.11	$\int \frac{(a+b \tan(c+dx^2))^2}{x} dx$	83
3.12	$\int \frac{(a+b \tan(c+dx^2))^2}{x^2} dx$	86
3.13	$\int \frac{x^3}{a+b \tan(c+dx^2)} dx$	89
3.14	$\int \frac{x^2}{a+b \tan(c+dx^2)} dx$	94
3.15	$\int \frac{x}{a+b \tan(c+dx^2)} dx$	97
3.16	$\int \frac{1}{a+b \tan(c+dx^2)} dx$	102
3.17	$\int \frac{1}{x(a+b \tan(c+dx^2))} dx$	105
3.18	$\int \frac{1}{x^2(a+b \tan(c+dx^2))} dx$	108
3.19	$\int \frac{x^3}{(a+b \tan(c+dx^2))^2} dx$	111
3.20	$\int \frac{x^2}{(a+b \tan(c+dx^2))^2} dx$	118
3.21	$\int \frac{x}{(a+b \tan(c+dx^2))^2} dx$	122
3.22	$\int \frac{1}{(a+b \tan(c+dx^2))^2} dx$	128
3.23	$\int \frac{1}{x(a+b \tan(c+dx^2))^2} dx$	132

3.24	$\int \frac{1}{x^2(a+b \tan(c+d\sqrt{x}))^2} dx$	137
3.25	$\int x^3(a+b \tan(c+d\sqrt{x})) dx$	142
3.26	$\int x^2(a+b \tan(c+d\sqrt{x})) dx$	150
3.27	$\int x(a+b \tan(c+d\sqrt{x})) dx$	157
3.28	$\int (a+b \tan(c+d\sqrt{x})) dx$	163
3.29	$\int \frac{a+b \tan(c+d\sqrt{x})}{x} dx$	167
3.30	$\int \frac{a+b \tan(c+d\sqrt{x})}{x^2} dx$	170
3.31	$\int x^2(a+b \tan(c+d\sqrt{x}))^2 dx$	173
3.32	$\int x(a+b \tan(c+d\sqrt{x}))^2 dx$	185
3.33	$\int (a+b \tan(c+d\sqrt{x}))^2 dx$	194
3.34	$\int \frac{(a+b \tan(c+d\sqrt{x}))^2}{x} dx$	200
3.35	$\int \frac{(a+b \tan(c+d\sqrt{x}))^2}{x^2} dx$	203
3.36	$\int \frac{x^3}{a+b \tan(c+d\sqrt{x})} dx$	207
3.37	$\int \frac{x^2}{a+b \tan(c+d\sqrt{x})} dx$	216
3.38	$\int \frac{x}{a+b \tan(c+d\sqrt{x})} dx$	224
3.39	$\int \frac{1}{a+b \tan(c+d\sqrt{x})} dx$	230
3.40	$\int \frac{1}{x(a+b \tan(c+d\sqrt{x}))} dx$	235
3.41	$\int \frac{1}{x^2(a+b \tan(c+d\sqrt{x}))} dx$	238
3.42	$\int \frac{x^2}{(a+b \tan(c+d\sqrt{x}))^2} dx$	241
3.43	$\int \frac{x}{(a+b \tan(c+d\sqrt{x}))^2} dx$	260
3.44	$\int \frac{1}{(a+b \tan(c+d\sqrt{x}))^2} dx$	274
3.45	$\int \frac{1}{x(a+b \tan(c+d\sqrt{x}))^2} dx$	281
3.46	$\int \frac{1}{x^2(a+b \tan(c+d\sqrt{x}))^2} dx$	286
3.47	$\int x^2(a+b \tan(c+d\sqrt[3]{x})) dx$	290
3.48	$\int x(a+b \tan(c+d\sqrt[3]{x})) dx$	300
3.49	$\int (a+b \tan(c+d\sqrt[3]{x})) dx$	307
3.50	$\int \frac{a+b \tan(c+d\sqrt[3]{x})}{x} dx$	312
3.51	$\int \frac{a+b \tan(c+d\sqrt[3]{x})}{x^2} dx$	316
3.52	$\int x^2(a+b \tan(c+d\sqrt[3]{x}))^2 dx$	320
3.53	$\int x(a+b \tan(c+d\sqrt[3]{x}))^2 dx$	337
3.54	$\int (a+b \tan(c+d\sqrt[3]{x}))^2 dx$	348
3.55	$\int \frac{(a+b \tan(c+d\sqrt[3]{x}))^2}{x} dx$	355
3.56	$\int \frac{(a+b \tan(c+d\sqrt[3]{x}))^2}{x^2} dx$	359
3.57	$\int \frac{x^3}{a+b \tan(c+d\sqrt[3]{x})} dx$	363

3.58	$\int \frac{x}{a+b \tan(c+d \sqrt[3]{x})} dx$	377
3.59	$\int \frac{1}{a+b \tan(c+d \sqrt[3]{x})} dx$	386
3.60	$\int \frac{1}{x(a+b \tan(c+d \sqrt[3]{x}))} dx$	393
3.61	$\int \frac{1}{x^2(a+b \tan(c+d \sqrt[3]{x}))} dx$	397
3.62	$\int \frac{x^2}{(a+b \tan(c+d \sqrt[3]{x}))^2} dx$	401
3.63	$\int \frac{x}{(a+b \tan(c+d \sqrt[3]{x}))^2} dx$	419
3.64	$\int \frac{1}{(a+b \tan(c+d \sqrt[3]{x}))^2} dx$	438
3.65	$\int \frac{1}{x(a+b \tan(c+d \sqrt[3]{x}))^2} dx$	451
3.66	$\int \frac{1}{x^2(a+b \tan(c+d \sqrt[3]{x}))^2} dx$	456

3.1 $\int x^3(a + b \tan(c + dx^2)) dx$

Optimal result	46
Rubi [A] (verified)	46
Mathematica [A] (verified)	48
Maple [F]	48
Fricas [B] (verification not implemented)	48
Sympy [F]	49
Maxima [F]	49
Giac [F]	49
Mupad [B] (verification not implemented)	50

Optimal result

Integrand size = 16, antiderivative size = 73

$$\int x^3(a + b \tan(c + dx^2)) dx = \frac{ax^4}{4} + \frac{1}{4}ibx^4 - \frac{bx^2 \log(1 + e^{2i(c+dx^2)})}{2d} + \frac{ib \operatorname{PolyLog}(2, -e^{2i(c+dx^2)})}{4d^2}$$

[Out] $\frac{1}{4}ax^4 + \frac{1}{4}Ib x^4 - \frac{1}{2}bx^2 \ln(1 + \exp(2I*(dx^2+c)))/d + \frac{1}{4}Ib \operatorname{polylog}(2, -\exp(2I*(dx^2+c)))/d^2$

Rubi [A] (verified)

Time = 0.16 (sec), antiderivative size = 73, normalized size of antiderivative = 1.00, number of steps used = 7, number of rules used = 6, $\frac{\text{number of rules}}{\text{integrand size}} = 0.375$, Rules used = {14, 3832, 3800, 2221, 2317, 2438}

$$\int x^3(a + b \tan(c + dx^2)) dx = \frac{ax^4}{4} + \frac{ib \operatorname{PolyLog}(2, -e^{2i(dx^2+c)})}{4d^2} - \frac{bx^2 \log(1 + e^{2i(c+dx^2)})}{2d} + \frac{1}{4}ibx^4$$

[In] $\operatorname{Int}[x^3*(a + b*\operatorname{Tan}[c + d*x^2]),x]$

[Out] $(ax^4)/4 + (I/4)*b*x^4 - (b*x^2*\operatorname{Log}[1 + E^((2*I)*(c + d*x^2))])/(2*d) + ((I/4)*b*\operatorname{PolyLog}[2, -E^((2*I)*(c + d*x^2))])/d^2$

Rule 14

```
Int[(u_)*((c_)*(x_))^(m_), x_Symbol] := Int[ExpandIntegrand[(c*x)^m*u, x], x] /; FreeQ[{c, m}, x] && SumQ[u] && !LinearQ[u, x] && !MatchQ[u, (a_ + (b_)*(v_)) /; FreeQ[{a, b}, x] && InverseFunctionQ[v]]
```

Rule 2221

```
Int[(((F_)^((g_)*((e_) + (f_)*(x_))))^(n_)*((c_) + (d_)*(x_))^(m_))/((a_) + (b_)*((F_)^((g_)*((e_) + (f_)*(x_))))^(n_)), x_Symbol] := Simp[((c + d*x)^m/(b*f*g*n*Log[F]))*Log[1 + b*((F^(g*(e + f*x)))^n/a)], x] - Dist[d*(m/(b*f*g*n*Log[F])), Int[(c + d*x)^(m - 1)*Log[1 + b*((F^(g*(e + f*x)))^n/a)], x], x] /; FreeQ[{F, a, b, c, d, e, f, g, n}, x] && IGtQ[m, 0]
```

Rule 2317

```
Int[Log[(a_) + (b_)*((F_)^((e_)*((c_) + (d_)*(x_))))^(n_)], x_Symbol] := Dist[1/(d*e*n*Log[F]), Subst[Int[Log[a + b*x]/x, x], x, (F^(e*(c + d*x)))^n], x] /; FreeQ[{F, a, b, c, d, e, n}, x] && GtQ[a, 0]
```

Rule 2438

```
Int[Log[(c_)*((d_) + (e_)*(x_))^(n_)], x_Symbol] := Simp[-PolyLog[2, (-c)*e*x^n]/n, x] /; FreeQ[{c, d, e, n}, x] && EqQ[c*d, 1]
```

Rule 3800

```
Int[(((c_) + (d_)*(x_))^(m_)*tan[(e_) + (f_)*(x_)]), x_Symbol] := Simp[I*((c + d*x)^(m + 1)/(d*(m + 1))), x] - Dist[2*I, Int[(c + d*x)^m*(E^(2*I*(e + f*x)))/(1 + E^(2*I*(e + f*x)))], x], x] /; FreeQ[{c, d, e, f}, x] && IGtQ[m, 0]
```

Rule 3832

```
Int[(x_)^(m_)*((a_) + (b_)*Tan[(c_) + (d_)*(x_)]^(n_))^(p_), x_Symbol] := Dist[1/n, Subst[Int[x^(Simplify[(m + 1)/n] - 1)*(a + b*Tan[c + d*x])^p, x], x, x^n], x] /; FreeQ[{a, b, c, d, m, n, p}, x] && IGtQ[Simplify[(m + 1)/n], 0] && IntegerQ[p]
```

Rubi steps

$$\begin{aligned} \text{integral} &= \int (ax^3 + bx^3 \tan(c + dx^2)) dx \\ &= \frac{ax^4}{4} + b \int x^3 \tan(c + dx^2) dx \\ &= \frac{ax^4}{4} + \frac{1}{2}b \text{Subst}\left(\int x \tan(c + dx) dx, x, x^2\right) \end{aligned}$$

$$\begin{aligned}
&= \frac{ax^4}{4} + \frac{1}{4}ibx^4 - (ib)\text{Subst}\left(\int \frac{e^{2i(c+dx)}x}{1+e^{2i(c+dx)}} dx, x, x^2\right) \\
&= \frac{ax^4}{4} + \frac{1}{4}ibx^4 - \frac{bx^2 \log\left(1+e^{2i(c+dx^2)}\right)}{2d} + \frac{b\text{Subst}\left(\int \log\left(1+e^{2i(c+dx)}\right) dx, x, x^2\right)}{2d} \\
&= \frac{ax^4}{4} + \frac{1}{4}ibx^4 - \frac{bx^2 \log\left(1+e^{2i(c+dx^2)}\right)}{2d} - \frac{(ib)\text{Subst}\left(\int \frac{\log(1+x)}{x} dx, x, e^{2i(c+dx^2)}\right)}{4d^2} \\
&= \frac{ax^4}{4} + \frac{1}{4}ibx^4 - \frac{bx^2 \log\left(1+e^{2i(c+dx^2)}\right)}{2d} + \frac{ib \text{PolyLog}\left(2, -e^{2i(c+dx^2)}\right)}{4d^2}
\end{aligned}$$

Mathematica [A] (verified)

Time = 0.04 (sec) , antiderivative size = 73, normalized size of antiderivative = 1.00

$$\begin{aligned}
\int x^3(a+b \tan(c+dx^2)) dx &= \frac{ax^4}{4} + \frac{1}{4}ibx^4 - \frac{bx^2 \log\left(1+e^{2i(c+dx^2)}\right)}{2d} \\
&\quad + \frac{ib \text{PolyLog}\left(2, -e^{2i(c+dx^2)}\right)}{4d^2}
\end{aligned}$$

[In] Integrate[x^3*(a + b*Tan[c + d*x^2]),x]

[Out] (a*x^4)/4 + (I/4)*b*x^4 - (b*x^2*Log[1 + E^((2*I)*(c + d*x^2))])/(2*d) + ((I/4)*b*PolyLog[2, -E^((2*I)*(c + d*x^2))])/d^2

Maple [F]

$$\int x^3(a+b \tan(dx^2+c)) dx$$

[In] int(x^3*(a+b*tan(d*x^2+c)),x)

[Out] int(x^3*(a+b*tan(d*x^2+c)),x)

Fricas [B] (verification not implemented)

Both result and optimal contain complex but leaf count of result is larger than twice the leaf count of optimal. 155 vs. 2(56) = 112.

Time = 0.27 (sec) , antiderivative size = 155, normalized size of antiderivative = 2.12

$$\begin{aligned}
&\int x^3(a+b \tan(c+dx^2)) dx \\
&= \frac{2ad^2x^4 - 2bdx^2 \log\left(-\frac{2(i \tan(dx^2+c)-1)}{\tan(dx^2+c)^2+1}\right) - 2bdx^2 \log\left(-\frac{2(-i \tan(dx^2+c)-1)}{\tan(dx^2+c)^2+1}\right) - i b \text{Li}_2\left(\frac{2(i \tan(dx^2+c)-1)}{\tan(dx^2+c)^2+1} + 1\right)}{8d^2}
\end{aligned}$$

[In] integrate(x^3*(a+b*tan(d*x^2+c)),x, algorithm="fricas")

[Out] $\frac{1}{8}(2ad^2x^4 - 2bdx^2 \log(-2*(I*\tan(dx^2 + c) - 1)/(\tan(dx^2 + c)^2 + 1)) - 2bdx^2 \log(-2*(-I*\tan(dx^2 + c) - 1)/(\tan(dx^2 + c)^2 + 1)) - I*b*dilog(2*(I*\tan(dx^2 + c) - 1)/(\tan(dx^2 + c)^2 + 1) + 1) + I*b*dilog(2*(-I*\tan(dx^2 + c) - 1)/(\tan(dx^2 + c)^2 + 1) + 1))/d^2$

Sympy [F]

$$\int x^3(a + b \tan(c + dx^2)) dx = \int x^3(a + b \tan(c + dx^2)) dx$$

[In] integrate(x**3*(a+b*tan(d*x**2+c)),x)

[Out] Integral(x**3*(a + b*tan(c + d*x**2)), x)

Maxima [F]

$$\int x^3(a + b \tan(c + dx^2)) dx = \int (b \tan(dx^2 + c) + a)x^3 dx$$

[In] integrate(x^3*(a+b*tan(d*x^2+c)),x, algorithm="maxima")

[Out] $\frac{1}{4}ax^4 + 2b \int x^3 \sin(2dx^2 + 2c) / (\cos(2dx^2 + 2c)^2 + \sin(2dx^2 + 2c)^2 + 2\cos(2dx^2 + 2c) + 1) dx$

Giac [F]

$$\int x^3(a + b \tan(c + dx^2)) dx = \int (b \tan(dx^2 + c) + a)x^3 dx$$

[In] integrate(x^3*(a+b*tan(d*x^2+c)),x, algorithm="giac")

[Out] integrate((b*tan(dx^2 + c) + a)*x^3, x)

Mupad [B] (verification not implemented)

Time = 0.48 (sec) , antiderivative size = 155, normalized size of antiderivative = 2.12

$$\int x^3 (a + b \tan(c + dx^2)) dx = \frac{ax^4}{4} - \frac{b \left(\pi \ln(\cos(dx^2)) + 2c \ln(e^{-dx^2 2i} e^{-c 2i} + 1) - \pi \ln(e^{-dx^2 2i} e^{-c 2i} + 1) - \ln(\cos(dx^2 + c)) (2c - \pi) \right)}{4}$$

```
[In] int(x^3*(a + b*tan(c + d*x^2)),x)
```

```
[Out] (a*x^4)/4 - (b*(2*c*log(exp(-d*x^2*2i)*exp(-c*2i) + 1) - pi*log(exp(-d*x^2*2i)*exp(-c*2i) + 1) + pi*log(cos(d*x^2)) - log(cos(c + d*x^2))*(2*c - pi) - pi*log(exp(d*x^2*2i) + 1) + polylog(2, -exp(-d*x^2*2i)*exp(-c*2i))*1i + d^2*x^4*1i + 2*d*x^2*log(exp(-d*x^2*2i)*exp(-c*2i) + 1) + c*d*x^2*2i))/(4*d^2)
```

3.2 $\int x^2(a + b \tan(c + dx^2)) dx$

Optimal result	51
Rubi [N/A]	51
Mathematica [N/A]	52
Maple [N/A] (verified)	52
Fricas [N/A]	52
Sympy [N/A]	52
Maxima [N/A]	53
Giac [N/A]	53
Mupad [N/A]	53

Optimal result

Integrand size = 16, antiderivative size = 16

$$\int x^2(a + b \tan(c + dx^2)) dx = \frac{ax^3}{3} + b \operatorname{Int}(x^2 \tan(c + dx^2), x)$$

[Out] $1/3*a*x^3+b*\operatorname{Unintegrable}(x^2*\tan(d*x^2+c), x)$

Rubi [N/A]

Not integrable

Time = 0.02 (sec) , antiderivative size = 16, normalized size of antiderivative = 1.00, number of steps used = 0, number of rules used = 0, $\frac{\text{number of rules}}{\text{integrand size}} = 0.000$, Rules used = {}

$$\int x^2(a + b \tan(c + dx^2)) dx = \int x^2(a + b \tan(c + dx^2)) dx$$

[In] $\operatorname{Int}[x^2*(a + b*\operatorname{Tan}[c + d*x^2]), x]$

[Out] $(a*x^3)/3 + b*\operatorname{Defer}[\operatorname{Int}[x^2*\operatorname{Tan}[c + d*x^2], x]$

Rubi steps

$$\begin{aligned} \text{integral} &= \int (ax^2 + bx^2 \tan(c + dx^2)) dx \\ &= \frac{ax^3}{3} + b \int x^2 \tan(c + dx^2) dx \end{aligned}$$

Mathematica [N/A]

Not integrable

Time = 2.76 (sec) , antiderivative size = 18, normalized size of antiderivative = 1.12

$$\int x^2(a + b \tan(c + dx^2)) dx = \int x^2(a + b \tan(c + dx^2)) dx$$

[In] Integrate[x^2*(a + b*Tan[c + d*x^2]),x]

[Out] Integrate[x^2*(a + b*Tan[c + d*x^2]), x]

Maple [N/A] (verified)

Not integrable

Time = 0.10 (sec) , antiderivative size = 16, normalized size of antiderivative = 1.00

$$\int x^2(a + b \tan(dx^2 + c)) dx$$

[In] int(x^2*(a+b*tan(d*x^2+c)),x)

[Out] int(x^2*(a+b*tan(d*x^2+c)),x)

Fricas [N/A]

Not integrable

Time = 0.24 (sec) , antiderivative size = 21, normalized size of antiderivative = 1.31

$$\int x^2(a + b \tan(c + dx^2)) dx = \int (b \tan(dx^2 + c) + a)x^2 dx$$

[In] integrate(x^2*(a+b*tan(d*x^2+c)),x, algorithm="fricas")

[Out] integral(b*x^2*tan(d*x^2 + c) + a*x^2, x)

Sympy [N/A]

Not integrable

Time = 0.58 (sec) , antiderivative size = 15, normalized size of antiderivative = 0.94

$$\int x^2(a + b \tan(c + dx^2)) dx = \int x^2(a + b \tan(c + dx^2)) dx$$

[In] integrate(x**2*(a+b*tan(d*x**2+c)),x)

[Out] Integral(x**2*(a + b*tan(c + d*x**2)), x)

Maxima [N/A]

Not integrable

Time = 0.30 (sec) , antiderivative size = 70, normalized size of antiderivative = 4.38

$$\int x^2(a + b \tan(c + dx^2)) dx = \int (b \tan(dx^2 + c) + a)x^2 dx$$

[In] integrate(x^2*(a+b*tan(d*x^2+c)),x, algorithm="maxima")

[Out] 1/3*a*x^3 + 2*b*integrate(x^2*sin(2*d*x^2 + 2*c)/(cos(2*d*x^2 + 2*c)^2 + sin(2*d*x^2 + 2*c)^2 + 2*cos(2*d*x^2 + 2*c) + 1), x)

Giac [N/A]

Not integrable

Time = 0.37 (sec) , antiderivative size = 18, normalized size of antiderivative = 1.12

$$\int x^2(a + b \tan(c + dx^2)) dx = \int (b \tan(dx^2 + c) + a)x^2 dx$$

[In] integrate(x^2*(a+b*tan(d*x^2+c)),x, algorithm="giac")

[Out] integrate((b*tan(d*x^2 + c) + a)*x^2, x)

Mupad [N/A]

Not integrable

Time = 3.64 (sec) , antiderivative size = 18, normalized size of antiderivative = 1.12

$$\int x^2(a + b \tan(c + dx^2)) dx = \int x^2(a + b \tan(dx^2 + c)) dx$$

[In] int(x^2*(a + b*tan(c + d*x^2)),x)

[Out] int(x^2*(a + b*tan(c + d*x^2)), x)

3.3 $\int x(a + b \tan(c + dx^2)) dx$

Optimal result	54
Rubi [A] (verified)	54
Mathematica [A] (verified)	55
Maple [A] (verified)	55
Fricas [A] (verification not implemented)	56
Sympy [A] (verification not implemented)	56
Maxima [A] (verification not implemented)	57
Giac [A] (verification not implemented)	57
Mupad [B] (verification not implemented)	57

Optimal result

Integrand size = 14, antiderivative size = 26

$$\int x(a + b \tan(c + dx^2)) dx = \frac{ax^2}{2} - \frac{b \log(\cos(c + dx^2))}{2d}$$

[Out] 1/2*a*x^2-1/2*b*ln(cos(d*x^2+c))/d

Rubi [A] (verified)

Time = 0.03 (sec), antiderivative size = 26, normalized size of antiderivative = 1.00, number of steps used = 4, number of rules used = 3, $\frac{\text{number of rules}}{\text{integrand size}} = 0.214$, Rules used = {14, 3832, 3556}

$$\int x(a + b \tan(c + dx^2)) dx = \frac{ax^2}{2} - \frac{b \log(\cos(c + dx^2))}{2d}$$

[In] Int[x*(a + b*Tan[c + d*x^2]),x]

[Out] (a*x^2)/2 - (b*Log[Cos[c + d*x^2]])/(2*d)

Rule 14

```
Int[(u_)*((c_.)*(x_))^(m_.), x_Symbol] := Int[ExpandIntegrand[(c*x)^m*u, x], x] /; FreeQ[{c, m}, x] && SumQ[u] && !LinearQ[u, x] && !MatchQ[u, (a_ + (b_.)*(v_)) /; FreeQ[{a, b}, x] && InverseFunctionQ[v]]
```

Rule 3556

```
Int[tan[(c_.) + (d_.)*(x_)], x_Symbol] := Simp[-Log[RemoveContent[Cos[c + d*x], x]]/d, x] /; FreeQ[{c, d}, x]
```

Rule 3832

```
Int[(x_)^(m_.)*((a_.) + (b_.)*Tan[(c_.) + (d_.)*(x_)^(n_)])^(p_.), x_Symbol
] := Dist[1/n, Subst[Int[x^(Simplify[(m + 1)/n] - 1)*(a + b*Tan[c + d*x])^p
, x], x, x^n], x] /; FreeQ[{a, b, c, d, m, n, p}, x] && IGtQ[Simplify[(m +
1)/n], 0] && IntegerQ[p]
```

Rubi steps

$$\begin{aligned}
\text{integral} &= \int (ax + bx \tan(c + dx^2)) dx \\
&= \frac{ax^2}{2} + b \int x \tan(c + dx^2) dx \\
&= \frac{ax^2}{2} + \frac{1}{2} b \text{Subst}\left(\int \tan(c + dx) dx, x, x^2\right) \\
&= \frac{ax^2}{2} - \frac{b \log(\cos(c + dx^2))}{2d}
\end{aligned}$$

Mathematica [A] (verified)

Time = 0.03 (sec) , antiderivative size = 26, normalized size of antiderivative = 1.00

$$\int x(a + b \tan(c + dx^2)) dx = \frac{ax^2}{2} - \frac{b \log(\cos(c + dx^2))}{2d}$$

[In] Integrate[x*(a + b*Tan[c + d*x^2]),x]

[Out] (a*x^2)/2 - (b*Log[Cos[c + d*x^2]])/(2*d)

Maple [A] (verified)

Time = 0.09 (sec) , antiderivative size = 23, normalized size of antiderivative = 0.88

method	result	size
parts	$\frac{ax^2}{2} - \frac{b \ln(\cos(dx^2+c))}{2d}$	23
norman	$\frac{ax^2}{2} + \frac{b \ln(1+\tan^2(dx^2+c))}{4d}$	27
derivativdivides	$\frac{(dx^2+c)a - b \ln(\cos(dx^2+c))}{2d}$	28
default	$\frac{(dx^2+c)a - b \ln(\cos(dx^2+c))}{2d}$	28
parallelrisc	$\frac{2adx^2 + b \ln(1+\tan^2(dx^2+c))}{4d}$	29
risc	$\frac{ibx^2}{2} + \frac{ax^2}{2} + \frac{ibc}{d} - \frac{b \ln(1+e^{2i(dx^2+c)})}{2d}$	43

[In] `int(x*(a+b*tan(d*x^2+c)),x,method=_RETURNVERBOSE)`

[Out] $1/2*a*x^2-1/2*b*\ln(\cos(d*x^2+c))/d$

Fricas [A] (verification not implemented)

none

Time = 0.26 (sec) , antiderivative size = 31, normalized size of antiderivative = 1.19

$$\int x(a + b \tan(c + dx^2)) dx = \frac{2 adx^2 - b \log\left(\frac{1}{\tan(dx^2+c)^2+1}\right)}{4d}$$

[In] `integrate(x*(a+b*tan(d*x^2+c)),x, algorithm="fricas")`

[Out] $1/4*(2*a*d*x^2 - b*\log(1/(\tan(d*x^2 + c)^2 + 1)))/d$

Sympy [A] (verification not implemented)

Time = 0.09 (sec) , antiderivative size = 36, normalized size of antiderivative = 1.38

$$\int x(a + b \tan(c + dx^2)) dx = \begin{cases} \frac{ax^2}{2} + \frac{b \log(\tan^2(c+dx^2)+1)}{4d} & \text{for } d \neq 0 \\ \frac{x^2(a+b \tan(c))}{2} & \text{otherwise} \end{cases}$$

[In] `integrate(x*(a+b*tan(d*x**2+c)),x)`

[Out] `Piecewise((a*x**2/2 + b*log(tan(c + d*x**2)**2 + 1)/(4*d), Ne(d, 0)), (x**2*(a + b*tan(c))/2, True))`

Maxima [A] (verification not implemented)

none

Time = 0.23 (sec) , antiderivative size = 22, normalized size of antiderivative = 0.85

$$\int x(a + b \tan(c + dx^2)) dx = \frac{1}{2} ax^2 + \frac{b \log(\sec(dx^2 + c))}{2d}$$

[In] integrate(x*(a+b*tan(d*x^2+c)),x, algorithm="maxima")

[Out] 1/2*a*x^2 + 1/2*b*log(sec(d*x^2 + c))/d

Giac [A] (verification not implemented)

none

Time = 0.30 (sec) , antiderivative size = 28, normalized size of antiderivative = 1.08

$$\int x(a + b \tan(c + dx^2)) dx = \frac{(dx^2 + c)a - b \log(|\cos(dx^2 + c)|)}{2d}$$

[In] integrate(x*(a+b*tan(d*x^2+c)),x, algorithm="giac")

[Out] 1/2*((d*x^2 + c)*a - b*log(abs(cos(d*x^2 + c))))/d

Mupad [B] (verification not implemented)

Time = 0.12 (sec) , antiderivative size = 26, normalized size of antiderivative = 1.00

$$\int x(a + b \tan(c + dx^2)) dx = \frac{ax^2}{2} + \frac{b \ln(\tan(dx^2 + c)^2 + 1)}{4d}$$

[In] int(x*(a + b*tan(c + d*x^2)),x)

[Out] (a*x^2)/2 + (b*log(tan(c + d*x^2)^2 + 1))/(4*d)

3.4 $\int (a + b \tan (c + dx^2)) dx$

Optimal result	58
Rubi [N/A]	58
Mathematica [N/A]	59
Maple [N/A] (verified)	59
Fricas [N/A]	59
Sympy [N/A]	59
Maxima [N/A]	60
Giac [N/A]	60
Mupad [N/A]	60

Optimal result

Integrand size = 12, antiderivative size = 12

$$\int (a + b \tan (c + dx^2)) dx = ax + b \operatorname{Int}(\tan (c + dx^2), x)$$

[Out] a*x+b*Unintegrable(tan(d*x^2+c),x)

Rubi [N/A]

Not integrable

Time = 0.01 (sec) , antiderivative size = 12, normalized size of antiderivative = 1.00, number of steps used = 0, number of rules used = 0, $\frac{\text{number of rules}}{\text{integrand size}} = 0.000$, Rules used = {}

$$\int (a + b \tan (c + dx^2)) dx = \int (a + b \tan (c + dx^2)) dx$$

[In] Int[a + b*Tan[c + d*x^2],x]

[Out] a*x + b*Defer[Int][Tan[c + d*x^2], x]

Rubi steps

$$\text{integral} = ax + b \int \tan (c + dx^2) dx$$

Mathematica [N/A]

Not integrable

Time = 1.15 (sec) , antiderivative size = 14, normalized size of antiderivative = 1.17

$$\int (a + b \tan (c + dx^2)) dx = \int (a + b \tan (c + dx^2)) dx$$

`[In] Integrate[a + b*Tan[c + d*x^2],x]``[Out] Integrate[a + b*Tan[c + d*x^2], x]`**Maple [N/A] (verified)**

Not integrable

Time = 0.14 (sec) , antiderivative size = 12, normalized size of antiderivative = 1.00

$$\int (a + b \tan (dx^2 + c)) dx$$

`[In] int(a+b*tan(d*x^2+c),x)``[Out] int(a+b*tan(d*x^2+c),x)`**Fricas [N/A]**

Not integrable

Time = 0.23 (sec) , antiderivative size = 14, normalized size of antiderivative = 1.17

$$\int (a + b \tan (c + dx^2)) dx = \int b \tan (dx^2 + c) + a dx$$

`[In] integrate(a+b*tan(d*x^2+c),x, algorithm="fricas")``[Out] integral(b*tan(d*x^2 + c) + a, x)`**Sympy [N/A]**

Not integrable

Time = 0.24 (sec) , antiderivative size = 12, normalized size of antiderivative = 1.00

$$\int (a + b \tan (c + dx^2)) dx = \int (a + b \tan (c + dx^2)) dx$$

`[In] integrate(a+b*tan(d*x**2+c),x)``[Out] Integral(a + b*tan(c + d*x**2), x)`

Maxima [N/A]

Not integrable

Time = 0.28 (sec) , antiderivative size = 64, normalized size of antiderivative = 5.33

$$\int (a + b \tan (c + dx^2)) dx = \int b \tan (dx^2 + c) + a dx$$

[In] integrate(a+b*tan(d*x^2+c),x, algorithm="maxima")

[Out] a*x + 2*b*integrate(sin(2*d*x^2 + 2*c)/(cos(2*d*x^2 + 2*c)^2 + sin(2*d*x^2 + 2*c)^2 + 2*cos(2*d*x^2 + 2*c) + 1), x)

Giac [N/A]

Not integrable

Time = 0.32 (sec) , antiderivative size = 14, normalized size of antiderivative = 1.17

$$\int (a + b \tan (c + dx^2)) dx = \int b \tan (dx^2 + c) + a dx$$

[In] integrate(a+b*tan(d*x^2+c),x, algorithm="giac")

[Out] integrate(b*tan(d*x^2 + c) + a, x)

Mupad [N/A]

Not integrable

Time = 4.44 (sec) , antiderivative size = 14, normalized size of antiderivative = 1.17

$$\int (a + b \tan (c + dx^2)) dx = \int a + b \tan(dx^2 + c) dx$$

[In] int(a + b*tan(c + d*x^2),x)

[Out] int(a + b*tan(c + d*x^2), x)

3.5 $\int \frac{a+b \tan(c+dx^2)}{x} dx$

Optimal result	61
Rubi [N/A]	61
Mathematica [N/A]	62
Maple [N/A] (verified)	62
Fricas [N/A]	62
Sympy [N/A]	62
Maxima [N/A]	63
Giac [N/A]	63
Mupad [N/A]	63

Optimal result

Integrand size = 16, antiderivative size = 16

$$\int \frac{a + b \tan(c + dx^2)}{x} dx = a \log(x) + b \operatorname{Int}\left(\frac{\tan(c + dx^2)}{x}, x\right)$$

[Out] a*ln(x)+b*Unintegrable(tan(d*x^2+c)/x,x)

Rubi [N/A]

Not integrable

Time = 0.02 (sec) , antiderivative size = 16, normalized size of antiderivative = 1.00, number of steps used = 0, number of rules used = 0, $\frac{\text{number of rules}}{\text{integrand size}} = 0.000$, Rules used = {}

$$\int \frac{a + b \tan(c + dx^2)}{x} dx = \int \frac{a + b \tan(c + dx^2)}{x} dx$$

[In] Int[(a + b*Tan[c + d*x^2])/x,x]

[Out] a*Log[x] + b*Defer[Int][Tan[c + d*x^2]/x, x]

Rubi steps

$$\begin{aligned} \text{integral} &= \int \left(\frac{a}{x} + \frac{b \tan(c + dx^2)}{x} \right) dx \\ &= a \log(x) + b \int \frac{\tan(c + dx^2)}{x} dx \end{aligned}$$

Mathematica [N/A]

Not integrable

Time = 1.70 (sec) , antiderivative size = 18, normalized size of antiderivative = 1.12

$$\int \frac{a + b \tan(c + dx^2)}{x} dx = \int \frac{a + b \tan(c + dx^2)}{x} dx$$

[In] Integrate[(a + b*Tan[c + d*x^2])/x,x]

[Out] Integrate[(a + b*Tan[c + d*x^2])/x, x]

Maple [N/A] (verified)

Not integrable

Time = 0.10 (sec) , antiderivative size = 16, normalized size of antiderivative = 1.00

$$\int \frac{a + b \tan(dx^2 + c)}{x} dx$$

[In] int((a+b*tan(d*x^2+c))/x,x)

[Out] int((a+b*tan(d*x^2+c))/x,x)

Fricas [N/A]

Not integrable

Time = 0.24 (sec) , antiderivative size = 18, normalized size of antiderivative = 1.12

$$\int \frac{a + b \tan(c + dx^2)}{x} dx = \int \frac{b \tan(dx^2 + c) + a}{x} dx$$

[In] integrate((a+b*tan(d*x^2+c))/x,x, algorithm="fricas")

[Out] integral((b*tan(d*x^2 + c) + a)/x, x)

Sympy [N/A]

Not integrable

Time = 0.65 (sec) , antiderivative size = 14, normalized size of antiderivative = 0.88

$$\int \frac{a + b \tan(c + dx^2)}{x} dx = \int \frac{a + b \tan(c + dx^2)}{x} dx$$

[In] integrate((a+b*tan(d*x**2+c))/x,x)

[Out] Integral((a + b*tan(c + d*x**2))/x, x)

Maxima [N/A]

Not integrable

Time = 0.31 (sec) , antiderivative size = 70, normalized size of antiderivative = 4.38

$$\int \frac{a + b \tan(c + dx^2)}{x} dx = \int \frac{b \tan(dx^2 + c) + a}{x} dx$$

[In] integrate((a+b*tan(d*x^2+c))/x,x, algorithm="maxima")

[Out] 2*b*integrate(sin(2*d*x^2 + 2*c)/(x*cos(2*d*x^2 + 2*c)^2 + x*sin(2*d*x^2 + 2*c)^2 + 2*x*cos(2*d*x^2 + 2*c) + x), x) + a*log(x)

Giac [N/A]

Not integrable

Time = 0.34 (sec) , antiderivative size = 18, normalized size of antiderivative = 1.12

$$\int \frac{a + b \tan(c + dx^2)}{x} dx = \int \frac{b \tan(dx^2 + c) + a}{x} dx$$

[In] integrate((a+b*tan(d*x^2+c))/x,x, algorithm="giac")

[Out] integrate((b*tan(d*x^2 + c) + a)/x, x)

Mupad [N/A]

Not integrable

Time = 3.76 (sec) , antiderivative size = 18, normalized size of antiderivative = 1.12

$$\int \frac{a + b \tan(c + dx^2)}{x} dx = \int \frac{a + b \tan(dx^2 + c)}{x} dx$$

[In] int((a + b*tan(c + d*x^2))/x,x)

[Out] int((a + b*tan(c + d*x^2))/x, x)

3.6 $\int \frac{a+b \tan(c+dx^2)}{x^2} dx$

Optimal result	64
Rubi [N/A]	64
Mathematica [N/A]	65
Maple [N/A] (verified)	65
Fricas [N/A]	65
Sympy [N/A]	65
Maxima [N/A]	66
Giac [N/A]	66
Mupad [N/A]	66

Optimal result

Integrand size = 16, antiderivative size = 16

$$\int \frac{a + b \tan(c + dx^2)}{x^2} dx = -\frac{a}{x} + b \operatorname{Int}\left(\frac{\tan(c + dx^2)}{x^2}, x\right)$$

[Out] `-a/x+b*Unintegrable(tan(d*x^2+c)/x^2,x)`

Rubi [N/A]

Not integrable

Time = 0.02 (sec) , antiderivative size = 16, normalized size of antiderivative = 1.00, number of steps used = 0, number of rules used = 0, $\frac{\text{number of rules}}{\text{integrand size}} = 0.000$, Rules used = {}

$$\int \frac{a + b \tan(c + dx^2)}{x^2} dx = \int \frac{a + b \tan(c + dx^2)}{x^2} dx$$

[In] `Int[(a + b*Tan[c + d*x^2])/x^2,x]`

[Out] `-(a/x) + b*Defer[Int][Tan[c + d*x^2]/x^2, x]`

Rubi steps

$$\begin{aligned} \text{integral} &= \int \left(\frac{a}{x^2} + \frac{b \tan(c + dx^2)}{x^2} \right) dx \\ &= -\frac{a}{x} + b \int \frac{\tan(c + dx^2)}{x^2} dx \end{aligned}$$

Mathematica [N/A]

Not integrable

Time = 1.64 (sec) , antiderivative size = 18, normalized size of antiderivative = 1.12

$$\int \frac{a + b \tan(c + dx^2)}{x^2} dx = \int \frac{a + b \tan(c + dx^2)}{x^2} dx$$

[In] Integrate[(a + b*Tan[c + d*x^2])/x^2,x]

[Out] Integrate[(a + b*Tan[c + d*x^2])/x^2, x]

Maple [N/A] (verified)

Not integrable

Time = 0.10 (sec) , antiderivative size = 16, normalized size of antiderivative = 1.00

$$\int \frac{a + b \tan(dx^2 + c)}{x^2} dx$$

[In] int((a+b*tan(d*x^2+c))/x^2,x)

[Out] int((a+b*tan(d*x^2+c))/x^2,x)

Fricas [N/A]

Not integrable

Time = 0.23 (sec) , antiderivative size = 18, normalized size of antiderivative = 1.12

$$\int \frac{a + b \tan(c + dx^2)}{x^2} dx = \int \frac{b \tan(dx^2 + c) + a}{x^2} dx$$

[In] integrate((a+b*tan(d*x^2+c))/x^2,x, algorithm="fricas")

[Out] integral((b*tan(d*x^2 + c) + a)/x^2, x)

Sympy [N/A]

Not integrable

Time = 0.38 (sec) , antiderivative size = 15, normalized size of antiderivative = 0.94

$$\int \frac{a + b \tan(c + dx^2)}{x^2} dx = \int \frac{a + b \tan(c + dx^2)}{x^2} dx$$

[In] integrate((a+b*tan(d*x**2+c))/x**2,x)

[Out] Integral((a + b*tan(c + d*x**2))/x**2, x)

Maxima [N/A]

Not integrable

Time = 0.34 (sec) , antiderivative size = 80, normalized size of antiderivative = 5.00

$$\int \frac{a + b \tan(c + dx^2)}{x^2} dx = \int \frac{b \tan(dx^2 + c) + a}{x^2} dx$$

[In] integrate((a+b*tan(d*x^2+c))/x^2,x, algorithm="maxima")

[Out] 2*b*integrate(sin(2*d*x^2 + 2*c)/(x^2*cos(2*d*x^2 + 2*c))^2 + x^2*sin(2*d*x^2 + 2*c)^2 + 2*x^2*cos(2*d*x^2 + 2*c) + x^2), x) - a/x

Giac [N/A]

Not integrable

Time = 0.37 (sec) , antiderivative size = 18, normalized size of antiderivative = 1.12

$$\int \frac{a + b \tan(c + dx^2)}{x^2} dx = \int \frac{b \tan(dx^2 + c) + a}{x^2} dx$$

[In] integrate((a+b*tan(d*x^2+c))/x^2,x, algorithm="giac")

[Out] integrate((b*tan(d*x^2 + c) + a)/x^2, x)

Mupad [N/A]

Not integrable

Time = 4.13 (sec) , antiderivative size = 18, normalized size of antiderivative = 1.12

$$\int \frac{a + b \tan(c + dx^2)}{x^2} dx = \int \frac{a + b \tan(dx^2 + c)}{x^2} dx$$

[In] int((a + b*tan(c + d*x^2))/x^2,x)

[Out] int((a + b*tan(c + d*x^2))/x^2, x)

3.7 $\int x^3(a + b \tan(c + dx^2))^2 dx$

Optimal result	67
Rubi [A] (verified)	67
Mathematica [A] (verified)	70
Maple [F]	70
Fricas [A] (verification not implemented)	70
Sympy [F]	71
Maxima [B] (verification not implemented)	71
Giac [F]	71
Mupad [F(-1)]	72

Optimal result

Integrand size = 18, antiderivative size = 126

$$\int x^3(a + b \tan(c + dx^2))^2 dx = \frac{a^2x^4}{4} + \frac{1}{2}iabx^4 - \frac{b^2x^4}{4} - \frac{abx^2 \log(1 + e^{2i(c+dx^2)})}{d} + \frac{b^2 \log(\cos(c + dx^2))}{2d^2} + \frac{iab \operatorname{PolyLog}(2, -e^{2i(c+dx^2)})}{2d^2} + \frac{b^2x^2 \tan(c + dx^2)}{2d}$$

[Out] 1/4*a^2*x^4+1/2*I*a*b*x^4-1/4*b^2*x^4-a*b*x^2*ln(1+exp(2*I*(d*x^2+c)))/d+1/2*b^2*ln(cos(d*x^2+c))/d^2+1/2*I*a*b*polylog(2,-exp(2*I*(d*x^2+c)))/d^2+1/2*b^2*x^2*tan(d*x^2+c)/d

Rubi [A] (verified)

Time = 0.27 (sec) , antiderivative size = 126, normalized size of antiderivative = 1.00, number of steps used = 10, number of rules used = 9, $\frac{\text{number of rules}}{\text{integrand size}} = 0.500$, Rules used = {3832, 3803, 3800, 2221, 2317, 2438, 3801, 3556, 30}

$$\int x^3(a + b \tan(c + dx^2))^2 dx = \frac{a^2x^4}{4} + \frac{iab \operatorname{PolyLog}(2, -e^{2i(dx^2+c)})}{2d^2} - \frac{abx^2 \log(1 + e^{2i(c+dx^2)})}{d} + \frac{1}{2}iabx^4 + \frac{b^2 \log(\cos(c + dx^2))}{2d^2} + \frac{b^2x^2 \tan(c + dx^2)}{2d} - \frac{b^2x^4}{4}$$

[In] Int[x^3*(a + b*Tan[c + d*x^2])^2,x]

[Out] $(a^2x^4)/4 + (I/2)abx^4 - (b^2x^4)/4 - (abx^2 \text{Log}[1 + E^{(2I)(c + dx^2)}])/d + (b^2 \text{Log}[\text{Cos}[c + dx^2]])/(2d^2) + ((I/2)ab \text{PolyLog}[2, -E^{(2I)(c + dx^2)}])/d^2 + (b^2x^2 \text{Tan}[c + dx^2])/(2d)$

Rule 30

$\text{Int}[(x_)^{(m_)}, x_Symbol] \rightarrow \text{Simp}[x^{(m+1)}/(m+1), x] \text{ ; FreeQ}[m, x] \ \&\& \ \text{NeQ}[m, -1]$

Rule 2221

$\text{Int}[(((F_)^{((g_)*(e_) + (f_)*(x_))})^{(n_)*((c_) + (d_)*(x_))^{(m_)})}/((a_) + (b_)*((F_)^{((g_)*(e_) + (f_)*(x_))})^{(n_)}), x_Symbol] \rightarrow \text{Simp}[\text{Log}[(c + dx)^m/(bfgn \text{Log}[F])] \text{Log}[1 + b((F^{(g(e + fx)))^n/a}], x] - \text{Dist}[d(m/(bfgn \text{Log}[F])), \text{Int}[(c + dx)^{(m-1)} \text{Log}[1 + b((F^{(g(e + fx)))^n/a}], x], x] \text{ ; FreeQ}\{F, a, b, c, d, e, f, g, n\}, x] \ \&\& \ \text{IGtQ}[m, 0]$

Rule 2317

$\text{Int}[\text{Log}[(a_) + (b_)*((F_)^{((e_)*((c_) + (d_)*(x_))})^{(n_)}], x_Symbol] \rightarrow \text{Dist}[1/(d*en \text{Log}[F]), \text{Subst}[\text{Int}[\text{Log}[a + b*x]/x, x], x, (F^{(e*(c + dx))})^n], x] \text{ ; FreeQ}\{F, a, b, c, d, e, n\}, x] \ \&\& \ \text{GtQ}[a, 0]$

Rule 2438

$\text{Int}[\text{Log}[(c_)*((d_) + (e_)*(x_)^{(n_)})]/(x_), x_Symbol] \rightarrow \text{Simp}[-\text{PolyLog}[2, (-c)*e*x^n]/n, x] \text{ ; FreeQ}\{c, d, e, n\}, x] \ \&\& \ \text{EqQ}[c*d, 1]$

Rule 3556

$\text{Int}[\text{tan}[(c_) + (d_)*(x_)], x_Symbol] \rightarrow \text{Simp}[-\text{Log}[\text{RemoveContent}[\text{Cos}[c + dx], x]]/d, x] \text{ ; FreeQ}\{c, d\}, x]$

Rule 3800

$\text{Int}[((c_) + (d_)*(x_))^{(m_)*\text{tan}[(e_) + (f_)*(x_)]}, x_Symbol] \rightarrow \text{Simp}[I*((c + dx)^{(m+1)}/(d*(m+1))), x] - \text{Dist}[2*I, \text{Int}[(c + dx)^m*(E^{(2I*(e + fx))}/(1 + E^{(2I*(e + fx))}))], x], x] \text{ ; FreeQ}\{c, d, e, f\}, x] \ \&\& \ \text{IGtQ}[m, 0]$

Rule 3801

$\text{Int}[((c_) + (d_)*(x_))^{(m_)*((b_)*\text{tan}[(e_) + (f_)*(x_)])^{(n_)}], x_Symbol] \rightarrow \text{Simp}[b*(c + dx)^m*((b*\text{Tan}[e + fx])^{(n-1)}/(f*(n-1))), x] + (-\text{Dist}[b*d*(m/(f*(n-1))), \text{Int}[(c + dx)^{(m-1)}*(b*\text{Tan}[e + fx])^{(n-1)}, x], x] - \text{Dist}[b^2, \text{Int}[(c + dx)^m*(b*\text{Tan}[e + fx])^{(n-2)}, x], x]) \text{ ; FreeQ}\{b, c, d, e, f\}, x] \ \&\& \ \text{GtQ}[n, 1] \ \&\& \ \text{GtQ}[m, 0]$

Rule 3803

```
Int[((c_.) + (d_.)*(x_))^(m_.)*((a_.) + (b_.)*tan[(e_.) + (f_.)*(x_)])^(n_.)
, x_Symbol] :> Int[ExpandIntegrand[(c + d*x)^m, (a + b*Tan[e + f*x])^n, x],
x] /; FreeQ[{a, b, c, d, e, f, m}, x] && IGtQ[m, 0] && IGtQ[n, 0]
```

Rule 3832

```
Int[(x_)^(m_.)*((a_.) + (b_.)*Tan[(c_.) + (d_.)*(x_)^(n_)])^(p_.), x_Symbol]
] :> Dist[1/n, Subst[Int[x^(Simplify[(m + 1)/n] - 1)*(a + b*Tan[c + d*x])^p
, x], x, x^n], x] /; FreeQ[{a, b, c, d, m, n, p}, x] && IGtQ[Simplify[(m +
1)/n], 0] && IntegerQ[p]
```

Rubi steps

$$\begin{aligned}
\text{integral} &= \frac{1}{2} \text{Subst} \left(\int x (a + b \tan(c + dx))^2 dx, x, x^2 \right) \\
&= \frac{1}{2} \text{Subst} \left(\int (a^2 x + 2abx \tan(c + dx) + b^2 x \tan^2(c + dx)) dx, x, x^2 \right) \\
&= \frac{a^2 x^4}{4} + (ab) \text{Subst} \left(\int x \tan(c + dx) dx, x, x^2 \right) + \frac{1}{2} b^2 \text{Subst} \left(\int x \tan^2(c + dx) dx, x, x^2 \right) \\
&= \frac{a^2 x^4}{4} + \frac{1}{2} iabx^4 + \frac{b^2 x^2 \tan(c + dx^2)}{2d} - (2iab) \text{Subst} \left(\int \frac{e^{2i(c+dx)} x}{1 + e^{2i(c+dx)}} dx, x, x^2 \right) \\
&\quad - \frac{1}{2} b^2 \text{Subst} \left(\int x dx, x, x^2 \right) - \frac{b^2 \text{Subst}(\int \tan(c + dx) dx, x, x^2)}{2d} \\
&= \frac{a^2 x^4}{4} + \frac{1}{2} iabx^4 - \frac{b^2 x^4}{4} - \frac{abx^2 \log(1 + e^{2i(c+dx^2)})}{d} + \frac{b^2 \log(\cos(c + dx^2))}{2d^2} \\
&\quad + \frac{b^2 x^2 \tan(c + dx^2)}{2d} + \frac{(ab) \text{Subst}(\int \log(1 + e^{2i(c+dx)}) dx, x, x^2)}{d} \\
&= \frac{a^2 x^4}{4} + \frac{1}{2} iabx^4 - \frac{b^2 x^4}{4} - \frac{abx^2 \log(1 + e^{2i(c+dx^2)})}{d} + \frac{b^2 \log(\cos(c + dx^2))}{2d^2} \\
&\quad + \frac{b^2 x^2 \tan(c + dx^2)}{2d} - \frac{(iab) \text{Subst}(\int \frac{\log(1+x)}{x} dx, x, e^{2i(c+dx^2)})}{2d^2} \\
&= \frac{a^2 x^4}{4} + \frac{1}{2} iabx^4 - \frac{b^2 x^4}{4} - \frac{abx^2 \log(1 + e^{2i(c+dx^2)})}{d} + \frac{b^2 \log(\cos(c + dx^2))}{2d^2} \\
&\quad + \frac{iab \text{PolyLog}(2, -e^{2i(c+dx^2)})}{2d^2} + \frac{b^2 x^2 \tan(c + dx^2)}{2d}
\end{aligned}$$

Mathematica [A] (verified)

Time = 5.23 (sec) , antiderivative size = 236, normalized size of antiderivative = 1.87

$$\int x^3 (a + b \tan(c + dx^2))^2 dx$$

$$= \frac{\sec(c) \left(-2ab \cos(c) \left(idx^2(\pi + 2 \arctan(\cot(c))) + \pi \log \left(1 + e^{-2idx^2} \right) + 2(dx^2 - \arctan(\cot(c))) \log \left(1 - e^{-2idx^2} \right) \right) \right)}{4d^2}$$

[In] Integrate[x^3*(a + b*Tan[c + d*x^2])^2,x]

[Out] (Sec[c]*(-2*a*b*Cos[c]*(I*d*x^2*(Pi + 2*ArcTan[Cot[c]]) + Pi*Log[1 + E^((-2*I)*d*x^2)] + 2*(d*x^2 - ArcTan[Cot[c]])*Log[1 - E^((2*I)*(d*x^2 - ArcTan[Cot[c]])]) - Pi*Log[Cos[d*x^2]] + 2*ArcTan[Cot[c]]*Log[Sin[d*x^2 - ArcTan[Cot[c]]]]) - I*PolyLog[2, E^((2*I)*(d*x^2 - ArcTan[Cot[c]])]) - (2*a*b*d^2*x^4*sqrt[Csc[c]^2]*Sin[c])/E^(I*ArcTan[Cot[c]]) + d^2*x^4*((a^2 - b^2)*Cos[c] + 2*a*b*Sin[c]) + 2*b^2*(Cos[c]*Log[Cos[c + d*x^2]] + d*x^2*Sin[c]) + 2*b^2*d*x^2*Sec[c + d*x^2]*Sin[d*x^2]))/(4*d^2)

Maple [F]

$$\int x^3 (a + b \tan(dx^2 + c))^2 dx$$

[In] int(x^3*(a+b*tan(d*x^2+c))^2,x)

[Out] int(x^3*(a+b*tan(d*x^2+c))^2,x)

Fricas [A] (verification not implemented)

none

Time = 0.25 (sec) , antiderivative size = 199, normalized size of antiderivative = 1.58

$$\int x^3 (a + b \tan(c + dx^2))^2 dx$$

$$= \frac{(a^2 - b^2)d^2x^4 + 2b^2dx^2 \tan(dx^2 + c) - i abLi_2\left(\frac{2(i \tan(dx^2+c)-1)}{\tan(dx^2+c)^2+1} + 1\right) + i abLi_2\left(\frac{2(-i \tan(dx^2+c)-1)}{\tan(dx^2+c)^2+1} + 1\right) - (2i ab \tan(dx^2+c) \log\left(\frac{2(i \tan(dx^2+c)-1)}{\tan(dx^2+c)^2+1} + 1\right) - 2i ab \tan(dx^2+c) \log\left(\frac{2(-i \tan(dx^2+c)-1)}{\tan(dx^2+c)^2+1} + 1\right))}{4d^2}$$

[In] integrate(x^3*(a+b*tan(d*x^2+c))^2,x, algorithm="fricas")

[Out] 1/4*((a^2 - b^2)*d^2*x^4 + 2*b^2*d*x^2*tan(d*x^2 + c) - I*a*b*dilog(2*(I*tan(d*x^2 + c) - 1)/(tan(d*x^2 + c)^2 + 1) + 1) + I*a*b*dilog(2*(-I*tan(d*x^2 + c) - 1)/(tan(d*x^2 + c)^2 + 1) + 1) - (2*a*b*d*x^2 - b^2)*log(-2*(I*tan(d*x^2 + c) - 1)/(tan(d*x^2 + c)^2 + 1)) - (2*a*b*d*x^2 - b^2)*log(-2*(-I*tan(d*x^2 + c) - 1)/(tan(d*x^2 + c)^2 + 1)))/d^2

Sympy [F]

$$\int x^3(a + b \tan(c + dx^2))^2 dx = \int x^3(a + b \tan(c + dx^2))^2 dx$$

```
[In] integrate(x**3*(a+b*tan(d*x**2+c))**2,x)
```

```
[Out] Integral(x**3*(a + b*tan(c + d*x**2))**2, x)
```

Maxima [B] (verification not implemented)

Both result and optimal contain complex but leaf count of result is larger than twice the leaf count of optimal. 398 vs. 2(105) = 210.

Time = 0.35 (sec) , antiderivative size = 398, normalized size of antiderivative = 3.16

$$\int x^3(a + b \tan(c + dx^2))^2 dx = \frac{1}{4} a^2 x^4 + \frac{(2ab + i b^2) d^2 x^4 - 2(2abdx^2 - b^2 + (2abdx^2 - b^2) \cos(2dx^2 + 2c) - (-2i abdx^2 + i b^2) \sin(2dx^2 + 2c))}{4}$$

```
[In] integrate(x^3*(a+b*tan(d*x^2+c))^2,x, algorithm="maxima")
```

```
[Out] 1/4*a^2*x^4 + ((2*a*b + I*b^2)*d^2*x^4 - 2*(2*a*b*d*x^2 - b^2 + (2*a*b*d*x^2 - b^2)*cos(2*d*x^2 + 2*c) - (-2*I*a*b*d*x^2 + I*b^2)*sin(2*d*x^2 + 2*c))*arctan2(sin(2*d*x^2 + 2*c), cos(2*d*x^2 + 2*c) + 1) + ((2*a*b + I*b^2)*d^2*x^4 - 4*b^2*d*x^2)*cos(2*d*x^2 + 2*c) + 2*(a*b*cos(2*d*x^2 + 2*c) + I*a*b*sin(2*d*x^2 + 2*c) + a*b)*dilog(-e^(2*I*d*x^2 + 2*I*c)) - (-2*I*a*b*d*x^2 + I*b^2 + (-2*I*a*b*d*x^2 + I*b^2)*cos(2*d*x^2 + 2*c) + (2*a*b*d*x^2 - b^2)*sin(2*d*x^2 + 2*c))*log(cos(2*d*x^2 + 2*c)^2 + sin(2*d*x^2 + 2*c)^2 + 2*cos(2*d*x^2 + 2*c) + 1) - ((-2*I*a*b + b^2)*d^2*x^4 + 4*I*b^2*d*x^2)*sin(2*d*x^2 + 2*c))/(-4*I*d^2*cos(2*d*x^2 + 2*c) + 4*d^2*sin(2*d*x^2 + 2*c) - 4*I*d^2)
```

Giac [F]

$$\int x^3(a + b \tan(c + dx^2))^2 dx = \int (b \tan(dx^2 + c) + a)^2 x^3 dx$$

```
[In] integrate(x^3*(a+b*tan(d*x^2+c))^2,x, algorithm="giac")
```

```
[Out] integrate((b*tan(d*x^2 + c) + a)^2*x^3, x)
```

Mupad [F(-1)]

Timed out.

$$\int x^3 (a + b \tan(c + dx^2))^2 dx = \int x^3 (a + b \tan(dx^2 + c))^2 dx$$

```
[In] int(x^3*(a + b*tan(c + d*x^2))^2,x)
```

```
[Out] int(x^3*(a + b*tan(c + d*x^2))^2, x)
```


3.8 $\int x^2(a + b \tan(c + dx^2))^2 dx$

Optimal result	73
Rubi [N/A]	73
Mathematica [N/A]	74
Maple [N/A] (verified)	74
Fricas [N/A]	74
Sympy [N/A]	74
Maxima [N/A]	75
Giac [N/A]	75
Mupad [N/A]	75

Optimal result

Integrand size = 18, antiderivative size = 18

$$\int x^2(a + b \tan(c + dx^2))^2 dx = \text{Int}\left(x^2(a + b \tan(c + dx^2))^2, x\right)$$

[Out] Unintegrable(x^2*(a+b*tan(d*x^2+c))^2,x)

Rubi [N/A]

Not integrable

Time = 0.03 (sec) , antiderivative size = 18, normalized size of antiderivative = 1.00, number of steps used = 0, number of rules used = 0, $\frac{\text{number of rules}}{\text{integrand size}} = 0.000$, Rules used = {}

$$\int x^2(a + b \tan(c + dx^2))^2 dx = \int x^2(a + b \tan(c + dx^2))^2 dx$$

[In] Int[x^2*(a + b*Tan[c + d*x^2])^2,x]

[Out] Defer[Int][x^2*(a + b*Tan[c + d*x^2])^2, x]

Rubi steps

$$\text{integral} = \int x^2(a + b \tan(c + dx^2))^2 dx$$

Mathematica [N/A]

Not integrable

Time = 5.44 (sec) , antiderivative size = 20, normalized size of antiderivative = 1.11

$$\int x^2(a + b \tan(c + dx^2))^2 dx = \int x^2(a + b \tan(c + dx^2))^2 dx$$

[In] Integrate[x^2*(a + b*Tan[c + d*x^2])^2,x]

[Out] Integrate[x^2*(a + b*Tan[c + d*x^2])^2, x]

Maple [N/A] (verified)

Not integrable

Time = 0.17 (sec) , antiderivative size = 18, normalized size of antiderivative = 1.00

$$\int x^2(a + b \tan(dx^2 + c))^2 dx$$

[In] int(x^2*(a+b*tan(d*x^2+c))^2,x)

[Out] int(x^2*(a+b*tan(d*x^2+c))^2,x)

Fricas [N/A]

Not integrable

Time = 0.24 (sec) , antiderivative size = 42, normalized size of antiderivative = 2.33

$$\int x^2(a + b \tan(c + dx^2))^2 dx = \int (b \tan(dx^2 + c) + a)^2 x^2 dx$$

[In] integrate(x^2*(a+b*tan(d*x^2+c))^2,x, algorithm="fricas")

[Out] integral(b^2*x^2*tan(d*x^2 + c)^2 + 2*a*b*x^2*tan(d*x^2 + c) + a^2*x^2, x)

Sympy [N/A]

Not integrable

Time = 0.81 (sec) , antiderivative size = 17, normalized size of antiderivative = 0.94

$$\int x^2(a + b \tan(c + dx^2))^2 dx = \int x^2(a + b \tan(c + dx^2))^2 dx$$

[In] integrate(x**2*(a+b*tan(d*x**2+c))**2,x)

[Out] Integral(x**2*(a + b*tan(c + d*x**2))**2, x)

Maxima [N/A]

Not integrable

Time = 0.38 (sec) , antiderivative size = 271, normalized size of antiderivative = 15.06

$$\int x^2 (a + b \tan(c + dx^2))^2 dx = \int (b \tan(dx^2 + c) + a)^2 x^2 dx$$

[In] integrate(x^2*(a+b*tan(d*x^2+c))^2,x, algorithm="maxima")

```
[Out] 1/3*a^2*x^3 - 1/3*(b^2*d*x^3*cos(2*d*x^2 + 2*c)^2 + b^2*d*x^3*sin(2*d*x^2 +
2*c)^2 + 2*b^2*d*x^3*cos(2*d*x^2 + 2*c) + b^2*d*x^3 - 3*b^2*x*sin(2*d*x^2
+ 2*c) - 3*(d*cos(2*d*x^2 + 2*c)^2 + d*sin(2*d*x^2 + 2*c)^2 + 2*d*cos(2*d*x
^2 + 2*c) + d)*integrate((4*a*b*d*x^2 - b^2)*sin(2*d*x^2 + 2*c)/(d*cos(2*d*
x^2 + 2*c)^2 + d*sin(2*d*x^2 + 2*c)^2 + 2*d*cos(2*d*x^2 + 2*c) + d), x)/(d
*cos(2*d*x^2 + 2*c)^2 + d*sin(2*d*x^2 + 2*c)^2 + 2*d*cos(2*d*x^2 + 2*c) + d
)
```

Giac [N/A]

Not integrable

Time = 0.59 (sec) , antiderivative size = 20, normalized size of antiderivative = 1.11

$$\int x^2 (a + b \tan(c + dx^2))^2 dx = \int (b \tan(dx^2 + c) + a)^2 x^2 dx$$

[In] integrate(x^2*(a+b*tan(d*x^2+c))^2,x, algorithm="giac")

[Out] integrate((b*tan(d*x^2 + c) + a)^2*x^2, x)

Mupad [N/A]

Not integrable

Time = 3.61 (sec) , antiderivative size = 20, normalized size of antiderivative = 1.11

$$\int x^2 (a + b \tan(c + dx^2))^2 dx = \int x^2 (a + b \tan(dx^2 + c))^2 dx$$

[In] int(x^2*(a + b*tan(c + d*x^2))^2,x)

[Out] int(x^2*(a + b*tan(c + d*x^2))^2, x)

3.9 $\int x(a + b \tan(c + dx^2))^2 dx$

Optimal result	76
Rubi [A] (verified)	76
Mathematica [C] (verified)	77
Maple [A] (verified)	77
Fricas [A] (verification not implemented)	78
Sympy [A] (verification not implemented)	78
Maxima [B] (verification not implemented)	79
Giac [A] (verification not implemented)	79
Mupad [B] (verification not implemented)	79

Optimal result

Integrand size = 16, antiderivative size = 51

$$\int x(a + b \tan(c + dx^2))^2 dx = \frac{1}{2}(a^2 - b^2)x^2 - \frac{ab \log(\cos(c + dx^2))}{d} + \frac{b^2 \tan(c + dx^2)}{2d}$$

[Out] 1/2*(a^2-b^2)*x^2-a*b*ln(cos(d*x^2+c))/d+1/2*b^2*tan(d*x^2+c)/d

Rubi [A] (verified)

Time = 0.06 (sec) , antiderivative size = 51, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 3, $\frac{\text{number of rules}}{\text{integrand size}} = 0.188$, Rules used = {3832, 3558, 3556}

$$\int x(a + b \tan(c + dx^2))^2 dx = \frac{1}{2}x^2(a^2 - b^2) - \frac{ab \log(\cos(c + dx^2))}{d} + \frac{b^2 \tan(c + dx^2)}{2d}$$

[In] Int[x*(a + b*Tan[c + d*x^2])^2,x]

[Out] ((a^2 - b^2)*x^2)/2 - (a*b*Log[Cos[c + d*x^2]])/d + (b^2*Tan[c + d*x^2])/(2*d)

Rule 3556

Int[tan[(c_.) + (d_.)*(x_)], x_Symbol] := Simp[-Log[RemoveContent[Cos[c + d*x], x]]/d, x] /; FreeQ[{c, d}, x]

Rule 3558

Int[((a_) + (b_.)*tan[(c_.) + (d_.)*(x_)])^2, x_Symbol] := Simp[(a^2 - b^2)*x, x] + (Dist[2*a*b, Int[Tan[c + d*x], x], x] + Simp[b^2*(Tan[c + d*x]/d),

x]) /; FreeQ[{a, b, c, d}, x]

Rule 3832

```
Int[(x_)^(m_.)*((a_.) + (b_.)*Tan[(c_.) + (d_.)*(x_)^(n_)])^(p_.), x_Symbol]
  :-> Dist[1/n, Subst[Int[x^(Simplify[(m + 1)/n] - 1)*(a + b*Tan[c + d*x])^p,
    x], x, x^n], x] /; FreeQ[{a, b, c, d, m, n, p}, x] && IGtQ[Simplify[(m +
  1)/n], 0] && IntegerQ[p]
```

Rubi steps

$$\begin{aligned} \text{integral} &= \frac{1}{2} \text{Subst} \left(\int (a + b \tan(c + dx))^2 dx, x, x^2 \right) \\ &= \frac{1}{2} (a^2 - b^2) x^2 + \frac{b^2 \tan(c + dx^2)}{2d} + (ab) \text{Subst} \left(\int \tan(c + dx) dx, x, x^2 \right) \\ &= \frac{1}{2} (a^2 - b^2) x^2 - \frac{ab \log(\cos(c + dx^2))}{d} + \frac{b^2 \tan(c + dx^2)}{2d} \end{aligned}$$

Mathematica [C] (verified)

Result contains complex when optimal does not.

Time = 0.23 (sec) , antiderivative size = 75, normalized size of antiderivative = 1.47

$$\begin{aligned} &\int x (a + b \tan(c + dx^2))^2 dx \\ &= \frac{-i((a + ib)^2 \log(i - \tan(c + dx^2)) - (a - ib)^2 \log(i + \tan(c + dx^2))) + 2b^2 \tan(c + dx^2)}{4d} \end{aligned}$$

[In] Integrate[x*(a + b*Tan[c + d*x^2])^2,x]

[Out] ((-I)*((a + I*b)^2*Log[I - Tan[c + d*x^2]] - (a - I*b)^2*Log[I + Tan[c + d*x^2]]) + 2*b^2*Tan[c + d*x^2])/(4*d)

Maple [A] (verified)

Time = 0.10 (sec) , antiderivative size = 52, normalized size of antiderivative = 1.02

method	result	size
parallelrisch	$\frac{a^2 dx^2 - b^2 dx^2 + ab \ln(1 + \tan^2(dx^2 + c)) + b^2 \tan(dx^2 + c)}{2d}$	52
norman	$\left(\frac{a^2}{2} - \frac{b^2}{2}\right) x^2 + \frac{b^2 \tan(dx^2 + c)}{2d} + \frac{ab \ln(1 + \tan^2(dx^2 + c))}{2d}$	53
derivativdivides	$\frac{b^2 \tan(dx^2 + c) + ab \ln(1 + \tan^2(dx^2 + c)) + (a^2 - b^2) \arctan(\tan(dx^2 + c))}{2d}$	54
default	$\frac{b^2 \tan(dx^2 + c) + ab \ln(1 + \tan^2(dx^2 + c)) + (a^2 - b^2) \arctan(\tan(dx^2 + c))}{2d}$	54
parts	$\frac{a^2 x^2}{2} + \frac{b^2 (\tan(dx^2 + c) - \arctan(\tan(dx^2 + c)))}{2d} - \frac{ab \ln(\cos(dx^2 + c))}{d}$	54
risch	$iab x^2 + \frac{a^2 x^2}{2} - \frac{x^2 b^2}{2} + \frac{2iabc}{d} + \frac{ib^2}{d(1 + e^{2i(dx^2 + c)})} - \frac{ab \ln(1 + e^{2i(dx^2 + c)})}{d}$	80

[In] `int(x*(a+b*tan(d*x^2+c))^2,x,method=_RETURNVERBOSE)`

[Out] $1/2*(a^2*d*x^2-b^2*d*x^2+a*b*\ln(1+\tan(d*x^2+c)^2)+b^2*\tan(d*x^2+c))/d$

Fricas [A] (verification not implemented)

none

Time = 0.25 (sec) , antiderivative size = 51, normalized size of antiderivative = 1.00

$$\int x(a + b \tan(c + dx^2))^2 dx = \frac{(a^2 - b^2)dx^2 - ab \log\left(\frac{1}{\tan(dx^2 + c)^2 + 1}\right) + b^2 \tan(dx^2 + c)}{2d}$$

[In] `integrate(x*(a+b*tan(d*x^2+c))^2,x, algorithm="fricas")`

[Out] $1/2*((a^2 - b^2)*d*x^2 - a*b*\log(1/(\tan(d*x^2 + c)^2 + 1)) + b^2*\tan(d*x^2 + c))/d$

Sympy [A] (verification not implemented)

Time = 0.10 (sec) , antiderivative size = 65, normalized size of antiderivative = 1.27

$$\int x(a + b \tan(c + dx^2))^2 dx = \begin{cases} \frac{a^2 x^2}{2} + \frac{ab \log(\tan^2(c + dx^2) + 1)}{2d} - \frac{b^2 x^2}{2} + \frac{b^2 \tan(c + dx^2)}{2d} & \text{for } d \neq 0 \\ \frac{x^2(a + b \tan(c))^2}{2} & \text{otherwise} \end{cases}$$

[In] `integrate(x*(a+b*tan(d*x**2+c))**2,x)`

[Out] `Piecewise((a**2*x**2/2 + a*b*log(tan(c + d*x**2)**2 + 1)/(2*d) - b**2*x**2/2 + b**2*tan(c + d*x**2)/(2*d), Ne(d, 0)), (x**2*(a + b*tan(c))**2/2, True))`

Maxima [B] (verification not implemented)

Leaf count of result is larger than twice the leaf count of optimal. 149 vs. $2(47) = 94$.

Time = 0.24 (sec) , antiderivative size = 149, normalized size of antiderivative = 2.92

$$\int x(a + b \tan(c + dx^2))^2 dx = \frac{1}{2} a^2 x^2 - \frac{\left(dx^2 \cos(2dx^2 + 2c)^2 + dx^2 \sin(2dx^2 + 2c)^2 + 2dx^2 \cos(2dx^2 + 2c) + dx^2 - 2 \sin(2dx^2 + 2c)\right) b^2}{2(d \cos(2dx^2 + 2c)^2 + d \sin(2dx^2 + 2c)^2 + 2d \cos(2dx^2 + 2c) + d)} + \frac{ab \log(\sec(dx^2 + c))}{d}$$

[In] integrate(x*(a+b*tan(d*x^2+c))^2,x, algorithm="maxima")

[Out] $\frac{1}{2} a^2 x^2 - \frac{1}{2} (d x^2 \cos(2 d x^2 + 2 c))^2 + d x^2 \sin(2 d x^2 + 2 c)^2 + 2 d x^2 \cos(2 d x^2 + 2 c) + d x^2 - 2 \sin(2 d x^2 + 2 c) b^2}{(d \cos(2 d x^2 + 2 c))^2 + d \sin(2 d x^2 + 2 c)^2 + 2 d \cos(2 d x^2 + 2 c) + d} + a b \log(\sec(d x^2 + c)) / d$

Giac [A] (verification not implemented)

none

Time = 0.34 (sec) , antiderivative size = 53, normalized size of antiderivative = 1.04

$$\int x(a + b \tan(c + dx^2))^2 dx = \frac{(dx^2 + c)a^2 - (dx^2 + c - \tan(dx^2 + c))b^2 - 2ab \log(|\cos(dx^2 + c)|)}{2d}$$

[In] integrate(x*(a+b*tan(d*x^2+c))^2,x, algorithm="giac")

[Out] $\frac{1}{2} ((d x^2 + c) a^2 - (d x^2 + c - \tan(d x^2 + c)) b^2 - 2 a b \log(\text{abs}(\cos(d x^2 + c)))) / d$

Mupad [B] (verification not implemented)

Time = 4.07 (sec) , antiderivative size = 52, normalized size of antiderivative = 1.02

$$\int x(a + b \tan(c + dx^2))^2 dx = x^2 \left(\frac{a^2}{2} - \frac{b^2}{2} \right) + \frac{b^2 \tan(dx^2 + c)}{2d} + \frac{ab \ln(\tan(dx^2 + c)^2 + 1)}{2d}$$

[In] int(x*(a + b*tan(c + d*x^2))^2,x)

[Out] $x^2 (a^2/2 - b^2/2) + (b^2 \tan(c + d x^2)) / (2 d) + (a b \log(\tan(c + d x^2)^2 + 1)) / (2 d)$

3.10 $\int (a + b \tan(c + dx^2))^2 dx$

Optimal result	80
Rubi [N/A]	80
Mathematica [N/A]	81
Maple [N/A] (verified)	81
Fricas [N/A]	81
Sympy [N/A]	81
Maxima [N/A]	82
Giac [N/A]	82
Mupad [N/A]	82

Optimal result

Integrand size = 14, antiderivative size = 14

$$\int (a + b \tan(c + dx^2))^2 dx = \text{Int}\left((a + b \tan(c + dx^2))^2, x\right)$$

[Out] Unintegrable((a+b*tan(d*x^2+c))^2,x)

Rubi [N/A]

Not integrable

Time = 0.01 (sec) , antiderivative size = 14, normalized size of antiderivative = 1.00, number of steps used = 0, number of rules used = 0, $\frac{\text{number of rules}}{\text{integrand size}} = 0.000$, Rules used = {}

$$\int (a + b \tan(c + dx^2))^2 dx = \int (a + b \tan(c + dx^2))^2 dx$$

[In] Int[(a + b*Tan[c + d*x^2])^2,x]

[Out] Defer[Int] [(a + b*Tan[c + d*x^2])^2, x]

Rubi steps

$$\text{integral} = \int (a + b \tan(c + dx^2))^2 dx$$

Mathematica [N/A]

Not integrable

Time = 1.89 (sec) , antiderivative size = 16, normalized size of antiderivative = 1.14

$$\int (a + b \tan (c + dx^2))^2 dx = \int (a + b \tan (c + dx^2))^2 dx$$

[In] Integrate[(a + b*Tan[c + d*x^2])^2,x]

[Out] Integrate[(a + b*Tan[c + d*x^2])^2, x]

Maple [N/A] (verified)

Not integrable

Time = 0.16 (sec) , antiderivative size = 14, normalized size of antiderivative = 1.00

$$\int (a + b \tan (dx^2 + c))^2 dx$$

[In] int((a+b*tan(d*x^2+c))^2,x)

[Out] int((a+b*tan(d*x^2+c))^2,x)

Fricas [N/A]

Not integrable

Time = 0.24 (sec) , antiderivative size = 32, normalized size of antiderivative = 2.29

$$\int (a + b \tan (c + dx^2))^2 dx = \int (b \tan (dx^2 + c) + a)^2 dx$$

[In] integrate((a+b*tan(d*x^2+c))^2,x, algorithm="fricas")

[Out] integral(b^2*tan(d*x^2 + c)^2 + 2*a*b*tan(d*x^2 + c) + a^2, x)

Sympy [N/A]

Not integrable

Time = 0.57 (sec) , antiderivative size = 14, normalized size of antiderivative = 1.00

$$\int (a + b \tan (c + dx^2))^2 dx = \int (a + b \tan (c + dx^2))^2 dx$$

[In] integrate((a+b*tan(d*x**2+c))**2,x)

[Out] Integral((a + b*tan(c + d*x**2))**2, x)

Maxima [N/A]

Not integrable

Time = 0.35 (sec) , antiderivative size = 288, normalized size of antiderivative = 20.57

$$\int (a + b \tan (c + dx^2))^2 dx = \int (b \tan (dx^2 + c) + a)^2 dx$$

[In] integrate((a+b*tan(d*x^2+c))^2,x, algorithm="maxima")

```
[Out] a^2*x - (b^2*d*x^2*cos(2*d*x^2 + 2*c)^2 + b^2*d*x^2*sin(2*d*x^2 + 2*c)^2 +
2*b^2*d*x^2*cos(2*d*x^2 + 2*c) + b^2*d*x^2 - b^2*sin(2*d*x^2 + 2*c) - (d*x*
cos(2*d*x^2 + 2*c)^2 + d*x*sin(2*d*x^2 + 2*c)^2 + 2*d*x*cos(2*d*x^2 + 2*c)
+ d*x)*integrate((4*a*b*d*x^2 + b^2)*sin(2*d*x^2 + 2*c)/(d*x^2*cos(2*d*x^2
+ 2*c)^2 + d*x^2*sin(2*d*x^2 + 2*c)^2 + 2*d*x^2*cos(2*d*x^2 + 2*c) + d*x^2)
, x))/(d*x*cos(2*d*x^2 + 2*c)^2 + d*x*sin(2*d*x^2 + 2*c)^2 + 2*d*x*cos(2*d*
x^2 + 2*c) + d*x)
```

Giac [N/A]

Not integrable

Time = 0.50 (sec) , antiderivative size = 16, normalized size of antiderivative = 1.14

$$\int (a + b \tan (c + dx^2))^2 dx = \int (b \tan (dx^2 + c) + a)^2 dx$$

[In] integrate((a+b*tan(d*x^2+c))^2,x, algorithm="giac")

[Out] integrate((b*tan(d*x^2 + c) + a)^2, x)

Mupad [N/A]

Not integrable

Time = 3.73 (sec) , antiderivative size = 16, normalized size of antiderivative = 1.14

$$\int (a + b \tan (c + dx^2))^2 dx = \int (a + b \tan (dx^2 + c))^2 dx$$

[In] int((a + b*tan(c + d*x^2))^2,x)

[Out] int((a + b*tan(c + d*x^2))^2, x)

3.11

$$\int \frac{(a+b \tan(c+dx^2))^2}{x} dx$$

Optimal result	83
Rubi [N/A]	83
Mathematica [N/A]	84
Maple [N/A] (verified)	84
Fricas [N/A]	84
Sympy [N/A]	84
Maxima [N/A]	85
Giac [N/A]	85
Mupad [N/A]	85

Optimal result

Integrand size = 18, antiderivative size = 18

$$\int \frac{(a+b \tan(c+dx^2))^2}{x} dx = \text{Int}\left(\frac{(a+b \tan(c+dx^2))^2}{x}, x\right)$$

[Out] Unintegrable((a+b*tan(d*x^2+c))^2/x,x)

Rubi [N/A]

Not integrable

Time = 0.02 (sec) , antiderivative size = 18, normalized size of antiderivative = 1.00, number of steps used = 0, number of rules used = 0, $\frac{\text{number of rules}}{\text{integrand size}} = 0.000$, Rules used = {}

$$\int \frac{(a+b \tan(c+dx^2))^2}{x} dx = \int \frac{(a+b \tan(c+dx^2))^2}{x} dx$$

[In] Int[(a + b*Tan[c + d*x^2])^2/x,x]

[Out] Defer[Int] [(a + b*Tan[c + d*x^2])^2/x, x]

Rubi steps

$$\text{integral} = \int \frac{(a+b \tan(c+dx^2))^2}{x} dx$$

Mathematica [N/A]

Not integrable

Time = 11.51 (sec) , antiderivative size = 20, normalized size of antiderivative = 1.11

$$\int \frac{(a + b \tan(c + dx^2))^2}{x} dx = \int \frac{(a + b \tan(c + dx^2))^2}{x} dx$$

[In] Integrate[(a + b*Tan[c + d*x^2])^2/x,x]

[Out] Integrate[(a + b*Tan[c + d*x^2])^2/x, x]

Maple [N/A] (verified)

Not integrable

Time = 0.17 (sec) , antiderivative size = 18, normalized size of antiderivative = 1.00

$$\int \frac{(a + b \tan(dx^2 + c))^2}{x} dx$$

[In] int((a+b*tan(d*x^2+c))^2/x,x)

[Out] int((a+b*tan(d*x^2+c))^2/x,x)

Fricas [N/A]

Not integrable

Time = 0.24 (sec) , antiderivative size = 36, normalized size of antiderivative = 2.00

$$\int \frac{(a + b \tan(c + dx^2))^2}{x} dx = \int \frac{(b \tan(dx^2 + c) + a)^2}{x} dx$$

[In] integrate((a+b*tan(d*x^2+c))^2/x,x, algorithm="fricas")

[Out] integral((b^2*tan(d*x^2 + c)^2 + 2*a*b*tan(d*x^2 + c) + a^2)/x, x)

Sympy [N/A]

Not integrable

Time = 2.14 (sec) , antiderivative size = 15, normalized size of antiderivative = 0.83

$$\int \frac{(a + b \tan(c + dx^2))^2}{x} dx = \int \frac{(a + b \tan(c + dx^2))^2}{x} dx$$

[In] integrate((a+b*tan(d*x**2+c))**2/x,x)

[Out] Integral((a + b*tan(c + d*x**2))**2/x, x)

Maxima [N/A]

Not integrable

Time = 0.42 (sec) , antiderivative size = 314, normalized size of antiderivative = 17.44

$$\int \frac{(a + b \tan(c + dx^2))^2}{x} dx = \int \frac{(b \tan(dx^2 + c) + a)^2}{x} dx$$

[In] integrate((a+b*tan(d*x^2+c))^2/x,x, algorithm="maxima")

```
[Out] a^2*log(x) - (b^2*d*x^2*cos(2*d*x^2 + 2*c)^2*log(x) + b^2*d*x^2*log(x)*sin(
2*d*x^2 + 2*c)^2 + 2*b^2*d*x^2*cos(2*d*x^2 + 2*c)*log(x) + b^2*d*x^2*log(x)
- b^2*sin(2*d*x^2 + 2*c) - (d*x^2*cos(2*d*x^2 + 2*c)^2 + d*x^2*sin(2*d*x^2
+ 2*c)^2 + 2*d*x^2*cos(2*d*x^2 + 2*c) + d*x^2)*integrate(2*(2*a*b*d*x^2 +
b^2)*sin(2*d*x^2 + 2*c)/(d*x^3*cos(2*d*x^2 + 2*c)^2 + d*x^3*sin(2*d*x^2 + 2
*c)^2 + 2*d*x^3*cos(2*d*x^2 + 2*c) + d*x^3), x))/(d*x^2*cos(2*d*x^2 + 2*c)^
2 + d*x^2*sin(2*d*x^2 + 2*c)^2 + 2*d*x^2*cos(2*d*x^2 + 2*c) + d*x^2)
```

Giac [N/A]

Not integrable

Time = 0.39 (sec) , antiderivative size = 20, normalized size of antiderivative = 1.11

$$\int \frac{(a + b \tan(c + dx^2))^2}{x} dx = \int \frac{(b \tan(dx^2 + c) + a)^2}{x} dx$$

[In] integrate((a+b*tan(d*x^2+c))^2/x,x, algorithm="giac")

[Out] integrate((b*tan(d*x^2 + c) + a)^2/x, x)

Mupad [N/A]

Not integrable

Time = 5.04 (sec) , antiderivative size = 20, normalized size of antiderivative = 1.11

$$\int \frac{(a + b \tan(c + dx^2))^2}{x} dx = \int \frac{(a + b \tan(dx^2 + c))^2}{x} dx$$

[In] int((a + b*tan(c + d*x^2))^2/x,x)

[Out] int((a + b*tan(c + d*x^2))^2/x, x)

3.12 $\int \frac{(a+b \tan(c+dx^2))^2}{x^2} dx$

Optimal result	86
Rubi [N/A]	86
Mathematica [N/A]	87
Maple [N/A] (verified)	87
Fricas [N/A]	87
Sympy [N/A]	87
Maxima [N/A]	88
Giac [N/A]	88
Mupad [N/A]	88

Optimal result

Integrand size = 18, antiderivative size = 18

$$\int \frac{(a + b \tan(c + dx^2))^2}{x^2} dx = \text{Int}\left(\frac{(a + b \tan(c + dx^2))^2}{x^2}, x\right)$$

[Out] Unintegrable((a+b*tan(d*x^2+c))^2/x^2,x)

Rubi [N/A]

Not integrable

Time = 0.03 (sec) , antiderivative size = 18, normalized size of antiderivative = 1.00, number of steps used = 0, number of rules used = 0, $\frac{\text{number of rules}}{\text{integrand size}} = 0.000$, Rules used = {}

$$\int \frac{(a + b \tan(c + dx^2))^2}{x^2} dx = \int \frac{(a + b \tan(c + dx^2))^2}{x^2} dx$$

[In] Int[(a + b*Tan[c + d*x^2])^2/x^2,x]

[Out] Defer[Int][(a + b*Tan[c + d*x^2])^2/x^2, x]

Rubi steps

$$\text{integral} = \int \frac{(a + b \tan(c + dx^2))^2}{x^2} dx$$

Mathematica [N/A]

Not integrable

Time = 4.97 (sec) , antiderivative size = 20, normalized size of antiderivative = 1.11

$$\int \frac{(a + b \tan(c + dx^2))^2}{x^2} dx = \int \frac{(a + b \tan(c + dx^2))^2}{x^2} dx$$

`[In] Integrate[(a + b*Tan[c + d*x^2])^2/x^2,x]``[Out] Integrate[(a + b*Tan[c + d*x^2])^2/x^2, x]`**Maple [N/A] (verified)**

Not integrable

Time = 0.21 (sec) , antiderivative size = 18, normalized size of antiderivative = 1.00

$$\int \frac{(a + b \tan(dx^2 + c))^2}{x^2} dx$$

`[In] int((a+b*tan(d*x^2+c))^2/x^2,x)``[Out] int((a+b*tan(d*x^2+c))^2/x^2,x)`**Fricas [N/A]**

Not integrable

Time = 0.24 (sec) , antiderivative size = 36, normalized size of antiderivative = 2.00

$$\int \frac{(a + b \tan(c + dx^2))^2}{x^2} dx = \int \frac{(b \tan(dx^2 + c) + a)^2}{x^2} dx$$

`[In] integrate((a+b*tan(d*x^2+c))^2/x^2,x, algorithm="fricas")``[Out] integral((b^2*tan(d*x^2 + c)^2 + 2*a*b*tan(d*x^2 + c) + a^2)/x^2, x)`**Sympy [N/A]**

Not integrable

Time = 0.63 (sec) , antiderivative size = 17, normalized size of antiderivative = 0.94

$$\int \frac{(a + b \tan(c + dx^2))^2}{x^2} dx = \int \frac{(a + b \tan(c + dx^2))^2}{x^2} dx$$

`[In] integrate((a+b*tan(d*x**2+c))**2/x**2,x)``[Out] Integral((a + b*tan(c + d*x**2))**2/x**2, x)`

Maxima [N/A]

Not integrable

Time = 0.41 (sec) , antiderivative size = 306, normalized size of antiderivative = 17.00

$$\int \frac{(a + b \tan(c + dx^2))^2}{x^2} dx = \int \frac{(b \tan(dx^2 + c) + a)^2}{x^2} dx$$

[In] integrate((a+b*tan(d*x^2+c))^2/x^2,x, algorithm="maxima")

```
[Out] -a^2/x + (b^2*d*x^2*cos(2*d*x^2 + 2*c)^2 + b^2*d*x^2*sin(2*d*x^2 + 2*c)^2 +
2*b^2*d*x^2*cos(2*d*x^2 + 2*c) + b^2*d*x^2 + b^2*sin(2*d*x^2 + 2*c) + (d*x
^3*cos(2*d*x^2 + 2*c)^2 + d*x^3*sin(2*d*x^2 + 2*c)^2 + 2*d*x^3*cos(2*d*x^2
+ 2*c) + d*x^3)*integrate((4*a*b*d*x^2 + 3*b^2)*sin(2*d*x^2 + 2*c)/(d*x^4*c
os(2*d*x^2 + 2*c)^2 + d*x^4*sin(2*d*x^2 + 2*c)^2 + 2*d*x^4*cos(2*d*x^2 + 2*
c) + d*x^4), x))/(d*x^3*cos(2*d*x^2 + 2*c)^2 + d*x^3*sin(2*d*x^2 + 2*c)^2 +
2*d*x^3*cos(2*d*x^2 + 2*c) + d*x^3)
```

Giac [N/A]

Not integrable

Time = 0.50 (sec) , antiderivative size = 20, normalized size of antiderivative = 1.11

$$\int \frac{(a + b \tan(c + dx^2))^2}{x^2} dx = \int \frac{(b \tan(dx^2 + c) + a)^2}{x^2} dx$$

[In] integrate((a+b*tan(d*x^2+c))^2/x^2,x, algorithm="giac")

[Out] integrate((b*tan(d*x^2 + c) + a)^2/x^2, x)

Mupad [N/A]

Not integrable

Time = 4.42 (sec) , antiderivative size = 20, normalized size of antiderivative = 1.11

$$\int \frac{(a + b \tan(c + dx^2))^2}{x^2} dx = \int \frac{(a + b \tan(dx^2 + c))^2}{x^2} dx$$

[In] int((a + b*tan(c + d*x^2))^2/x^2,x)

[Out] int((a + b*tan(c + d*x^2))^2/x^2, x)

3.13 $\int \frac{x^3}{a+b \tan(c+dx^2)} dx$

Optimal result	89
Rubi [A] (verified)	89
Mathematica [A] (verified)	91
Maple [F]	91
Fricas [B] (verification not implemented)	92
Sympy [F]	92
Maxima [B] (verification not implemented)	93
Giac [F]	93
Mupad [F(-1)]	93

Optimal result

Integrand size = 18, antiderivative size = 122

$$\int \frac{x^3}{a+b \tan(c+dx^2)} dx = \frac{x^4}{4(a+ib)} + \frac{bx^2 \log\left(1 + \frac{(a^2+b^2)e^{2i(c+dx^2)}}{(a+ib)^2}\right)}{2(a^2+b^2)d} - \frac{ib \operatorname{PolyLog}\left(2, -\frac{(a^2+b^2)e^{2i(c+dx^2)}}{(a+ib)^2}\right)}{4(a^2+b^2)d^2}$$

[Out] $1/4*x^4/(a+I*b)+1/2*b*x^2*\ln(1+(a^2+b^2)*\exp(2*I*(d*x^2+c)))/(a+I*b)^2/(a^2+b^2)/d-1/4*I*b*\operatorname{polylog}(2,-(a^2+b^2)*\exp(2*I*(d*x^2+c)))/(a+I*b)^2/(a^2+b^2)/d^2$

Rubi [A] (verified)

Time = 0.26 (sec) , antiderivative size = 122, normalized size of antiderivative = 1.00, number of steps used = 5, number of rules used = 5, $\frac{\text{number of rules}}{\text{integrand size}} = 0.278$, Rules used = {3832, 3813, 2221, 2317, 2438}

$$\int \frac{x^3}{a+b \tan(c+dx^2)} dx = -\frac{ib \operatorname{PolyLog}\left(2, -\frac{(a^2+b^2)e^{2i(dx^2+c)}}{(a+ib)^2}\right)}{4d^2(a^2+b^2)} + \frac{bx^2 \log\left(1 + \frac{(a^2+b^2)e^{2i(c+dx^2)}}{(a+ib)^2}\right)}{2d(a^2+b^2)} + \frac{x^4}{4(a+ib)}$$

[In] $\operatorname{Int}[x^3/(a + b*\operatorname{Tan}[c + d*x^2]),x]$

```
[Out] x^4/(4*(a + I*b)) + (b*x^2*Log[1 + ((a^2 + b^2)*E^((2*I)*(c + d*x^2)))/(a + I*b)^2])/(2*(a^2 + b^2)*d) - ((I/4)*b*PolyLog[2, -(((a^2 + b^2)*E^((2*I)*(c + d*x^2)))/(a + I*b)^2)])/(a^2 + b^2)*d^2
```

Rule 2221

```
Int[(((F_)^((g_)*(e_) + (f_)*(x_)))^(n_))*((c_) + (d_)*(x_))^(m_)]/((a_) + (b_))*((F_)^((g_)*(e_) + (f_)*(x_)))^(n_), x_Symbol] := Simp[(c + d*x)^m/(b*f*g*n*Log[F])]*Log[1 + b*((F^(g*(e + f*x)))^n/a)], x] - Dist[d*(m/(b*f*g*n*Log[F])), Int[(c + d*x)^(m - 1)*Log[1 + b*((F^(g*(e + f*x)))^n/a)], x], x] /; FreeQ[{F, a, b, c, d, e, f, g, n}, x] && IGtQ[m, 0]
```

Rule 2317

```
Int[Log[(a_) + (b_)*((F_)^((e_)*((c_) + (d_)*(x_)))^(n_))], x_Symbol] := Dist[1/(d*e*n*Log[F]), Subst[Int[Log[a + b*x]/x, x], x, (F^(e*(c + d*x)))^n], x] /; FreeQ[{F, a, b, c, d, e, n}, x] && GtQ[a, 0]
```

Rule 2438

```
Int[Log[(c_)*((d_) + (e_)*(x_)^(n_))]/(x_), x_Symbol] := Simp[-PolyLog[2, (-c)*e*x^n]/n, x] /; FreeQ[{c, d, e, n}, x] && EqQ[c*d, 1]
```

Rule 3813

```
Int[((c_) + (d_)*(x_))^(m_)/((a_) + (b_)*tan[(e_) + (f_)*(x_)]), x_Symbol] := Simp[(c + d*x)^(m + 1)/(d*(m + 1)*(a + I*b)), x] + Dist[2*I*b, Int[(c + d*x)^m*(E^Simp[2*I*(e + f*x), x])/((a + I*b)^2 + (a^2 + b^2)*E^Simp[2*I*(e + f*x), x])], x] /; FreeQ[{a, b, c, d, e, f}, x] && NeQ[a^2 + b^2, 0] && IGtQ[m, 0]
```

Rule 3832

```
Int[(x_)^(m_)*((a_) + (b_)*Tan[(c_) + (d_)*(x_)^(n_)])^(p_), x_Symbol] := Dist[1/n, Subst[Int[x^(Simplify[(m + 1)/n] - 1)*(a + b*Tan[c + d*x])^p, x], x, x^n], x] /; FreeQ[{a, b, c, d, m, n, p}, x] && IGtQ[Simplify[(m + 1)/n], 0] && IntegerQ[p]
```

Rubi steps

$$\begin{aligned} \text{integral} &= \frac{1}{2} \text{Subst} \left(\int \frac{x}{a + b \tan(c + dx)} dx, x, x^2 \right) \\ &= \frac{x^4}{4(a + ib)} + (ib) \text{Subst} \left(\int \frac{e^{2i(c+dx)} x}{(a + ib)^2 + (a^2 + b^2) e^{2i(c+dx)}} dx, x, x^2 \right) \end{aligned}$$

$$\begin{aligned}
&= \frac{x^4}{4(a+ib)} + \frac{bx^2 \log\left(1 + \frac{(a^2+b^2)e^{2i(c+dx^2)}}{(a+ib)^2}\right)}{2(a^2+b^2)d} - \frac{b \text{Subst}\left(\int \log\left(1 + \frac{(a^2+b^2)e^{2i(c+dx^2)}}{(a+ib)^2}\right) dx, x, x^2\right)}{2(a^2+b^2)d} \\
&= \frac{x^4}{4(a+ib)} + \frac{bx^2 \log\left(1 + \frac{(a^2+b^2)e^{2i(c+dx^2)}}{(a+ib)^2}\right)}{2(a^2+b^2)d} + \frac{(ib) \text{Subst}\left(\int \frac{\log\left(1 + \frac{(a^2+b^2)x}{(a+ib)^2}\right)}{x} dx, x, e^{2i(c+dx^2)}\right)}{4(a^2+b^2)d^2} \\
&= \frac{x^4}{4(a+ib)} + \frac{bx^2 \log\left(1 + \frac{(a^2+b^2)e^{2i(c+dx^2)}}{(a+ib)^2}\right)}{2(a^2+b^2)d} - \frac{ib \text{PolyLog}\left(2, -\frac{(a^2+b^2)e^{2i(c+dx^2)}}{(a+ib)^2}\right)}{4(a^2+b^2)d^2}
\end{aligned}$$

Mathematica [A] (verified)

Time = 1.23 (sec) , antiderivative size = 110, normalized size of antiderivative = 0.90

$$\begin{aligned}
&\int \frac{x^3}{a + b \tan(c + dx^2)} dx \\
&= \frac{dx^2 \left((a+ib)dx^2 + 2b \log\left(1 + \frac{(a+ib)e^{-2i(c+dx^2)}}{a-ib}\right) \right) + ib \text{PolyLog}\left(2, \frac{(-a-ib)e^{-2i(c+dx^2)}}{a-ib}\right)}{4(a^2+b^2)d^2}
\end{aligned}$$

[In] Integrate[x^3/(a + b*Tan[c + d*x^2]),x]

[Out] (d*x^2*((a + I*b)*d*x^2 + 2*b*Log[1 + (a + I*b)/((a - I*b)*E^((2*I)*(c + d*x^2))])) + I*b*PolyLog[2, (-a - I*b)/((a - I*b)*E^((2*I)*(c + d*x^2)))]/(4*(a^2 + b^2)*d^2)

Maple [F]

$$\int \frac{x^3}{a + b \tan(dx^2 + c)} dx$$

[In] int(x^3/(a+b*tan(d*x^2+c)),x)

[Out] int(x^3/(a+b*tan(d*x^2+c)),x)

Fricas [B] (verification not implemented)

Both result and optimal contain complex but leaf count of result is larger than twice the leaf count of optimal. 536 vs. $2(103) = 206$.

Time = 0.26 (sec) , antiderivative size = 536, normalized size of antiderivative = 4.39

$$\int \frac{x^3}{a + b \tan(c + dx^2)} dx$$

$$= \frac{2ad^2x^4 - 2bc \log\left(\frac{(iab+b^2)\tan(dx^2+c)^2 - a^2 + iab + (ia^2+ib^2)\tan(dx^2+c)}{\tan(dx^2+c)^2+1}\right) - 2bc \log\left(\frac{(iab-b^2)\tan(dx^2+c)^2 + a^2 + iab + (ia^2+ib^2)\tan(dx^2+c)}{\tan(dx^2+c)^2+1}\right)}{d^2}$$

```
[In] integrate(x^3/(a+b*tan(d*x^2+c)),x, algorithm="fricas")
```

```
[Out] 1/8*(2*a*d^2*x^4 - 2*b*c*log(((I*a*b + b^2)*tan(d*x^2 + c)^2 - a^2 + I*a*b + (I*a^2 + I*b^2)*tan(d*x^2 + c))/(tan(d*x^2 + c)^2 + 1)) - 2*b*c*log(((I*a*b - b^2)*tan(d*x^2 + c)^2 + a^2 + I*a*b + (I*a^2 + I*b^2)*tan(d*x^2 + c))/(tan(d*x^2 + c)^2 + 1)) + I*b*dilog(2*((I*a*b - b^2)*tan(d*x^2 + c)^2 - a^2 - I*a*b + (I*a^2 - 2*a*b - I*b^2)*tan(d*x^2 + c))/((a^2 + b^2)*tan(d*x^2 + c)^2 + a^2 + b^2) + 1) - I*b*dilog(2*((-I*a*b - b^2)*tan(d*x^2 + c)^2 - a^2 + I*a*b + (-I*a^2 - 2*a*b + I*b^2)*tan(d*x^2 + c))/((a^2 + b^2)*tan(d*x^2 + c)^2 + a^2 + b^2) + 1) + 2*(b*d*x^2 + b*c)*log(-2*((I*a*b - b^2)*tan(d*x^2 + c)^2 - a^2 - I*a*b + (I*a^2 - 2*a*b - I*b^2)*tan(d*x^2 + c))/((a^2 + b^2)*tan(d*x^2 + c)^2 + a^2 + b^2)) + 2*(b*d*x^2 + b*c)*log(-2*((-I*a*b - b^2)*tan(d*x^2 + c)^2 - a^2 + I*a*b + (-I*a^2 - 2*a*b + I*b^2)*tan(d*x^2 + c))/((a^2 + b^2)*tan(d*x^2 + c)^2 + a^2 + b^2)))/((a^2 + b^2)*d^2)
```

Sympy [F]

$$\int \frac{x^3}{a + b \tan(c + dx^2)} dx = \int \frac{x^3}{a + b \tan(c + dx^2)} dx$$

```
[In] integrate(x**3/(a+b*tan(d*x**2+c)),x)
```

```
[Out] Integral(x**3/(a + b*tan(c + d*x**2)), x)
```

Maxima [B] (verification not implemented)

Both result and optimal contain complex but leaf count of result is larger than twice the leaf count of optimal. 267 vs. $2(103) = 206$.

Time = 0.29 (sec) , antiderivative size = 267, normalized size of antiderivative = 2.19

$$\int \frac{x^3}{a + b \tan(c + dx^2)} dx$$

$$= \frac{(a - ib)d^2x^4 - 2ibdx^2 \arctan\left(\frac{2ab \cos(2dx^2+2c) - (a^2-b^2) \sin(2dx^2+2c)}{a^2+b^2}\right), \frac{2ab \sin(2dx^2+2c) + a^2+b^2 + (a^2-b^2) \cos(2dx^2+2c)}{a^2+b^2}}{}$$

[In] integrate(x^3/(a+b*tan(d*x^2+c)),x, algorithm="maxima")

[Out] $\frac{1}{4} * ((a - I*b)*d^2*x^4 - 2*I*b*d*x^2*\arctan2((2*a*b*\cos(2*d*x^2 + 2*c) - (a^2 - b^2)*\sin(2*d*x^2 + 2*c))/(a^2 + b^2), (2*a*b*\sin(2*d*x^2 + 2*c) + a^2 + b^2 + (a^2 - b^2)*\cos(2*d*x^2 + 2*c))/(a^2 + b^2)) + b*d*x^2*\log(((a^2 + b^2)*\cos(2*d*x^2 + 2*c)^2 + 4*a*b*\sin(2*d*x^2 + 2*c) + (a^2 + b^2)*\sin(2*d*x^2 + 2*c)^2 + a^2 + b^2 + 2*(a^2 - b^2)*\cos(2*d*x^2 + 2*c))/(a^2 + b^2)) - I*b*\operatorname{dilog}((I*a + b)*e^{(2*I*d*x^2 + 2*I*c)/(-I*a + b)})/(a^2 + b^2)*d^2)$

Giac [F]

$$\int \frac{x^3}{a + b \tan(c + dx^2)} dx = \int \frac{x^3}{b \tan(dx^2 + c) + a} dx$$

[In] integrate(x^3/(a+b*tan(d*x^2+c)),x, algorithm="giac")

[Out] integrate(x^3/(b*tan(d*x^2 + c) + a), x)

Mupad [F(-1)]

Timed out.

$$\int \frac{x^3}{a + b \tan(c + dx^2)} dx = \int \frac{x^3}{a + b \tan(dx^2 + c)} dx$$

[In] int(x^3/(a + b*tan(c + d*x^2)),x)

[Out] int(x^3/(a + b*tan(c + d*x^2)), x)

3.14 $\int \frac{x^2}{a+b \tan(c+dx^2)} dx$

Optimal result	94
Rubi [N/A]	94
Mathematica [N/A]	95
Maple [N/A] (verified)	95
Fricas [N/A]	95
Sympy [N/A]	95
Maxima [N/A]	96
Giac [N/A]	96
Mupad [N/A]	96

Optimal result

Integrand size = 18, antiderivative size = 18

$$\int \frac{x^2}{a+b \tan(c+dx^2)} dx = \text{Int}\left(\frac{x^2}{a+b \tan(c+dx^2)}, x\right)$$

[Out] Unintegrable(x^2/(a+b*tan(d*x^2+c)),x)

Rubi [N/A]

Not integrable

Time = 0.03 (sec) , antiderivative size = 18, normalized size of antiderivative = 1.00, number of steps used = 0, number of rules used = 0, $\frac{\text{number of rules}}{\text{integrand size}} = 0.000$, Rules used = {}

$$\int \frac{x^2}{a+b \tan(c+dx^2)} dx = \int \frac{x^2}{a+b \tan(c+dx^2)} dx$$

[In] Int[x^2/(a + b*Tan[c + d*x^2]),x]

[Out] Defer[Int][x^2/(a + b*Tan[c + d*x^2]), x]

Rubi steps

$$\text{integral} = \int \frac{x^2}{a+b \tan(c+dx^2)} dx$$

Mathematica [N/A]

Not integrable

Time = 3.33 (sec) , antiderivative size = 20, normalized size of antiderivative = 1.11

$$\int \frac{x^2}{a + b \tan(c + dx^2)} dx = \int \frac{x^2}{a + b \tan(c + dx^2)} dx$$

`[In] Integrate[x^2/(a + b*Tan[c + d*x^2]),x]``[Out] Integrate[x^2/(a + b*Tan[c + d*x^2]), x]`**Maple [N/A] (verified)**

Not integrable

Time = 0.14 (sec) , antiderivative size = 18, normalized size of antiderivative = 1.00

$$\int \frac{x^2}{a + b \tan(dx^2 + c)} dx$$

`[In] int(x^2/(a+b*tan(d*x^2+c)),x)``[Out] int(x^2/(a+b*tan(d*x^2+c)),x)`**Fricas [N/A]**

Not integrable

Time = 0.24 (sec) , antiderivative size = 20, normalized size of antiderivative = 1.11

$$\int \frac{x^2}{a + b \tan(c + dx^2)} dx = \int \frac{x^2}{b \tan(dx^2 + c) + a} dx$$

`[In] integrate(x^2/(a+b*tan(d*x^2+c)),x, algorithm="fricas")``[Out] integral(x^2/(b*tan(d*x^2 + c) + a), x)`**Sympy [N/A]**

Not integrable

Time = 0.36 (sec) , antiderivative size = 15, normalized size of antiderivative = 0.83

$$\int \frac{x^2}{a + b \tan(c + dx^2)} dx = \int \frac{x^2}{a + b \tan(c + dx^2)} dx$$

`[In] integrate(x**2/(a+b*tan(d*x**2+c)),x)``[Out] Integral(x**2/(a + b*tan(c + d*x**2)), x)`

Maxima [N/A]

Not integrable

Time = 0.66 (sec) , antiderivative size = 196, normalized size of antiderivative = 10.89

$$\int \frac{x^2}{a + b \tan(c + dx^2)} dx = \int \frac{x^2}{b \tan(dx^2 + c) + a} dx$$

[In] integrate(x^2/(a+b*tan(d*x^2+c)),x, algorithm="maxima")

[Out] 1/3*(a*x^3 + 6*(a^2*b + b^3)*integrate((2*a*b*x^2*cos(2*d*x^2 + 2*c) - (a^2 - b^2)*x^2*sin(2*d*x^2 + 2*c))/(a^4 + 2*a^2*b^2 + b^4 + (a^4 + 2*a^2*b^2 + b^4)*cos(2*d*x^2 + 2*c)^2 + (a^4 + 2*a^2*b^2 + b^4)*sin(2*d*x^2 + 2*c)^2 + 2*(a^4 - b^4)*cos(2*d*x^2 + 2*c) + 4*(a^3*b + a*b^3)*sin(2*d*x^2 + 2*c)), x)/(a^2 + b^2)

Giac [N/A]

Not integrable

Time = 0.47 (sec) , antiderivative size = 20, normalized size of antiderivative = 1.11

$$\int \frac{x^2}{a + b \tan(c + dx^2)} dx = \int \frac{x^2}{b \tan(dx^2 + c) + a} dx$$

[In] integrate(x^2/(a+b*tan(d*x^2+c)),x, algorithm="giac")

[Out] integrate(x^2/(b*tan(d*x^2 + c) + a), x)

Mupad [N/A]

Not integrable

Time = 4.00 (sec) , antiderivative size = 20, normalized size of antiderivative = 1.11

$$\int \frac{x^2}{a + b \tan(c + dx^2)} dx = \int \frac{x^2}{a + b \tan(dx^2 + c)} dx$$

[In] int(x^2/(a + b*tan(c + d*x^2)),x)

[Out] int(x^2/(a + b*tan(c + d*x^2)), x)

3.15 $\int \frac{x}{a+b \tan(c+dx^2)} dx$

Optimal result	97
Rubi [A] (verified)	97
Mathematica [C] (verified)	98
Maple [A] (verified)	99
Fricas [A] (verification not implemented)	99
Sympy [C] (verification not implemented)	99
Maxima [B] (verification not implemented)	100
Giac [A] (verification not implemented)	101
Mupad [B] (verification not implemented)	101

Optimal result

Integrand size = 16, antiderivative size = 57

$$\int \frac{x}{a+b \tan(c+dx^2)} dx = \frac{ax^2}{2(a^2+b^2)} + \frac{b \log(a \cos(c+dx^2) + b \sin(c+dx^2))}{2(a^2+b^2)d}$$

[Out] $1/2*a*x^2/(a^2+b^2)+1/2*b*\ln(a*\cos(d*x^2+c)+b*\sin(d*x^2+c))/(a^2+b^2)/d$

Rubi [A] (verified)

Time = 0.10 (sec), antiderivative size = 57, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 3, $\frac{\text{number of rules}}{\text{integrand size}} = 0.188$, Rules used = {3832, 3565, 3611}

$$\int \frac{x}{a+b \tan(c+dx^2)} dx = \frac{b \log(a \cos(c+dx^2) + b \sin(c+dx^2))}{2d(a^2+b^2)} + \frac{ax^2}{2(a^2+b^2)}$$

[In] Int[x/(a + b*Tan[c + d*x^2]),x]

[Out] $(a*x^2)/(2*(a^2 + b^2)) + (b*\text{Log}[a*\text{Cos}[c + d*x^2] + b*\text{Sin}[c + d*x^2]])/(2*(a^2 + b^2)*d)$

Rule 3565

Int[((a_) + (b_)*tan[(c_) + (d_)*(x_)])^(-1), x_Symbol] := Simp[a*(x/(a^2 + b^2)), x] + Dist[b/(a^2 + b^2), Int[(b - a*Tan[c + d*x])/(a + b*Tan[c + d*x]), x], x] /; FreeQ[{a, b, c, d}, x] && NeQ[a^2 + b^2, 0]

Rule 3611

Int[((c_) + (d_)*tan[(e_) + (f_)*(x_)])/((a_) + (b_)*tan[(e_) + (f_)*(x_)]), x_Symbol] := Simp[(c/(b*f))*Log[RemoveContent[a*Cos[e + f*x] + b*Si

```
n[e + f*x], x]], x] /; FreeQ[{a, b, c, d, e, f}, x] && NeQ[b*c - a*d, 0] &&
NeQ[a^2 + b^2, 0] && EqQ[a*c + b*d, 0]
```

Rule 3832

```
Int[(x_)^(m_.)*((a_.) + (b_.)*Tan[(c_.) + (d_.)*(x_)^(n_)])^(p_.), x_Symbol
] :> Dist[1/n, Subst[Int[x^(Simplify[(m + 1)/n] - 1)*(a + b*Tan[c + d*x])^p
, x], x, x^n], x] /; FreeQ[{a, b, c, d, m, n, p}, x] && IGtQ[Simplify[(m +
1)/n], 0] && IntegerQ[p]
```

Rubi steps

$$\begin{aligned} \text{integral} &= \frac{1}{2} \text{Subst} \left(\int \frac{1}{a + b \tan(c + dx)} dx, x, x^2 \right) \\ &= \frac{ax^2}{2(a^2 + b^2)} + \frac{b \text{Subst} \left(\int \frac{b - a \tan(c + dx)}{a + b \tan(c + dx)} dx, x, x^2 \right)}{2(a^2 + b^2)} \\ &= \frac{ax^2}{2(a^2 + b^2)} + \frac{b \log(a \cos(c + dx^2) + b \sin(c + dx^2))}{2(a^2 + b^2)d} \end{aligned}$$

Mathematica [C] (verified)

Result contains complex when optimal does not.

Time = 0.16 (sec) , antiderivative size = 82, normalized size of antiderivative = 1.44

$$\begin{aligned} &\int \frac{x}{a + b \tan(c + dx^2)} dx \\ &= \frac{(-ia - b) \log(i - \tan(c + dx^2)) + i(a + ib) \log(i + \tan(c + dx^2)) + 2b \log(a + b \tan(c + dx^2))}{4(a^2 + b^2)d} \end{aligned}$$

```
[In] Integrate[x/(a + b*Tan[c + d*x^2]),x]
```

```
[Out] (((-I)*a - b)*Log[I - Tan[c + d*x^2]] + I*(a + I*b)*Log[I + Tan[c + d*x^2]]
+ 2*b*Log[a + b*Tan[c + d*x^2]])/(4*(a^2 + b^2)*d)
```

Maple [A] (verified)

Time = 0.13 (sec) , antiderivative size = 55, normalized size of antiderivative = 0.96

method	result	size
parallelrisc	$\frac{2adx^2 + 2b \ln(a + b \tan(dx^2 + c)) - b \ln(1 + \tan^2(dx^2 + c))}{4d(a^2 + b^2)}$	55
derivativedivides	$\frac{-\frac{b \ln(1 + \tan^2(dx^2 + c))}{2} + a \arctan(\tan(dx^2 + c))}{a^2 + b^2} + \frac{b \ln(a + b \tan(dx^2 + c))}{a^2 + b^2}$	69
default	$\frac{-\frac{b \ln(1 + \tan^2(dx^2 + c))}{2} + a \arctan(\tan(dx^2 + c))}{a^2 + b^2} + \frac{b \ln(a + b \tan(dx^2 + c))}{a^2 + b^2}$	69
norman	$\frac{ax^2}{2a^2 + 2b^2} - \frac{b \ln(1 + \tan^2(dx^2 + c))}{4d(a^2 + b^2)} + \frac{b \ln(a + b \tan(dx^2 + c))}{2d(a^2 + b^2)}$	73
risc	$-\frac{x^2}{2(ib-a)} - \frac{ibx^2}{a^2 + b^2} - \frac{ibc}{d(a^2 + b^2)} + \frac{b \ln\left(e^{2i(dx^2 + c)} - \frac{ib+a}{ib-a}\right)}{2d(a^2 + b^2)}$	96

[In] `int(x/(a+b*tan(d*x^2+c)),x,method=_RETURNVERBOSE)`

[Out] $1/4*(2*a*d*x^2+2*b*\ln(a+b*\tan(d*x^2+c))-b*\ln(1+\tan(d*x^2+c)^2))/d/(a^2+b^2)$

Fricas [A] (verification not implemented)

none

Time = 0.25 (sec) , antiderivative size = 70, normalized size of antiderivative = 1.23

$$\int \frac{x}{a + b \tan(c + dx^2)} dx = \frac{2adx^2 + b \log\left(\frac{b^2 \tan(dx^2 + c)^2 + 2ab \tan(dx^2 + c) + a^2}{\tan(dx^2 + c)^2 + 1}\right)}{4(a^2 + b^2)d}$$

[In] `integrate(x/(a+b*tan(d*x^2+c)),x, algorithm="fricas")`

[Out] $1/4*(2*a*d*x^2 + b*\log((b^2*\tan(d*x^2 + c)^2 + 2*a*b*\tan(d*x^2 + c) + a^2)/(\tan(d*x^2 + c)^2 + 1)))/((a^2 + b^2)*d)$

Sympy [C] (verification not implemented)

Result contains complex when optimal does not.

Time = 0.54 (sec) , antiderivative size = 359, normalized size of antiderivative = 6.30

$$\int \frac{x}{a + b \tan(c + dx^2)} dx$$

$$= \begin{cases} \frac{\infty x^2}{\tan(c)} & \text{for } a = 0 \wedge b \neq 0 \\ \frac{x^2}{2a} & \text{for } b = 0 \\ \frac{i \left(\operatorname{atan}(\tan(c+dx^2)) + \pi \left\lfloor \frac{c+dx^2 - \frac{\pi}{2}}{\pi} \right\rfloor \right) \tan(c+dx^2)}{4bd \tan(c+dx^2) - 4ibd} + \frac{\operatorname{atan}(\tan(c+dx^2)) + \pi \left\lfloor \frac{c+dx^2 - \frac{\pi}{2}}{\pi} \right\rfloor}{4bd \tan(c+dx^2) - 4ibd} + \frac{i}{4bd \tan(c+dx^2) - 4ibd} & \text{for } a = -ib \\ -\frac{i \left(\operatorname{atan}(\tan(c+dx^2)) + \pi \left\lfloor \frac{c+dx^2 - \frac{\pi}{2}}{\pi} \right\rfloor \right) \tan(c+dx^2)}{4bd \tan(c+dx^2) + 4ibd} + \frac{\operatorname{atan}(\tan(c+dx^2)) + \pi \left\lfloor \frac{c+dx^2 - \frac{\pi}{2}}{\pi} \right\rfloor}{4bd \tan(c+dx^2) + 4ibd} - \frac{i}{4bd \tan(c+dx^2) + 4ibd} & \text{for } a = ib \\ \frac{x^2}{2(a+b \tan(c))} & \text{for } d = 0 \\ \frac{2adx^2}{4a^2d+4b^2d} + \frac{2b \log\left(\frac{a}{b} + \tan(c+dx^2)\right)}{4a^2d+4b^2d} - \frac{b \log(\tan^2(c+dx^2)+1)}{4a^2d+4b^2d} & \text{otherwise} \end{cases}$$

[In] integrate(x/(a+b*tan(d*x**2+c)),x)

[Out] Piecewise((zoo*x**2/tan(c), Eq(a, 0) & Eq(b, 0) & Eq(d, 0)), (x**2/(2*a), Eq(b, 0)), (I*(atan(tan(c + d*x**2)) + pi*floor((c + d*x**2 - pi/2)/pi))*tan(c + d*x**2)/(4*b*d*tan(c + d*x**2) - 4*I*b*d) + (atan(tan(c + d*x**2)) + pi*floor((c + d*x**2 - pi/2)/pi))/(4*b*d*tan(c + d*x**2) - 4*I*b*d) + I/(4*b*d*tan(c + d*x**2) - 4*I*b*d), Eq(a, -I*b)), (-I*(atan(tan(c + d*x**2)) + pi*floor((c + d*x**2 - pi/2)/pi))*tan(c + d*x**2)/(4*b*d*tan(c + d*x**2) + 4*I*b*d) + (atan(tan(c + d*x**2)) + pi*floor((c + d*x**2 - pi/2)/pi))/(4*b*d*tan(c + d*x**2) + 4*I*b*d) - I/(4*b*d*tan(c + d*x**2) + 4*I*b*d), Eq(a, I*b)), (x**2/(2*(a + b*tan(c))), Eq(d, 0)), (2*a*d*x**2/(4*a**2*d + 4*b**2*d) + 2*b*log(a/b + tan(c + d*x**2))/(4*a**2*d + 4*b**2*d) - b*log(tan(c + d*x**2)**2 + 1)/(4*a**2*d + 4*b**2*d), True))

Maxima [B] (verification not implemented)

Leaf count of result is larger than twice the leaf count of optimal. 143 vs. 2(53) = 106.

Time = 0.30 (sec) , antiderivative size = 143, normalized size of antiderivative = 2.51

$$\int \frac{x}{a + b \tan(c + dx^2)} dx$$

$$= \frac{2 a d x^2 + b \log\left(\frac{(a^2+b^2) \cos(2 d x^2+2 c)+4 a b \sin(2 d x^2+2 c)+(a^2+b^2) \sin(2 d x^2+2 c)^2+a^2+b^2+2(a^2-b^2) \cos(2 d x^2+2 c)}{(a^2+b^2) \cos(2 c)^2+(a^2+b^2) \sin(2 c)^2}\right)}{4(a^2+b^2)d}$$

[In] integrate(x/(a+b*tan(d*x^2+c)),x, algorithm="maxima")

[Out] 1/4*(2*a*d*x^2 + b*log(((a^2 + b^2)*cos(2*d*x^2 + 2*c))^2 + 4*a*b*sin(2*d*x^2 + 2*c) + (a^2 + b^2)*sin(2*d*x^2 + 2*c)^2 + a^2 + b^2 + 2*(a^2 - b^2)*cos

$(2*d*x^2 + 2*c)/((a^2 + b^2)*\cos(2*c)^2 + (a^2 + b^2)*\sin(2*c)^2)/((a^2 + b^2)*d)$

Giac [A] (verification not implemented)

none

Time = 0.30 (sec) , antiderivative size = 86, normalized size of antiderivative = 1.51

$$\int \frac{x}{a + b \tan(c + dx^2)} dx = \frac{b^2 \log(|b \tan(dx^2 + c) + a|)}{2(a^2bd + b^3d)} + \frac{(dx^2 + c)a}{2(a^2d + b^2d)} - \frac{b \log(\tan(dx^2 + c)^2 + 1)}{4(a^2d + b^2d)}$$

[In] integrate(x/(a+b*tan(d*x^2+c)),x, algorithm="giac")

[Out] 1/2*b^2*log(abs(b*tan(d*x^2 + c) + a))/(a^2*b*d + b^3*d) + 1/2*(d*x^2 + c)*a/(a^2*d + b^2*d) - 1/4*b*log(tan(d*x^2 + c)^2 + 1)/(a^2*d + b^2*d)

Mupad [B] (verification not implemented)

Time = 3.54 (sec) , antiderivative size = 65, normalized size of antiderivative = 1.14

$$\int \frac{x}{a + b \tan(c + dx^2)} dx = \frac{\frac{b \ln(a + b \tan(dx^2 + c))}{2} - \frac{b \ln(\tan(dx^2 + c)^2 + 1)}{4}}{d(a^2 + b^2)} + \frac{ax^2}{2(a^2 + b^2)}$$

[In] int(x/(a + b*tan(c + d*x^2)),x)

[Out] ((b*log(a + b*tan(c + d*x^2)))/2 - (b*log(tan(c + d*x^2)^2 + 1))/4)/(d*(a^2 + b^2)) + (a*x^2)/(2*(a^2 + b^2))

3.16 $\int \frac{1}{a+b \tan(c+dx^2)} dx$

Optimal result	102
Rubi [N/A]	102
Mathematica [N/A]	103
Maple [N/A] (verified)	103
Fricas [N/A]	103
Sympy [N/A]	103
Maxima [N/A]	104
Giac [N/A]	104
Mupad [N/A]	104

Optimal result

Integrand size = 14, antiderivative size = 14

$$\int \frac{1}{a+b \tan(c+dx^2)} dx = \text{Int}\left(\frac{1}{a+b \tan(c+dx^2)}, x\right)$$

[Out] Unintegrable(1/(a+b*tan(d*x^2+c)),x)

Rubi [N/A]

Not integrable

Time = 0.01 (sec) , antiderivative size = 14, normalized size of antiderivative = 1.00, number of steps used = 0, number of rules used = 0, $\frac{\text{number of rules}}{\text{integrand size}} = 0.000$, Rules used = {}

$$\int \frac{1}{a+b \tan(c+dx^2)} dx = \int \frac{1}{a+b \tan(c+dx^2)} dx$$

[In] Int[(a + b*Tan[c + d*x^2])^(-1),x]

[Out] Defer[Int] [(a + b*Tan[c + d*x^2])^(-1), x]

Rubi steps

$$\text{integral} = \int \frac{1}{a+b \tan(c+dx^2)} dx$$

Mathematica [N/A]

Not integrable

Time = 1.41 (sec) , antiderivative size = 16, normalized size of antiderivative = 1.14

$$\int \frac{1}{a + b \tan(c + dx^2)} dx = \int \frac{1}{a + b \tan(c + dx^2)} dx$$

[In] Integrate[(a + b*Tan[c + d*x^2])^(-1),x]

[Out] Integrate[(a + b*Tan[c + d*x^2])^(-1), x]

Maple [N/A] (verified)

Not integrable

Time = 0.13 (sec) , antiderivative size = 14, normalized size of antiderivative = 1.00

$$\int \frac{1}{a + b \tan(dx^2 + c)} dx$$

[In] int(1/(a+b*tan(d*x^2+c)),x)

[Out] int(1/(a+b*tan(d*x^2+c)),x)

Fricas [N/A]

Not integrable

Time = 0.24 (sec) , antiderivative size = 16, normalized size of antiderivative = 1.14

$$\int \frac{1}{a + b \tan(c + dx^2)} dx = \int \frac{1}{b \tan(dx^2 + c) + a} dx$$

[In] integrate(1/(a+b*tan(d*x^2+c)),x, algorithm="fricas")

[Out] integral(1/(b*tan(d*x^2 + c) + a), x)

Sympy [N/A]

Not integrable

Time = 0.29 (sec) , antiderivative size = 14, normalized size of antiderivative = 1.00

$$\int \frac{1}{a + b \tan(c + dx^2)} dx = \int \frac{1}{a + b \tan(c + dx^2)} dx$$

[In] integrate(1/(a+b*tan(d*x**2+c)),x)

[Out] Integral(1/(a + b*tan(c + d*x**2)), x)

Maxima [N/A]

Not integrable

Time = 0.44 (sec) , antiderivative size = 187, normalized size of antiderivative = 13.36

$$\int \frac{1}{a + b \tan(c + dx^2)} dx = \int \frac{1}{b \tan(dx^2 + c) + a} dx$$

```
[In] integrate(1/(a+b*tan(d*x^2+c)),x, algorithm="maxima")
```

```
[Out] (a*x + 2*(a^2*b + b^3)*integrate((2*a*b*cos(2*d*x^2 + 2*c) - (a^2 - b^2)*sin(2*d*x^2 + 2*c))/(a^4 + 2*a^2*b^2 + b^4 + (a^4 + 2*a^2*b^2 + b^4)*cos(2*d*x^2 + 2*c)^2 + (a^4 + 2*a^2*b^2 + b^4)*sin(2*d*x^2 + 2*c)^2 + 2*(a^4 - b^4)*cos(2*d*x^2 + 2*c) + 4*(a^3*b + a*b^3)*sin(2*d*x^2 + 2*c)), x))/(a^2 + b^2)
```

Giac [N/A]

Not integrable

Time = 0.36 (sec) , antiderivative size = 16, normalized size of antiderivative = 1.14

$$\int \frac{1}{a + b \tan(c + dx^2)} dx = \int \frac{1}{b \tan(dx^2 + c) + a} dx$$

```
[In] integrate(1/(a+b*tan(d*x^2+c)),x, algorithm="giac")
```

```
[Out] integrate(1/(b*tan(d*x^2 + c) + a), x)
```

Mupad [N/A]

Not integrable

Time = 3.56 (sec) , antiderivative size = 16, normalized size of antiderivative = 1.14

$$\int \frac{1}{a + b \tan(c + dx^2)} dx = \int \frac{1}{a + b \tan(dx^2 + c)} dx$$

```
[In] int(1/(a + b*tan(c + d*x^2)),x)
```

```
[Out] int(1/(a + b*tan(c + d*x^2)), x)
```


3.17 $\int \frac{1}{x(a+b \tan(c+dx^2))} dx$

Optimal result	105
Rubi [N/A]	105
Mathematica [N/A]	106
Maple [N/A] (verified)	106
Fricas [N/A]	106
Sympy [N/A]	106
Maxima [N/A]	107
Giac [N/A]	107
Mupad [N/A]	107

Optimal result

Integrand size = 18, antiderivative size = 18

$$\int \frac{1}{x(a+b \tan(c+dx^2))} dx = \text{Int}\left(\frac{1}{x(a+b \tan(c+dx^2))}, x\right)$$

[Out] Unintegrable(1/x/(a+b*tan(d*x^2+c)),x)

Rubi [N/A]

Not integrable

Time = 0.03 (sec), antiderivative size = 18, normalized size of antiderivative = 1.00, number of steps used = 0, number of rules used = 0, $\frac{\text{number of rules}}{\text{integrand size}} = 0.000$, Rules used = {}

$$\int \frac{1}{x(a+b \tan(c+dx^2))} dx = \int \frac{1}{x(a+b \tan(c+dx^2))} dx$$

[In] Int[1/(x*(a + b*Tan[c + d*x^2])),x]

[Out] Defer[Int][1/(x*(a + b*Tan[c + d*x^2])), x]

Rubi steps

$$\text{integral} = \int \frac{1}{x(a+b \tan(c+dx^2))} dx$$

Mathematica [N/A]

Not integrable

Time = 1.35 (sec) , antiderivative size = 20, normalized size of antiderivative = 1.11

$$\int \frac{1}{x(a + b \tan(c + dx^2))} dx = \int \frac{1}{x(a + b \tan(c + dx^2))} dx$$

[In] Integrate[1/(x*(a + b*Tan[c + d*x^2])),x]

[Out] Integrate[1/(x*(a + b*Tan[c + d*x^2])), x]

Maple [N/A] (verified)

Not integrable

Time = 0.14 (sec) , antiderivative size = 18, normalized size of antiderivative = 1.00

$$\int \frac{1}{x(a + b \tan(dx^2 + c))} dx$$

[In] int(1/x/(a+b*tan(d*x^2+c)),x)

[Out] int(1/x/(a+b*tan(d*x^2+c)),x)

Fricas [N/A]

Not integrable

Time = 0.23 (sec) , antiderivative size = 19, normalized size of antiderivative = 1.06

$$\int \frac{1}{x(a + b \tan(c + dx^2))} dx = \int \frac{1}{(b \tan(dx^2 + c) + a)x} dx$$

[In] integrate(1/x/(a+b*tan(d*x^2+c)),x, algorithm="fricas")

[Out] integral(1/(b*x*tan(d*x^2 + c) + a*x), x)

Sympy [N/A]

Not integrable

Time = 0.76 (sec) , antiderivative size = 15, normalized size of antiderivative = 0.83

$$\int \frac{1}{x(a + b \tan(c + dx^2))} dx = \int \frac{1}{x(a + b \tan(c + dx^2))} dx$$

[In] integrate(1/x/(a+b*tan(d*x**2+c)),x)

[Out] Integral(1/(x*(a + b*tan(c + d*x**2))), x)

Maxima [N/A]

Not integrable

Time = 0.55 (sec) , antiderivative size = 510, normalized size of antiderivative = 28.33

$$\int \frac{1}{x(a + b \tan(c + dx^2))} dx = \int \frac{1}{(b \tan(dx^2 + c) + a)x} dx$$

[In] integrate(1/x/(a+b*tan(d*x^2+c)),x, algorithm="maxima")

[Out] $-(2*(a^2*b + b^3)*\text{integrate}((a^2*\sin(2*d*x^2 + 2*c) - (2*a*b*\cos(2*c) + b^2*\sin(2*c))*\cos(2*d*x^2) - (b^2*\cos(2*c) - 2*a*b*\sin(2*c))*\sin(2*d*x^2)))/(a^4*x*\cos(2*d*x^2 + 2*c)^2 + a^4*x*\sin(2*d*x^2 + 2*c)^2 + ((4*a^2*b^2 + b^4)*\cos(2*c)^2 + (4*a^2*b^2 + b^4)*\sin(2*c)^2)*x*\cos(2*d*x^2)^2 + ((4*a^2*b^2 + b^4)*\cos(2*c)^2 + (4*a^2*b^2 + b^4)*\sin(2*c)^2)*x*\sin(2*d*x^2)^2 - 2*((a^2*b^2 + b^4)*\cos(2*c) - 2*(a^3*b + a*b^3)*\sin(2*c))*x*\cos(2*d*x^2) + 2*(2*(a^3*b + a*b^3)*\cos(2*c) + (a^2*b^2 + b^4)*\sin(2*c))*x*\sin(2*d*x^2) + (a^4 + 2*a^2*b^2 + b^4)*x - 2*((a^2*b^2*\cos(2*c) - 2*a^3*b*\sin(2*c))*x*\cos(2*d*x^2) - (2*a^3*b*\cos(2*c) + a^2*b^2*\sin(2*c))*x*\sin(2*d*x^2) - (a^4 + a^2*b^2)*x*\cos(2*d*x^2 + 2*c) - 2*((2*a^3*b*\cos(2*c) + a^2*b^2*\sin(2*c))*x*\cos(2*d*x^2) + (a^2*b^2*\cos(2*c) - 2*a^3*b*\sin(2*c))*x*\sin(2*d*x^2))*\sin(2*d*x^2 + 2*c)), x) - a*\log(x))/(a^2 + b^2)$

Giac [N/A]

Not integrable

Time = 0.34 (sec) , antiderivative size = 20, normalized size of antiderivative = 1.11

$$\int \frac{1}{x(a + b \tan(c + dx^2))} dx = \int \frac{1}{(b \tan(dx^2 + c) + a)x} dx$$

[In] integrate(1/x/(a+b*tan(d*x^2+c)),x, algorithm="giac")

[Out] integrate(1/((b*tan(d*x^2 + c) + a)*x), x)

Mupad [N/A]

Not integrable

Time = 4.35 (sec) , antiderivative size = 20, normalized size of antiderivative = 1.11

$$\int \frac{1}{x(a + b \tan(c + dx^2))} dx = \int \frac{1}{x(a + b \tan(dx^2 + c))} dx$$

[In] int(1/(x*(a + b*tan(c + d*x^2))),x)

[Out] int(1/(x*(a + b*tan(c + d*x^2))), x)

$$3.18 \quad \int \frac{1}{x^2(a+b \tan(c+dx^2))} dx$$

Optimal result	108
Rubi [N/A]	108
Mathematica [N/A]	109
Maple [N/A] (verified)	109
Fricas [N/A]	109
Sympy [N/A]	109
Maxima [N/A]	110
Giac [N/A]	110
Mupad [N/A]	110

Optimal result

Integrand size = 18, antiderivative size = 18

$$\int \frac{1}{x^2(a+b \tan(c+dx^2))} dx = \text{Int}\left(\frac{1}{x^2(a+b \tan(c+dx^2))}, x\right)$$

[Out] Unintegrable(1/x^2/(a+b*tan(d*x^2+c)),x)

Rubi [N/A]

Not integrable

Time = 0.03 (sec) , antiderivative size = 18, normalized size of antiderivative = 1.00, number of steps used = 0, number of rules used = 0, $\frac{\text{number of rules}}{\text{integrand size}} = 0.000$, Rules used = {}

$$\int \frac{1}{x^2(a+b \tan(c+dx^2))} dx = \int \frac{1}{x^2(a+b \tan(c+dx^2))} dx$$

[In] Int[1/(x^2*(a + b*Tan[c + d*x^2])),x]

[Out] Defer[Int][1/(x^2*(a + b*Tan[c + d*x^2])), x]

Rubi steps

$$\text{integral} = \int \frac{1}{x^2(a+b \tan(c+dx^2))} dx$$

Mathematica [N/A]

Not integrable

Time = 2.88 (sec) , antiderivative size = 20, normalized size of antiderivative = 1.11

$$\int \frac{1}{x^2 (a + b \tan (c + dx^2))} dx = \int \frac{1}{x^2 (a + b \tan (c + dx^2))} dx$$

[In] Integrate[1/(x^2*(a + b*Tan[c + d*x^2])),x]

[Out] Integrate[1/(x^2*(a + b*Tan[c + d*x^2])), x]

Maple [N/A] (verified)

Not integrable

Time = 0.13 (sec) , antiderivative size = 18, normalized size of antiderivative = 1.00

$$\int \frac{1}{x^2 (a + b \tan (dx^2 + c))} dx$$

[In] int(1/x^2/(a+b*tan(d*x^2+c)),x)

[Out] int(1/x^2/(a+b*tan(d*x^2+c)),x)

Fricas [N/A]

Not integrable

Time = 0.24 (sec) , antiderivative size = 23, normalized size of antiderivative = 1.28

$$\int \frac{1}{x^2 (a + b \tan (c + dx^2))} dx = \int \frac{1}{(b \tan (dx^2 + c) + a)x^2} dx$$

[In] integrate(1/x^2/(a+b*tan(d*x^2+c)),x, algorithm="fricas")

[Out] integral(1/(b*x^2*tan(d*x^2 + c) + a*x^2), x)

Sympy [N/A]

Not integrable

Time = 0.64 (sec) , antiderivative size = 17, normalized size of antiderivative = 0.94

$$\int \frac{1}{x^2 (a + b \tan (c + dx^2))} dx = \int \frac{1}{x^2 (a + b \tan (c + dx^2))} dx$$

[In] integrate(1/x**2/(a+b*tan(d*x**2+c)),x)

[Out] Integral(1/(x**2*(a + b*tan(c + d*x**2))), x)

Maxima [N/A]

Not integrable

Time = 0.56 (sec) , antiderivative size = 534, normalized size of antiderivative = 29.67

$$\int \frac{1}{x^2 (a + b \tan(c + dx^2))} dx = \int \frac{1}{(b \tan(dx^2 + c) + a)x^2} dx$$

[In] integrate(1/x^2/(a+b*tan(d*x^2+c)),x, algorithm="maxima")

```
[Out] -(2*(a^2*b + b^3)*x*integrate((a^2*sin(2*d*x^2 + 2*c) - (2*a*b*cos(2*c) + b^2*sin(2*c))*cos(2*d*x^2) - (b^2*cos(2*c) - 2*a*b*sin(2*c))*sin(2*d*x^2))/(a^4*x^2*cos(2*d*x^2 + 2*c)^2 + a^4*x^2*sin(2*d*x^2 + 2*c)^2 + ((4*a^2*b^2 + b^4)*cos(2*c)^2 + (4*a^2*b^2 + b^4)*sin(2*c)^2)*x^2*cos(2*d*x^2)^2 + ((4*a^2*b^2 + b^4)*cos(2*c)^2 + (4*a^2*b^2 + b^4)*sin(2*c)^2)*x^2*sin(2*d*x^2)^2 - 2*((a^2*b^2 + b^4)*cos(2*c) - 2*(a^3*b + a*b^3)*sin(2*c))*x^2*cos(2*d*x^2) + 2*(2*(a^3*b + a*b^3)*cos(2*c) + (a^2*b^2 + b^4)*sin(2*c))*x^2*sin(2*d*x^2) + (a^4 + 2*a^2*b^2 + b^4)*x^2 - 2*((a^2*b^2*cos(2*c) - 2*a^3*b*sin(2*c))*x^2*cos(2*d*x^2) - (2*a^3*b*cos(2*c) + a^2*b^2*sin(2*c))*x^2*sin(2*d*x^2) - (a^4 + a^2*b^2)*x^2)*cos(2*d*x^2 + 2*c) - 2*((2*a^3*b*cos(2*c) + a^2*b^2*sin(2*c))*x^2*cos(2*d*x^2) + (a^2*b^2*cos(2*c) - 2*a^3*b*sin(2*c))*x^2*sin(2*d*x^2))*sin(2*d*x^2 + 2*c)), x) + a)/((a^2 + b^2)*x)
```

Giac [N/A]

Not integrable

Time = 0.46 (sec) , antiderivative size = 20, normalized size of antiderivative = 1.11

$$\int \frac{1}{x^2 (a + b \tan(c + dx^2))} dx = \int \frac{1}{(b \tan(dx^2 + c) + a)x^2} dx$$

[In] integrate(1/x^2/(a+b*tan(d*x^2+c)),x, algorithm="giac")

[Out] integrate(1/((b*tan(d*x^2 + c) + a)*x^2), x)

Mupad [N/A]

Not integrable

Time = 4.02 (sec) , antiderivative size = 20, normalized size of antiderivative = 1.11

$$\int \frac{1}{x^2 (a + b \tan(c + dx^2))} dx = \int \frac{1}{x^2 (a + b \tan(dx^2 + c))} dx$$

[In] int(1/(x^2*(a + b*tan(c + d*x^2))),x)

[Out] int(1/(x^2*(a + b*tan(c + d*x^2))), x)

$$3.19 \quad \int \frac{x^3}{(a+b \tan(c+dx^2))^2} dx$$

Optimal result	111
Rubi [A] (verified)	111
Mathematica [B] (verified)	114
Maple [F]	114
Fricas [B] (verification not implemented)	115
Sympy [F]	115
Maxima [B] (verification not implemented)	116
Giac [F]	116
Mupad [F(-1)]	117

Optimal result

Integrand size = 18, antiderivative size = 202

$$\int \frac{x^3}{(a+b \tan(c+dx^2))^2} dx = -\frac{x^4}{4(a^2+b^2)} + \frac{(b+2adx^2)^2}{8a(a+ib)(a^2+b^2)d^2} + \frac{b(b+2adx^2) \log\left(1 + \frac{(a^2+b^2)e^{2i(c+dx^2)}}{(a+ib)^2}\right)}{2(a^2+b^2)^2 d^2} - \frac{iab \operatorname{PolyLog}\left(2, -\frac{(a^2+b^2)e^{2i(c+dx^2)}}{(a+ib)^2}\right)}{2(a^2+b^2)^2 d^2} - \frac{bx^2}{2(a^2+b^2)d(a+b \tan(c+dx^2))}$$

[Out] $-1/4*x^4/(a^2+b^2)+1/8*(2*a*d*x^2+b)^2/a/(a+I*b)/(a^2+b^2)/d^2+1/2*b*(2*a*d*x^2+b)*\ln(1+(a^2+b^2)*\exp(2*I*(d*x^2+c))/(a+I*b)^2)/(a^2+b^2)^2/d^2-1/2*I*a*b*\operatorname{polylog}(2,-(a^2+b^2)*\exp(2*I*(d*x^2+c))/(a+I*b)^2)/(a^2+b^2)^2/d^2-1/2*b*x^2/(a^2+b^2)/d/(a+b*\tan(d*x^2+c))$

Rubi [A] (verified)

Time = 0.39 (sec) , antiderivative size = 202, normalized size of antiderivative = 1.00, number of steps used = 6, number of rules used = 6, $\frac{\text{number of rules}}{\text{integrand size}} = 0.333$, Rules used

= {3832, 3814, 3813, 2221, 2317, 2438}

$$\int \frac{x^3}{(a + b \tan(c + dx^2))^2} dx = -\frac{iab \operatorname{PolyLog}\left(2, -\frac{(a^2+b^2)e^{2i(dx^2+c)}}{(a+ib)^2}\right)}{2d^2(a^2+b^2)^2} + \frac{b(2adx^2+b) \log\left(1 + \frac{(a^2+b^2)e^{2i(c+dx^2)}}{(a+ib)^2}\right)}{2d^2(a^2+b^2)^2} - \frac{bx^2}{2d(a^2+b^2)(a+b \tan(c+dx^2))} + \frac{(2adx^2+b)^2}{8ad^2(a+ib)(a^2+b^2)} - \frac{x^4}{4(a^2+b^2)}$$

[In] Int[x^3/(a + b*Tan[c + d*x^2])^2,x]

[Out] -1/4*x^4/(a^2 + b^2) + (b + 2*a*d*x^2)^2/(8*a*(a + I*b)*(a^2 + b^2)*d^2) + (b*(b + 2*a*d*x^2)*Log[1 + ((a^2 + b^2)*E^((2*I)*(c + d*x^2)))/(a + I*b)^2])/(2*(a^2 + b^2)^2*d^2) - ((I/2)*a*b*PolyLog[2, -(((a^2 + b^2)*E^((2*I)*(c + d*x^2)))/(a + I*b)^2))]/((a^2 + b^2)^2*d^2) - (b*x^2)/(2*(a^2 + b^2)*d*(a + b*Tan[c + d*x^2]))

Rule 2221

Int[(((F_)^((g_)*((e_) + (f_)*(x_))))^(n_)*((c_) + (d_)*(x_))^(m_))/((a_) + (b_)*((F_)^((g_)*((e_) + (f_)*(x_))))^(n_)), x_Symbol] := Simp[((c + d*x)^m/(b*f*g*n*Log[F]))*Log[1 + b*((F^(g*(e + f*x)))^n/a)], x] - Dist[d*(m/(b*f*g*n*Log[F])), Int[(c + d*x)^(m-1)*Log[1 + b*((F^(g*(e + f*x)))^n/a)], x], x] /; FreeQ[{F, a, b, c, d, e, f, g, n}, x] && IGtQ[m, 0]

Rule 2317

Int[Log[(a_) + (b_)*((F_)^((e_)*((c_) + (d_)*(x_))))^(n_)], x_Symbol] := Dist[1/(d*e*n*Log[F]), Subst[Int[Log[a + b*x]/x, x], x, (F^(e*(c + d*x)))^n], x] /; FreeQ[{F, a, b, c, d, e, n}, x] && GtQ[a, 0]

Rule 2438

Int[Log[(c_)*((d_) + (e_)*(x_)^(n_))]/(x_), x_Symbol] := Simp[-PolyLog[2, (-c)*e*x^n]/n, x] /; FreeQ[{c, d, e, n}, x] && EqQ[c*d, 1]

Rule 3813

Int[(((c_) + (d_)*(x_))^(m_))/((a_) + (b_)*tan[(e_) + (f_)*(x_)]), x_Symbol] := Simp[(c + d*x)^(m+1)/(d*(m+1)*(a + I*b)), x] + Dist[2*I*b, Int[(c + d*x)^m*(E^Simp[2*I*(e + f*x), x])/((a + I*b)^2 + (a^2 + b^2)*E^Simp[2*I*(e + f*x), x])], x] /; FreeQ[{a, b, c, d, e, f}, x] && NeQ[a^2 + b^2,

0] && IGtQ[m, 0]

Rule 3814

Int[((c_.) + (d_.)*(x_))/((a_) + (b_.)*tan[(e_.) + (f_.)*(x_)])^2, x_Symbol] :> Simp[-(c + d*x)^2/(2*d*(a^2 + b^2)), x] + (Dist[1/(f*(a^2 + b^2)), Int[(b*d + 2*a*c*f + 2*a*d*f*x)/(a + b*Tan[e + f*x]), x], x] - Simp[b*((c + d*x)/(f*(a^2 + b^2)*(a + b*Tan[e + f*x]))), x]) /; FreeQ[{a, b, c, d, e, f}, x] && NeQ[a^2 + b^2, 0]

Rule 3832

Int[(x_)^(m_.)*((a_.) + (b_.)*Tan[(c_.) + (d_.)*(x_)^(n_)])^(p_.), x_Symbol] :> Dist[1/n, Subst[Int[x^(Simplify[(m + 1)/n] - 1)*(a + b*Tan[c + d*x])^p, x], x, x^n], x] /; FreeQ[{a, b, c, d, m, n, p}, x] && IGtQ[Simplify[(m + 1)/n], 0] && IntegerQ[p]

Rubi steps

$$\begin{aligned}
 \text{integral} &= \frac{1}{2} \text{Subst} \left(\int \frac{x}{(a + b \tan(c + dx))^2} dx, x, x^2 \right) \\
 &= -\frac{x^4}{4(a^2 + b^2)} - \frac{bx^2}{2(a^2 + b^2)d(a + b \tan(c + dx^2))} + \frac{\text{Subst} \left(\int \frac{b+2adx}{a+b \tan(c+dx)} dx, x, x^2 \right)}{2(a^2 + b^2)d} \\
 &= -\frac{x^4}{4(a^2 + b^2)} + \frac{(b + 2adx^2)^2}{8a(a + ib)(a^2 + b^2)d^2} - \frac{bx^2}{2(a^2 + b^2)d(a + b \tan(c + dx^2))} \\
 &\quad + \frac{(ib) \text{Subst} \left(\int \frac{e^{2i(c+dx)}(b+2adx)}{(a+ib)^2 + (a^2+b^2)e^{2i(c+dx)}} dx, x, x^2 \right)}{(a^2 + b^2)d} \\
 &= -\frac{x^4}{4(a^2 + b^2)} + \frac{(b + 2adx^2)^2}{8a(a + ib)(a^2 + b^2)d^2} + \frac{b(b + 2adx^2) \log \left(1 + \frac{(a^2+b^2)e^{2i(c+dx^2)}}{(a+ib)^2} \right)}{2(a^2 + b^2)^2 d^2} \\
 &\quad - \frac{bx^2}{2(a^2 + b^2)d(a + b \tan(c + dx^2))} - \frac{(ab) \text{Subst} \left(\int \log \left(1 + \frac{(a^2+b^2)e^{2i(c+dx)}}{(a+ib)^2} \right) dx, x, x^2 \right)}{(a^2 + b^2)^2 d} \\
 &= -\frac{x^4}{4(a^2 + b^2)} + \frac{(b + 2adx^2)^2}{8a(a + ib)(a^2 + b^2)d^2} + \frac{b(b + 2adx^2) \log \left(1 + \frac{(a^2+b^2)e^{2i(c+dx^2)}}{(a+ib)^2} \right)}{2(a^2 + b^2)^2 d^2} \\
 &\quad - \frac{bx^2}{2(a^2 + b^2)d(a + b \tan(c + dx^2))} + \frac{(iab) \text{Subst} \left(\int \frac{\log \left(1 + \frac{(a^2+b^2)x}{(a+ib)^2} \right)}{x} dx, x, e^{2i(c+dx^2)} \right)}{2(a^2 + b^2)^2 d^2}
 \end{aligned}$$

$$= -\frac{x^4}{4(a^2 + b^2)} + \frac{(b + 2adx^2)^2}{8a(a + ib)(a^2 + b^2)d^2} + \frac{b(b + 2adx^2) \log\left(1 + \frac{(a^2 + b^2)e^{2i(c + dx^2)}}{(a + ib)^2}\right)}{2(a^2 + b^2)^2 d^2}$$

$$- \frac{iab \operatorname{PolyLog}\left(2, -\frac{(a^2 + b^2)e^{2i(c + dx^2)}}{(a + ib)^2}\right)}{2(a^2 + b^2)^2 d^2} - \frac{bx^2}{2(a^2 + b^2)d(a + b \tan(c + dx^2))}$$

Mathematica [B] (verified)

Both result and optimal contain complex but leaf count is larger than twice the leaf count of optimal. 460 vs. $2(202) = 404$.

Time = 5.77 (sec) , antiderivative size = 460, normalized size of antiderivative = 2.28

$$\int \frac{x^3}{(a + b \tan(c + dx^2))^2} dx$$

$$= \frac{\sec^2(c + dx^2)(a \cos(c + dx^2) + b \sin(c + dx^2)) \left(2b^2(a^2 + b^2) dx^2 \sin(c + dx^2) - a(a^2 + b^2)(c - dx^2)(c + dx^2) \right)}{(a + b \tan(c + dx^2))^2}$$

```
[In] Integrate[x^3/(a + b*Tan[c + d*x^2])^2,x]
```

```
[Out] (Sec[c + d*x^2]^2*(a*Cos[c + d*x^2] + b*Sin[c + d*x^2])*(2*b^2*(a^2 + b^2)*
d*x^2*Sin[c + d*x^2] - a*(a^2 + b^2)*(c - d*x^2)*(c + d*x^2)*(a*Cos[c + d*x
^2] + b*Sin[c + d*x^2]) - 2*b^2*(b*(c + d*x^2) - a*Log[a*Cos[c + d*x^2] + b
*Sin[c + d*x^2]])*(a*Cos[c + d*x^2] + b*Sin[c + d*x^2]) + 4*a*b*c*(b*(c + d
*x^2) - a*Log[a*Cos[c + d*x^2] + b*Sin[c + d*x^2]])*(a*Cos[c + d*x^2] + b*S
in[c + d*x^2]) - 2*a*b*(Sqrt[1 + a^2/b^2]*b*E^(I*ArcTan[a/b])*(c + d*x^2)^2
+ a*((-I)*(c + d*x^2)*(Pi - 2*ArcTan[a/b]) - Pi*Log[1 + E^((-2*I)*(c + d*x
^2))]) - 2*(c + d*x^2 + ArcTan[a/b])*Log[1 - E^((2*I)*(c + d*x^2 + ArcTan[a/
b]))] + Pi*Log[Cos[c + d*x^2]] + 2*ArcTan[a/b]*Log[Sin[c + d*x^2 + ArcTan[a
/b]]] + I*PolyLog[2, E^((2*I)*(c + d*x^2 + ArcTan[a/b]))])*(a*Cos[c + d*x^
2] + b*Sin[c + d*x^2])))/(4*a*(a^2 + b^2)^2*d^2*(a + b*Tan[c + d*x^2])^2)
```

Maple [F]

$$\int \frac{x^3}{(a + b \tan(dx^2 + c))^2} dx$$

```
[In] int(x^3/(a+b*tan(d*x^2+c))^2,x)
```

```
[Out] int(x^3/(a+b*tan(d*x^2+c))^2,x)
```

Fricas [B] (verification not implemented)

Both result and optimal contain complex but leaf count of result is larger than twice the leaf count of optimal. 800 vs. $2(179) = 358$.

Time = 0.26 (sec) , antiderivative size = 800, normalized size of antiderivative = 3.96

$$\int \frac{x^3}{(a + b \tan(c + dx^2))^2} dx$$

$$(a^3 - ab^2)d^2x^4 - 2b^3dx^2 + (iab^2 \tan(dx^2 + c) + ia^2b) \operatorname{Li}_2\left(\frac{2((iab - b^2) \tan(dx^2 + c))^2 - a^2 - iab + (ia^2 - 2ab - ib^2) \tan(dx^2 + c)}{(a^2 + b^2) \tan(dx^2 + c)^2 + a^2 + b^2}\right)$$

[In] integrate(x^3/(a+b*tan(d*x^2+c))^2,x, algorithm="fricas")

[Out] 1/4*((a^3 - a*b^2)*d^2*x^4 - 2*b^3*d*x^2 + (I*a*b^2*tan(d*x^2 + c) + I*a^2*b)*dilog(2*((I*a*b - b^2)*tan(d*x^2 + c))^2 - a^2 - I*a*b + (I*a^2 - 2*a*b - I*b^2)*tan(d*x^2 + c))/((a^2 + b^2)*tan(d*x^2 + c)^2 + a^2 + b^2) + 1) + (-I*a*b^2*tan(d*x^2 + c) - I*a^2*b)*dilog(2*((-I*a*b - b^2)*tan(d*x^2 + c))^2 - a^2 + I*a*b + (-I*a^2 - 2*a*b + I*b^2)*tan(d*x^2 + c))/((a^2 + b^2)*tan(d*x^2 + c)^2 + a^2 + b^2) + 1) + 2*(a^2*b*d*x^2 + a^2*b*c + (a*b^2*d*x^2 + a*b^2*c)*tan(d*x^2 + c))*log(-2*((I*a*b - b^2)*tan(d*x^2 + c))^2 - a^2 - I*a*b + (I*a^2 - 2*a*b - I*b^2)*tan(d*x^2 + c))/((a^2 + b^2)*tan(d*x^2 + c)^2 + a^2 + b^2)) + 2*(a^2*b*d*x^2 + a^2*b*c + (a*b^2*d*x^2 + a*b^2*c)*tan(d*x^2 + c))*log(-2*((-I*a*b - b^2)*tan(d*x^2 + c))^2 - a^2 + I*a*b + (-I*a^2 - 2*a*b + I*b^2)*tan(d*x^2 + c))/((a^2 + b^2)*tan(d*x^2 + c)^2 + a^2 + b^2)) - (2*a^2*b*c - a*b^2 + (2*a*b^2*c - b^3)*tan(d*x^2 + c))*log(((I*a*b + b^2)*tan(d*x^2 + c))^2 - a^2 + I*a*b + (I*a^2 + I*b^2)*tan(d*x^2 + c))/(tan(d*x^2 + c)^2 + 1)) - (2*a^2*b*c - a*b^2 + (2*a*b^2*c - b^3)*tan(d*x^2 + c))*log(((I*a*b - b^2)*tan(d*x^2 + c))^2 + a^2 + I*a*b + (I*a^2 + I*b^2)*tan(d*x^2 + c))/(tan(d*x^2 + c)^2 + 1)) + ((a^2*b - b^3)*d^2*x^4 + 2*a*b^2*d*x^2)*tan(d*x^2 + c))/((a^4*b + 2*a^2*b^3 + b^5)*d^2*tan(d*x^2 + c) + (a^5 + 2*a^3*b^2 + a*b^4)*d^2)

Sympy [F]

$$\int \frac{x^3}{(a + b \tan(c + dx^2))^2} dx = \int \frac{x^3}{(a + b \tan(c + dx^2))^2} dx$$

[In] integrate(x**3/(a+b*tan(d*x**2+c))**2,x)

[Out] Integral(x**3/(a + b*tan(c + d*x**2))**2, x)

Maxima [B] (verification not implemented)

Both result and optimal contain complex but leaf count of result is larger than twice the leaf count of optimal. 1001 vs. $2(179) = 358$.

Time = 0.36 (sec) , antiderivative size = 1001, normalized size of antiderivative = 4.96

$$\int \frac{x^3}{(a + b \tan(c + dx^2))^2} dx = \text{Too large to display}$$

[In] integrate(x^3/(a+b*tan(d*x^2+c))^2,x, algorithm="maxima")

[Out] $\frac{1}{4}((a^3 - I a^2 b + a b^2 - I b^3) d^2 x^4 - 2(-I a b^2 + b^3 + (-I a b^2 - b^3) \cos(2 d x^2 + 2 c) + (a b^2 - I b^3) \sin(2 d x^2 + 2 c)) \arctan 2(-b \cos(2 d x^2 + 2 c) + a \sin(2 d x^2 + 2 c) + b, a \cos(2 d x^2 + 2 c) + b \sin(2 d x^2 + 2 c) + a) - 4((I a^2 b + a b^2) d x^2 \cos(2 d x^2 + 2 c) - (a^2 b - I a b^2) d x^2 \sin(2 d x^2 + 2 c) + (I a^2 b - a b^2) d x^2) \arctan 2((2 a b \cos(2 d x^2 + 2 c) - (a^2 - b^2) \sin(2 d x^2 + 2 c)) / (a^2 + b^2), (2 a b \sin(2 d x^2 + 2 c) + a^2 + b^2 + (a^2 - b^2) \cos(2 d x^2 + 2 c)) / (a^2 + b^2)) + ((a^3 - 3 I a^2 b - 3 a b^2 + I b^3) d^2 x^4 - 4(I a b^2 + b^3) d x^2 \cos(2 d x^2 + 2 c) - 2(I a^2 b - a b^2 + (I a^2 b + a b^2) \cos(2 d x^2 + 2 c) - (a^2 b - I a b^2) \sin(2 d x^2 + 2 c)) \operatorname{dilog}((I a + b) e^{(2 I d x^2 + 2 I c)} / (-I a + b)) + (a b^2 + I b^3 + (a b^2 - I b^3) \cos(2 d x^2 + 2 c) + (I a b^2 + b^3) \sin(2 d x^2 + 2 c)) \log((a^2 + b^2) \cos(2 d x^2 + 2 c)^2 + 4 a b \sin(2 d x^2 + 2 c) + (a^2 + b^2) \sin(2 d x^2 + 2 c)^2 + a^2 + b^2 + 2(a^2 - b^2) \cos(2 d x^2 + 2 c)) + 2((a^2 b - I a b^2) d x^2 \cos(2 d x^2 + 2 c) - (-I a^2 b - a b^2) d x^2 \sin(2 d x^2 + 2 c) + (a^2 b + I a b^2) d x^2) \log(((a^2 + b^2) \cos(2 d x^2 + 2 c))^2 + 4 a b \sin(2 d x^2 + 2 c) + (a^2 + b^2) \sin(2 d x^2 + 2 c)^2 + a^2 + b^2 + 2(a^2 - b^2) \cos(2 d x^2 + 2 c)) / (a^2 + b^2)) + ((I a^3 + 3 a^2 b - 3 I a b^2 - b^3) d^2 x^4 + 4(a b^2 - I b^3) d x^2 \sin(2 d x^2 + 2 c)) / ((a^5 - I a^4 b + 2 a^3 b^2 - 2 I a^2 b^3 + a b^4 - I b^5) d^2 \cos(2 d x^2 + 2 c) - (-I a^5 - a^4 b - 2 I a^3 b^2 - 2 a^2 b^3 - I a b^4 - b^5) d^2 \sin(2 d x^2 + 2 c) + (a^5 + I a^4 b + 2 a^3 b^2 + 2 I a^2 b^3 + a b^4 + I b^5) d^2)$

Giac [F]

$$\int \frac{x^3}{(a + b \tan(c + dx^2))^2} dx = \int \frac{x^3}{(b \tan(dx^2 + c) + a)^2} dx$$

[In] integrate(x^3/(a+b*tan(d*x^2+c))^2,x, algorithm="giac")

[Out] integrate(x^3/(b*tan(d*x^2 + c) + a)^2, x)

Mupad [F(-1)]

Timed out.

$$\int \frac{x^3}{(a + b \tan(c + dx^2))^2} dx = \int \frac{x^3}{(a + b \tan(dx^2 + c))^2} dx$$

```
[In] int(x^3/(a + b*tan(c + d*x^2))^2,x)
```

```
[Out] int(x^3/(a + b*tan(c + d*x^2))^2, x)
```

$$3.20 \quad \int \frac{x^2}{(a+b \tan(c+dx^2))^2} dx$$

Optimal result	118
Rubi [N/A]	118
Mathematica [N/A]	119
Maple [N/A] (verified)	119
Fricas [N/A]	119
Sympy [N/A]	119
Maxima [N/A]	120
Giac [N/A]	120
Mupad [N/A]	121

Optimal result

Integrand size = 18, antiderivative size = 18

$$\int \frac{x^2}{(a+b \tan(c+dx^2))^2} dx = \text{Int}\left(\frac{x^2}{(a+b \tan(c+dx^2))^2}, x\right)$$

[Out] Unintegrable(x^2/(a+b*tan(d*x^2+c))^2,x)

Rubi [N/A]

Not integrable

Time = 0.03 (sec) , antiderivative size = 18, normalized size of antiderivative = 1.00, number of steps used = 0, number of rules used = 0, $\frac{\text{number of rules}}{\text{integrand size}} = 0.000$, Rules used = {}

$$\int \frac{x^2}{(a+b \tan(c+dx^2))^2} dx = \int \frac{x^2}{(a+b \tan(c+dx^2))^2} dx$$

[In] Int[x^2/(a + b*Tan[c + d*x^2])^2,x]

[Out] Defer[Int][x^2/(a + b*Tan[c + d*x^2])^2, x]

Rubi steps

$$\text{integral} = \int \frac{x^2}{(a+b \tan(c+dx^2))^2} dx$$

Mathematica [N/A]

Not integrable

Time = 8.34 (sec) , antiderivative size = 20, normalized size of antiderivative = 1.11

$$\int \frac{x^2}{(a + b \tan(c + dx^2))^2} dx = \int \frac{x^2}{(a + b \tan(c + dx^2))^2} dx$$

[In] Integrate[x^2/(a + b*Tan[c + d*x^2])^2,x]

[Out] Integrate[x^2/(a + b*Tan[c + d*x^2])^2, x]

Maple [N/A] (verified)

Not integrable

Time = 0.17 (sec) , antiderivative size = 18, normalized size of antiderivative = 1.00

$$\int \frac{x^2}{(a + b \tan(dx^2 + c))^2} dx$$

[In] int(x^2/(a+b*tan(d*x^2+c))^2,x)

[Out] int(x^2/(a+b*tan(d*x^2+c))^2,x)

Fricas [N/A]

Not integrable

Time = 0.25 (sec) , antiderivative size = 38, normalized size of antiderivative = 2.11

$$\int \frac{x^2}{(a + b \tan(c + dx^2))^2} dx = \int \frac{x^2}{(b \tan(dx^2 + c) + a)^2} dx$$

[In] integrate(x^2/(a+b*tan(d*x^2+c))^2,x, algorithm="fricas")

[Out] integral(x^2/(b^2*tan(d*x^2 + c)^2 + 2*a*b*tan(d*x^2 + c) + a^2), x)

Sympy [N/A]

Not integrable

Time = 1.07 (sec) , antiderivative size = 17, normalized size of antiderivative = 0.94

$$\int \frac{x^2}{(a + b \tan(c + dx^2))^2} dx = \int \frac{x^2}{(a + b \tan(c + dx^2))^2} dx$$

[In] integrate(x**2/(a+b*tan(d*x**2+c))**2,x)

[Out] Integral(x**2/(a + b*tan(c + d*x**2))**2, x)

Maxima [N/A]

Not integrable

Time = 10.41 (sec) , antiderivative size = 764, normalized size of antiderivative = 42.44

$$\int \frac{x^2}{(a + b \tan(c + dx^2))^2} dx = \int \frac{x^2}{(b \tan(dx^2 + c) + a)^2} dx$$

[In] integrate(x^2/(a+b*tan(d*x^2+c))^2,x, algorithm="maxima")

```
[Out] 1/3*((a^4 - b^4)*d*x^3*cos(2*d*x^2 + 2*c)^2 + (a^4 - b^4)*d*x^3*sin(2*d*x^2 + 2*c)^2 + (a^4 - b^4)*d*x^3 - 2*(3*a*b^3*x - (a^4 - 2*a^2*b^2 + b^4)*d*x^3)*cos(2*d*x^2 + 2*c) + 3*((a^6 + 3*a^4*b^2 + 3*a^2*b^4 + b^6)*d*cos(2*d*x^2 + 2*c)^2 + (a^6 + 3*a^4*b^2 + 3*a^2*b^4 + b^6)*d*sin(2*d*x^2 + 2*c)^2 + 2*(a^6 + a^4*b^2 - a^2*b^4 - b^6)*d*cos(2*d*x^2 + 2*c) + 4*(a^5*b + 2*a^3*b^3 + a*b^5)*d*sin(2*d*x^2 + 2*c) + (a^6 + 3*a^4*b^2 + 3*a^2*b^4 + b^6)*d)*integrate((2*(4*a^2*b^2*d*x^2 + a*b^3)*cos(2*d*x^2 + 2*c) - (a^2*b^2 - b^4 + 4*(a^3*b - a*b^3)*d*x^2)*sin(2*d*x^2 + 2*c))/((a^6 + 3*a^4*b^2 + 3*a^2*b^4 + b^6)*d*cos(2*d*x^2 + 2*c)^2 + (a^6 + 3*a^4*b^2 + 3*a^2*b^4 + b^6)*d*sin(2*d*x^2 + 2*c)^2 + 2*(a^6 + a^4*b^2 - a^2*b^4 - b^6)*d*cos(2*d*x^2 + 2*c) + 4*(a^5*b + 2*a^3*b^3 + a*b^5)*d*sin(2*d*x^2 + 2*c) + (a^6 + 3*a^4*b^2 + 3*a^2*b^4 + b^6)*d), x) + (4*(a^3*b - a*b^3)*d*x^3 + 3*(a^2*b^2 - b^4)*x)*sin(2*d*x^2 + 2*c))/((a^6 + 3*a^4*b^2 + 3*a^2*b^4 + b^6)*d*cos(2*d*x^2 + 2*c)^2 + (a^6 + 3*a^4*b^2 + 3*a^2*b^4 + b^6)*d*sin(2*d*x^2 + 2*c)^2 + 2*(a^6 + a^4*b^2 - a^2*b^4 - b^6)*d*cos(2*d*x^2 + 2*c) + 4*(a^5*b + 2*a^3*b^3 + a*b^5)*d*sin(2*d*x^2 + 2*c) + (a^6 + 3*a^4*b^2 + 3*a^2*b^4 + b^6)*d)
```

Giac [N/A]

Not integrable

Time = 0.61 (sec) , antiderivative size = 20, normalized size of antiderivative = 1.11

$$\int \frac{x^2}{(a + b \tan(c + dx^2))^2} dx = \int \frac{x^2}{(b \tan(dx^2 + c) + a)^2} dx$$

[In] integrate(x^2/(a+b*tan(d*x^2+c))^2,x, algorithm="giac")

[Out] integrate(x^2/(b*tan(d*x^2 + c) + a)^2, x)

Mupad [N/A]

Not integrable

Time = 4.12 (sec) , antiderivative size = 20, normalized size of antiderivative = 1.11

$$\int \frac{x^2}{(a + b \tan(c + dx^2))^2} dx = \int \frac{x^2}{(a + b \tan(dx^2 + c))^2} dx$$

```
[In] int(x^2/(a + b*tan(c + d*x^2))^2,x)
```

```
[Out] int(x^2/(a + b*tan(c + d*x^2))^2, x)
```

3.21 $\int \frac{x}{(a+b \tan(c+dx^2))^2} dx$

Optimal result	122
Rubi [A] (verified)	122
Mathematica [C] (verified)	124
Maple [A] (verified)	124
Fricas [A] (verification not implemented)	125
Sympy [C] (verification not implemented)	125
Maxima [B] (verification not implemented)	126
Giac [A] (verification not implemented)	127
Mupad [B] (verification not implemented)	127

Optimal result

Integrand size = 16, antiderivative size = 94

$$\int \frac{x}{(a+b \tan(c+dx^2))^2} dx = \frac{(a^2 - b^2)x^2}{2(a^2 + b^2)^2} + \frac{ab \log(a \cos(c+dx^2) + b \sin(c+dx^2))}{(a^2 + b^2)^2 d} - \frac{b}{2(a^2 + b^2)d(a+b \tan(c+dx^2))}$$

[Out] 1/2*(a^2-b^2)*x^2/(a^2+b^2)^2+a*b*ln(a*cos(d*x^2+c)+b*sin(d*x^2+c))/(a^2+b^2)^2/d-1/2*b/(a^2+b^2)/d/(a+b*tan(d*x^2+c))

Rubi [A] (verified)

Time = 0.15 (sec) , antiderivative size = 94, normalized size of antiderivative = 1.00, number of steps used = 4, number of rules used = 4, $\frac{\text{number of rules}}{\text{integrand size}} = 0.250$, Rules used = {3832, 3564, 3612, 3611}

$$\int \frac{x}{(a+b \tan(c+dx^2))^2} dx = -\frac{b}{2d(a^2 + b^2)(a+b \tan(c+dx^2))} + \frac{ab \log(a \cos(c+dx^2) + b \sin(c+dx^2))}{d(a^2 + b^2)^2} + \frac{x^2(a^2 - b^2)}{2(a^2 + b^2)^2}$$

[In] Int[x/(a + b*Tan[c + d*x^2])^2,x]

[Out] ((a^2 - b^2)*x^2)/(2*(a^2 + b^2)^2) + (a*b*Log[a*Cos[c + d*x^2] + b*Sin[c + d*x^2]])/((a^2 + b^2)^2*d) - b/(2*(a^2 + b^2)*d*(a + b*Tan[c + d*x^2]))

Rule 3564

Int[((a_) + (b_)*tan[(c_) + (d_)*(x_)])^(n_), x_Symbol] :> Simp[b*((a + b*Tan[c + d*x])^(n + 1)/(d*(n + 1)*(a^2 + b^2))), x] + Dist[1/(a^2 + b^2),

Int[(a - b*Tan[c + d*x])*(a + b*Tan[c + d*x])^(n + 1), x], x] /; FreeQ[{a, b, c, d}, x] && NeQ[a^2 + b^2, 0] && LtQ[n, -1]

Rule 3611

Int[((c_) + (d_)*tan[(e_) + (f_)*(x_)])/((a_) + (b_)*tan[(e_) + (f_)*(x_)]), x_Symbol] := Simp[(c/(b*f))*Log[RemoveContent[a*Cos[e + f*x] + b*Sin[e + f*x], x]], x] /; FreeQ[{a, b, c, d, e, f}, x] && NeQ[b*c - a*d, 0] && NeQ[a^2 + b^2, 0] && EqQ[a*c + b*d, 0]

Rule 3612

Int[((c_) + (d_)*tan[(e_) + (f_)*(x_)])/((a_) + (b_)*tan[(e_) + (f_)*(x_)]), x_Symbol] := Simp[(a*c + b*d)*(x/(a^2 + b^2)), x] + Dist[(b*c - a*d)/(a^2 + b^2), Int[(b - a*Tan[e + f*x])/(a + b*Tan[e + f*x]), x], x] /; FreeQ[{a, b, c, d, e, f}, x] && NeQ[b*c - a*d, 0] && NeQ[a^2 + b^2, 0] && NeQ[a*c + b*d, 0]

Rule 3832

Int[(x_)^(m_)*((a_) + (b_)*Tan[(c_) + (d_)*(x_)^(n_)])^(p_), x_Symbol] := Dist[1/n, Subst[Int[x^(Simplify[(m + 1)/n] - 1)*(a + b*Tan[c + d*x])^p, x], x, x^n], x] /; FreeQ[{a, b, c, d, m, n, p}, x] && IGtQ[Simplify[(m + 1)/n], 0] && IntegerQ[p]

Rubi steps

$$\begin{aligned}
 \text{integral} &= \frac{1}{2} \text{Subst} \left(\int \frac{1}{(a + b \tan(c + dx))^2} dx, x, x^2 \right) \\
 &= -\frac{b}{2(a^2 + b^2)d(a + b \tan(c + dx^2))} + \frac{\text{Subst} \left(\int \frac{a - b \tan(c + dx)}{a + b \tan(c + dx)} dx, x, x^2 \right)}{2(a^2 + b^2)} \\
 &= \frac{(a^2 - b^2)x^2}{2(a^2 + b^2)^2} - \frac{b}{2(a^2 + b^2)d(a + b \tan(c + dx^2))} + \frac{(ab) \text{Subst} \left(\int \frac{b - a \tan(c + dx)}{a + b \tan(c + dx)} dx, x, x^2 \right)}{(a^2 + b^2)^2} \\
 &= \frac{(a^2 - b^2)x^2}{2(a^2 + b^2)^2} + \frac{ab \log(a \cos(c + dx^2) + b \sin(c + dx^2))}{(a^2 + b^2)^2 d} - \frac{b}{2(a^2 + b^2)d(a + b \tan(c + dx^2))}
 \end{aligned}$$

Mathematica [C] (verified)

Result contains complex when optimal does not.

Time = 0.99 (sec) , antiderivative size = 114, normalized size of antiderivative = 1.21

$$\int \frac{x}{(a + b \tan(c + dx^2))^2} dx$$

$$= \frac{-\frac{i \log(i - \tan(c + dx^2))}{(a + ib)^2} + \frac{i \log(i + \tan(c + dx^2))}{(a - ib)^2} + \frac{2b \left(2a \log(a + b \tan(c + dx^2)) - \frac{a^2 + b^2}{a + b \tan(c + dx^2)} \right)}{(a^2 + b^2)^2}}{4d}$$

[In] Integrate[x/(a + b*Tan[c + d*x^2])^2,x]

[Out] (((-I)*Log[I - Tan[c + d*x^2]])/(a + I*b)^2 + (I*Log[I + Tan[c + d*x^2]])/(a - I*b)^2 + (2*b*(2*a*Log[a + b*Tan[c + d*x^2]] - (a^2 + b^2)/(a + b*Tan[c + d*x^2])))/(a^2 + b^2)^2)/(4*d)

Maple [A] (verified)

Time = 0.15 (sec) , antiderivative size = 106, normalized size of antiderivative = 1.13

method	result
derivativdivides	$\frac{-\frac{b}{(a^2+b^2)(a+b \tan(dx^2+c))} + \frac{2ab \ln(a+b \tan(dx^2+c))}{(a^2+b^2)^2} + \frac{-ab \ln(1+\tan^2(dx^2+c)) + (a^2-b^2) \arctan(\tan(dx^2+c))}{(a^2+b^2)^2}}{2d}$
default	$\frac{-\frac{b}{(a^2+b^2)(a+b \tan(dx^2+c))} + \frac{2ab \ln(a+b \tan(dx^2+c))}{(a^2+b^2)^2} + \frac{-ab \ln(1+\tan^2(dx^2+c)) + (a^2-b^2) \arctan(\tan(dx^2+c))}{(a^2+b^2)^2}}{2d}$
norman	$\frac{\frac{(a^2-b^2)ax^2}{2a^4+4a^2b^2+2b^4} + \frac{b(a^2-b^2)x^2 \tan(dx^2+c)}{2a^4+4a^2b^2+2b^4} + \frac{b^2 \tan(dx^2+c)}{2a(a^2+b^2)d}}{a+b \tan(dx^2+c)} + \frac{ab \ln(a+b \tan(dx^2+c))}{d(a^4+2a^2b^2+b^4)} - \frac{ab \ln(1+\tan^2(dx^2+c))}{2d(a^4+2a^2b^2+b^4)}$
risch	$-\frac{x^2}{2(2iab-a^2+b^2)} - \frac{2iabx^2}{a^4+2a^2b^2+b^4} - \frac{2iabc}{d(a^4+2a^2b^2+b^4)} - \frac{ib^2}{(-ia+b)d(ia+b)^2 \left(e^{2i(dx^2+c)} b + ia e^{2i(dx^2+c)} - b + ia \right)}$
parallelrisc	$-\frac{-x^2 \tan(dx^2+c)a^2b^2d + x^2 \tan(dx^2+c)b^4d - x^2a^3bd + x^2ab^3d + \ln(1+\tan^2(dx^2+c)) \tan(dx^2+c)ab^3 - 2 \ln(a+b \tan(dx^2+c))}{2(a+b \tan(dx^2+c))(a^4+2a^2b^2+b^4)}$

[In] int(x/(a+b*tan(d*x^2+c))^2,x,method=_RETURNVERBOSE)

[Out] 1/2/d*(-b/(a^2+b^2)/(a+b*tan(d*x^2+c))+2*a*b/(a^2+b^2)^2*ln(a+b*tan(d*x^2+c)))+1/(a^2+b^2)^2*(-a*b*ln(1+tan(d*x^2+c)^2)+(a^2-b^2)*arctan(tan(d*x^2+c)))

Fricas [A] (verification not implemented)

none

Time = 0.25 (sec) , antiderivative size = 169, normalized size of antiderivative = 1.80

$$\int \frac{x}{(a + b \tan(c + dx^2))^2} dx$$

$$= \frac{(a^3 - ab^2)dx^2 - b^3 + (ab^2 \tan(dx^2 + c) + a^2b) \log\left(\frac{b^2 \tan(dx^2+c)^2 + 2ab \tan(dx^2+c) + a^2}{\tan(dx^2+c)^2 + 1}\right) + ((a^2b - b^3)dx^2 + ab^2)}{2((a^4b + 2a^2b^3 + b^5)d \tan(dx^2 + c) + (a^5 + 2a^3b^2 + ab^4)d)}$$

[In] integrate(x/(a+b*tan(d*x^2+c))^2,x, algorithm="fricas")

```
[Out] 1/2*((a^3 - a*b^2)*d*x^2 - b^3 + (a*b^2*tan(d*x^2 + c) + a^2*b)*log((b^2*tan(d*x^2 + c)^2 + 2*a*b*tan(d*x^2 + c) + a^2)/(tan(d*x^2 + c)^2 + 1)) + ((a^2*b - b^3)*d*x^2 + a*b^2)*tan(d*x^2 + c))/((a^4*b + 2*a^2*b^3 + b^5)*d*tan(d*x^2 + c) + (a^5 + 2*a^3*b^2 + a*b^4)*d)
```

Sympy [C] (verification not implemented)

Result contains complex when optimal does not.

Time = 0.78 (sec) , antiderivative size = 1584, normalized size of antiderivative = 16.85

$$\int \frac{x}{(a + b \tan(c + dx^2))^2} dx = \text{Too large to display}$$

[In] integrate(x/(a+b*tan(d*x**2+c))**2,x)

```
[Out] Piecewise((zoo*x**2/tan(c)**2, Eq(a, 0) & Eq(b, 0) & Eq(d, 0)), (x**2/(2*a**2), Eq(b, 0)), (- (atan(tan(c + d*x**2)) + pi*floor((c + d*x**2 - pi/2)/pi)) * tan(c + d*x**2)**2 / (8*b**2*d*tan(c + d*x**2)**2 - 16*I*b**2*d*tan(c + d*x**2) - 8*b**2*d) + 2*I*(atan(tan(c + d*x**2)) + pi*floor((c + d*x**2 - pi/2)/pi)) * tan(c + d*x**2) / (8*b**2*d*tan(c + d*x**2)**2 - 16*I*b**2*d*tan(c + d*x**2) - 8*b**2*d) + (atan(tan(c + d*x**2)) + pi*floor((c + d*x**2 - pi/2)/pi)) / (8*b**2*d*tan(c + d*x**2)**2 - 16*I*b**2*d*tan(c + d*x**2) - 8*b**2*d) + 2*I / (8*b**2*d*tan(c + d*x**2)**2 - 16*I*b**2*d*tan(c + d*x**2) - 8*b**2*d), Eq(a, -I*b)), (- (atan(tan(c + d*x**2)) + pi*floor((c + d*x**2 - pi/2)/pi)) * tan(c + d*x**2)**2 / (8*b**2*d*tan(c + d*x**2)**2 + 16*I*b**2*d*tan(c + d*x**2) - 8*b**2*d) - 2*I*(atan(tan(c + d*x**2)) + pi*floor((c + d*x**2 - pi/2)/pi)) * tan(c + d*x**2) / (8*b**2*d*tan(c + d*x**2)**2 + 16*I*b**2*d*tan(c + d*x**2) - 8*b**2*d) + (atan(tan(c + d*x**2)) + pi*floor((c + d*x**2 - pi/2)/pi)) / (8*b**2*d*tan(c + d*x**2)**2 + 16*I*b**2*d*tan(c + d*x**2) - 8*b**2*d) - tan(c + d*x**2) / (8*b**2*d*tan(c + d*x**2)**2 + 16*I*b**2
```

```

*d*tan(c + d*x**2) - 8*b**2*d) - 2*I/(8*b**2*d*tan(c + d*x**2)**2 + 16*I*b*
**2*d*tan(c + d*x**2) - 8*b**2*d), Eq(a, I*b)), (x**2/(2*(a + b*tan(c))**2),
Eq(d, 0)), (a**3*d*x**2/(2*a**5*d + 2*a**4*b*d*tan(c + d*x**2) + 4*a**3*b*
**2*d + 4*a**2*b**3*d*tan(c + d*x**2) + 2*a*b**4*d + 2*b**5*d*tan(c + d*x**2
)) + a**2*b*d*x**2*tan(c + d*x**2)/(2*a**5*d + 2*a**4*b*d*tan(c + d*x**2) +
4*a**3*b**2*d + 4*a**2*b**3*d*tan(c + d*x**2) + 2*a*b**4*d + 2*b**5*d*tan(
c + d*x**2)) + 2*a**2*b*log(a/b + tan(c + d*x**2))/(2*a**5*d + 2*a**4*b*d*t
an(c + d*x**2) + 4*a**3*b**2*d + 4*a**2*b**3*d*tan(c + d*x**2) + 2*a*b**4*d
+ 2*b**5*d*tan(c + d*x**2)) - a**2*b*log(tan(c + d*x**2)**2 + 1)/(2*a**5*d
+ 2*a**4*b*d*tan(c + d*x**2) + 4*a**3*b**2*d + 4*a**2*b**3*d*tan(c + d*x**
2) + 2*a*b**4*d + 2*b**5*d*tan(c + d*x**2)) - a**2*b/(2*a**5*d + 2*a**4*b*d
*tan(c + d*x**2) + 4*a**3*b**2*d + 4*a**2*b**3*d*tan(c + d*x**2) + 2*a*b**4
*d + 2*b**5*d*tan(c + d*x**2)) - a*b**2*d*x**2/(2*a**5*d + 2*a**4*b*d*tan(c
+ d*x**2) + 4*a**3*b**2*d + 4*a**2*b**3*d*tan(c + d*x**2) + 2*a*b**4*d + 2
*b**5*d*tan(c + d*x**2)) + 2*a*b**2*log(a/b + tan(c + d*x**2))*tan(c + d*x*
**2)/(2*a**5*d + 2*a**4*b*d*tan(c + d*x**2) + 4*a**3*b**2*d + 4*a**2*b**3*d*
tan(c + d*x**2) + 2*a*b**4*d + 2*b**5*d*tan(c + d*x**2)) - a*b**2*log(tan(c
+ d*x**2)**2 + 1)*tan(c + d*x**2)/(2*a**5*d + 2*a**4*b*d*tan(c + d*x**2) +
4*a**3*b**2*d + 4*a**2*b**3*d*tan(c + d*x**2) + 2*a*b**4*d + 2*b**5*d*tan(
c + d*x**2)) - b**3*d*x**2*tan(c + d*x**2)/(2*a**5*d + 2*a**4*b*d*tan(c + d
*x**2) + 4*a**3*b**2*d + 4*a**2*b**3*d*tan(c + d*x**2) + 2*a*b**4*d + 2*b**
5*d*tan(c + d*x**2)) - b**3/(2*a**5*d + 2*a**4*b*d*tan(c + d*x**2) + 4*a**3
*b**2*d + 4*a**2*b**3*d*tan(c + d*x**2) + 2*a*b**4*d + 2*b**5*d*tan(c + d*x
**2)), True))

```

Maxima [B] (verification not implemented)

Leaf count of result is larger than twice the leaf count of optimal. 556 vs. $2(90) = 180$.

Time = 0.37 (sec) , antiderivative size = 556, normalized size of antiderivative = 5.91

$$\int \frac{x}{(a + b \tan(c + dx^2))^2} dx$$

$$= \frac{(a^4 - b^4)dx^2 \cos(2dx^2 + 2c)^2 + (a^4 - b^4)dx^2 \sin(2dx^2 + 2c)^2 + (a^4 - b^4)dx^2 - 2(2ab^3 - (a^4 - 2a^2b^2 + b^4)dx^2 \cos(2dx^2 + 2c)) \log((a^2 + b^2) \cos(2dx^2 + 2c)^2 + 4ab \sin(2dx^2 + 2c) + (a^2 + b^2) \sin(2dx^2 + 2c)^2 + a^2 + b^2 + 2((a^6 + 3a^4b^2 - 3a^2b^4 - b^6) \cos(2dx^2 + 2c) + (a^6 + 3a^4b^2 - 3a^2b^4 - b^6) \sin(2dx^2 + 2c))}{2((a^6 + 3a^4b^2 - 3a^2b^4 - b^6) \cos(2dx^2 + 2c) + (a^6 + 3a^4b^2 - 3a^2b^4 - b^6) \sin(2dx^2 + 2c))}$$

[In] integrate(x/(a+b*tan(d*x^2+c))^2,x, algorithm="maxima")

```

[Out] 1/2*((a^4 - b^4)*d*x^2*cos(2*d*x^2 + 2*c)^2 + (a^4 - b^4)*d*x^2*sin(2*d*x^2
+ 2*c)^2 + (a^4 - b^4)*d*x^2 - 2*(2*a*b^3 - (a^4 - 2*a^2*b^2 + b^4)*d*x^2)
*cos(2*d*x^2 + 2*c) + (4*a^2*b^2*sin(2*d*x^2 + 2*c) + a^3*b + a*b^3 + (a^3*b
+ a*b^3)*cos(2*d*x^2 + 2*c)^2 + (a^3*b + a*b^3)*sin(2*d*x^2 + 2*c)^2 + 2*
(a^3*b - a*b^3)*cos(2*d*x^2 + 2*c))*log(((a^2 + b^2)*cos(2*d*x^2 + 2*c)^2 +
4*a*b*sin(2*d*x^2 + 2*c) + (a^2 + b^2)*sin(2*d*x^2 + 2*c)^2 + a^2 + b^2 +

```

$$\frac{2*(a^2 - b^2)*\cos(2*d*x^2 + 2*c)}{((a^2 + b^2)*\cos(2*c)^2 + (a^2 + b^2)*\sin(2*c)^2)} + \frac{2*(a^2*b^2 - b^4 + 2*(a^3*b - a*b^3)*d*x^2)*\sin(2*d*x^2 + 2*c)}{((a^6 + 3*a^4*b^2 + 3*a^2*b^4 + b^6)*d*\cos(2*d*x^2 + 2*c)^2 + (a^6 + 3*a^4*b^2 + 3*a^2*b^4 + b^6)*d*\sin(2*d*x^2 + 2*c)^2 + 2*(a^6 + a^4*b^2 - a^2*b^4 - b^6)*d*\cos(2*d*x^2 + 2*c) + 4*(a^5*b + 2*a^3*b^3 + a*b^5)*d*\sin(2*d*x^2 + 2*c) + (a^6 + 3*a^4*b^2 + 3*a^2*b^4 + b^6)*d}$$

Giac [A] (verification not implemented)

none

Time = 0.36 (sec) , antiderivative size = 159, normalized size of antiderivative = 1.69

$$\int \frac{x}{(a + b \tan(c + dx^2))^2} dx = \frac{ab^2 \log(|b \tan(dx^2 + c) + a|)}{a^4bd + 2a^2b^3d + b^5d} - \frac{ab \log(\tan(dx^2 + c)^2 + 1)}{2(a^4d + 2a^2b^2d + b^4d)} + \frac{(dx^2 + c)(a^2 - b^2)}{2(a^4d + 2a^2b^2d + b^4d)} - \frac{a^2b + b^3}{2(a^2 + b^2)^2(b \tan(dx^2 + c) + a)d}$$

[In] integrate(x/(a+b*tan(d*x^2+c))^2,x, algorithm="giac")

[Out] a*b^2*log(abs(b*tan(d*x^2 + c) + a))/(a^4*b*d + 2*a^2*b^3*d + b^5*d) - 1/2*a*b*log(tan(d*x^2 + c)^2 + 1)/(a^4*d + 2*a^2*b^2*d + b^4*d) + 1/2*(d*x^2 + c)*(a^2 - b^2)/(a^4*d + 2*a^2*b^2*d + b^4*d) - 1/2*(a^2*b + b^3)/((a^2 + b^2)^2*(b*tan(d*x^2 + c) + a)*d)

Mupad [B] (verification not implemented)

Time = 3.86 (sec) , antiderivative size = 173, normalized size of antiderivative = 1.84

$$\int \frac{x}{(a + b \tan(c + dx^2))^2} dx = \frac{\frac{x^2 \tan(dx^2+c) \left(\frac{a^2b}{2} - \frac{b^3}{2}\right)}{(a^2+b^2)^2} - \frac{x^2 \left(\frac{ab^2}{2} - \frac{a^3}{2}\right)}{(a^2+b^2)^2} + \frac{b^2 \tan(dx^2+c)}{2ad(a^2+b^2)}}{a + b \tan(dx^2 + c)} - \frac{ab \ln(\tan(dx^2 + c)^2 + 1)}{2(da^4 + 2da^2b^2 + db^4)} + \frac{ab \ln(a + b \tan(dx^2 + c))}{d(a^2 + b^2)^2}$$

[In] int(x/(a + b*tan(c + d*x^2))^2,x)

[Out] ((x^2*tan(c + d*x^2)*((a^2*b)/2 - b^3/2))/(a^2 + b^2)^2 - (x^2*((a*b^2)/2 - a^3/2))/(a^2 + b^2)^2 + (b^2*tan(c + d*x^2))/(2*a*d*(a^2 + b^2)))/(a + b*tan(c + d*x^2)) - (a*b*log(tan(c + d*x^2)^2 + 1))/(2*(a^4*d + b^4*d + 2*a^2*b^2*d)) + (a*b*log(a + b*tan(c + d*x^2)))/(d*(a^2 + b^2)^2)

$$3.22 \quad \int \frac{1}{(a+b \tan(c+dx^2))^2} dx$$

Optimal result	128
Rubi [N/A]	128
Mathematica [N/A]	129
Maple [N/A] (verified)	129
Fricas [N/A]	129
Sympy [N/A]	129
Maxima [N/A]	130
Giac [N/A]	131
Mupad [N/A]	131

Optimal result

Integrand size = 14, antiderivative size = 14

$$\int \frac{1}{(a+b \tan(c+dx^2))^2} dx = \text{Int}\left(\frac{1}{(a+b \tan(c+dx^2))^2}, x\right)$$

[Out] Unintegrable(1/(a+b*tan(d*x^2+c))^2,x)

Rubi [N/A]

Not integrable

Time = 0.01 (sec) , antiderivative size = 14, normalized size of antiderivative = 1.00, number of steps used = 0, number of rules used = 0, $\frac{\text{number of rules}}{\text{integrand size}} = 0.000$, Rules used = {}

$$\int \frac{1}{(a+b \tan(c+dx^2))^2} dx = \int \frac{1}{(a+b \tan(c+dx^2))^2} dx$$

[In] Int[(a + b*Tan[c + d*x^2])^(-2), x]

[Out] Defer[Int] [(a + b*Tan[c + d*x^2])^(-2), x]

Rubi steps

$$\text{integral} = \int \frac{1}{(a+b \tan(c+dx^2))^2} dx$$

Mathematica [N/A]

Not integrable

Time = 6.81 (sec) , antiderivative size = 16, normalized size of antiderivative = 1.14

$$\int \frac{1}{(a + b \tan(c + dx^2))^2} dx = \int \frac{1}{(a + b \tan(c + dx^2))^2} dx$$

[In] Integrate[(a + b*Tan[c + d*x^2])^(-2), x]

[Out] Integrate[(a + b*Tan[c + d*x^2])^(-2), x]

Maple [N/A] (verified)

Not integrable

Time = 0.18 (sec) , antiderivative size = 14, normalized size of antiderivative = 1.00

$$\int \frac{1}{(a + b \tan(dx^2 + c))^2} dx$$

[In] int(1/(a+b*tan(d*x^2+c))^2,x)

[Out] int(1/(a+b*tan(d*x^2+c))^2,x)

Fricas [N/A]

Not integrable

Time = 0.24 (sec) , antiderivative size = 34, normalized size of antiderivative = 2.43

$$\int \frac{1}{(a + b \tan(c + dx^2))^2} dx = \int \frac{1}{(b \tan(dx^2 + c) + a)^2} dx$$

[In] integrate(1/(a+b*tan(d*x^2+c))^2,x, algorithm="fricas")

[Out] integral(1/(b^2*tan(d*x^2 + c)^2 + 2*a*b*tan(d*x^2 + c) + a^2), x)

Sympy [N/A]

Not integrable

Time = 0.61 (sec) , antiderivative size = 15, normalized size of antiderivative = 1.07

$$\int \frac{1}{(a + b \tan(c + dx^2))^2} dx = \int \frac{1}{(a + b \tan(c + dx^2))^2} dx$$

[In] integrate(1/(a+b*tan(d*x**2+c))**2,x)

[Out] Integral((a + b*tan(c + d*x**2))**(-2), x)

Maxima [N/A]

Not integrable

Time = 1.42 (sec) , antiderivative size = 2550, normalized size of antiderivative = 182.14

$$\int \frac{1}{(a + b \tan(c + dx^2))^2} dx = \int \frac{1}{(b \tan(dx^2 + c) + a)^2} dx$$

```
[In] integrate(1/(a+b*tan(d*x^2+c))^2,x, algorithm="maxima")
```

```
[Out] ((a^6 + a^4*b^2)*d*x^2*cos(2*d*x^2 + 2*c)^2 + (a^6 + a^4*b^2)*d*x^2*sin(2*d*x^2 + 2*c)^2 + (a^6 + a^4*b^2 - a^2*b^4 - b^6)*d*x^2 - (b^6*sin(2*c) + ((a^4*b^2 + 5*a^2*b^4 - b^6)*cos(2*c) - 2*(a^5*b - 2*a*b^5)*sin(2*c))*d*x^2 + 2*(a^3*b^3 + a*b^5)*cos(2*c))*cos(2*d*x^2) - (((a^2*b^4 + b^6)*cos(2*c) - 2*(a^5*b + 2*a^3*b^3 + a*b^5)*sin(2*c))*d*x^2*cos(2*d*x^2) - (2*(a^5*b + 2*a^3*b^3 + a*b^5)*cos(2*c) + (a^2*b^4 + b^6)*sin(2*c))*d*x^2*sin(2*d*x^2) - (2*a^6 + 2*a^4*b^2 + 3*a^2*b^4 + b^6)*d*x^2)*cos(2*d*x^2 + 2*c) - (a^8*d*x*cos(2*d*x^2 + 2*c)^2 + a^8*d*x*sin(2*d*x^2 + 2*c)^2 + ((4*a^6*b^2 + 8*a^4*b^4 + 4*a^2*b^6 + b^8)*cos(2*c)^2 + (4*a^6*b^2 + 8*a^4*b^4 + 4*a^2*b^6 + b^8)*sin(2*c)^2)*d*x*cos(2*d*x^2)^2 + ((4*a^6*b^2 + 8*a^4*b^4 + 4*a^2*b^6 + b^8)*cos(2*c)^2 + (4*a^6*b^2 + 8*a^4*b^4 + 4*a^2*b^6 + b^8)*sin(2*c)^2)*d*x*sin(2*d*x^2)^2 - 2*((a^4*b^4 + 2*a^2*b^6 + b^8)*cos(2*c) - 2*(a^7*b + 3*a^5*b^3 + 3*a^3*b^5 + a*b^7)*sin(2*c))*d*x*cos(2*d*x^2) + 2*(2*(a^7*b + 3*a^5*b^3 + 3*a^3*b^5 + a*b^7)*cos(2*c) + (a^4*b^4 + 2*a^2*b^6 + b^8)*sin(2*c))*d*x*sin(2*d*x^2) + (a^8 + 4*a^6*b^2 + 6*a^4*b^4 + 4*a^2*b^6 + b^8)*d*x - 2*((a^4*b^4*cos(2*c) - 2*(a^7*b + a^5*b^3)*sin(2*c))*d*x*cos(2*d*x^2) - (a^4*b^4*sin(2*c) + 2*(a^7*b + a^5*b^3)*cos(2*c))*d*x*sin(2*d*x^2) - (a^8 + 2*a^6*b^2 + a^4*b^4)*d*x)*cos(2*d*x^2 + 2*c) - 2*((a^4*b^4*sin(2*c) + 2*(a^7*b + a^5*b^3)*cos(2*c))*d*x*cos(2*d*x^2) + (a^4*b^4*cos(2*c) - 2*(a^7*b + a^5*b^3)*sin(2*c))*d*x*sin(2*d*x^2))*sin(2*d*x^2 + 2*c))*integrate((b^6*sin(2*c) - 4*(a*b^5*sin(2*c) + 2*(a^4*b^2 + a^2*b^4)*cos(2*c))*d*x^2 + 2*(a^3*b^3 + a*b^5)*cos(2*c))*cos(2*d*x^2) + (b^6*cos(2*c) - 4*(a*b^5*cos(2*c) - 2*(a^4*b^2 + a^2*b^4)*sin(2*c))*d*x^2 - 2*(a^3*b^3 + a*b^5)*sin(2*c))*sin(2*d*x^2) + (4*a^5*b*d*x^2 - a^4*b^2)*sin(2*d*x^2 + 2*c))/(a^8*d*x^2*cos(2*d*x^2 + 2*c)^2 + a^8*d*x^2*sin(2*d*x^2 + 2*c)^2 + ((4*a^6*b^2 + 8*a^4*b^4 + 4*a^2*b^6 + b^8)*cos(2*c)^2 + (4*a^6*b^2 + 8*a^4*b^4 + 4*a^2*b^6 + b^8)*sin(2*c)^2)*d*x^2*cos(2*d*x^2)^2 + ((4*a^6*b^2 + 8*a^4*b^4 + 4*a^2*b^6 + b^8)*cos(2*c)^2 + (4*a^6*b^2 + 8*a^4*b^4 + 4*a^2*b^6 + b^8)*sin(2*c)^2)*d*x^2*sin(2*d*x^2)^2 - 2*((a^4*b^4 + 2*a^2*b^6 + b^8)*cos(2*c) - 2*(a^7*b + 3*a^5*b^3 + 3*a^3*b^5 + a*b^7)*sin(2*c))*d*x^2*cos(2*d*x^2) + 2*(2*(a^7*b + 3*a^5*b^3 + 3*a^3*b^5 + a*b^7)*cos(2*c) + (a^4*b^4 + 2*a^2*b^6 + b^8)*sin(2*c))*d*x^2*sin(2*d*x^2) + (a^8 + 4*a^6*b^2 + 6*a^4*b^4 + 4*a^2*b^6 + b^8)*d*x^2 - 2*((a^4*b^4*cos(2*c) - 2*(a^7*b + a^5*b^3)*sin(2*c))*d*x^2*cos(2*d*x^2) - (a^4*b^4*sin(2*c) + 2*(a^7*b + a^5*b^3)*cos(2*c))*d*x^2*sin(2*d*x^2) - (a^8 + 2*a^6*b^2 + a^4*b^4)*d*x^2)*cos(2*d*x^2 + 2*c) - 2*((a^4*b^4*sin(2*c) + 2*(a^7*b + a^5*b^3)*cos(2*c))*d*x^2*cos(2*d*x^2) + (a^4*b^4*cos(2*c) - 2*(a^7*b + a^5*b^3)*sin(2*c))*d*x^2*sin(2*d*x^2))*sin(2*d*x^2 + 2*c))
```

```

*b + a^5*b^3)*cos(2*c))*d*x^2*cos(2*d*x^2) + (a^4*b^4*cos(2*c) - 2*(a^7*b +
a^5*b^3)*sin(2*c))*d*x^2*sin(2*d*x^2))*sin(2*d*x^2 + 2*c)), x) - (b^6*cos(
2*c) - (2*(a^5*b - 2*a*b^5)*cos(2*c) + (4*a^4*b^2 + 5*a^2*b^4 - b^6)*sin(2*
c))*d*x^2 - 2*(a^3*b^3 + a*b^5)*sin(2*c))*sin(2*d*x^2) + (2*a^5*b*d*x^2 + a
^4*b^2 - (2*(a^5*b + 2*a^3*b^3 + a*b^5)*cos(2*c) + (a^2*b^4 + b^6)*sin(2*c)
)*d*x^2*cos(2*d*x^2) - ((a^2*b^4 + b^6)*cos(2*c) - 2*(a^5*b + 2*a^3*b^3 + a
*b^5)*sin(2*c))*d*x^2*sin(2*d*x^2))*sin(2*d*x^2 + 2*c))/(a^8*d*x*cos(2*d*x^
2 + 2*c)^2 + a^8*d*x*sin(2*d*x^2 + 2*c)^2 + ((4*a^6*b^2 + 8*a^4*b^4 + 4*a^2
*b^6 + b^8)*cos(2*c)^2 + (4*a^6*b^2 + 8*a^4*b^4 + 4*a^2*b^6 + b^8)*sin(2*c)
^2)*d*x*cos(2*d*x^2)^2 + ((4*a^6*b^2 + 8*a^4*b^4 + 4*a^2*b^6 + b^8)*cos(2*c)
)^2 + (4*a^6*b^2 + 8*a^4*b^4 + 4*a^2*b^6 + b^8)*sin(2*c)^2)*d*x*sin(2*d*x^2
)^2 - 2*((a^4*b^4 + 2*a^2*b^6 + b^8)*cos(2*c) - 2*(a^7*b + 3*a^5*b^3 + 3*a^
3*b^5 + a*b^7)*sin(2*c))*d*x*cos(2*d*x^2) + 2*(2*(a^7*b + 3*a^5*b^3 + 3*a^
3*b^5 + a*b^7)*cos(2*c) + (a^4*b^4 + 2*a^2*b^6 + b^8)*sin(2*c))*d*x*sin(2*d*
x^2) + (a^8 + 4*a^6*b^2 + 6*a^4*b^4 + 4*a^2*b^6 + b^8)*d*x - 2*((a^4*b^4*co
s(2*c) - 2*(a^7*b + a^5*b^3)*sin(2*c))*d*x*cos(2*d*x^2) - (a^4*b^4*sin(2*c)
+ 2*(a^7*b + a^5*b^3)*cos(2*c))*d*x*sin(2*d*x^2) - (a^8 + 2*a^6*b^2 + a^4*
b^4)*d*x)*cos(2*d*x^2 + 2*c) - 2*((a^4*b^4*sin(2*c) + 2*(a^7*b + a^5*b^3)*c
os(2*c))*d*x*cos(2*d*x^2) + (a^4*b^4*cos(2*c) - 2*(a^7*b + a^5*b^3)*sin(2*c)
))*d*x*sin(2*d*x^2))*sin(2*d*x^2 + 2*c))

```

Giac [N/A]

Not integrable

Time = 0.43 (sec) , antiderivative size = 16, normalized size of antiderivative = 1.14

$$\int \frac{1}{(a + b \tan(c + dx^2))^2} dx = \int \frac{1}{(b \tan(dx^2 + c) + a)^2} dx$$

```
[In] integrate(1/(a+b*tan(d*x^2+c))^2,x, algorithm="giac")
```

```
[Out] integrate((b*tan(d*x^2 + c) + a)^(-2), x)
```

Mupad [N/A]

Not integrable

Time = 4.28 (sec) , antiderivative size = 16, normalized size of antiderivative = 1.14

$$\int \frac{1}{(a + b \tan(c + dx^2))^2} dx = \int \frac{1}{(a + b \tan(dx^2 + c))^2} dx$$

```
[In] int(1/(a + b*tan(c + d*x^2))^2,x)
```

```
[Out] int(1/(a + b*tan(c + d*x^2))^2, x)
```

3.23

$$\int \frac{1}{x(a+b \tan(c+dx^2))^2} dx$$

Optimal result	132
Rubi [N/A]	132
Mathematica [N/A]	133
Maple [N/A] (verified)	133
Fricas [N/A]	133
Sympy [N/A]	133
Maxima [N/A]	134
Giac [N/A]	136
Mupad [N/A]	136

Optimal result

Integrand size = 18, antiderivative size = 18

$$\int \frac{1}{x(a+b \tan(c+dx^2))^2} dx = \text{Int}\left(\frac{1}{x(a+b \tan(c+dx^2))^2}, x\right)$$

[Out] Unintegrable(1/x/(a+b*tan(d*x^2+c))^2,x)

Rubi [N/A]

Not integrable

Time = 0.03 (sec) , antiderivative size = 18, normalized size of antiderivative = 1.00, number of steps used = 0, number of rules used = 0, $\frac{\text{number of rules}}{\text{integrand size}} = 0.000$, Rules used = {}

$$\int \frac{1}{x(a+b \tan(c+dx^2))^2} dx = \int \frac{1}{x(a+b \tan(c+dx^2))^2} dx$$

[In] Int[1/(x*(a + b*Tan[c + d*x^2])^2),x]

[Out] Defer[Int][1/(x*(a + b*Tan[c + d*x^2])^2), x]

Rubi steps

$$\text{integral} = \int \frac{1}{x(a+b \tan(c+dx^2))^2} dx$$

Mathematica [N/A]

Not integrable

Time = 12.87 (sec) , antiderivative size = 20, normalized size of antiderivative = 1.11

$$\int \frac{1}{x(a + b \tan(c + dx^2))^2} dx = \int \frac{1}{x(a + b \tan(c + dx^2))^2} dx$$

[In] Integrate[1/(x*(a + b*Tan[c + d*x^2])^2), x]

[Out] Integrate[1/(x*(a + b*Tan[c + d*x^2])^2), x]

Maple [N/A] (verified)

Not integrable

Time = 0.21 (sec) , antiderivative size = 18, normalized size of antiderivative = 1.00

$$\int \frac{1}{x(a + b \tan(dx^2 + c))^2} dx$$

[In] int(1/x/(a+b*tan(d*x^2+c))^2,x)

[Out] int(1/x/(a+b*tan(d*x^2+c))^2,x)

Fricas [N/A]

Not integrable

Time = 0.24 (sec) , antiderivative size = 38, normalized size of antiderivative = 2.11

$$\int \frac{1}{x(a + b \tan(c + dx^2))^2} dx = \int \frac{1}{(b \tan(dx^2 + c) + a)^2 x} dx$$

[In] integrate(1/x/(a+b*tan(d*x^2+c))^2,x, algorithm="fricas")

[Out] integral(1/(b^2*x*tan(d*x^2 + c)^2 + 2*a*b*x*tan(d*x^2 + c) + a^2*x), x)

Sympy [N/A]

Not integrable

Time = 1.14 (sec) , antiderivative size = 17, normalized size of antiderivative = 0.94

$$\int \frac{1}{x(a + b \tan(c + dx^2))^2} dx = \int \frac{1}{x(a + b \tan(c + dx^2))^2} dx$$

[In] integrate(1/x/(a+b*tan(d*x**2+c))**2,x)

[Out] Integral(1/(x*(a + b*tan(c + d*x**2))**2), x)

Maxima [N/A]

Not integrable

Time = 1.32 (sec) , antiderivative size = 3616, normalized size of antiderivative = 200.89

$$\int \frac{1}{x(a + b \tan(c + dx^2))^2} dx = \int \frac{1}{(b \tan(dx^2 + c) + a)^2 x} dx$$

[In] integrate(1/x/(a+b*tan(d*x^2+c))^2,x, algorithm="maxima")

[Out] (((4*a^8*b^2 + 4*a^6*b^4 - 4*a^4*b^6 - 3*a^2*b^8 - b^10)*cos(2*c)^2 + (4*a^8*b^2 + 4*a^6*b^4 - 4*a^4*b^6 - 3*a^2*b^8 - b^10)*sin(2*c)^2)*d*x^2*cos(2*d*x^2)^2*log(x) + (a^10 - a^8*b^2)*d*x^2*cos(2*d*x^2 + 2*c)^2*log(x) + ((4*a^8*b^2 + 4*a^6*b^4 - 4*a^4*b^6 - 3*a^2*b^8 - b^10)*cos(2*c)^2 + (4*a^8*b^2 + 4*a^6*b^4 - 4*a^4*b^6 - 3*a^2*b^8 - b^10)*sin(2*c)^2)*d*x^2*log(x)*sin(2*d*x^2)^2 + (a^10 - a^8*b^2)*d*x^2*log(x)*sin(2*d*x^2 + 2*c)^2 + (a^10 + 3*a^8*b^2 + 2*a^6*b^4 - 2*a^4*b^6 - 3*a^2*b^8 - b^10)*d*x^2*log(x) - (2*((a^6*b^4 + a^4*b^6 - a^2*b^8 - b^10)*cos(2*c) - 2*(a^9*b + 2*a^7*b^3 - 2*a^3*b^7 - a*b^9)*sin(2*c))*d*x^2*log(x) + 2*(a^7*b^3 + 3*a^5*b^5 + 3*a^3*b^7 + a*b^9)*cos(2*c) + (a^4*b^6 + 2*a^2*b^8 + b^10)*sin(2*c))*cos(2*d*x^2) - 2*((a^6*b^4 - a^4*b^6)*cos(2*c) - 2*(a^9*b - a^5*b^5)*sin(2*c))*d*x^2*cos(2*d*x^2)*log(x) - (2*(a^9*b - a^5*b^5)*cos(2*c) + (a^6*b^4 - a^4*b^6)*sin(2*c))*d*x^2*log(x)*sin(2*d*x^2) - (a^10 + a^8*b^2 - a^6*b^4 - a^4*b^6)*d*x^2*log(x))*cos(2*d*x^2 + 2*c) - (((4*a^10*b^2 + 16*a^8*b^4 + 24*a^6*b^6 + 17*a^4*b^8 + 6*a^2*b^10 + b^12)*cos(2*c)^2 + (4*a^10*b^2 + 16*a^8*b^4 + 24*a^6*b^6 + 17*a^4*b^8 + 6*a^2*b^10 + b^12)*sin(2*c)^2)*d*x^2*cos(2*d*x^2)^2 + (a^12 + 2*a^10*b^2 + a^8*b^4)*d*x^2*cos(2*d*x^2 + 2*c)^2 + ((4*a^10*b^2 + 16*a^8*b^4 + 24*a^6*b^6 + 17*a^4*b^8 + 6*a^2*b^10 + b^12)*cos(2*c)^2 + (4*a^10*b^2 + 16*a^8*b^4 + 24*a^6*b^6 + 17*a^4*b^8 + 6*a^2*b^10 + b^12)*sin(2*c)^2)*d*x^2*sin(2*d*x^2)^2 + (a^12 + 2*a^10*b^2 + a^8*b^4)*d*x^2*sin(2*d*x^2 + 2*c)^2 - 2*((a^8*b^4 + 4*a^6*b^6 + 6*a^4*b^8 + 4*a^2*b^10 + b^12)*cos(2*c) - 2*(a^11*b + 5*a^9*b^3 + 10*a^7*b^5 + 10*a^5*b^7 + 5*a^3*b^9 + a*b^11)*sin(2*c))*d*x^2*cos(2*d*x^2) + 2*(2*(a^11*b + 5*a^9*b^3 + 10*a^7*b^5 + 10*a^5*b^7 + 5*a^3*b^9 + a*b^11)*cos(2*c) + (a^8*b^4 + 4*a^6*b^6 + 6*a^4*b^8 + 4*a^2*b^10 + b^12)*sin(2*c))*d*x^2*sin(2*d*x^2) + (a^12 + 6*a^10*b^2 + 15*a^8*b^4 + 20*a^6*b^6 + 15*a^4*b^8 + 6*a^2*b^10 + b^12)*d*x^2 - 2*((a^8*b^4 + 2*a^6*b^6 + a^4*b^8)*cos(2*c) - 2*(a^11*b + 3*a^9*b^3 + 3*a^7*b^5 + a^5*b^7)*sin(2*c))*d*x^2*cos(2*d*x^2) - (2*(a^11*b + 3*a^9*b^3 + 3*a^7*b^5 + a^5*b^7)*cos(2*c) + (a^8*b^4 + 2*a^6*b^6 + a^4*b^8)*sin(2*c))*d*x^2*sin(2*d*x^2) - (a^12 + 4*a^10*b^2 + 6*a^8*b^4 + 4*a^6*b^6 + a^4*b^8)*d*x^2*cos(2*d*x^2 + 2*c) - 2*((2*(a^11*b + 3*a^9*b^3 + 3*a^7*b^5 + a^5*b^7)*cos(2*c) + (a^8*b^4 + 2*a^6*b^6 + a^4*b^8)*sin(2*c))*d*x^2*cos(2*d*x^2) + ((a^8*b^4 + 2*a^6*b^6 + a^4*b^8)*cos(2*c) - 2*(a^11*b + 3*a^9*b^3 + 3*a^7*b^5 + a^5*b^7)*sin(2*c))*d*x^2*sin(2*d*x^2))*sin(2*d*x^2 + 2*c))*integrate(2*((b^6*sin(2*c) - 2*(a*b^5*sin(2*c) + 2*(a^4*b^2 + a^2*b^4)*cos(2*c))*d*x^2 + 2*(a^3*b^3 + a*b^5)*

$$\begin{aligned}
& \cos(2*c)) * \cos(2*d*x^2) + (b^6 * \cos(2*c) - 2*(a*b^5 * \cos(2*c) - 2*(a^4*b^2 + a \\
& ^2*b^4) * \sin(2*c)) * d*x^2 - 2*(a^3*b^3 + a*b^5) * \sin(2*c)) * \sin(2*d*x^2) + (2*a \\
& ^5*b*d*x^2 - a^4*b^2) * \sin(2*d*x^2 + 2*c)) / (a^8*d*x^3 * \cos(2*d*x^2 + 2*c)^2 + \\
& a^8*d*x^3 * \sin(2*d*x^2 + 2*c)^2 + ((4*a^6*b^2 + 8*a^4*b^4 + 4*a^2*b^6 + b^8 \\
&) * \cos(2*c)^2 + (4*a^6*b^2 + 8*a^4*b^4 + 4*a^2*b^6 + b^8) * \sin(2*c)^2) * d*x^3 * \\
& \cos(2*d*x^2)^2 + ((4*a^6*b^2 + 8*a^4*b^4 + 4*a^2*b^6 + b^8) * \cos(2*c)^2 + (4 \\
& *a^6*b^2 + 8*a^4*b^4 + 4*a^2*b^6 + b^8) * \sin(2*c)^2) * d*x^3 * \sin(2*d*x^2)^2 - \\
& 2*((a^4*b^4 + 2*a^2*b^6 + b^8) * \cos(2*c) - 2*(a^7*b + 3*a^5*b^3 + 3*a^3*b^5 \\
& + a*b^7) * \sin(2*c)) * d*x^3 * \cos(2*d*x^2) + 2*(2*(a^7*b + 3*a^5*b^3 + 3*a^3*b^5 \\
& + a*b^7) * \cos(2*c) + (a^4*b^4 + 2*a^2*b^6 + b^8) * \sin(2*c)) * d*x^3 * \sin(2*d*x^ \\
& 2) + (a^8 + 4*a^6*b^2 + 6*a^4*b^4 + 4*a^2*b^6 + b^8) * d*x^3 - 2*((a^4*b^4 * \cos \\
& (2*c) - 2*(a^7*b + a^5*b^3) * \sin(2*c)) * d*x^3 * \cos(2*d*x^2) - (a^4*b^4 * \sin(2* \\
& c) + 2*(a^7*b + a^5*b^3) * \cos(2*c)) * d*x^3 * \sin(2*d*x^2) - (a^8 + 2*a^6*b^2 + \\
& a^4*b^4) * d*x^3) * \cos(2*d*x^2 + 2*c) - 2*((a^4*b^4 * \sin(2*c) + 2*(a^7*b + a^5* \\
& b^3) * \cos(2*c)) * d*x^3 * \cos(2*d*x^2) + (a^4*b^4 * \cos(2*c) - 2*(a^7*b + a^5*b^3) \\
& * \sin(2*c)) * d*x^3 * \sin(2*d*x^2)) * \sin(2*d*x^2 + 2*c)), x) + (2*(2*(a^9*b + 2*a \\
& ^7*b^3 - 2*a^3*b^7 - a*b^9) * \cos(2*c) + (a^6*b^4 + a^4*b^6 - a^2*b^8 - b^10) \\
& * \sin(2*c)) * d*x^2 * \log(x) - (a^4*b^6 + 2*a^2*b^8 + b^10) * \cos(2*c) + 2*(a^7*b^ \\
& 3 + 3*a^5*b^5 + 3*a^3*b^7 + a*b^9) * \sin(2*c)) * \sin(2*d*x^2) + (a^8*b^2 + 2*a^ \\
& 6*b^4 + a^4*b^6 - 2*(2*(a^9*b - a^5*b^5) * \cos(2*c) + (a^6*b^4 - a^4*b^6) * \sin \\
& (2*c)) * d*x^2 * \cos(2*d*x^2) * \log(x) - 2*((a^6*b^4 - a^4*b^6) * \cos(2*c) - 2*(a^9 \\
& *b - a^5*b^5) * \sin(2*c)) * d*x^2 * \log(x) * \sin(2*d*x^2)) * \sin(2*d*x^2 + 2*c)) / (((4 \\
& *a^10*b^2 + 16*a^8*b^4 + 24*a^6*b^6 + 17*a^4*b^8 + 6*a^2*b^10 + b^12) * \cos(2 \\
& *c)^2 + (4*a^10*b^2 + 16*a^8*b^4 + 24*a^6*b^6 + 17*a^4*b^8 + 6*a^2*b^10 + b \\
& ^12) * \sin(2*c)^2) * d*x^2 * \cos(2*d*x^2)^2 + (a^12 + 2*a^10*b^2 + a^8*b^4) * d*x^2 \\
& * \cos(2*d*x^2 + 2*c)^2 + ((4*a^10*b^2 + 16*a^8*b^4 + 24*a^6*b^6 + 17*a^4*b^8 \\
& + 6*a^2*b^10 + b^12) * \cos(2*c)^2 + (4*a^10*b^2 + 16*a^8*b^4 + 24*a^6*b^6 + \\
& 17*a^4*b^8 + 6*a^2*b^10 + b^12) * \sin(2*c)^2) * d*x^2 * \sin(2*d*x^2)^2 + (a^12 + \\
& 2*a^10*b^2 + a^8*b^4) * d*x^2 * \sin(2*d*x^2 + 2*c)^2 - 2*((a^8*b^4 + 4*a^6*b^6 \\
& + 6*a^4*b^8 + 4*a^2*b^10 + b^12) * \cos(2*c) - 2*(a^11*b + 5*a^9*b^3 + 10*a^7* \\
& b^5 + 10*a^5*b^7 + 5*a^3*b^9 + a*b^11) * \sin(2*c)) * d*x^2 * \cos(2*d*x^2) + 2*(2* \\
& (a^11*b + 5*a^9*b^3 + 10*a^7*b^5 + 10*a^5*b^7 + 5*a^3*b^9 + a*b^11) * \cos(2*c) \\
&) + (a^8*b^4 + 4*a^6*b^6 + 6*a^4*b^8 + 4*a^2*b^10 + b^12) * \sin(2*c)) * d*x^2 * \sin \\
& (2*d*x^2) + (a^12 + 6*a^10*b^2 + 15*a^8*b^4 + 20*a^6*b^6 + 15*a^4*b^8 + 6 \\
& *a^2*b^10 + b^12) * d*x^2 - 2*((a^8*b^4 + 2*a^6*b^6 + a^4*b^8) * \cos(2*c) - 2* \\
& (a^11*b + 3*a^9*b^3 + 3*a^7*b^5 + a^5*b^7) * \sin(2*c)) * d*x^2 * \cos(2*d*x^2) - (\\
& 2*(a^11*b + 3*a^9*b^3 + 3*a^7*b^5 + a^5*b^7) * \cos(2*c) + (a^8*b^4 + 2*a^6*b^ \\
& 6 + a^4*b^8) * \sin(2*c)) * d*x^2 * \sin(2*d*x^2) - (a^12 + 4*a^10*b^2 + 6*a^8*b^4 \\
& + 4*a^6*b^6 + a^4*b^8) * d*x^2 * \cos(2*d*x^2 + 2*c) - 2*((2*(a^11*b + 3*a^9*b^ \\
& 3 + 3*a^7*b^5 + a^5*b^7) * \cos(2*c) + (a^8*b^4 + 2*a^6*b^6 + a^4*b^8) * \sin(2*c) \\
&)) * d*x^2 * \cos(2*d*x^2) + ((a^8*b^4 + 2*a^6*b^6 + a^4*b^8) * \cos(2*c) - 2*(a^11 \\
& *b + 3*a^9*b^3 + 3*a^7*b^5 + a^5*b^7) * \sin(2*c)) * d*x^2 * \sin(2*d*x^2)) * \sin(2*d \\
& *x^2 + 2*c))
\end{aligned}$$

Giac [N/A]

Not integrable

Time = 0.45 (sec) , antiderivative size = 20, normalized size of antiderivative = 1.11

$$\int \frac{1}{x(a + b \tan(c + dx^2))^2} dx = \int \frac{1}{(b \tan(dx^2 + c) + a)^2 x} dx$$

[In] integrate(1/x/(a+b*tan(d*x^2+c))^2,x, algorithm="giac")

[Out] integrate(1/((b*tan(d*x^2 + c) + a)^2*x), x)

Mupad [N/A]

Not integrable

Time = 4.17 (sec) , antiderivative size = 20, normalized size of antiderivative = 1.11

$$\int \frac{1}{x(a + b \tan(c + dx^2))^2} dx = \int \frac{1}{x(a + b \tan(dx^2 + c))^2} dx$$

[In] int(1/(x*(a + b*tan(c + d*x^2))^2),x)

[Out] int(1/(x*(a + b*tan(c + d*x^2))^2), x)

$$3.24 \quad \int \frac{1}{x^2 (a + b \tan(c + dx^2))^2} dx$$

Optimal result	137
Rubi [N/A]	137
Mathematica [N/A]	138
Maple [N/A] (verified)	138
Fricas [N/A]	138
Sympy [N/A]	139
Maxima [N/A]	139
Giac [N/A]	140
Mupad [N/A]	141

Optimal result

Integrand size = 18, antiderivative size = 18

$$\int \frac{1}{x^2 (a + b \tan(c + dx^2))^2} dx = \text{Int}\left(\frac{1}{x^2 (a + b \tan(c + dx^2))^2}, x\right)$$

[Out] Unintegrable(1/x^2/(a+b*tan(d*x^2+c))^2,x)

Rubi [N/A]

Not integrable

Time = 0.03 (sec) , antiderivative size = 18, normalized size of antiderivative = 1.00, number of steps used = 0, number of rules used = 0, $\frac{\text{number of rules}}{\text{integrand size}} = 0.000$, Rules used = {}

$$\int \frac{1}{x^2 (a + b \tan(c + dx^2))^2} dx = \int \frac{1}{x^2 (a + b \tan(c + dx^2))^2} dx$$

[In] Int[1/(x^2*(a + b*Tan[c + d*x^2]))^2,x]

[Out] Defer[Int][1/(x^2*(a + b*Tan[c + d*x^2]))^2), x]

Rubi steps

$$\text{integral} = \int \frac{1}{x^2 (a + b \tan(c + dx^2))^2} dx$$

Mathematica [N/A]

Not integrable

Time = 9.76 (sec) , antiderivative size = 20, normalized size of antiderivative = 1.11

$$\int \frac{1}{x^2 (a + b \tan(c + dx^2))^2} dx = \int \frac{1}{x^2 (a + b \tan(c + dx^2))^2} dx$$

[In] Integrate[1/(x^2*(a + b*Tan[c + d*x^2])^2),x]

[Out] Integrate[1/(x^2*(a + b*Tan[c + d*x^2])^2), x]

Maple [N/A] (verified)

Not integrable

Time = 0.18 (sec) , antiderivative size = 18, normalized size of antiderivative = 1.00

$$\int \frac{1}{x^2 (a + b \tan(dx^2 + c))^2} dx$$

[In] int(1/x^2/(a+b*tan(d*x^2+c))^2,x)

[Out] int(1/x^2/(a+b*tan(d*x^2+c))^2,x)

Fricas [N/A]

Not integrable

Time = 0.25 (sec) , antiderivative size = 44, normalized size of antiderivative = 2.44

$$\int \frac{1}{x^2 (a + b \tan(c + dx^2))^2} dx = \int \frac{1}{(b \tan(dx^2 + c) + a)^2 x^2} dx$$

[In] integrate(1/x^2/(a+b*tan(d*x^2+c))^2,x, algorithm="fricas")

[Out] integral(1/(b^2*x^2*tan(d*x^2 + c)^2 + 2*a*b*x^2*tan(d*x^2 + c) + a^2*x^2), x)

Sympy [N/A]

Not integrable

Time = 0.99 (sec) , antiderivative size = 19, normalized size of antiderivative = 1.06

$$\int \frac{1}{x^2 (a + b \tan(c + dx^2))^2} dx = \int \frac{1}{x^2 (a + b \tan(c + dx^2))^2} dx$$

[In] integrate(1/x**2/(a+b*tan(d*x**2+c))**2,x)

[Out] Integral(1/(x**2*(a + b*tan(c + d*x**2))**2), x)

Maxima [N/A]

Not integrable

Time = 1.41 (sec) , antiderivative size = 2599, normalized size of antiderivative = 144.39

$$\int \frac{1}{x^2 (a + b \tan(c + dx^2))^2} dx = \int \frac{1}{(b \tan(dx^2 + c) + a)^2 x^2} dx$$

[In] integrate(1/x^2/(a+b*tan(d*x^2+c))^2,x, algorithm="maxima")

```
[Out] -((a^6 + a^4*b^2)*d*x^2*cos(2*d*x^2 + 2*c)^2 + (a^6 + a^4*b^2)*d*x^2*sin(2*
d*x^2 + 2*c)^2 + (a^6 + a^4*b^2 - a^2*b^4 - b^6)*d*x^2 + (b^6*sin(2*c) - ((
4*a^4*b^2 + 5*a^2*b^4 - b^6)*cos(2*c) - 2*(a^5*b - 2*a*b^5)*sin(2*c))*d*x^2
+ 2*(a^3*b^3 + a*b^5)*cos(2*c))*cos(2*d*x^2) - (((a^2*b^4 + b^6)*cos(2*c)
- 2*(a^5*b + 2*a^3*b^3 + a*b^5)*sin(2*c))*d*x^2*cos(2*d*x^2) - (2*(a^5*b +
2*a^3*b^3 + a*b^5)*cos(2*c) + (a^2*b^4 + b^6)*sin(2*c))*d*x^2*sin(2*d*x^2)
- (2*a^6 + 2*a^4*b^2 + 3*a^2*b^4 + b^6)*d*x^2)*cos(2*d*x^2 + 2*c) + (a^8*d*
x^3*cos(2*d*x^2 + 2*c)^2 + a^8*d*x^3*sin(2*d*x^2 + 2*c)^2 + ((4*a^6*b^2 + 8
*a^4*b^4 + 4*a^2*b^6 + b^8)*cos(2*c)^2 + (4*a^6*b^2 + 8*a^4*b^4 + 4*a^2*b^6
+ b^8)*sin(2*c)^2)*d*x^3*cos(2*d*x^2)^2 + ((4*a^6*b^2 + 8*a^4*b^4 + 4*a^2*
b^6 + b^8)*cos(2*c)^2 + (4*a^6*b^2 + 8*a^4*b^4 + 4*a^2*b^6 + b^8)*sin(2*c)^
2)*d*x^3*sin(2*d*x^2)^2 - 2*((a^4*b^4 + 2*a^2*b^6 + b^8)*cos(2*c) - 2*(a^7*
b + 3*a^5*b^3 + 3*a^3*b^5 + a*b^7)*sin(2*c))*d*x^3*cos(2*d*x^2) + 2*(2*(a^7
*b + 3*a^5*b^3 + 3*a^3*b^5 + a*b^7)*cos(2*c) + (a^4*b^4 + 2*a^2*b^6 + b^8)*
sin(2*c))*d*x^3*sin(2*d*x^2) + (a^8 + 4*a^6*b^2 + 6*a^4*b^4 + 4*a^2*b^6 + b
^8)*d*x^3 - 2*((a^4*b^4*cos(2*c) - 2*(a^7*b + a^5*b^3)*sin(2*c))*d*x^3*cos(
2*d*x^2) - (a^4*b^4*sin(2*c) + 2*(a^7*b + a^5*b^3)*cos(2*c))*d*x^3*sin(2*d*
x^2) - (a^8 + 2*a^6*b^2 + a^4*b^4)*d*x^3)*cos(2*d*x^2 + 2*c) - 2*((a^4*b^4*
sin(2*c) + 2*(a^7*b + a^5*b^3)*cos(2*c))*d*x^3*cos(2*d*x^2) + (a^4*b^4*cos(
2*c) - 2*(a^7*b + a^5*b^3)*sin(2*c))*d*x^3*sin(2*d*x^2))*sin(2*d*x^2 + 2*c)
)*integrate(((3*b^6*sin(2*c) - 4*(a*b^5*sin(2*c) + 2*(a^4*b^2 + a^2*b^4)*co
s(2*c))*d*x^2 + 6*(a^3*b^3 + a*b^5)*cos(2*c))*cos(2*d*x^2) + (3*b^6*cos(2*c)
```

) - 4*(a*b^5*cos(2*c) - 2*(a^4*b^2 + a^2*b^4)*sin(2*c))*d*x^2 - 6*(a^3*b^3 + a*b^5)*sin(2*c))*sin(2*d*x^2) + (4*a^5*b*d*x^2 - 3*a^4*b^2)*sin(2*d*x^2 + 2*c))/(a^8*d*x^4*cos(2*d*x^2 + 2*c)^2 + a^8*d*x^4*sin(2*d*x^2 + 2*c)^2 + (4*a^6*b^2 + 8*a^4*b^4 + 4*a^2*b^6 + b^8)*cos(2*c)^2 + (4*a^6*b^2 + 8*a^4*b^4 + 4*a^2*b^6 + b^8)*sin(2*c)^2)*d*x^4*cos(2*d*x^2)^2 + ((4*a^6*b^2 + 8*a^4*b^4 + 4*a^2*b^6 + b^8)*cos(2*c)^2 + (4*a^6*b^2 + 8*a^4*b^4 + 4*a^2*b^6 + b^8)*sin(2*c)^2)*d*x^4*sin(2*d*x^2)^2 - 2*((a^4*b^4 + 2*a^2*b^6 + b^8)*cos(2*c) - 2*(a^7*b + 3*a^5*b^3 + 3*a^3*b^5 + a*b^7)*sin(2*c))*d*x^4*cos(2*d*x^2) + 2*(2*(a^7*b + 3*a^5*b^3 + 3*a^3*b^5 + a*b^7)*cos(2*c) + (a^4*b^4 + 2*a^2*b^6 + b^8)*sin(2*c))*d*x^4*sin(2*d*x^2) + (a^8 + 4*a^6*b^2 + 6*a^4*b^4 + 4*a^2*b^6 + b^8)*d*x^4 - 2*((a^4*b^4*cos(2*c) - 2*(a^7*b + a^5*b^3)*sin(2*c))*d*x^4*cos(2*d*x^2) - (a^4*b^4*sin(2*c) + 2*(a^7*b + a^5*b^3)*cos(2*c))*d*x^4*sin(2*d*x^2) - (a^8 + 2*a^6*b^2 + a^4*b^4)*d*x^4)*cos(2*d*x^2 + 2*c) - 2*((a^4*b^4*sin(2*c) + 2*(a^7*b + a^5*b^3)*cos(2*c))*d*x^4*cos(2*d*x^2) + (a^4*b^4*cos(2*c) - 2*(a^7*b + a^5*b^3)*sin(2*c))*d*x^4*sin(2*d*x^2))*sin(2*d*x^2 + 2*c)), x) + (b^6*cos(2*c) + (2*(a^5*b - 2*a*b^5)*cos(2*c) + (4*a^4*b^2 + 5*a^2*b^4 - b^6)*sin(2*c))*d*x^2 - 2*(a^3*b^3 + a*b^5)*sin(2*c))*sin(2*d*x^2) + (2*a^5*b*d*x^2 - a^4*b^2 - (2*(a^5*b + 2*a^3*b^3 + a*b^5)*cos(2*c) + (a^2*b^4 + b^6)*sin(2*c))*d*x^2*cos(2*d*x^2) - ((a^2*b^4 + b^6)*cos(2*c) - 2*(a^5*b + 2*a^3*b^3 + a*b^5)*sin(2*c))*d*x^2*sin(2*d*x^2))*sin(2*d*x^2 + 2*c))/(a^8*d*x^3*cos(2*d*x^2 + 2*c)^2 + a^8*d*x^3*sin(2*d*x^2 + 2*c)^2 + ((4*a^6*b^2 + 8*a^4*b^4 + 4*a^2*b^6 + b^8)*cos(2*c)^2 + (4*a^6*b^2 + 8*a^4*b^4 + 4*a^2*b^6 + b^8)*sin(2*c)^2)*d*x^3*cos(2*d*x^2)^2 + ((4*a^6*b^2 + 8*a^4*b^4 + 4*a^2*b^6 + b^8)*cos(2*c)^2 + (4*a^6*b^2 + 8*a^4*b^4 + 4*a^2*b^6 + b^8)*sin(2*c)^2)*d*x^3*sin(2*d*x^2)^2 - 2*((a^4*b^4 + 2*a^2*b^6 + b^8)*cos(2*c) - 2*(a^7*b + 3*a^5*b^3 + 3*a^3*b^5 + a*b^7)*sin(2*c))*d*x^3*cos(2*d*x^2) + 2*(2*(a^7*b + 3*a^5*b^3 + 3*a^3*b^5 + a*b^7)*cos(2*c) + (a^4*b^4 + 2*a^2*b^6 + b^8)*sin(2*c))*d*x^3*sin(2*d*x^2) + (a^8 + 4*a^6*b^2 + 6*a^4*b^4 + 4*a^2*b^6 + b^8)*d*x^3 - 2*((a^4*b^4*cos(2*c) - 2*(a^7*b + a^5*b^3)*sin(2*c))*d*x^3*cos(2*d*x^2) - (a^4*b^4*sin(2*c) + 2*(a^7*b + a^5*b^3)*cos(2*c))*d*x^3*sin(2*d*x^2) - (a^8 + 2*a^6*b^2 + a^4*b^4)*d*x^3)*cos(2*d*x^2 + 2*c) - 2*((a^4*b^4*sin(2*c) + 2*(a^7*b + a^5*b^3)*cos(2*c))*d*x^3*cos(2*d*x^2) + (a^4*b^4*cos(2*c) - 2*(a^7*b + a^5*b^3)*sin(2*c))*d*x^3*sin(2*d*x^2))*sin(2*d*x^2 + 2*c))

Giac [N/A]

Not integrable

Time = 0.51 (sec) , antiderivative size = 20, normalized size of antiderivative = 1.11

$$\int \frac{1}{x^2 (a + b \tan(c + dx^2))^2} dx = \int \frac{1}{(b \tan(dx^2 + c) + a)^2 x^2} dx$$

[In] integrate(1/x^2/(a+b*tan(d*x^2+c))^2,x, algorithm="giac")

[Out] integrate(1/((b*tan(d*x^2 + c) + a)^2*x^2), x)

Mupad [N/A]

Not integrable

Time = 4.38 (sec) , antiderivative size = 20, normalized size of antiderivative = 1.11

$$\int \frac{1}{x^2 (a + b \tan(c + dx^2))^2} dx = \int \frac{1}{x^2 (a + b \tan(dx^2 + c))^2} dx$$

```
[In] int(1/(x^2*(a + b*tan(c + d*x^2))^2),x)
```

```
[Out] int(1/(x^2*(a + b*tan(c + d*x^2))^2), x)
```

3.25 $\int x^3 (a + b \tan (c + d\sqrt{x})) dx$

Optimal result	142
Rubi [A] (verified)	143
Mathematica [A] (verified)	147
Maple [F]	147
Fricas [F]	148
Sympy [F]	148
Maxima [B] (verification not implemented)	148
Giac [F]	149
Mupad [F(-1)]	149

Optimal result

Integrand size = 18, antiderivative size = 261

$$\begin{aligned}
 \int x^3 (a + b \tan (c + d\sqrt{x})) dx = & \frac{ax^4}{4} + \frac{1}{4}ibx^4 - \frac{2bx^{7/2} \log \left(1 + e^{2i(c+d\sqrt{x})} \right)}{d} \\
 & + \frac{7ibx^3 \text{PolyLog} \left(2, -e^{2i(c+d\sqrt{x})} \right)}{d^2} \\
 & - \frac{21bx^{5/2} \text{PolyLog} \left(3, -e^{2i(c+d\sqrt{x})} \right)}{d^3} \\
 & - \frac{105ibx^2 \text{PolyLog} \left(4, -e^{2i(c+d\sqrt{x})} \right)}{2d^4} \\
 & + \frac{105bx^{3/2} \text{PolyLog} \left(5, -e^{2i(c+d\sqrt{x})} \right)}{d^5} \\
 & + \frac{315ibx \text{PolyLog} \left(6, -e^{2i(c+d\sqrt{x})} \right)}{2d^6} \\
 & - \frac{315b\sqrt{x} \text{PolyLog} \left(7, -e^{2i(c+d\sqrt{x})} \right)}{2d^7} \\
 & - \frac{315ib \text{PolyLog} \left(8, -e^{2i(c+d\sqrt{x})} \right)}{4d^8}
 \end{aligned}$$

```
[Out] 1/4*a*x^4+1/4*I*b*x^4-2*b*x^(7/2)*ln(1+exp(2*I*(c+d*x^(1/2))))/d+7*I*b*x^3*
polylog(2,-exp(2*I*(c+d*x^(1/2))))/d^2-21*b*x^(5/2)*polylog(3,-exp(2*I*(c+d
*x^(1/2))))/d^3-105/2*I*b*x^2*polylog(4,-exp(2*I*(c+d*x^(1/2))))/d^4+105*b*
x^(3/2)*polylog(5,-exp(2*I*(c+d*x^(1/2))))/d^5+315/2*I*b*x*polylog(6,-exp(2
*I*(c+d*x^(1/2))))/d^6-315/4*I*b*polylog(8,-exp(2*I*(c+d*x^(1/2))))/d^8-315
/2*b*polylog(7,-exp(2*I*(c+d*x^(1/2))))*x^(1/2)/d^7
```

Rubi [A] (verified)

Time = 0.42 (sec) , antiderivative size = 261, normalized size of antiderivative = 1.00, number of steps used = 13, number of rules used = 8, $\frac{\text{number of rules}}{\text{integrand size}} = 0.444$, Rules used = {14, 3832, 3800, 2221, 2611, 6744, 2320, 6724}

$$\int x^3(a + b \tan(c + d\sqrt{x})) dx = \frac{ax^4}{4} - \frac{315ib \operatorname{PolyLog}\left(8, -e^{2i(c+d\sqrt{x})}\right)}{4d^8} - \frac{315b\sqrt{x} \operatorname{PolyLog}\left(7, -e^{2i(c+d\sqrt{x})}\right)}{2d^7} + \frac{315ibx \operatorname{PolyLog}\left(6, -e^{2i(c+d\sqrt{x})}\right)}{2d^6} + \frac{105bx^{3/2} \operatorname{PolyLog}\left(5, -e^{2i(c+d\sqrt{x})}\right)}{d^5} - \frac{105ibx^2 \operatorname{PolyLog}\left(4, -e^{2i(c+d\sqrt{x})}\right)}{2d^4} - \frac{21bx^{5/2} \operatorname{PolyLog}\left(3, -e^{2i(c+d\sqrt{x})}\right)}{d^3} + \frac{7ibx^3 \operatorname{PolyLog}\left(2, -e^{2i(c+d\sqrt{x})}\right)}{d^2} - \frac{2bx^{7/2} \log\left(1 + e^{2i(c+d\sqrt{x})}\right)}{d} + \frac{1}{4}ibx^4$$

[In] Int[x^3*(a + b*Tan[c + d*Sqrt[x]]),x]

[Out] (a*x^4)/4 + (I/4)*b*x^4 - (2*b*x^(7/2)*Log[1 + E^((2*I)*(c + d*Sqrt[x]))])/d + ((7*I)*b*x^3*PolyLog[2, -E^((2*I)*(c + d*Sqrt[x]))])/d^2 - (21*b*x^(5/2)*PolyLog[3, -E^((2*I)*(c + d*Sqrt[x]))])/d^3 - (((105*I)/2)*b*x^2*PolyLog[4, -E^((2*I)*(c + d*Sqrt[x]))])/d^4 + (105*b*x^(3/2)*PolyLog[5, -E^((2*I)*(c + d*Sqrt[x]))])/d^5 + (((315*I)/2)*b*x*PolyLog[6, -E^((2*I)*(c + d*Sqrt[x]))])/d^6 - (315*b*Sqrt[x]*PolyLog[7, -E^((2*I)*(c + d*Sqrt[x]))])/(2*d^7) - (((315*I)/4)*b*PolyLog[8, -E^((2*I)*(c + d*Sqrt[x]))])/d^8

Rule 14

Int[(u_)*((c_)*(x_)^(m_)), x_Symbol] :> Int[ExpandIntegrand[(c*x)^m*u, x], x] /; FreeQ[{c, m}, x] && SumQ[u] && !LinearQ[u, x] && !MatchQ[u, (a_ + (b_)*(v_)) /; FreeQ[{a, b}, x] && InverseFunctionQ[v]]

Rule 2221

Int[(((F_)^((g_)*((e_) + (f_)*(x_))))^(n_)*((c_) + (d_)*(x_))^(m_))/((a_) + (b_)*((F_)^((g_)*((e_) + (f_)*(x_))))^(n_)), x_Symbol] :> Simp

```

[((c + d*x)^m/(b*f*g*n*Log[F]))*Log[1 + b*((F^(g*(e + f*x)))^n/a)], x] - Dist[d*(m/(b*f*g*n*Log[F])), Int[(c + d*x)^(m - 1)*Log[1 + b*((F^(g*(e + f*x)))^n/a)], x], x] /; FreeQ[{F, a, b, c, d, e, f, g, n}, x] && IGtQ[m, 0]

```

Rule 2320

```

Int[u_, x_Symbol] := With[{v = FunctionOfExponential[u, x]}, Dist[v/D[v, x], Subst[Int[FunctionOfExponentialFunction[u, x]/x, x], x, v], x] /; FunctionOfExponentialQ[u, x] && !MatchQ[u, (w_)*((a_.)*(v_)^(n_))^(m_)] /; FreeQ[{a, m, n}, x] && IntegerQ[m*n] && !MatchQ[u, E^((c_.)*((a_.) + (b_.)*x))*(F_) [v_] /; FreeQ[{a, b, c}, x] && InverseFunctionQ[F[x]]]

```

Rule 2611

```

Int[Log[1 + (e_.)*((F_)^((c_.)*((a_.) + (b_.)*(x_))))^(n_.)]*((f_.) + (g_.)*(x_))^(m_.), x_Symbol] := Simp[(-f + g*x)^m*(PolyLog[2, (-e)*(F^(c*(a + b*x)))^n]/(b*c*n*Log[F])), x] + Dist[g*(m/(b*c*n*Log[F])), Int[(f + g*x)^(m - 1)*PolyLog[2, (-e)*(F^(c*(a + b*x)))^n], x], x] /; FreeQ[{F, a, b, c, e, f, g, n}, x] && GtQ[m, 0]

```

Rule 3800

```

Int[((c_.) + (d_.)*(x_))^(m_.)*tan[(e_.) + (f_.)*(x_)], x_Symbol] := Simp[I*((c + d*x)^(m + 1)/(d*(m + 1))), x] - Dist[2*I, Int[(c + d*x)^m*(E^(2*I*(e + f*x)))/(1 + E^(2*I*(e + f*x))), x], x] /; FreeQ[{c, d, e, f}, x] && IGtQ[m, 0]

```

Rule 3832

```

Int[(x_)^(m_.)*((a_.) + (b_.)*Tan[(c_.) + (d_.)*(x_)^(n_)])^(p_.), x_Symbol] := Dist[1/n, Subst[Int[x^(Simplify[(m + 1)/n] - 1)*(a + b*Tan[c + d*x])^p, x], x, x^n], x] /; FreeQ[{a, b, c, d, m, n, p}, x] && IGtQ[Simplify[(m + 1)/n], 0] && IntegerQ[p]

```

Rule 6724

```

Int[PolyLog[n_, (c_.)*((a_.) + (b_.)*(x_))^(p_.)]/((d_.) + (e_.)*(x_)), x_Symbol] := Simp[PolyLog[n + 1, c*(a + b*x)^p]/(e*p), x] /; FreeQ[{a, b, c, d, e, n, p}, x] && EqQ[b*d, a*e]

```

Rule 6744

```

Int[((e_.) + (f_.)*(x_))^(m_.)*PolyLog[n_, (d_.)*((F_)^((c_.)*((a_.) + (b_.)*(x_))))^(p_.)], x_Symbol] := Simp[(e + f*x)^m*(PolyLog[n + 1, d*(F^(c*(a + b*x)))^p]/(b*c*p*Log[F])), x] - Dist[f*(m/(b*c*p*Log[F])), Int[(e + f*x)^(m - 1)*PolyLog[n + 1, d*(F^(c*(a + b*x)))^p], x], x] /; FreeQ[{F, a, b, c,

```


d, e, f, n, p}, x] && GtQ[m, 0]

Rubi steps

$$\begin{aligned}
\text{integral} &= \int (ax^3 + bx^3 \tan(c + d\sqrt{x})) dx \\
&= \frac{ax^4}{4} + b \int x^3 \tan(c + d\sqrt{x}) dx \\
&= \frac{ax^4}{4} + (2b)\text{Subst}\left(\int x^7 \tan(c + dx) dx, x, \sqrt{x}\right) \\
&= \frac{ax^4}{4} + \frac{1}{4}ibx^4 - (4ib)\text{Subst}\left(\int \frac{e^{2i(c+dx)}x^7}{1 + e^{2i(c+dx)}} dx, x, \sqrt{x}\right) \\
&= \frac{ax^4}{4} + \frac{1}{4}ibx^4 - \frac{2bx^{7/2} \log\left(1 + e^{2i(c+d\sqrt{x})}\right)}{d} + \frac{(14b)\text{Subst}\left(\int x^6 \log\left(1 + e^{2i(c+dx)}\right) dx, x, \sqrt{x}\right)}{d} \\
&= \frac{ax^4}{4} + \frac{1}{4}ibx^4 - \frac{2bx^{7/2} \log\left(1 + e^{2i(c+d\sqrt{x})}\right)}{d} + \frac{7ibx^3 \text{PolyLog}\left(2, -e^{2i(c+d\sqrt{x})}\right)}{d^2} \\
&\quad - \frac{(42ib)\text{Subst}\left(\int x^5 \text{PolyLog}\left(2, -e^{2i(c+dx)}\right) dx, x, \sqrt{x}\right)}{d^2} \\
&= \frac{ax^4}{4} + \frac{1}{4}ibx^4 - \frac{2bx^{7/2} \log\left(1 + e^{2i(c+d\sqrt{x})}\right)}{d} + \frac{7ibx^3 \text{PolyLog}\left(2, -e^{2i(c+d\sqrt{x})}\right)}{d^2} \\
&\quad - \frac{21bx^{5/2} \text{PolyLog}\left(3, -e^{2i(c+d\sqrt{x})}\right)}{d^3} + \frac{(105b)\text{Subst}\left(\int x^4 \text{PolyLog}\left(3, -e^{2i(c+dx)}\right) dx, x, \sqrt{x}\right)}{d^3} \\
&= \frac{ax^4}{4} + \frac{1}{4}ibx^4 - \frac{2bx^{7/2} \log\left(1 + e^{2i(c+d\sqrt{x})}\right)}{d} + \frac{7ibx^3 \text{PolyLog}\left(2, -e^{2i(c+d\sqrt{x})}\right)}{d^2} \\
&\quad - \frac{21bx^{5/2} \text{PolyLog}\left(3, -e^{2i(c+d\sqrt{x})}\right)}{d^3} - \frac{105ibx^2 \text{PolyLog}\left(4, -e^{2i(c+d\sqrt{x})}\right)}{2d^4} \\
&\quad + \frac{(210ib)\text{Subst}\left(\int x^3 \text{PolyLog}\left(4, -e^{2i(c+dx)}\right) dx, x, \sqrt{x}\right)}{d^4} \\
&= \frac{ax^4}{4} + \frac{1}{4}ibx^4 - \frac{2bx^{7/2} \log\left(1 + e^{2i(c+d\sqrt{x})}\right)}{d} \\
&\quad + \frac{7ibx^3 \text{PolyLog}\left(2, -e^{2i(c+d\sqrt{x})}\right)}{d^2} - \frac{21bx^{5/2} \text{PolyLog}\left(3, -e^{2i(c+d\sqrt{x})}\right)}{d^3} \\
&\quad - \frac{105ibx^2 \text{PolyLog}\left(4, -e^{2i(c+d\sqrt{x})}\right)}{2d^4} + \frac{105bx^{3/2} \text{PolyLog}\left(5, -e^{2i(c+d\sqrt{x})}\right)}{d^5} \\
&\quad - \frac{(315b)\text{Subst}\left(\int x^2 \text{PolyLog}\left(5, -e^{2i(c+dx)}\right) dx, x, \sqrt{x}\right)}{d^5}
\end{aligned}$$

$$\begin{aligned}
&= \frac{ax^4}{4} + \frac{1}{4}ibx^4 - \frac{2bx^{7/2} \log\left(1 + e^{2i(c+d\sqrt{x})}\right)}{d} + \frac{7ibx^3 \text{PolyLog}\left(2, -e^{2i(c+d\sqrt{x})}\right)}{d^2} \\
&\quad - \frac{21bx^{5/2} \text{PolyLog}\left(3, -e^{2i(c+d\sqrt{x})}\right)}{d^3} - \frac{105ibx^2 \text{PolyLog}\left(4, -e^{2i(c+d\sqrt{x})}\right)}{2d^4} \\
&\quad + \frac{105bx^{3/2} \text{PolyLog}\left(5, -e^{2i(c+d\sqrt{x})}\right)}{d^5} + \frac{315ibx \text{PolyLog}\left(6, -e^{2i(c+d\sqrt{x})}\right)}{2d^6} \\
&\quad - \frac{(315ib)\text{Subst}\left(\int x \text{PolyLog}\left(6, -e^{2i(c+dx)}\right) dx, x, \sqrt{x}\right)}{d^6} \\
&= \frac{ax^4}{4} + \frac{1}{4}ibx^4 - \frac{2bx^{7/2} \log\left(1 + e^{2i(c+d\sqrt{x})}\right)}{d} + \frac{7ibx^3 \text{PolyLog}\left(2, -e^{2i(c+d\sqrt{x})}\right)}{d^2} \\
&\quad - \frac{21bx^{5/2} \text{PolyLog}\left(3, -e^{2i(c+d\sqrt{x})}\right)}{d^3} - \frac{105ibx^2 \text{PolyLog}\left(4, -e^{2i(c+d\sqrt{x})}\right)}{2d^4} \\
&\quad + \frac{105bx^{3/2} \text{PolyLog}\left(5, -e^{2i(c+d\sqrt{x})}\right)}{d^5} + \frac{315ibx \text{PolyLog}\left(6, -e^{2i(c+d\sqrt{x})}\right)}{2d^6} \\
&\quad - \frac{315b\sqrt{x} \text{PolyLog}\left(7, -e^{2i(c+d\sqrt{x})}\right)}{2d^7} + \frac{(315b)\text{Subst}\left(\int \text{PolyLog}\left(7, -e^{2i(c+dx)}\right) dx, x, \sqrt{x}\right)}{2d^7} \\
&= \frac{ax^4}{4} + \frac{1}{4}ibx^4 - \frac{2bx^{7/2} \log\left(1 + e^{2i(c+d\sqrt{x})}\right)}{d} + \frac{7ibx^3 \text{PolyLog}\left(2, -e^{2i(c+d\sqrt{x})}\right)}{d^2} \\
&\quad - \frac{21bx^{5/2} \text{PolyLog}\left(3, -e^{2i(c+d\sqrt{x})}\right)}{d^3} - \frac{105ibx^2 \text{PolyLog}\left(4, -e^{2i(c+d\sqrt{x})}\right)}{2d^4} \\
&\quad + \frac{105bx^{3/2} \text{PolyLog}\left(5, -e^{2i(c+d\sqrt{x})}\right)}{d^5} + \frac{315ibx \text{PolyLog}\left(6, -e^{2i(c+d\sqrt{x})}\right)}{2d^6} \\
&\quad - \frac{315b\sqrt{x} \text{PolyLog}\left(7, -e^{2i(c+d\sqrt{x})}\right)}{2d^7} - \frac{(315ib)\text{Subst}\left(\int \frac{\text{PolyLog}(7, -x)}{x} dx, x, e^{2i(c+d\sqrt{x})}\right)}{4d^8} \\
&= \frac{ax^4}{4} + \frac{1}{4}ibx^4 - \frac{2bx^{7/2} \log\left(1 + e^{2i(c+d\sqrt{x})}\right)}{d} + \frac{7ibx^3 \text{PolyLog}\left(2, -e^{2i(c+d\sqrt{x})}\right)}{d^2} \\
&\quad - \frac{21bx^{5/2} \text{PolyLog}\left(3, -e^{2i(c+d\sqrt{x})}\right)}{d^3} - \frac{105ibx^2 \text{PolyLog}\left(4, -e^{2i(c+d\sqrt{x})}\right)}{2d^4} \\
&\quad + \frac{105bx^{3/2} \text{PolyLog}\left(5, -e^{2i(c+d\sqrt{x})}\right)}{d^5} + \frac{315ibx \text{PolyLog}\left(6, -e^{2i(c+d\sqrt{x})}\right)}{2d^6} \\
&\quad - \frac{315b\sqrt{x} \text{PolyLog}\left(7, -e^{2i(c+d\sqrt{x})}\right)}{2d^7} - \frac{315ib \text{PolyLog}\left(8, -e^{2i(c+d\sqrt{x})}\right)}{4d^8}
\end{aligned}$$

Mathematica [A] (verified)

Time = 0.07 (sec) , antiderivative size = 261, normalized size of antiderivative = 1.00

$$\begin{aligned}
\int x^3(a + b \tan(c + d\sqrt{x})) dx &= \frac{ax^4}{4} + \frac{1}{4}ibx^4 - \frac{2bx^{7/2} \log(1 + e^{2i(c+d\sqrt{x})})}{d} \\
&+ \frac{7ibx^3 \text{PolyLog}(2, -e^{2i(c+d\sqrt{x})})}{d^2} \\
&- \frac{21bx^{5/2} \text{PolyLog}(3, -e^{2i(c+d\sqrt{x})})}{d^3} \\
&- \frac{105ibx^2 \text{PolyLog}(4, -e^{2i(c+d\sqrt{x})})}{2d^4} \\
&+ \frac{105bx^{3/2} \text{PolyLog}(5, -e^{2i(c+d\sqrt{x})})}{d^5} \\
&+ \frac{315ibx \text{PolyLog}(6, -e^{2i(c+d\sqrt{x})})}{2d^6} \\
&- \frac{315b\sqrt{x} \text{PolyLog}(7, -e^{2i(c+d\sqrt{x})})}{2d^7} \\
&- \frac{315ib \text{PolyLog}(8, -e^{2i(c+d\sqrt{x})})}{4d^8}
\end{aligned}$$

[In] Integrate[x^3*(a + b*Tan[c + d*Sqrt[x]]),x]

```
[Out] (a*x^4)/4 + (I/4)*b*x^4 - (2*b*x^(7/2)*Log[1 + E^((2*I)*(c + d*Sqrt[x]))])/
d + ((7*I)*b*x^3*PolyLog[2, -E^((2*I)*(c + d*Sqrt[x]))])/d^2 - (21*b*x^(5/2)
)*PolyLog[3, -E^((2*I)*(c + d*Sqrt[x]))])/d^3 - (((105*I)/2)*b*x^2*PolyLog[
4, -E^((2*I)*(c + d*Sqrt[x]))])/d^4 + (105*b*x^(3/2)*PolyLog[5, -E^((2*I)*(
c + d*Sqrt[x]))])/d^5 + (((315*I)/2)*b*x*PolyLog[6, -E^((2*I)*(c + d*Sqrt[x]
))])/d^6 - (315*b*Sqrt[x]*PolyLog[7, -E^((2*I)*(c + d*Sqrt[x]))])/(2*d^7)
- (((315*I)/4)*b*PolyLog[8, -E^((2*I)*(c + d*Sqrt[x]))])/d^8
```

Maple [F]

$$\int x^3(a + b \tan(c + d\sqrt{x})) dx$$

[In] int(x^3*(a+b*tan(c+d*x^(1/2))),x)

[Out] int(x^3*(a+b*tan(c+d*x^(1/2))),x)

Fricas [F]

$$\int x^3(a + b \tan(c + d\sqrt{x})) dx = \int (b \tan(d\sqrt{x} + c) + a)x^3 dx$$

```
[In] integrate(x^3*(a+b*tan(c+d*x^(1/2))),x, algorithm="fricas")
```

```
[Out] integral(b*x^3*tan(d*sqrt(x) + c) + a*x^3, x)
```

Sympy [F]

$$\int x^3(a + b \tan(c + d\sqrt{x})) dx = \int x^3(a + b \tan(c + d\sqrt{x})) dx$$

```
[In] integrate(x**3*(a+b*tan(c+d*x**(1/2))),x)
```

```
[Out] Integral(x**3*(a + b*tan(c + d*sqrt(x))), x)
```

Maxima [B] (verification not implemented)

Both result and optimal contain complex but leaf count of result is larger than twice the leaf count of optimal. 937 vs. 2(198) = 396.

Time = 0.46 (sec) , antiderivative size = 937, normalized size of antiderivative = 3.59

$$\int x^3(a + b \tan(c + d\sqrt{x})) dx = \text{Too large to display}$$

```
[In] integrate(x^3*(a+b*tan(c+d*x^(1/2))),x, algorithm="maxima")
```

```
[Out] 1/420*(105*(d*sqrt(x) + c)^8*a + 105*I*(d*sqrt(x) + c)^8*b - 840*(d*sqrt(x) + c)^7*a*c - 840*I*(d*sqrt(x) + c)^7*b*c + 2940*(d*sqrt(x) + c)^6*a*c^2 + 2940*I*(d*sqrt(x) + c)^6*b*c^2 - 5880*(d*sqrt(x) + c)^5*a*c^3 - 5880*I*(d*sqrt(x) + c)^5*b*c^3 + 7350*(d*sqrt(x) + c)^4*a*c^4 + 7350*I*(d*sqrt(x) + c)^4*b*c^4 - 5880*(d*sqrt(x) + c)^3*a*c^5 - 5880*I*(d*sqrt(x) + c)^3*b*c^5 + 2940*(d*sqrt(x) + c)^2*a*c^6 + 2940*I*(d*sqrt(x) + c)^2*b*c^6 - 840*(d*sqrt(x) + c)*a*c^7 - 840*b*c^7*log(sec(d*sqrt(x) + c)) + 8*(-960*I*(d*sqrt(x) + c)^7*b + 3920*I*(d*sqrt(x) + c)^6*b*c - 7056*I*(d*sqrt(x) + c)^5*b*c^2 + 7350*I*(d*sqrt(x) + c)^4*b*c^3 - 4900*I*(d*sqrt(x) + c)^3*b*c^4 + 2205*I*(d*sqrt(x) + c)^2*b*c^5 - 735*I*(d*sqrt(x) + c)*b*c^6)*arctan2(sin(2*d*sqrt(x) + 2*c), cos(2*d*sqrt(x) + 2*c) + 1) + 420*(64*I*(d*sqrt(x) + c)^6*b - 224*I*(d*sqrt(x) + c)^5*b*c + 336*I*(d*sqrt(x) + c)^4*b*c^2 - 280*I*(d*sqrt(x) + c)^3*b*c^3 + 140*I*(d*sqrt(x) + c)^2*b*c^4 - 42*I*(d*sqrt(x) + c)*b*c^5 + 7*I*b*c^6)*dilog(-e^(2*I*d*sqrt(x) + 2*I*c)) - 4*(960*(d*sqrt(x) + c)^7*b
```

$$\begin{aligned}
& - 3920*(d*\sqrt{x} + c)^6*b*c + 7056*(d*\sqrt{x} + c)^5*b*c^2 - 7350*(d*\sqrt{x} \\
& (x) + c)^4*b*c^3 + 4900*(d*\sqrt{x} + c)^3*b*c^4 - 2205*(d*\sqrt{x} + c)^2*b*c \\
& ^5 + 735*(d*\sqrt{x} + c)*b*c^6)*\log(\cos(2*d*\sqrt{x} + 2*c)^2 + \sin(2*d*\sqrt{x} \\
& (x) + 2*c)^2 + 2*\cos(2*d*\sqrt{x} + 2*c) + 1) - 302400*I*b*\text{polylog}(8, -e^{(2* \\
& I*d*\sqrt{x} + 2*I*c)}) - 50400*(12*(d*\sqrt{x} + c)*b - 7*b*c)*\text{polylog}(7, -e^{ \\
& (2*I*d*\sqrt{x} + 2*I*c)}) + 10080*(60*I*(d*\sqrt{x} + c)^2*b - 70*I*(d*\sqrt{x} \\
&) + c)*b*c + 21*I*b*c^2)*\text{polylog}(6, -e^{(2*I*d*\sqrt{x} + 2*I*c)}) + 2520*(160 \\
& *(d*\sqrt{x} + c)^3*b - 280*(d*\sqrt{x} + c)^2*b*c + 168*(d*\sqrt{x} + c)*b*c^2 - \\
& 35*b*c^3)*\text{polylog}(5, -e^{(2*I*d*\sqrt{x} + 2*I*c)}) + 840*(-240*I*(d*\sqrt{x} \\
& (x) + c)^4*b + 560*I*(d*\sqrt{x} + c)^3*b*c - 504*I*(d*\sqrt{x} + c)^2*b*c^2 + \\
& 210*I*(d*\sqrt{x} + c)*b*c^3 - 35*I*b*c^4)*\text{polylog}(4, -e^{(2*I*d*\sqrt{x} + 2 \\
& *I*c)}) - 420*(192*(d*\sqrt{x} + c)^5*b - 560*(d*\sqrt{x} + c)^4*b*c + 672*(d* \\
& \sqrt{x} + c)^3*b*c^2 - 420*(d*\sqrt{x} + c)^2*b*c^3 + 140*(d*\sqrt{x} + c)*b* \\
& c^4 - 21*b*c^5)*\text{polylog}(3, -e^{(2*I*d*\sqrt{x} + 2*I*c)})/d^8
\end{aligned}$$

Giac [F]

$$\int x^3(a + b \tan(c + d\sqrt{x})) dx = \int (b \tan(d\sqrt{x} + c) + a)x^3 dx$$

[In] integrate(x^3*(a+b*tan(c+d*x^(1/2))),x, algorithm="giac")

[Out] integrate((b*tan(d*sqrt(x) + c) + a)*x^3, x)

Mupad [F(-1)]

Timed out.

$$\int x^3(a + b \tan(c + d\sqrt{x})) dx = \int x^3(a + b \tan(c + d\sqrt{x})) dx$$

[In] int(x^3*(a + b*tan(c + d*x^(1/2))),x)

[Out] int(x^3*(a + b*tan(c + d*x^(1/2))), x)

3.26 $\int x^2 (a + b \tan (c + d\sqrt{x})) dx$

Optimal result	150
Rubi [A] (verified)	151
Mathematica [A] (verified)	154
Maple [F]	155
Fricas [F]	155
Sympy [F]	155
Maxima [B] (verification not implemented)	155
Giac [F]	156
Mupad [F(-1)]	156

Optimal result

Integrand size = 18, antiderivative size = 195

$$\int x^2 (a + b \tan (c + d\sqrt{x})) dx = \frac{ax^3}{3} + \frac{1}{3}ibx^3 - \frac{2bx^{5/2} \log (1 + e^{2i(c+d\sqrt{x})})}{d} + \frac{5ibx^2 \text{PolyLog} (2, -e^{2i(c+d\sqrt{x})})}{d^2} - \frac{10bx^{3/2} \text{PolyLog} (3, -e^{2i(c+d\sqrt{x})})}{d^3} - \frac{15ibx \text{PolyLog} (4, -e^{2i(c+d\sqrt{x})})}{d^4} + \frac{15b\sqrt{x} \text{PolyLog} (5, -e^{2i(c+d\sqrt{x})})}{d^5} + \frac{15ib \text{PolyLog} (6, -e^{2i(c+d\sqrt{x})})}{2d^6}$$

```
[Out] 1/3*a*x^3+1/3*I*b*x^3-2*b*x^(5/2)*ln(1+exp(2*I*(c+d*x^(1/2))))/d+5*I*b*x^2*
polylog(2,-exp(2*I*(c+d*x^(1/2))))/d^2-10*b*x^(3/2)*polylog(3,-exp(2*I*(c+d
*x^(1/2))))/d^3-15*I*b*x*polylog(4,-exp(2*I*(c+d*x^(1/2))))/d^4+15/2*I*b*po
lylog(6,-exp(2*I*(c+d*x^(1/2))))/d^6+15*b*polylog(5,-exp(2*I*(c+d*x^(1/2)))
)*x^(1/2)/d^5
```

Rubi [A] (verified)

Time = 0.33 (sec) , antiderivative size = 195, normalized size of antiderivative = 1.00, number of steps used = 11, number of rules used = 8, $\frac{\text{number of rules}}{\text{integrand size}} = 0.444$, Rules used = {14, 3832, 3800, 2221, 2611, 6744, 2320, 6724}

$$\int x^2(a + b \tan(c + d\sqrt{x})) dx = \frac{ax^3}{3} + \frac{15ib \operatorname{PolyLog}\left(6, -e^{2i(c+d\sqrt{x})}\right)}{2d^6} + \frac{15b\sqrt{x} \operatorname{PolyLog}\left(5, -e^{2i(c+d\sqrt{x})}\right)}{d^5} - \frac{15ibx \operatorname{PolyLog}\left(4, -e^{2i(c+d\sqrt{x})}\right)}{d^4} - \frac{10bx^{3/2} \operatorname{PolyLog}\left(3, -e^{2i(c+d\sqrt{x})}\right)}{d^3} + \frac{5ibx^2 \operatorname{PolyLog}\left(2, -e^{2i(c+d\sqrt{x})}\right)}{d^2} - \frac{2bx^{5/2} \log\left(1 + e^{2i(c+d\sqrt{x})}\right)}{d} + \frac{1}{3}ibx^3$$

[In] Int[x^2*(a + b*Tan[c + d*Sqrt[x]]),x]

[Out] (a*x^3)/3 + (I/3)*b*x^3 - (2*b*x^(5/2)*Log[1 + E^((2*I)*(c + d*Sqrt[x]))])/d + ((5*I)*b*x^2*PolyLog[2, -E^((2*I)*(c + d*Sqrt[x]))])/d^2 - (10*b*x^(3/2)*PolyLog[3, -E^((2*I)*(c + d*Sqrt[x]))])/d^3 - ((15*I)*b*x*PolyLog[4, -E^((2*I)*(c + d*Sqrt[x]))])/d^4 + (15*b*Sqrt[x]*PolyLog[5, -E^((2*I)*(c + d*Sqrt[x]))])/d^5 + (((15*I)/2)*b*PolyLog[6, -E^((2*I)*(c + d*Sqrt[x]))])/d^6

Rule 14

Int[(u_)*((c_)*(x_))^(m_), x_Symbol] :> Int[ExpandIntegrand[(c*x)^m*u, x], x] /; FreeQ[{c, m}, x] && SumQ[u] && !LinearQ[u, x] && !MatchQ[u, (a_ + (b_)*(v_)) /; FreeQ[{a, b}, x] && InverseFunctionQ[v]]

Rule 2221

Int[(((F_)^((g_)*((e_) + (f_)*(x_))))^(n_))*((c_) + (d_)*(x_))^(m_)]/((a_) + (b_)*((F_)^((g_)*((e_) + (f_)*(x_))))^(n_)), x_Symbol] :> Simp[(((c + d*x)^m/(b*f*g*n*Log[F]))*Log[1 + b*((F^(g*(e + f*x)))^n/a)], x] - Dist[d*(m/(b*f*g*n*Log[F])), Int[(c + d*x)^(m - 1)*Log[1 + b*((F^(g*(e + f*x)))^n/a)], x], x] /; FreeQ[{F, a, b, c, d, e, f, g, n}, x] && IGtQ[m, 0]

Rule 2320

```
Int[u_, x_Symbol] := With[{v = FunctionOfExponential[u, x]}, Dist[v/D[v, x]
, Subst[Int[FunctionOfExponentialFunction[u, x]/x, x], x, v], x]] /; Functi
onOfExponentialQ[u, x] && !MatchQ[u, (w_)*((a_)*(v_)^(n_))^(m_)] /; FreeQ[
{a, m, n}, x] && IntegerQ[m*n] && !MatchQ[u, E^((c_)*((a_) + (b_)*x))*
(F_)^v_] /; FreeQ[{a, b, c}, x] && InverseFunctionQ[F[x]]]
```

Rule 2611

```
Int[Log[1 + (e_)*((F_)^((c_)*((a_) + (b_)*(x_))))^(n_)]*((f_) + (g_)
*(x_))^(m_), x_Symbol] := Simp[(-f + g*x)^m*(PolyLog[2, (-e)*(F^(c*(a +
b*x)))^n]/(b*c*n*Log[F])), x] + Dist[g*(m/(b*c*n*Log[F])), Int[(f + g*x)^(m
- 1)*PolyLog[2, (-e)*(F^(c*(a + b*x)))^n], x], x] /; FreeQ[{F, a, b, c, e,
f, g, n}, x] && GtQ[m, 0]
```

Rule 3800

```
Int[((c_) + (d_)*(x_))^(m_)*tan[(e_) + (f_)*(x_)], x_Symbol] := Simp[I
*((c + d*x)^(m + 1)/(d*(m + 1))), x] - Dist[2*I, Int[(c + d*x)^m*(E^(2*I*(e
+ f*x)))/(1 + E^(2*I*(e + f*x))), x], x] /; FreeQ[{c, d, e, f}, x] && IGtQ
[m, 0]
```

Rule 3832

```
Int[(x_)^(m_)*((a_) + (b_)*Tan[(c_) + (d_)*(x_)^(n_)])^(p_), x_Symbol
] := Dist[1/n, Subst[Int[x^(Simplify[(m + 1)/n] - 1)*(a + b*Tan[c + d*x])^p
, x], x, x^n], x] /; FreeQ[{a, b, c, d, m, n, p}, x] && IGtQ[Simplify[(m +
1)/n], 0] && IntegerQ[p]
```

Rule 6724

```
Int[PolyLog[n_, (c_)*((a_) + (b_)*(x_))^(p_)]/((d_) + (e_)*(x_)), x_S
ymbol] := Simp[PolyLog[n + 1, c*(a + b*x)^p]/(e*p), x] /; FreeQ[{a, b, c, d
, e, n, p}, x] && EqQ[b*d, a*e]
```

Rule 6744

```
Int[((e_) + (f_)*(x_))^(m_)*PolyLog[n_, (d_)*((F_)^((c_)*((a_) + (b_)
*(x_))))^(p_)], x_Symbol] := Simp[(e + f*x)^m*(PolyLog[n + 1, d*(F^(c*(a
+ b*x)))^p]/(b*c*p*Log[F])), x] - Dist[f*(m/(b*c*p*Log[F])), Int[(e + f*x)^(
m - 1)*PolyLog[n + 1, d*(F^(c*(a + b*x)))^p], x], x] /; FreeQ[{F, a, b, c,
d, e, f, n, p}, x] && GtQ[m, 0]
```

Rubi steps

$$\text{integral} = \int (ax^2 + bx^2 \tan(c + d\sqrt{x})) dx$$

$$\begin{aligned}
&= \frac{ax^3}{3} + b \int x^2 \tan(c + d\sqrt{x}) dx \\
&= \frac{ax^3}{3} + (2b)\text{Subst}\left(\int x^5 \tan(c + dx) dx, x, \sqrt{x}\right) \\
&= \frac{ax^3}{3} + \frac{1}{3}ibx^3 - (4ib)\text{Subst}\left(\int \frac{e^{2i(c+dx)}x^5}{1 + e^{2i(c+dx)}} dx, x, \sqrt{x}\right) \\
&= \frac{ax^3}{3} + \frac{1}{3}ibx^3 - \frac{2bx^{5/2} \log\left(1 + e^{2i(c+d\sqrt{x})}\right)}{d} + \frac{(10b)\text{Subst}\left(\int x^4 \log\left(1 + e^{2i(c+dx)}\right) dx, x, \sqrt{x}\right)}{d} \\
&= \frac{ax^3}{3} + \frac{1}{3}ibx^3 - \frac{2bx^{5/2} \log\left(1 + e^{2i(c+d\sqrt{x})}\right)}{d} + \frac{5ibx^2 \text{PolyLog}\left(2, -e^{2i(c+d\sqrt{x})}\right)}{d^2} \\
&\quad - \frac{(20ib)\text{Subst}\left(\int x^3 \text{PolyLog}\left(2, -e^{2i(c+dx)}\right) dx, x, \sqrt{x}\right)}{d^2} \\
&= \frac{ax^3}{3} + \frac{1}{3}ibx^3 - \frac{2bx^{5/2} \log\left(1 + e^{2i(c+d\sqrt{x})}\right)}{d} + \frac{5ibx^2 \text{PolyLog}\left(2, -e^{2i(c+d\sqrt{x})}\right)}{d^2} \\
&\quad - \frac{10bx^{3/2} \text{PolyLog}\left(3, -e^{2i(c+d\sqrt{x})}\right)}{d^3} + \frac{(30b)\text{Subst}\left(\int x^2 \text{PolyLog}\left(3, -e^{2i(c+dx)}\right) dx, x, \sqrt{x}\right)}{d^3} \\
&= \frac{ax^3}{3} + \frac{1}{3}ibx^3 - \frac{2bx^{5/2} \log\left(1 + e^{2i(c+d\sqrt{x})}\right)}{d} + \frac{5ibx^2 \text{PolyLog}\left(2, -e^{2i(c+d\sqrt{x})}\right)}{d^2} \\
&\quad - \frac{10bx^{3/2} \text{PolyLog}\left(3, -e^{2i(c+d\sqrt{x})}\right)}{d^3} - \frac{15ibx \text{PolyLog}\left(4, -e^{2i(c+d\sqrt{x})}\right)}{d^4} \\
&\quad + \frac{(30ib)\text{Subst}\left(\int x \text{PolyLog}\left(4, -e^{2i(c+dx)}\right) dx, x, \sqrt{x}\right)}{d^4} \\
&= \frac{ax^3}{3} + \frac{1}{3}ibx^3 - \frac{2bx^{5/2} \log\left(1 + e^{2i(c+d\sqrt{x})}\right)}{d} \\
&\quad + \frac{5ibx^2 \text{PolyLog}\left(2, -e^{2i(c+d\sqrt{x})}\right)}{d^2} - \frac{10bx^{3/2} \text{PolyLog}\left(3, -e^{2i(c+d\sqrt{x})}\right)}{d^3} \\
&\quad - \frac{15ibx \text{PolyLog}\left(4, -e^{2i(c+d\sqrt{x})}\right)}{d^4} + \frac{15b\sqrt{x} \text{PolyLog}\left(5, -e^{2i(c+d\sqrt{x})}\right)}{d^5} \\
&\quad - \frac{(15b)\text{Subst}\left(\int \text{PolyLog}\left(5, -e^{2i(c+dx)}\right) dx, x, \sqrt{x}\right)}{d^5}
\end{aligned}$$

$$\begin{aligned}
&= \frac{ax^3}{3} + \frac{1}{3}ibx^3 - \frac{2bx^{5/2} \log\left(1 + e^{2i(c+d\sqrt{x})}\right)}{d} + \frac{5ibx^2 \text{PolyLog}\left(2, -e^{2i(c+d\sqrt{x})}\right)}{d^2} \\
&\quad - \frac{10bx^{3/2} \text{PolyLog}\left(3, -e^{2i(c+d\sqrt{x})}\right)}{d^3} - \frac{15ibx \text{PolyLog}\left(4, -e^{2i(c+d\sqrt{x})}\right)}{d^4} \\
&\quad + \frac{15b\sqrt{x} \text{PolyLog}\left(5, -e^{2i(c+d\sqrt{x})}\right)}{d^5} + \frac{(15ib) \text{Subst}\left(\int \frac{\text{PolyLog}(5, -x)}{x} dx, x, e^{2i(c+d\sqrt{x})}\right)}{2d^6} \\
&= \frac{ax^3}{3} + \frac{1}{3}ibx^3 - \frac{2bx^{5/2} \log\left(1 + e^{2i(c+d\sqrt{x})}\right)}{d} + \frac{5ibx^2 \text{PolyLog}\left(2, -e^{2i(c+d\sqrt{x})}\right)}{d^2} \\
&\quad - \frac{10bx^{3/2} \text{PolyLog}\left(3, -e^{2i(c+d\sqrt{x})}\right)}{d^3} - \frac{15ibx \text{PolyLog}\left(4, -e^{2i(c+d\sqrt{x})}\right)}{d^4} \\
&\quad + \frac{15b\sqrt{x} \text{PolyLog}\left(5, -e^{2i(c+d\sqrt{x})}\right)}{d^5} + \frac{15ib \text{PolyLog}\left(6, -e^{2i(c+d\sqrt{x})}\right)}{2d^6}
\end{aligned}$$

Mathematica [A] (verified)

Time = 0.03 (sec) , antiderivative size = 195, normalized size of antiderivative = 1.00

$$\begin{aligned}
\int x^2(a + b \tan(c + d\sqrt{x})) dx &= \frac{ax^3}{3} + \frac{1}{3}ibx^3 - \frac{2bx^{5/2} \log\left(1 + e^{2i(c+d\sqrt{x})}\right)}{d} \\
&\quad + \frac{5ibx^2 \text{PolyLog}\left(2, -e^{2i(c+d\sqrt{x})}\right)}{d^2} \\
&\quad - \frac{10bx^{3/2} \text{PolyLog}\left(3, -e^{2i(c+d\sqrt{x})}\right)}{d^3} \\
&\quad - \frac{15ibx \text{PolyLog}\left(4, -e^{2i(c+d\sqrt{x})}\right)}{d^4} \\
&\quad + \frac{15b\sqrt{x} \text{PolyLog}\left(5, -e^{2i(c+d\sqrt{x})}\right)}{d^5} \\
&\quad + \frac{15ib \text{PolyLog}\left(6, -e^{2i(c+d\sqrt{x})}\right)}{2d^6}
\end{aligned}$$

[In] Integrate[x^2*(a + b*Tan[c + d*Sqrt[x]]),x]

[Out] (a*x^3)/3 + (I/3)*b*x^3 - (2*b*x^(5/2)*Log[1 + E^((2*I)*(c + d*Sqrt[x]))])/d + ((5*I)*b*x^2*PolyLog[2, -E^((2*I)*(c + d*Sqrt[x]))])/d^2 - (10*b*x^(3/2)*PolyLog[3, -E^((2*I)*(c + d*Sqrt[x]))])/d^3 - ((15*I)*b*x*PolyLog[4, -E^((2*I)*(c + d*Sqrt[x]))])/d^4 + (15*b*Sqrt[x]*PolyLog[5, -E^((2*I)*(c + d*Sqrt[x]))])/d^5 + (((15*I)/2)*b*PolyLog[6, -E^((2*I)*(c + d*Sqrt[x]))])/d^6


```

*b*c^3 + 75*(d*sqrt(x) + c)^2*a*c^4 + 75*I*(d*sqrt(x) + c)^2*b*c^4 - 30*(d*
sqrt(x) + c)*a*c^5 - 30*b*c^5*log(sec(d*sqrt(x) + c)) + 2*(-48*I*(d*sqrt(x)
+ c)^5*b + 150*I*(d*sqrt(x) + c)^4*b*c - 200*I*(d*sqrt(x) + c)^3*b*c^2 + 1
50*I*(d*sqrt(x) + c)^2*b*c^3 - 75*I*(d*sqrt(x) + c)*b*c^4)*arctan2(sin(2*d*
sqrt(x) + 2*c), cos(2*d*sqrt(x) + 2*c) + 1) + 15*(16*I*(d*sqrt(x) + c)^4*b
- 40*I*(d*sqrt(x) + c)^3*b*c + 40*I*(d*sqrt(x) + c)^2*b*c^2 - 20*I*(d*sqrt(
x) + c)*b*c^3 + 5*I*b*c^4)*dilog(-e^(2*I*d*sqrt(x) + 2*I*c)) - (48*(d*sqrt(
x) + c)^5*b - 150*(d*sqrt(x) + c)^4*b*c + 200*(d*sqrt(x) + c)^3*b*c^2 - 150
*(d*sqrt(x) + c)^2*b*c^3 + 75*(d*sqrt(x) + c)*b*c^4)*log(cos(2*d*sqrt(x) +
2*c)^2 + sin(2*d*sqrt(x) + 2*c)^2 + 2*cos(2*d*sqrt(x) + 2*c) + 1) + 360*I*b
*polylog(6, -e^(2*I*d*sqrt(x) + 2*I*c)) + 90*(8*(d*sqrt(x) + c)*b - 5*b*c)*
polylog(5, -e^(2*I*d*sqrt(x) + 2*I*c)) + 60*(-12*I*(d*sqrt(x) + c)^2*b + 15
*I*(d*sqrt(x) + c)*b*c - 5*I*b*c^2)*polylog(4, -e^(2*I*d*sqrt(x) + 2*I*c))
- 30*(16*(d*sqrt(x) + c)^3*b - 30*(d*sqrt(x) + c)^2*b*c + 20*(d*sqrt(x) + c
)*b*c^2 - 5*b*c^3)*polylog(3, -e^(2*I*d*sqrt(x) + 2*I*c)))/d^6

```

Giac [F]

$$\int x^2(a + b \tan(c + d\sqrt{x})) dx = \int (b \tan(d\sqrt{x} + c) + a)x^2 dx$$

```
[In] integrate(x^2*(a+b*tan(c+d*x^(1/2))),x, algorithm="giac")
```

```
[Out] integrate((b*tan(d*sqrt(x) + c) + a)*x^2, x)
```

Mupad [F(-1)]

Timed out.

$$\int x^2(a + b \tan(c + d\sqrt{x})) dx = \int x^2(a + b \tan(c + d\sqrt{x})) dx$$

```
[In] int(x^2*(a + b*tan(c + d*x^(1/2))),x)
```

```
[Out] int(x^2*(a + b*tan(c + d*x^(1/2))), x)
```

3.27 $\int x(a + b \tan(c + d\sqrt{x})) dx$

Optimal result	157
Rubi [A] (verified)	157
Mathematica [A] (verified)	160
Maple [F]	161
Fricas [F]	161
Sympy [F]	161
Maxima [B] (verification not implemented)	161
Giac [F]	162
Mupad [F(-1)]	162

Optimal result

Integrand size = 16, antiderivative size = 135

$$\int x(a + b \tan(c + d\sqrt{x})) dx = \frac{ax^2}{2} + \frac{1}{2}ibx^2 - \frac{2bx^{3/2} \log(1 + e^{2i(c+d\sqrt{x})})}{d} + \frac{3ibx \operatorname{PolyLog}(2, -e^{2i(c+d\sqrt{x})})}{d^2} - \frac{3b\sqrt{x} \operatorname{PolyLog}(3, -e^{2i(c+d\sqrt{x})})}{d^3} - \frac{3ib \operatorname{PolyLog}(4, -e^{2i(c+d\sqrt{x})})}{2d^4}$$

[Out] 1/2*a*x^2+1/2*I*b*x^2-2*b*x^(3/2)*ln(1+exp(2*I*(c+d*x^(1/2))))/d+3*I*b*x*polylog(2,-exp(2*I*(c+d*x^(1/2))))/d^2-3/2*I*b*polylog(4,-exp(2*I*(c+d*x^(1/2))))/d^3-3*b*polylog(3,-exp(2*I*(c+d*x^(1/2))))*x^(1/2)/d^3

Rubi [A] (verified)

Time = 0.23 (sec) , antiderivative size = 135, normalized size of antiderivative = 1.00, number of steps used = 9, number of rules used = 8, $\frac{\text{number of rules}}{\text{integrand size}} = 0.500$, Rules used

= {14, 3832, 3800, 2221, 2611, 6744, 2320, 6724}

$$\int x(a + b \tan(c + d\sqrt{x})) dx = \frac{ax^2}{2} - \frac{3ib \operatorname{PolyLog}\left(4, -e^{2i(c+d\sqrt{x})}\right)}{2d^4} - \frac{3b\sqrt{x} \operatorname{PolyLog}\left(3, -e^{2i(c+d\sqrt{x})}\right)}{d^3} + \frac{3ibx \operatorname{PolyLog}\left(2, -e^{2i(c+d\sqrt{x})}\right)}{d^2} - \frac{2bx^{3/2} \log\left(1 + e^{2i(c+d\sqrt{x})}\right)}{d} + \frac{1}{2}ibx^2$$

[In] Int[x*(a + b*Tan[c + d*Sqrt[x]]),x]

[Out] (a*x^2)/2 + (I/2)*b*x^2 - (2*b*x^(3/2)*Log[1 + E^((2*I)*(c + d*Sqrt[x]))])/d + ((3*I)*b*x*PolyLog[2, -E^((2*I)*(c + d*Sqrt[x]))])/d^2 - (3*b*Sqrt[x]*PolyLog[3, -E^((2*I)*(c + d*Sqrt[x]))])/d^3 - ((3*I)/2)*b*PolyLog[4, -E^((2*I)*(c + d*Sqrt[x]))])/d^4

Rule 14

```
Int[(u_)*((c_)*(x_))^(m_), x_Symbol] := Int[ExpandIntegrand[(c*x)^m*u, x], x] /; FreeQ[{c, m}, x] && SumQ[u] && !LinearQ[u, x] && !MatchQ[u, (a_ + (b_)*(v_)) /; FreeQ[{a, b}, x] && InverseFunctionQ[v]]
```

Rule 2221

```
Int[(((F_)^((g_)*((e_) + (f_)*(x_))))^(n_))*((c_) + (d_)*(x_))^(m_)] / ((a_) + (b_)*((F_)^((g_)*((e_) + (f_)*(x_))))^(n_)), x_Symbol] := Simp[((c + d*x)^m/(b*f*g*n*Log[F]))*Log[1 + b*((F^(g*(e + f*x)))^n/a)], x] - Dist[d*(m/(b*f*g*n*Log[F])), Int[(c + d*x)^(m - 1)*Log[1 + b*((F^(g*(e + f*x)))^n/a)], x], x] /; FreeQ[{F, a, b, c, d, e, f, g, n}, x] && IGtQ[m, 0]
```

Rule 2320

```
Int[u_, x_Symbol] := With[{v = FunctionOfExponential[u, x]}, Dist[v/D[v, x], Subst[Int[FunctionOfExponentialFunction[u, x]/x, x], x, v], x] /; FunctionOfExponentialQ[u, x] && !MatchQ[u, (w_)*((a_)*(v_)^(n_))^(m_)] /; FreeQ[{a, m, n}, x] && IntegerQ[m*n] && !MatchQ[u, E^((c_)*((a_) + (b_)*x))*(F_)[v_] /; FreeQ[{a, b, c}, x] && InverseFunctionQ[F[x]]]
```

Rule 2611

```
Int[Log[1 + (e_)*((F_)^((c_)*((a_) + (b_)*(x_))))^(n_)]*((f_) + (g_)*(x_))^(m_), x_Symbol] := Simp[(-f + g*x)^m*(PolyLog[2, (-e)*(F^(c*(a + b*x)))^n]/(b*c*n*Log[F])), x] + Dist[g*(m/(b*c*n*Log[F])), Int[(f + g*x)^m
```

$- 1) * \text{PolyLog}[2, (-e) * (F^{(c*(a + b*x))})^n], x], x] /;$ FreeQ[{F, a, b, c, e, f, g, n}, x] && GtQ[m, 0]

Rule 3800

$\text{Int}[(c + d*x)^m * \tan[e + f*x], x_Symbol] \rightarrow \text{Simp}[I * ((c + d*x)^{m+1} / (d*(m+1))), x] - \text{Dist}[2*I, \text{Int}[(c + d*x)^m * (E^{2*I*(e + f*x)}) / (1 + E^{2*I*(e + f*x)})], x], x] /;$ FreeQ[{c, d, e, f}, x] && IGtQ[m, 0]

Rule 3832

$\text{Int}[x^m * ((a + b*Tan[c + d*x])^n)^p, x_Symbol] \rightarrow \text{Dist}[1/n, \text{Subst}[\text{Int}[x^{(\text{Simplify}[(m+1)/n] - 1) * (a + b*Tan[c + d*x])^p}, x], x, x^n], x] /;$ FreeQ[{a, b, c, d, m, n, p}, x] && IGtQ[Simplify[(m+1)/n], 0] && IntegerQ[p]

Rule 6724

$\text{Int}[\text{PolyLog}[n, (c + d*x)^p] / ((d + e*x)), x_Symbol] \rightarrow \text{Simp}[\text{PolyLog}[n + 1, c*(a + b*x)^p / (e*p), x] /;$ FreeQ[{a, b, c, d, e, n, p}, x] && EqQ[b*d, a*e]

Rule 6744

$\text{Int}[(e + f*x)^m * \text{PolyLog}[n, (d + e*x)^p] / (b*c*p * \text{Log}[F]), x_Symbol] \rightarrow \text{Simp}[(e + f*x)^m * (\text{PolyLog}[n + 1, d*(F^{(c*(a + b*x))})^p] / (b*c*p * \text{Log}[F])), x] - \text{Dist}[f*(m / (b*c*p * \text{Log}[F])), \text{Int}[(e + f*x)^{m-1} * \text{PolyLog}[n + 1, d*(F^{(c*(a + b*x))})^p], x], x] /;$ FreeQ[{F, a, b, c, d, e, f, n, p}, x] && GtQ[m, 0]

Rubi steps

$$\begin{aligned}
 \text{integral} &= \int (ax + bx \tan(c + d\sqrt{x})) dx \\
 &= \frac{ax^2}{2} + b \int x \tan(c + d\sqrt{x}) dx \\
 &= \frac{ax^2}{2} + (2b) \text{Subst}\left(\int x^3 \tan(c + dx) dx, x, \sqrt{x}\right) \\
 &= \frac{ax^2}{2} + \frac{1}{2} ibx^2 - (4ib) \text{Subst}\left(\int \frac{e^{2i(c+dx)} x^3}{1 + e^{2i(c+dx)}} dx, x, \sqrt{x}\right) \\
 &= \frac{ax^2}{2} + \frac{1}{2} ibx^2 - \frac{2bx^{3/2} \log\left(1 + e^{2i(c+d\sqrt{x})}\right)}{d} + \frac{(6b) \text{Subst}\left(\int x^2 \log\left(1 + e^{2i(c+dx)}\right) dx, x, \sqrt{x}\right)}{d}
 \end{aligned}$$

$$\begin{aligned}
&= \frac{ax^2}{2} + \frac{1}{2}ibx^2 - \frac{2bx^{3/2} \log\left(1 + e^{2i(c+d\sqrt{x})}\right)}{d} + \frac{3ibx \operatorname{PolyLog}\left(2, -e^{2i(c+d\sqrt{x})}\right)}{d^2} \\
&\quad - \frac{(6ib)\operatorname{Subst}\left(\int x \operatorname{PolyLog}\left(2, -e^{2i(c+dx)}\right) dx, x, \sqrt{x}\right)}{d^2} \\
&= \frac{ax^2}{2} + \frac{1}{2}ibx^2 - \frac{2bx^{3/2} \log\left(1 + e^{2i(c+d\sqrt{x})}\right)}{d} + \frac{3ibx \operatorname{PolyLog}\left(2, -e^{2i(c+d\sqrt{x})}\right)}{d^2} \\
&\quad - \frac{3b\sqrt{x} \operatorname{PolyLog}\left(3, -e^{2i(c+d\sqrt{x})}\right)}{d^3} + \frac{(3b)\operatorname{Subst}\left(\int \operatorname{PolyLog}\left(3, -e^{2i(c+dx)}\right) dx, x, \sqrt{x}\right)}{d^3} \\
&= \frac{ax^2}{2} + \frac{1}{2}ibx^2 - \frac{2bx^{3/2} \log\left(1 + e^{2i(c+d\sqrt{x})}\right)}{d} + \frac{3ibx \operatorname{PolyLog}\left(2, -e^{2i(c+d\sqrt{x})}\right)}{d^2} \\
&\quad - \frac{3b\sqrt{x} \operatorname{PolyLog}\left(3, -e^{2i(c+d\sqrt{x})}\right)}{d^3} - \frac{(3ib)\operatorname{Subst}\left(\int \frac{\operatorname{PolyLog}(3, -x)}{x} dx, x, e^{2i(c+d\sqrt{x})}\right)}{2d^4} \\
&= \frac{ax^2}{2} + \frac{1}{2}ibx^2 - \frac{2bx^{3/2} \log\left(1 + e^{2i(c+d\sqrt{x})}\right)}{d} + \frac{3ibx \operatorname{PolyLog}\left(2, -e^{2i(c+d\sqrt{x})}\right)}{d^2} \\
&\quad - \frac{3b\sqrt{x} \operatorname{PolyLog}\left(3, -e^{2i(c+d\sqrt{x})}\right)}{d^3} - \frac{3ib \operatorname{PolyLog}\left(4, -e^{2i(c+d\sqrt{x})}\right)}{2d^4}
\end{aligned}$$

Mathematica [A] (verified)

Time = 0.03 (sec) , antiderivative size = 135, normalized size of antiderivative = 1.00

$$\begin{aligned}
\int x(a + b \tan(c + d\sqrt{x})) dx &= \frac{ax^2}{2} + \frac{1}{2}ibx^2 - \frac{2bx^{3/2} \log\left(1 + e^{2i(c+d\sqrt{x})}\right)}{d} \\
&\quad + \frac{3ibx \operatorname{PolyLog}\left(2, -e^{2i(c+d\sqrt{x})}\right)}{d^2} \\
&\quad - \frac{3b\sqrt{x} \operatorname{PolyLog}\left(3, -e^{2i(c+d\sqrt{x})}\right)}{d^3} \\
&\quad - \frac{3ib \operatorname{PolyLog}\left(4, -e^{2i(c+d\sqrt{x})}\right)}{2d^4}
\end{aligned}$$

[In] Integrate[x*(a + b*Tan[c + d*Sqrt[x]]),x]

[Out] (a*x^2)/2 + (I/2)*b*x^2 - (2*b*x^(3/2)*Log[1 + E^((2*I)*(c + d*Sqrt[x]))])/d + ((3*I)*b*x*PolyLog[2, -E^((2*I)*(c + d*Sqrt[x]))])/d^2 - (3*b*Sqrt[x]*PolyLog[3, -E^((2*I)*(c + d*Sqrt[x]))])/d^3 - (((3*I)/2)*b*PolyLog[4, -E^((2*I)*(c + d*Sqrt[x]))])/d^4

Maple [F]

$$\int x(a + b \tan(c + d\sqrt{x})) dx$$

```
[In] int(x*(a+b*tan(c+d*x^(1/2))),x)
```

```
[Out] int(x*(a+b*tan(c+d*x^(1/2))),x)
```

Fricas [F]

$$\int x(a + b \tan(c + d\sqrt{x})) dx = \int (b \tan(d\sqrt{x} + c) + a)x dx$$

```
[In] integrate(x*(a+b*tan(c+d*x^(1/2))),x, algorithm="fricas")
```

```
[Out] integral(b*x*tan(d*sqrt(x) + c) + a*x, x)
```

Sympy [F]

$$\int x(a + b \tan(c + d\sqrt{x})) dx = \int x(a + b \tan(c + d\sqrt{x})) dx$$

```
[In] integrate(x*(a+b*tan(c+d*x**(1/2))),x)
```

```
[Out] Integral(x*(a + b*tan(c + d*sqrt(x))), x)
```

Maxima [B] (verification not implemented)

Both result and optimal contain complex but leaf count of result is larger than twice the leaf count of optimal. 359 vs. 2(102) = 204.

Time = 0.39 (sec) , antiderivative size = 359, normalized size of antiderivative = 2.66

$$\int x(a + b \tan(c + d\sqrt{x})) dx$$

$$= \frac{3(d\sqrt{x} + c)^4 a + 3i(d\sqrt{x} + c)^4 b - 12(d\sqrt{x} + c)^3 ac - 12i(d\sqrt{x} + c)^3 bc + 18(d\sqrt{x} + c)^2 ac^2 + 18i(d\sqrt{x} + c)^2 bc^2 - 12(d\sqrt{x} + c) a c^3 - 12i(d\sqrt{x} + c) b c^3 + 18(d\sqrt{x} + c) a c^2 + 18i(d\sqrt{x} + c) b c^2 - 12(d\sqrt{x} + c) a c - 12i(d\sqrt{x} + c) b c + 18(d\sqrt{x} + c) a + 18i(d\sqrt{x} + c) b}{6}$$

```
[In] integrate(x*(a+b*tan(c+d*x^(1/2))),x, algorithm="maxima")
```

```
[Out] 1/6*(3*(d*sqrt(x) + c)^4*a + 3*I*(d*sqrt(x) + c)^4*b - 12*(d*sqrt(x) + c)^3*a*c - 12*I*(d*sqrt(x) + c)^3*b*c + 18*(d*sqrt(x) + c)^2*a*c^2 + 18*I*(d*sqrt(x) + c)^2*b*c^2 - 12*(d*sqrt(x) + c)*a*c^3 - 12*I*(d*sqrt(x) + c)*b*c^3 + 18*(d*sqrt(x) + c)*a*c + 18*I*(d*sqrt(x) + c)*b*c)
```

+ c)) + 4*(-4*I*(d*sqrt(x) + c)^3*b + 9*I*(d*sqrt(x) + c)^2*b*c - 9*I*(d*sqrt(x) + c)*b*c^2)*arctan2(sin(2*d*sqrt(x) + 2*c), cos(2*d*sqrt(x) + 2*c) + 1) + 6*(4*I*(d*sqrt(x) + c)^2*b - 6*I*(d*sqrt(x) + c)*b*c + 3*I*b*c^2)*dilog(-e^(2*I*d*sqrt(x) + 2*I*c)) - 2*(4*(d*sqrt(x) + c)^3*b - 9*(d*sqrt(x) + c)^2*b*c + 9*(d*sqrt(x) + c)*b*c^2)*log(cos(2*d*sqrt(x) + 2*c)^2 + sin(2*d*sqrt(x) + 2*c)^2 + 2*cos(2*d*sqrt(x) + 2*c) + 1) - 12*I*b*polylog(4, -e^(2*I*d*sqrt(x) + 2*I*c)) - 6*(4*(d*sqrt(x) + c)*b - 3*b*c)*polylog(3, -e^(2*I*d*sqrt(x) + 2*I*c)))/d^4

Giac [F]

$$\int x(a + b \tan(c + d\sqrt{x})) dx = \int (b \tan(d\sqrt{x} + c) + a)x dx$$

[In] integrate(x*(a+b*tan(c+d*x^(1/2))),x, algorithm="giac")

[Out] integrate((b*tan(d*sqrt(x) + c) + a)*x, x)

Mupad [F(-1)]

Timed out.

$$\int x(a + b \tan(c + d\sqrt{x})) dx = \int x(a + b \tan(c + d\sqrt{x})) dx$$

[In] int(x*(a + b*tan(c + d*x^(1/2))),x)

[Out] int(x*(a + b*tan(c + d*x^(1/2))), x)

3.28 $\int (a + b \tan(c + d\sqrt{x})) dx$

Optimal result	163
Rubi [A] (verified)	163
Mathematica [A] (verified)	165
Maple [F]	165
Fricas [B] (verification not implemented)	165
Sympy [F]	166
Maxima [F]	166
Giac [F]	166
Mupad [B] (verification not implemented)	166

Optimal result

Integrand size = 14, antiderivative size = 66

$$\int (a + b \tan(c + d\sqrt{x})) dx = ax + ibx - \frac{2b\sqrt{x} \log(1 + e^{2i(c+d\sqrt{x})})}{d} + \frac{ib \operatorname{PolyLog}(2, -e^{2i(c+d\sqrt{x})})}{d^2}$$

[Out] a*x+I*b*x+I*b*polylog(2,-exp(2*I*(c+d*x^(1/2))))/d^2-2*b*ln(1+exp(2*I*(c+d*x^(1/2))))*x^(1/2)/d

Rubi [A] (verified)

Time = 0.11 (sec) , antiderivative size = 66, normalized size of antiderivative = 1.00, number of steps used = 6, number of rules used = 5, $\frac{\text{number of rules}}{\text{integrand size}} = 0.357$, Rules used = {3824, 3800, 2221, 2317, 2438}

$$\int (a + b \tan(c + d\sqrt{x})) dx = ax + \frac{ib \operatorname{PolyLog}(2, -e^{2i(c+d\sqrt{x})})}{d^2} - \frac{2b\sqrt{x} \log(1 + e^{2i(c+d\sqrt{x})})}{d} + ibx$$

[In] Int[a + b*Tan[c + d*Sqrt[x]],x]

[Out] a*x + I*b*x - (2*b*Sqrt[x]*Log[1 + E^((2*I)*(c + d*Sqrt[x]))])/d + (I*b*PolyLog[2, -E^((2*I)*(c + d*Sqrt[x]))])/d^2

Rule 2221

```
Int[(((F_)^((g_)*(e_) + (f_)*(x_)))^(n_))*((c_) + (d_)*(x_))^(m_)]/
((a_) + (b_)*((F_)^((g_)*(e_) + (f_)*(x_)))^(n_)), x_Symbol] := Simp
[((c + d*x)^m/(b*f*g*n*Log[F]))*Log[1 + b*((F^(g*(e + f*x)))^n/a)], x] - Di
st[d*(m/(b*f*g*n*Log[F])), Int[(c + d*x)^(m - 1)*Log[1 + b*((F^(g*(e + f*x)
))^n/a)], x], x] /; FreeQ[{F, a, b, c, d, e, f, g, n}, x] && IGtQ[m, 0]
```

Rule 2317

```
Int[Log[(a_) + (b_)*((F_)^((e_)*((c_) + (d_)*(x_)))^(n_))], x_Symbol]
:= Dist[1/(d*e*n*Log[F]), Subst[Int[Log[a + b*x]/x, x], x, (F^(e*(c + d*x)
))^n], x] /; FreeQ[{F, a, b, c, d, e, n}, x] && GtQ[a, 0]
```

Rule 2438

```
Int[Log[(c_)*((d_) + (e_)*(x_)^(n_))]/(x_), x_Symbol] := Simp[-PolyLog[2
, (-c)*e*x^n]/n, x] /; FreeQ[{c, d, e, n}, x] && EqQ[c*d, 1]
```

Rule 3800

```
Int[(((c_) + (d_)*(x_))^(m_))*tan[(e_) + (f_)*(x_)], x_Symbol] := Simp[I
*((c + d*x)^(m + 1)/(d*(m + 1))), x] - Dist[2*I, Int[(c + d*x)^m*(E^(2*I*(e
 + f*x)))/(1 + E^(2*I*(e + f*x))), x], x] /; FreeQ[{c, d, e, f}, x] && IGtQ
[m, 0]
```

Rule 3824

```
Int[(((a_) + (b_)*Tan[(c_) + (d_)*(x_)^(n_)])^(p_)), x_Symbol] := Dist[1
/n, Subst[Int[x^(1/n - 1)*(a + b*Tan[c + d*x])^p, x], x, x^n], x] /; FreeQ[
{a, b, c, d, p}, x] && IGtQ[1/n, 0] && IntegerQ[p]
```

Rubi steps

$$\text{integral} = ax + b \int \tan(c + d\sqrt{x}) dx$$

$$= ax + (2b)\text{Subst}\left(\int x \tan(c + dx) dx, x, \sqrt{x}\right)$$

$$= ax + ibx - (4ib)\text{Subst}\left(\int \frac{e^{2i(c+dx)}x}{1 + e^{2i(c+dx)}} dx, x, \sqrt{x}\right)$$

$$= ax + ibx - \frac{2b\sqrt{x} \log\left(1 + e^{2i(c+d\sqrt{x})}\right)}{d} + \frac{(2b)\text{Subst}\left(\int \log\left(1 + e^{2i(c+dx)}\right) dx, x, \sqrt{x}\right)}{d}$$

$$= ax + ibx - \frac{2b\sqrt{x} \log\left(1 + e^{2i(c+d\sqrt{x})}\right)}{d} - \frac{(ib)\text{Subst}\left(\int \frac{\log(1+x)}{x} dx, x, e^{2i(c+d\sqrt{x})}\right)}{d^2}$$

$$= ax + ibx - \frac{2b\sqrt{x} \log\left(1 + e^{2i(c+d\sqrt{x})}\right)}{d} + \frac{ib \operatorname{PolyLog}\left(2, -e^{2i(c+d\sqrt{x})}\right)}{d^2}$$

Mathematica [A] (verified)

Time = 0.02 (sec) , antiderivative size = 66, normalized size of antiderivative = 1.00

$$\int (a + b \tan(c + d\sqrt{x})) dx = ax + ibx - \frac{2b\sqrt{x} \log\left(1 + e^{2i(c+d\sqrt{x})}\right)}{d} + \frac{ib \operatorname{PolyLog}\left(2, -e^{2i(c+d\sqrt{x})}\right)}{d^2}$$

[In] Integrate[a + b*Tan[c + d*Sqrt[x]],x]

[Out] a*x + I*b*x - (2*b*Sqrt[x]*Log[1 + E^((2*I)*(c + d*Sqrt[x]))])/d + (I*b*PolyLog[2, -E^((2*I)*(c + d*Sqrt[x]))])/d^2

Maple [F]

$$\int (a + b \tan(c + d\sqrt{x})) dx$$

[In] int(a+b*tan(c+d*x^(1/2)),x)

[Out] int(a+b*tan(c+d*x^(1/2)),x)

Fricas [B] (verification not implemented)

Both result and optimal contain complex but leaf count of result is larger than twice the leaf count of optimal. 153 vs. 2(51) = 102.

Time = 0.27 (sec) , antiderivative size = 153, normalized size of antiderivative = 2.32

$$\int (a + b \tan(c + d\sqrt{x})) dx = \frac{2ad^2x - 2bd\sqrt{x} \log\left(-\frac{2(i \tan(d\sqrt{x}+c)-1)}{\tan(d\sqrt{x}+c)^2+1}\right) - 2bd\sqrt{x} \log\left(-\frac{2(-i \tan(d\sqrt{x}+c)-1)}{\tan(d\sqrt{x}+c)^2+1}\right) - i b \operatorname{Li}_2\left(\frac{2(i \tan(d\sqrt{x}+c)-1)}{\tan(d\sqrt{x}+c)^2+1}\right) + i b \operatorname{Li}_2\left(\frac{2(-i \tan(d\sqrt{x}+c)-1)}{\tan(d\sqrt{x}+c)^2+1}\right)}{2d^2}$$

[In] integrate(a+b*tan(c+d*x^(1/2)),x, algorithm="fricas")

[Out] 1/2*(2*a*d^2*x - 2*b*d*sqrt(x)*log(-2*(I*tan(d*sqrt(x) + c) - 1)/(tan(d*sqrt(x) + c)^2 + 1)) - 2*b*d*sqrt(x)*log(-2*(-I*tan(d*sqrt(x) + c) - 1)/(tan(d*sqrt(x) + c)^2 + 1)) - I*b*dilog(2*(I*tan(d*sqrt(x) + c) - 1)/(tan(d*sqrt(x) + c)^2 + 1) + 1) + I*b*dilog(2*(-I*tan(d*sqrt(x) + c) - 1)/(tan(d*sqrt(x) + c)^2 + 1) + 1))/d^2

Sympy [F]

$$\int (a + b \tan(c + d\sqrt{x})) dx = \int (a + b \tan(c + d\sqrt{x})) dx$$

```
[In] integrate(a+b*tan(c+d*x**(1/2)),x)
```

```
[Out] Integral(a + b*tan(c + d*sqrt(x)), x)
```

Maxima [F]

$$\int (a + b \tan(c + d\sqrt{x})) dx = \int b \tan(d\sqrt{x} + c) + a dx$$

```
[In] integrate(a+b*tan(c+d*x^(1/2)),x, algorithm="maxima")
```

```
[Out] a*x + 2*b*integrate(sin(2*d*sqrt(x) + 2*c)/(cos(2*d*sqrt(x) + 2*c)^2 + sin(2*d*sqrt(x) + 2*c)^2 + 2*cos(2*d*sqrt(x) + 2*c) + 1), x)
```

Giac [F]

$$\int (a + b \tan(c + d\sqrt{x})) dx = \int b \tan(d\sqrt{x} + c) + a dx$$

```
[In] integrate(a+b*tan(c+d*x^(1/2)),x, algorithm="giac")
```

```
[Out] integrate(b*tan(d*sqrt(x) + c) + a, x)
```

Mupad [B] (verification not implemented)

Time = 3.95 (sec) , antiderivative size = 150, normalized size of antiderivative = 2.27

$$\int (a + b \tan(c + d\sqrt{x})) dx = a x - \frac{b(\pi \ln(\cos(d\sqrt{x})) + 2c \ln(e^{-d\sqrt{x}2i} e^{-c2i} + 1) - \pi \ln(e^{-d\sqrt{x}2i} e^{-c2i} + 1) - \ln(\cos(c + d\sqrt{x}))) (2c - \pi)}{d^2}$$

```
[In] int(a + b*tan(c + d*x^(1/2)),x)
```

```
[Out] a*x - (b*(2*c*log(exp(-d*x^(1/2)*2i)*exp(-c*2i) + 1) - pi*log(exp(-d*x^(1/2)*2i)*exp(-c*2i) + 1) + pi*log(cos(d*x^(1/2)))) - log(cos(c + d*x^(1/2)))*(2*c - pi) - pi*log(exp(d*x^(1/2)*2i) + 1) + d^2*x*1i + polylog(2, -exp(-d*x^(1/2)*2i)*exp(-c*2i))*1i + 2*d*x^(1/2)*log(exp(-d*x^(1/2)*2i)*exp(-c*2i) + 1) + c*d*x^(1/2)*2i))/d^2
```

3.29 $\int \frac{a+b \tan(c+d\sqrt{x})}{x} dx$

Optimal result	167
Rubi [N/A]	167
Mathematica [N/A]	168
Maple [N/A] (verified)	168
Fricas [N/A]	168
Sympy [N/A]	168
Maxima [N/A]	169
Giac [N/A]	169
Mupad [N/A]	169

Optimal result

Integrand size = 18, antiderivative size = 18

$$\int \frac{a + b \tan(c + d\sqrt{x})}{x} dx = a \log(x) + b \operatorname{Int}\left(\frac{\tan(c + d\sqrt{x})}{x}, x\right)$$

[Out] a*ln(x)+b*Unintegrable(tan(c+d*x^(1/2))/x,x)

Rubi [N/A]

Not integrable

Time = 0.02 (sec) , antiderivative size = 18, normalized size of antiderivative = 1.00, number of steps used = 0, number of rules used = 0, $\frac{\text{number of rules}}{\text{integrand size}} = 0.000$, Rules used = {}

$$\int \frac{a + b \tan(c + d\sqrt{x})}{x} dx = \int \frac{a + b \tan(c + d\sqrt{x})}{x} dx$$

[In] Int[(a + b*Tan[c + d*Sqrt[x]])/x,x]

[Out] a*Log[x] + b*Defer[Int][Tan[c + d*Sqrt[x]]/x, x]

Rubi steps

$$\begin{aligned} \text{integral} &= \int \left(\frac{a}{x} + \frac{b \tan(c + d\sqrt{x})}{x} \right) dx \\ &= a \log(x) + b \int \frac{\tan(c + d\sqrt{x})}{x} dx \end{aligned}$$

Mathematica [N/A]

Not integrable

Time = 5.25 (sec) , antiderivative size = 20, normalized size of antiderivative = 1.11

$$\int \frac{a + b \tan(c + d\sqrt{x})}{x} dx = \int \frac{a + b \tan(c + d\sqrt{x})}{x} dx$$

[In] Integrate[(a + b*Tan[c + d*Sqrt[x]])/x,x]

[Out] Integrate[(a + b*Tan[c + d*Sqrt[x]])/x, x]

Maple [N/A] (verified)

Not integrable

Time = 0.45 (sec) , antiderivative size = 16, normalized size of antiderivative = 0.89

$$\int \frac{a + b \tan(c + d\sqrt{x})}{x} dx$$

[In] int((a+b*tan(c+d*x^(1/2)))/x,x)

[Out] int((a+b*tan(c+d*x^(1/2)))/x,x)

Fricas [N/A]

Not integrable

Time = 0.23 (sec) , antiderivative size = 18, normalized size of antiderivative = 1.00

$$\int \frac{a + b \tan(c + d\sqrt{x})}{x} dx = \int \frac{b \tan(d\sqrt{x} + c) + a}{x} dx$$

[In] integrate((a+b*tan(c+d*x^(1/2)))/x,x, algorithm="fricas")

[Out] integral((b*tan(d*sqrt(x) + c) + a)/x, x)

Sympy [N/A]

Not integrable

Time = 1.55 (sec) , antiderivative size = 15, normalized size of antiderivative = 0.83

$$\int \frac{a + b \tan(c + d\sqrt{x})}{x} dx = \int \frac{a + b \tan(c + d\sqrt{x})}{x} dx$$

[In] integrate((a+b*tan(c+d*x**(1/2)))/x,x)

[Out] Integral((a + b*tan(c + d*sqrt(x)))/x, x)

Maxima [N/A]

Not integrable

Time = 0.53 (sec) , antiderivative size = 68, normalized size of antiderivative = 3.78

$$\int \frac{a + b \tan(c + d\sqrt{x})}{x} dx = \int \frac{b \tan(d\sqrt{x} + c) + a}{x} dx$$

[In] integrate((a+b*tan(c+d*x^(1/2)))/x,x, algorithm="maxima")

[Out] 2*b*integrate(sin(2*d*sqrt(x) + 2*c)/((cos(2*d*sqrt(x) + 2*c)^2 + sin(2*d*sqrt(x) + 2*c)^2 + 2*cos(2*d*sqrt(x) + 2*c) + 1)*x), x) + a*log(x)

Giac [N/A]

Not integrable

Time = 0.48 (sec) , antiderivative size = 18, normalized size of antiderivative = 1.00

$$\int \frac{a + b \tan(c + d\sqrt{x})}{x} dx = \int \frac{b \tan(d\sqrt{x} + c) + a}{x} dx$$

[In] integrate((a+b*tan(c+d*x^(1/2)))/x,x, algorithm="giac")

[Out] integrate((b*tan(d*sqrt(x) + c) + a)/x, x)

Mupad [N/A]

Not integrable

Time = 4.05 (sec) , antiderivative size = 18, normalized size of antiderivative = 1.00

$$\int \frac{a + b \tan(c + d\sqrt{x})}{x} dx = \int \frac{a + b \tan(c + d\sqrt{x})}{x} dx$$

[In] int((a + b*tan(c + d*x^(1/2)))/x,x)

[Out] int((a + b*tan(c + d*x^(1/2)))/x, x)

3.30 $\int \frac{a+b \tan(c+d\sqrt{x})}{x^2} dx$

Optimal result	170
Rubi [N/A]	170
Mathematica [N/A]	171
Maple [N/A] (verified)	171
Fricas [N/A]	171
Sympy [N/A]	171
Maxima [N/A]	172
Giac [N/A]	172
Mupad [N/A]	172

Optimal result

Integrand size = 18, antiderivative size = 18

$$\int \frac{a + b \tan(c + d\sqrt{x})}{x^2} dx = -\frac{a}{x} + b \operatorname{Int}\left(\frac{\tan(c + d\sqrt{x})}{x^2}, x\right)$$

[Out] `-a/x+b*Unintegrable(tan(c+d*x^(1/2))/x^2,x)`

Rubi [N/A]

Not integrable

Time = 0.02 (sec) , antiderivative size = 18, normalized size of antiderivative = 1.00, number of steps used = 0, number of rules used = 0, $\frac{\text{number of rules}}{\text{integrand size}} = 0.000$, Rules used = {}

$$\int \frac{a + b \tan(c + d\sqrt{x})}{x^2} dx = \int \frac{a + b \tan(c + d\sqrt{x})}{x^2} dx$$

[In] `Int[(a + b*Tan[c + d*Sqrt[x]])/x^2,x]`

[Out] `-(a/x) + b*Defer[Int][Tan[c + d*Sqrt[x]]/x^2, x]`

Rubi steps

$$\begin{aligned} \text{integral} &= \int \left(\frac{a}{x^2} + \frac{b \tan(c + d\sqrt{x})}{x^2} \right) dx \\ &= -\frac{a}{x} + b \int \frac{\tan(c + d\sqrt{x})}{x^2} dx \end{aligned}$$

Mathematica [N/A]

Not integrable

Time = 12.48 (sec) , antiderivative size = 20, normalized size of antiderivative = 1.11

$$\int \frac{a + b \tan(c + d\sqrt{x})}{x^2} dx = \int \frac{a + b \tan(c + d\sqrt{x})}{x^2} dx$$

[In] Integrate[(a + b*Tan[c + d*Sqrt[x]])/x^2,x]

[Out] Integrate[(a + b*Tan[c + d*Sqrt[x]])/x^2, x]

Maple [N/A] (verified)

Not integrable

Time = 0.37 (sec) , antiderivative size = 16, normalized size of antiderivative = 0.89

$$\int \frac{a + b \tan(c + d\sqrt{x})}{x^2} dx$$

[In] int((a+b*tan(c+d*x^(1/2)))/x^2,x)

[Out] int((a+b*tan(c+d*x^(1/2)))/x^2,x)

Fricas [N/A]

Not integrable

Time = 0.24 (sec) , antiderivative size = 18, normalized size of antiderivative = 1.00

$$\int \frac{a + b \tan(c + d\sqrt{x})}{x^2} dx = \int \frac{b \tan(d\sqrt{x} + c) + a}{x^2} dx$$

[In] integrate((a+b*tan(c+d*x^(1/2)))/x^2,x, algorithm="fricas")

[Out] integral((b*tan(d*sqrt(x) + c) + a)/x^2, x)

Sympy [N/A]

Not integrable

Time = 0.78 (sec) , antiderivative size = 17, normalized size of antiderivative = 0.94

$$\int \frac{a + b \tan(c + d\sqrt{x})}{x^2} dx = \int \frac{a + b \tan(c + d\sqrt{x})}{x^2} dx$$

[In] integrate((a+b*tan(c+d*x**(1/2)))/x**2,x)

[Out] Integral((a + b*tan(c + d*sqrt(x)))/x**2, x)

Maxima [N/A]

Not integrable

Time = 0.54 (sec) , antiderivative size = 72, normalized size of antiderivative = 4.00

$$\int \frac{a + b \tan(c + d\sqrt{x})}{x^2} dx = \int \frac{b \tan(d\sqrt{x} + c) + a}{x^2} dx$$

[In] integrate((a+b*tan(c+d*x^(1/2)))/x^2,x, algorithm="maxima")

[Out] (2*b*x*integrate(sin(2*d*sqrt(x) + 2*c)/((cos(2*d*sqrt(x) + 2*c)^2 + sin(2*d*sqrt(x) + 2*c)^2 + 2*cos(2*d*sqrt(x) + 2*c) + 1)*x^2), x) - a)/x

Giac [N/A]

Not integrable

Time = 0.49 (sec) , antiderivative size = 18, normalized size of antiderivative = 1.00

$$\int \frac{a + b \tan(c + d\sqrt{x})}{x^2} dx = \int \frac{b \tan(d\sqrt{x} + c) + a}{x^2} dx$$

[In] integrate((a+b*tan(c+d*x^(1/2)))/x^2,x, algorithm="giac")

[Out] integrate((b*tan(d*sqrt(x) + c) + a)/x^2, x)

Mupad [N/A]

Not integrable

Time = 4.45 (sec) , antiderivative size = 18, normalized size of antiderivative = 1.00

$$\int \frac{a + b \tan(c + d\sqrt{x})}{x^2} dx = \int \frac{a + b \tan(c + d\sqrt{x})}{x^2} dx$$

[In] int((a + b*tan(c + d*x^(1/2)))/x^2,x)

[Out] int((a + b*tan(c + d*x^(1/2)))/x^2, x)

3.31 $\int x^2 (a + b \tan (c + d\sqrt{x}))^2 dx$

Optimal result	174
Rubi [A] (verified)	175
Mathematica [A] (verified)	181
Maple [F]	181
Fricas [F]	182
Sympy [F]	182
Maxima [B] (verification not implemented)	182
Giac [F]	184
Mupad [F(-1)]	184

Optimal result

Integrand size = 20, antiderivative size = 402

$$\begin{aligned}
 \int x^2 (a + b \tan(c + d\sqrt{x}))^2 dx = & -\frac{2ib^2x^{5/2}}{d} + \frac{a^2x^3}{3} + \frac{2}{3}iabx^3 - \frac{b^2x^3}{3} \\
 & + \frac{10b^2x^2 \log\left(1 + e^{2i(c+d\sqrt{x})}\right)}{d^2} \\
 & - \frac{4abx^{5/2} \log\left(1 + e^{2i(c+d\sqrt{x})}\right)}{d} \\
 & - \frac{20ib^2x^{3/2} \text{PolyLog}\left(2, -e^{2i(c+d\sqrt{x})}\right)}{d^3} \\
 & + \frac{10iabx^2 \text{PolyLog}\left(2, -e^{2i(c+d\sqrt{x})}\right)}{d^2} \\
 & + \frac{30b^2x \text{PolyLog}\left(3, -e^{2i(c+d\sqrt{x})}\right)}{d^4} \\
 & - \frac{20abx^{3/2} \text{PolyLog}\left(3, -e^{2i(c+d\sqrt{x})}\right)}{d^3} \\
 & + \frac{30ib^2\sqrt{x} \text{PolyLog}\left(4, -e^{2i(c+d\sqrt{x})}\right)}{d^5} \\
 & - \frac{30iabx \text{PolyLog}\left(4, -e^{2i(c+d\sqrt{x})}\right)}{d^4} \\
 & - \frac{15b^2 \text{PolyLog}\left(5, -e^{2i(c+d\sqrt{x})}\right)}{d^6} \\
 & + \frac{30ab\sqrt{x} \text{PolyLog}\left(5, -e^{2i(c+d\sqrt{x})}\right)}{d^5} \\
 & + \frac{15iab \text{PolyLog}\left(6, -e^{2i(c+d\sqrt{x})}\right)}{d^6} \\
 & + \frac{2b^2x^{5/2} \tan(c + d\sqrt{x})}{d}
 \end{aligned}$$

[Out] 10*I*a*b*x^2*polylog(2,-exp(2*I*(c+d*x^(1/2))))/d^2+1/3*a^2*x^3-2*I*b^2*x^(5/2)/d-1/3*b^2*x^3+10*b^2*x^2*ln(1+exp(2*I*(c+d*x^(1/2))))/d^2-4*a*b*x^(5/2)*ln(1+exp(2*I*(c+d*x^(1/2))))/d-30*I*a*b*x*polylog(4,-exp(2*I*(c+d*x^(1/2))))/d^4+2/3*I*a*b*x^3+30*b^2*x*polylog(3,-exp(2*I*(c+d*x^(1/2))))/d^4-20*a*b*x^(3/2)*polylog(3,-exp(2*I*(c+d*x^(1/2))))/d^3-20*I*b^2*x^(3/2)*polylog(2,-exp(2*I*(c+d*x^(1/2))))/d^3-15*b^2*polylog(5,-exp(2*I*(c+d*x^(1/2))))/d^6+15*I*a*b*polylog(6,-exp(2*I*(c+d*x^(1/2))))/d^6+30*I*b^2*polylog(4,-exp(2*

$I*(c+d*x^(1/2)))*x^(1/2)/d^5+30*a*b*polylog(5,-exp(2*I*(c+d*x^(1/2))))*x^(1/2)/d^5+2*b^2*x^(5/2)*tan(c+d*x^(1/2))/d$

Rubi [A] (verified)

Time = 0.70 (sec) , antiderivative size = 402, normalized size of antiderivative = 1.00, number of steps used = 20, number of rules used = 10, $\frac{\text{number of rules}}{\text{integrand size}} = 0.500$, Rules used = {3832, 3803, 3800, 2221, 2611, 6744, 2320, 6724, 3801, 30}

$$\int x^2(a + b \tan(c + d\sqrt{x}))^2 dx = \frac{a^2 x^3}{3} + \frac{15iab \operatorname{PolyLog}\left(6, -e^{2i(c+d\sqrt{x})}\right)}{d^6} + \frac{30ab\sqrt{x} \operatorname{PolyLog}\left(5, -e^{2i(c+d\sqrt{x})}\right)}{d^5} - \frac{30iabx \operatorname{PolyLog}\left(4, -e^{2i(c+d\sqrt{x})}\right)}{d^4} - \frac{20abx^{3/2} \operatorname{PolyLog}\left(3, -e^{2i(c+d\sqrt{x})}\right)}{d^3} + \frac{10iabx^2 \operatorname{PolyLog}\left(2, -e^{2i(c+d\sqrt{x})}\right)}{d^2} - \frac{4abx^{5/2} \log\left(1 + e^{2i(c+d\sqrt{x})}\right)}{d} + \frac{2}{3}iabx^3 - \frac{15b^2 \operatorname{PolyLog}\left(5, -e^{2i(c+d\sqrt{x})}\right)}{d^6} + \frac{30ib^2\sqrt{x} \operatorname{PolyLog}\left(4, -e^{2i(c+d\sqrt{x})}\right)}{d^5} + \frac{30b^2x \operatorname{PolyLog}\left(3, -e^{2i(c+d\sqrt{x})}\right)}{d^4} - \frac{20ib^2x^{3/2} \operatorname{PolyLog}\left(2, -e^{2i(c+d\sqrt{x})}\right)}{d^3} + \frac{10b^2x^2 \log\left(1 + e^{2i(c+d\sqrt{x})}\right)}{d^2} + \frac{2b^2x^{5/2} \tan(c + d\sqrt{x})}{d} - \frac{2ib^2x^{5/2}}{d} - \frac{b^2x^3}{3}$$

[In] Int[x^2*(a + b*Tan[c + d*Sqrt[x]])^2,x]

[Out] ((-2*I)*b^2*x^(5/2))/d + (a^2*x^3)/3 + ((2*I)/3)*a*b*x^3 - (b^2*x^3)/3 + (10*b^2*x^2*Log[1 + E^((2*I)*(c + d*Sqrt[x]))])/d^2 - (4*a*b*x^(5/2)*Log[1 +

$$\begin{aligned} & E^{\left((2I)(c + d\sqrt{x})\right)}/d - \left((20I)b^2x^{(3/2)}\text{PolyLog}[2, -E^{\left((2I)(c + d\sqrt{x})\right)}\right. \\ & \left. + d\sqrt{x}\right) \right)/d^3 + \left((10I)abx^2\text{PolyLog}[2, -E^{\left((2I)(c + d\sqrt{x})\right)}\right) \right)/d^2 + \left(30b^2x\text{PolyLog}[3, -E^{\left((2I)(c + d\sqrt{x})\right)}\right) \right)/d^4 - \left(20abx^{(3/2)}\text{PolyLog}[3, -E^{\left((2I)(c + d\sqrt{x})\right)}\right) \right)/d^3 + \left((30I)b^2\sqrt{x}\text{PolyLog}[4, -E^{\left((2I)(c + d\sqrt{x})\right)}\right) \right)/d^5 - \left((30I)abx\text{PolyLog}[4, -E^{\left((2I)(c + d\sqrt{x})\right)}\right) \right)/d^4 - \left(15b^2\text{PolyLog}[5, -E^{\left((2I)(c + d\sqrt{x})\right)}\right) \right)/d^6 + \left(30ab\sqrt{x}\text{PolyLog}[5, -E^{\left((2I)(c + d\sqrt{x})\right)}\right) \right)/d^5 + \left((15I)ab\text{PolyLog}[6, -E^{\left((2I)(c + d\sqrt{x})\right)}\right) \right)/d^6 + \left(2b^2x^{(5/2)}\text{Tan}[c + d\sqrt{x}]\right)/d \end{aligned}$$
Rule 30

```
Int[(x_)^(m_), x_Symbol] := Simp[x^(m + 1)/(m + 1), x] /; FreeQ[m, x] && NeQ[m, -1]
```

Rule 2221

```
Int[(((F_)^((g_)*(e_) + (f_)*(x_)))^(n_))*((c_) + (d_)*(x_)^(m_))/((a_) + (b_)*((F_)^((g_)*(e_) + (f_)*(x_)))^(n_)), x_Symbol] := Simp[((c + d*x)^m/(b*f*g*n*Log[F]))*Log[1 + b*((F^(g*(e + f*x)))^n/a)], x] - Dist[d*(m/(b*f*g*n*Log[F])), Int[(c + d*x)^(m - 1)*Log[1 + b*((F^(g*(e + f*x)))^n/a)], x], x] /; FreeQ[{F, a, b, c, d, e, f, g, n}, x] && IGtQ[m, 0]
```

Rule 2320

```
Int[u_, x_Symbol] := With[{v = FunctionOfExponential[u, x]}, Dist[v/D[v, x], Subst[Int[FunctionOfExponentialFunction[u, x]/x, x], x, v], x] /; FunctionOfExponentialQ[u, x] && !MatchQ[u, (w_)*((a_)*(v_)^(n_))^(m_)] /; FreeQ[{a, m, n}, x] && IntegerQ[m*n] && !MatchQ[u, E^((c_)*((a_) + (b_)*x))* (F_)[v_] /; FreeQ[{a, b, c}, x] && InverseFunctionQ[F[x]]]
```

Rule 2611

```
Int[Log[1 + (e_)*((F_)^((c_)*((a_) + (b_)*(x_)))^(n_))]*((f_) + (g_)*(x_))^(m_), x_Symbol] := Simp[(-f + g*x)^m*(PolyLog[2, (-e)*(F^(c*(a + b*x)))^n]/(b*c*n*Log[F])), x] + Dist[g*(m/(b*c*n*Log[F])), Int[(f + g*x)^(m - 1)*PolyLog[2, (-e)*(F^(c*(a + b*x)))^n], x], x] /; FreeQ[{F, a, b, c, e, f, g, n}, x] && GtQ[m, 0]
```

Rule 3800

```
Int[(((c_) + (d_)*(x_))^(m_))*tan[(e_) + (f_)*(x_)], x_Symbol] := Simp[I*((c + d*x)^(m + 1)/(d*(m + 1))), x] - Dist[2*I, Int[(c + d*x)^m*(E^(2*I*(e + f*x)))/(1 + E^(2*I*(e + f*x))), x], x] /; FreeQ[{c, d, e, f}, x] && IGtQ[m, 0]
```

Rule 3801


```
Int[((c_.) + (d_.)*(x_))^(m_.)*((b_.)*tan[(e_.) + (f_.)*(x_)])^(n_), x_Symbol]
:> Simp[b*(c + d*x)^m*((b*Tan[e + f*x])^(n - 1)/(f*(n - 1))), x] + (-Dist[
b*d*(m/(f*(n - 1))), Int[(c + d*x)^(m - 1)*(b*Tan[e + f*x])^(n - 1), x],
x] - Dist[b^2, Int[(c + d*x)^m*(b*Tan[e + f*x])^(n - 2), x], x]) /; FreeQ[
{b, c, d, e, f}, x] && GtQ[n, 1] && GtQ[m, 0]
```

Rule 3803

```
Int[((c_.) + (d_.)*(x_))^(m_.)*((a_.) + (b_.)*tan[(e_.) + (f_.)*(x_)])^(n_.)
, x_Symbol] :> Int[ExpandIntegrand[(c + d*x)^m, (a + b*Tan[e + f*x])^n, x],
x] /; FreeQ[{a, b, c, d, e, f, m}, x] && IGtQ[m, 0] && IGtQ[n, 0]
```

Rule 3832

```
Int[(x_)^(m_.)*((a_.) + (b_.)*Tan[(c_.) + (d_.)*(x_)^(n_)])^(p_.), x_Symbol]
:> Dist[1/n, Subst[Int[x^(Simplify[(m + 1)/n] - 1)*(a + b*Tan[c + d*x])^p
, x], x, x^n], x] /; FreeQ[{a, b, c, d, m, n, p}, x] && IGtQ[Simplify[(m +
1)/n], 0] && IntegerQ[p]
```

Rule 6724

```
Int[PolyLog[n_, (c_.)*((a_.) + (b_.)*(x_))^(p_.)]/((d_.) + (e_.)*(x_)), x_S
ymbol] :> Simp[PolyLog[n + 1, c*(a + b*x)^p]/(e*p), x] /; FreeQ[{a, b, c, d
, e, n, p}, x] && EqQ[b*d, a*e]
```

Rule 6744

```
Int[((e_.) + (f_.)*(x_))^(m_.)*PolyLog[n_, (d_.)*((F_)^((c_.)*((a_.) + (b_.
)*(x_)))^(p_.)], x_Symbol] :> Simp[(e + f*x)^m*(PolyLog[n + 1, d*(F^(c*(a
+ b*x)))^p]/(b*c*p*Log[F])), x] - Dist[f*(m/(b*c*p*Log[F])), Int[(e + f*x)^(
m - 1)*PolyLog[n + 1, d*(F^(c*(a + b*x)))^p], x], x] /; FreeQ[{F, a, b, c,
d, e, f, n, p}, x] && GtQ[m, 0]
```

Rubi steps

$$\begin{aligned}
\text{integral} &= 2\text{Subst}\left(\int x^5(a + b \tan(c + dx))^2 dx, x, \sqrt{x}\right) \\
&= 2\text{Subst}\left(\int (a^2x^5 + 2abx^5 \tan(c + dx) + b^2x^5 \tan^2(c + dx)) dx, x, \sqrt{x}\right) \\
&= \frac{a^2x^3}{3} + (4ab)\text{Subst}\left(\int x^5 \tan(c + dx) dx, x, \sqrt{x}\right) \\
&\quad + (2b^2)\text{Subst}\left(\int x^5 \tan^2(c + dx) dx, x, \sqrt{x}\right)
\end{aligned}$$

$$\begin{aligned}
&= \frac{a^2 x^3}{3} + \frac{2}{3} i a b x^3 + \frac{2b^2 x^{5/2} \tan(c + d\sqrt{x})}{d} - (8iab) \text{Subst} \left(\int \frac{e^{2i(c+dx)} x^5}{1 + e^{2i(c+dx)}} dx, x, \sqrt{x} \right) \\
&\quad - (2b^2) \text{Subst} \left(\int x^5 dx, x, \sqrt{x} \right) - \frac{(10b^2) \text{Subst} \left(\int x^4 \tan(c + dx) dx, x, \sqrt{x} \right)}{d} \\
&= -\frac{2ib^2 x^{5/2}}{d} + \frac{a^2 x^3}{3} + \frac{2}{3} i a b x^3 - \frac{b^2 x^3}{3} - \frac{4abx^{5/2} \log(1 + e^{2i(c+d\sqrt{x})})}{d} + \frac{2b^2 x^{5/2} \tan(c + d\sqrt{x})}{d} \\
&\quad + \frac{(20ab) \text{Subst} \left(\int x^4 \log(1 + e^{2i(c+dx)}) dx, x, \sqrt{x} \right)}{d} + \frac{(20ib^2) \text{Subst} \left(\int \frac{e^{2i(c+dx)} x^4}{1 + e^{2i(c+dx)}} dx, x, \sqrt{x} \right)}{d} \\
&= -\frac{2ib^2 x^{5/2}}{d} + \frac{a^2 x^3}{3} + \frac{2}{3} i a b x^3 - \frac{b^2 x^3}{3} + \frac{10b^2 x^2 \log(1 + e^{2i(c+d\sqrt{x})})}{d^2} \\
&\quad - \frac{4abx^{5/2} \log(1 + e^{2i(c+d\sqrt{x})})}{d} + \frac{10iabx^2 \text{PolyLog}(2, -e^{2i(c+d\sqrt{x})})}{d^2} \\
&\quad + \frac{2b^2 x^{5/2} \tan(c + d\sqrt{x})}{d} - \frac{(40iab) \text{Subst} \left(\int x^3 \text{PolyLog}(2, -e^{2i(c+dx)}) dx, x, \sqrt{x} \right)}{d^2} \\
&\quad - \frac{(40b^2) \text{Subst} \left(\int x^3 \log(1 + e^{2i(c+dx)}) dx, x, \sqrt{x} \right)}{d^2} \\
&= -\frac{2ib^2 x^{5/2}}{d} + \frac{a^2 x^3}{3} + \frac{2}{3} i a b x^3 - \frac{b^2 x^3}{3} + \frac{10b^2 x^2 \log(1 + e^{2i(c+d\sqrt{x})})}{d^2} \\
&\quad - \frac{4abx^{5/2} \log(1 + e^{2i(c+d\sqrt{x})})}{d} - \frac{20ib^2 x^{3/2} \text{PolyLog}(2, -e^{2i(c+d\sqrt{x})})}{d^3} \\
&\quad + \frac{10iabx^2 \text{PolyLog}(2, -e^{2i(c+d\sqrt{x})})}{d^2} - \frac{20abx^{3/2} \text{PolyLog}(3, -e^{2i(c+d\sqrt{x})})}{d^3} \\
&\quad + \frac{2b^2 x^{5/2} \tan(c + d\sqrt{x})}{d} + \frac{(60ab) \text{Subst} \left(\int x^2 \text{PolyLog}(3, -e^{2i(c+dx)}) dx, x, \sqrt{x} \right)}{d^3} \\
&\quad + \frac{(60ib^2) \text{Subst} \left(\int x^2 \text{PolyLog}(2, -e^{2i(c+dx)}) dx, x, \sqrt{x} \right)}{d^3}
\end{aligned}$$

$$\begin{aligned}
&= -\frac{2ib^2x^{5/2}}{d} + \frac{a^2x^3}{3} + \frac{2}{3}iabx^3 - \frac{b^2x^3}{3} + \frac{10b^2x^2 \log\left(1 + e^{2i(c+d\sqrt{x})}\right)}{d^2} \\
&\quad - \frac{4abx^{5/2} \log\left(1 + e^{2i(c+d\sqrt{x})}\right)}{d} - \frac{20ib^2x^{3/2} \text{PolyLog}\left(2, -e^{2i(c+d\sqrt{x})}\right)}{d^3} \\
&\quad + \frac{10iabx^2 \text{PolyLog}\left(2, -e^{2i(c+d\sqrt{x})}\right)}{d^2} + \frac{30b^2x \text{PolyLog}\left(3, -e^{2i(c+d\sqrt{x})}\right)}{d^4} \\
&\quad - \frac{20abx^{3/2} \text{PolyLog}\left(3, -e^{2i(c+d\sqrt{x})}\right)}{d^3} - \frac{30iabx \text{PolyLog}\left(4, -e^{2i(c+d\sqrt{x})}\right)}{d^4} \\
&\quad + \frac{2b^2x^{5/2} \tan(c + d\sqrt{x})}{d} + \frac{(60iab) \text{Subst}\left(\int x \text{PolyLog}\left(4, -e^{2i(c+dx)}\right) dx, x, \sqrt{x}\right)}{d^4} \\
&\quad - \frac{(60b^2) \text{Subst}\left(\int x \text{PolyLog}\left(3, -e^{2i(c+dx)}\right) dx, x, \sqrt{x}\right)}{d^4} \\
&= -\frac{2ib^2x^{5/2}}{d} + \frac{a^2x^3}{3} + \frac{2}{3}iabx^3 - \frac{b^2x^3}{3} + \frac{10b^2x^2 \log\left(1 + e^{2i(c+d\sqrt{x})}\right)}{d^2} \\
&\quad - \frac{4abx^{5/2} \log\left(1 + e^{2i(c+d\sqrt{x})}\right)}{d} - \frac{20ib^2x^{3/2} \text{PolyLog}\left(2, -e^{2i(c+d\sqrt{x})}\right)}{d^3} \\
&\quad + \frac{10iabx^2 \text{PolyLog}\left(2, -e^{2i(c+d\sqrt{x})}\right)}{d^2} + \frac{30b^2x \text{PolyLog}\left(3, -e^{2i(c+d\sqrt{x})}\right)}{d^4} \\
&\quad - \frac{20abx^{3/2} \text{PolyLog}\left(3, -e^{2i(c+d\sqrt{x})}\right)}{d^3} + \frac{30ib^2\sqrt{x} \text{PolyLog}\left(4, -e^{2i(c+d\sqrt{x})}\right)}{d^5} \\
&\quad - \frac{30iabx \text{PolyLog}\left(4, -e^{2i(c+d\sqrt{x})}\right)}{d^4} + \frac{30ab\sqrt{x} \text{PolyLog}\left(5, -e^{2i(c+d\sqrt{x})}\right)}{d^5} \\
&\quad + \frac{2b^2x^{5/2} \tan(c + d\sqrt{x})}{d} - \frac{(30ab) \text{Subst}\left(\int \text{PolyLog}\left(5, -e^{2i(c+dx)}\right) dx, x, \sqrt{x}\right)}{d^5} \\
&\quad - \frac{(30ib^2) \text{Subst}\left(\int \text{PolyLog}\left(4, -e^{2i(c+dx)}\right) dx, x, \sqrt{x}\right)}{d^5}
\end{aligned}$$

$$\begin{aligned}
&= -\frac{2ib^2x^{5/2}}{d} + \frac{a^2x^3}{3} + \frac{2}{3}iabx^3 - \frac{b^2x^3}{3} + \frac{10b^2x^2 \log(1 + e^{2i(c+d\sqrt{x})})}{d^2} \\
&\quad - \frac{4abx^{5/2} \log(1 + e^{2i(c+d\sqrt{x})})}{d} - \frac{20ib^2x^{3/2} \text{PolyLog}(2, -e^{2i(c+d\sqrt{x})})}{d^3} \\
&\quad + \frac{10iabx^2 \text{PolyLog}(2, -e^{2i(c+d\sqrt{x})})}{d^2} + \frac{30b^2x \text{PolyLog}(3, -e^{2i(c+d\sqrt{x})})}{d^4} \\
&\quad - \frac{20abx^{3/2} \text{PolyLog}(3, -e^{2i(c+d\sqrt{x})})}{d^3} + \frac{30ib^2\sqrt{x} \text{PolyLog}(4, -e^{2i(c+d\sqrt{x})})}{d^5} \\
&\quad - \frac{30iabx \text{PolyLog}(4, -e^{2i(c+d\sqrt{x})})}{d^4} + \frac{30ab\sqrt{x} \text{PolyLog}(5, -e^{2i(c+d\sqrt{x})})}{d^5} \\
&\quad + \frac{2b^2x^{5/2} \tan(c + d\sqrt{x})}{d} + \frac{(15iab) \text{Subst}\left(\int \frac{\text{PolyLog}(5, -x)}{x} dx, x, e^{2i(c+d\sqrt{x})}\right)}{d^6} \\
&\quad - \frac{(15b^2) \text{Subst}\left(\int \frac{\text{PolyLog}(4, -x)}{x} dx, x, e^{2i(c+d\sqrt{x})}\right)}{d^6} \\
&= -\frac{2ib^2x^{5/2}}{d} + \frac{a^2x^3}{3} + \frac{2}{3}iabx^3 - \frac{b^2x^3}{3} + \frac{10b^2x^2 \log(1 + e^{2i(c+d\sqrt{x})})}{d^2} \\
&\quad - \frac{4abx^{5/2} \log(1 + e^{2i(c+d\sqrt{x})})}{d} - \frac{20ib^2x^{3/2} \text{PolyLog}(2, -e^{2i(c+d\sqrt{x})})}{d^3} \\
&\quad + \frac{10iabx^2 \text{PolyLog}(2, -e^{2i(c+d\sqrt{x})})}{d^2} + \frac{30b^2x \text{PolyLog}(3, -e^{2i(c+d\sqrt{x})})}{d^4} \\
&\quad - \frac{20abx^{3/2} \text{PolyLog}(3, -e^{2i(c+d\sqrt{x})})}{d^3} \\
&\quad + \frac{30ib^2\sqrt{x} \text{PolyLog}(4, -e^{2i(c+d\sqrt{x})})}{d^5} - \frac{30iabx \text{PolyLog}(4, -e^{2i(c+d\sqrt{x})})}{d^4} \\
&\quad - \frac{15b^2 \text{PolyLog}(5, -e^{2i(c+d\sqrt{x})})}{d^6} + \frac{30ab\sqrt{x} \text{PolyLog}(5, -e^{2i(c+d\sqrt{x})})}{d^5} \\
&\quad + \frac{15iab \text{PolyLog}(6, -e^{2i(c+d\sqrt{x})})}{d^6} + \frac{2b^2x^{5/2} \tan(c + d\sqrt{x})}{d}
\end{aligned}$$

Mathematica [A] (verified)

Time = 3.81 (sec) , antiderivative size = 567, normalized size of antiderivative = 1.41

$$\int x^2 (a + b \tan(c + d\sqrt{x}))^2 dx$$

$$= \frac{1}{3} \left(-\frac{i b e^{2ic} \left(-12 b d^5 e^{-2ic} x^{5/2} + 4 a d^6 e^{-2ic} x^3 + 30 i b d^4 e^{-2ic} (1 + e^{2ic}) x^2 \log \left(1 + e^{-2i(c+d\sqrt{x})} \right) - 12 i a d^5 e^{-2ic} \right)}{d} + \frac{6 b^2 x^{5/2} \sec(c) \sec(c + d\sqrt{x}) \sin(d\sqrt{x})}{d} + x^3 (a^2 - b^2 + 2 a b \tan(c)) \right)$$

[In] Integrate[x^2*(a + b*Tan[c + d*Sqrt[x]])^2,x]

```
[Out] (((-I)*b*E^((2*I)*c))*((-12*b*d^5*x^(5/2))/E^((2*I)*c) + (4*a*d^6*x^3)/E^((2*I)*c) + ((30*I)*b*d^4*(1 + E^((2*I)*c))*x^2*Log[1 + E^((-2*I)*(c + d*Sqrt[x]))])/E^((2*I)*c) - ((12*I)*a*d^5*(1 + E^((2*I)*c))*x^(5/2)*Log[1 + E^((-2*I)*(c + d*Sqrt[x]))])/E^((2*I)*c) - 60*b*d^3*(1 + E^((-2*I)*c))*x^(3/2)*PolyLog[2, -E^((-2*I)*(c + d*Sqrt[x]))] + 30*a*d^4*(1 + E^((-2*I)*c))*x^2*PolyLog[2, -E^((-2*I)*(c + d*Sqrt[x]))] + ((90*I)*b*d^2*(1 + E^((2*I)*c))*x*PolyLog[3, -E^((-2*I)*(c + d*Sqrt[x]))])/E^((2*I)*c) - ((60*I)*a*d^3*(1 + E^((2*I)*c))*x^(3/2)*PolyLog[3, -E^((-2*I)*(c + d*Sqrt[x]))])/E^((2*I)*c) + 90*b*d*(1 + E^((-2*I)*c))*Sqrt[x]*PolyLog[4, -E^((-2*I)*(c + d*Sqrt[x]))] - 90*a*d^2*(1 + E^((-2*I)*c))*x*PolyLog[4, -E^((-2*I)*(c + d*Sqrt[x]))] - ((45*I)*b*(1 + E^((2*I)*c))*PolyLog[5, -E^((-2*I)*(c + d*Sqrt[x]))])/E^((2*I)*c) + ((90*I)*a*d*(1 + E^((2*I)*c))*Sqrt[x]*PolyLog[5, -E^((-2*I)*(c + d*Sqrt[x]))])/E^((2*I)*c) + 45*a*(1 + E^((-2*I)*c))*PolyLog[6, -E^((-2*I)*(c + d*Sqrt[x]))])/E^((2*I)*c) + (6*b^2*x^(5/2)*Sec[c]*Sec[c + d*Sqrt[x]]*Sin[d*Sqrt[x]])/d + x^3*(a^2 - b^2 + 2*a*b*Tan[c])/3
```

Maple [F]

$$\int x^2 (a + b \tan(c + d\sqrt{x}))^2 dx$$

[In] int(x^2*(a+b*tan(c+d*x^(1/2)))^2,x)

[Out] int(x^2*(a+b*tan(c+d*x^(1/2)))^2,x)

Fricas [F]

$$\int x^2(a + b \tan(c + d\sqrt{x}))^2 dx = \int (b \tan(d\sqrt{x} + c) + a)^2 x^2 dx$$

[In] integrate(x^2*(a+b*tan(c+d*x^(1/2)))^2,x, algorithm="fricas")

[Out] integral(b^2*x^2*tan(d*sqrt(x) + c)^2 + 2*a*b*x^2*tan(d*sqrt(x) + c) + a^2*x^2, x)

Sympy [F]

$$\int x^2(a + b \tan(c + d\sqrt{x}))^2 dx = \int x^2(a + b \tan(c + d\sqrt{x}))^2 dx$$

[In] integrate(x**2*(a+b*tan(c+d*x**(1/2)))**2,x)

[Out] Integral(x**2*(a + b*tan(c + d*sqrt(x)))**2, x)

Maxima [B] (verification not implemented)

Both result and optimal contain complex but leaf count of result is larger than twice the leaf count of optimal. 2421 vs. $2(320) = 640$.

Time = 0.60 (sec) , antiderivative size = 2421, normalized size of antiderivative = 6.02

$$\int x^2(a + b \tan(c + d\sqrt{x}))^2 dx = \text{Too large to display}$$

[In] integrate(x^2*(a+b*tan(c+d*x^(1/2)))^2,x, algorithm="maxima")

[Out] $\frac{1}{3}((d\sqrt{x} + c)^6 a^2 - 6(d\sqrt{x} + c)^5 a^2 c + 15(d\sqrt{x} + c)^4 a^2 c^2 - 20(d\sqrt{x} + c)^3 a^2 c^3 + 15(d\sqrt{x} + c)^2 a^2 c^4 - 6(d\sqrt{x} + c) a^2 c^5 - 12 a b c^5 \log(\sec(d\sqrt{x} + c)) - 6(30 I (d\sqrt{x} + c) b^2 c^5 - 5(2 a b + I b^2)(d\sqrt{x} + c)^6 + 30(2 a b + I b^2)(d\sqrt{x} + c)^5 c - 75(2 a b + I b^2)(d\sqrt{x} + c)^4 c^2 + 100(2 a b + I b^2)(d\sqrt{x} + c)^3 c^3 - 75(2 a b + I b^2)(d\sqrt{x} + c)^2 c^4 + 60 b^2 c^5 + 2(96(d\sqrt{x} + c)^5 a b - 75 b^2 c^4 - 150(2 a b c + b^2)(d\sqrt{x} + c)^4 + 400(a b c^2 + b^2 c)(d\sqrt{x} + c)^3 - 150(2 a b c^3 + 3 b^2 c^2)(d\sqrt{x} + c)^2 + 150(a b c^4 + 2 b^2 c^3)(d\sqrt{x} + c) + (96(d\sqrt{x} + c)^5 a b - 75 b^2 c^4 - 150(2 a b c + b^2)(d\sqrt{x} + c)^4 + 400(a b c^2 + b^2 c)(d\sqrt{x} + c)^3 - 150(2 a b c^3 + 3 b^2 c^2)(d\sqrt{x} + c)^2 + 150(a b c^4 + 2 b^2 c^3)(d\sqrt{x} + c)) \cos(2 d\sqrt{x} + 2 c) - (-96 I (d\sqrt{x} + c)^5 a b + 75 I b^2 c^4 + 15$

$$\begin{aligned}
& 0*(2*I*a*b*c + I*b^2)*(d*\sqrt{x} + c)^4 + 400*(-I*a*b*c^2 - I*b^2*c)*(d*\sqrt{x} + c)^3 + 150*(2*I*a*b*c^3 + 3*I*b^2*c^2)*(d*\sqrt{x} + c)^2 + 150*(-I*a*b*c^4 - 2*I*b^2*c^3)*(d*\sqrt{x} + c)*\sin(2*d*\sqrt{x} + 2*c)*\arctan2(\sin(2*d*\sqrt{x} + 2*c), \cos(2*d*\sqrt{x} + 2*c) + 1) - 5*((2*a*b + I*b^2)*(d*\sqrt{x} + c)^6 - 6*(2*b^2 + (2*a*b + I*b^2)*c)*(d*\sqrt{x} + c)^5 + 15*(4*b^2*c + (2*a*b + I*b^2)*c^2)*(d*\sqrt{x} + c)^4 - 20*(6*b^2*c^2 + (2*a*b + I*b^2)*c^3)*(d*\sqrt{x} + c)^3 + 15*(8*b^2*c^3 + (2*a*b + I*b^2)*c^4)*(d*\sqrt{x} + c)^2 + 6*(-I*b^2*c^5 - 10*b^2*c^4)*(d*\sqrt{x} + c))*\cos(2*d*\sqrt{x} + 2*c) - 30*(16*(d*\sqrt{x} + c)^4*a*b + 5*a*b*c^4 + 10*b^2*c^3 - 20*(2*a*b*c + b^2)*(d*\sqrt{x} + c)^3 + 40*(a*b*c^2 + b^2*c)*(d*\sqrt{x} + c)^2 - 10*(2*a*b*c^3 + 3*b^2*c^2)*(d*\sqrt{x} + c) + (16*(d*\sqrt{x} + c)^4*a*b + 5*a*b*c^4 + 10*b^2*c^3 - 20*(2*a*b*c + b^2)*(d*\sqrt{x} + c)^3 + 40*(a*b*c^2 + b^2*c)*(d*\sqrt{x} + c)^2 - 10*(2*a*b*c^3 + 3*b^2*c^2)*(d*\sqrt{x} + c))*\cos(2*d*\sqrt{x} + 2*c) + (16*I*(d*\sqrt{x} + c)^4*a*b + 5*I*a*b*c^4 + 10*I*b^2*c^3 + 20*(-2*I*a*b*c - I*b^2)*(d*\sqrt{x} + c)^3 + 40*(I*a*b*c^2 + I*b^2*c)*(d*\sqrt{x} + c)^2 + 10*(-2*I*a*b*c^3 - 3*I*b^2*c^2)*(d*\sqrt{x} + c))*\sin(2*d*\sqrt{x} + 2*c))*\operatorname{dilog}(-e^(2*I*d*\sqrt{x} + 2*I*c)) + (-96*I*(d*\sqrt{x} + c)^5*a*b + 75*I*b^2*c^4 - 150*(-2*I*a*b*c - I*b^2)*(d*\sqrt{x} + c)^4 - 400*(I*a*b*c^2 + I*b^2*c)*(d*\sqrt{x} + c)^3 - 150*(-2*I*a*b*c^3 - 3*I*b^2*c^2)*(d*\sqrt{x} + c)^2 - 150*(I*a*b*c^4 + 2*I*b^2*c^3)*(d*\sqrt{x} + c) + (-96*I*(d*\sqrt{x} + c)^5*a*b + 75*I*b^2*c^4 - 150*(-2*I*a*b*c - I*b^2)*(d*\sqrt{x} + c)^4 - 400*(I*a*b*c^2 + I*b^2*c)*(d*\sqrt{x} + c)^3 - 150*(-2*I*a*b*c^3 - 3*I*b^2*c^2)*(d*\sqrt{x} + c)^2 - 150*(I*a*b*c^4 + 2*I*b^2*c^3)*(d*\sqrt{x} + c))*\cos(2*d*\sqrt{x} + 2*c) + (96*(d*\sqrt{x} + c)^5*a*b - 75*b^2*c^4 - 150*(2*a*b*c + b^2)*(d*\sqrt{x} + c)^4 + 400*(a*b*c^2 + b^2*c)*(d*\sqrt{x} + c)^3 - 150*(2*a*b*c^3 + 3*b^2*c^2)*(d*\sqrt{x} + c)^2 + 150*(a*b*c^4 + 2*b^2*c^3)*(d*\sqrt{x} + c))*\sin(2*d*\sqrt{x} + 2*c))*\log(\cos(2*d*\sqrt{x} + 2*c)^2 + \sin(2*d*\sqrt{x} + 2*c)^2 + 2*\cos(2*d*\sqrt{x} + 2*c) + 1) - 720*(a*b*\cos(2*d*\sqrt{x} + 2*c) + I*a*b*\sin(2*d*\sqrt{x} + 2*c) + a*b)*\operatorname{polylog}(6, -e^(2*I*d*\sqrt{x} + 2*I*c)) - 90*(-16*I*(d*\sqrt{x} + c)*a*b + 10*I*a*b*c + 5*I*b^2 + (-16*I*(d*\sqrt{x} + c)*a*b + 10*I*a*b*c + 5*I*b^2)*\cos(2*d*\sqrt{x} + 2*c) + (16*(d*\sqrt{x} + c)*a*b - 10*a*b*c - 5*b^2)*\sin(2*d*\sqrt{x} + 2*c))*\operatorname{polylog}(5, -e^(2*I*d*\sqrt{x} + 2*I*c)) + 60*(24*(d*\sqrt{x} + c)^2*a*b + 10*a*b*c^2 + 10*b^2*c - 15*(2*a*b*c + b^2)*(d*\sqrt{x} + c) + (24*(d*\sqrt{x} + c)^2*a*b + 10*a*b*c^2 + 10*b^2*c - 15*(2*a*b*c + b^2)*(d*\sqrt{x} + c))*\cos(2*d*\sqrt{x} + 2*c) - (-24*I*(d*\sqrt{x} + c)^2*a*b - 10*I*a*b*c^2 - 10*I*b^2*c + 15*(2*I*a*b*c + I*b^2)*(d*\sqrt{x} + c))*\sin(2*d*\sqrt{x} + 2*c))*\operatorname{polylog}(4, -e^(2*I*d*\sqrt{x} + 2*I*c)) - 30*(32*I*(d*\sqrt{x} + c)^3*a*b - 10*I*a*b*c^3 - 15*I*b^2*c^2 + 30*(-2*I*a*b*c - I*b^2)*(d*\sqrt{x} + c)^2 + 40*(I*a*b*c^2 + I*b^2*c)*(d*\sqrt{x} + c) + (32*I*(d*\sqrt{x} + c)^3*a*b - 10*I*a*b*c^3 - 15*I*b^2*c^2 + 30*(-2*I*a*b*c - I*b^2)*(d*\sqrt{x} + c)^2 + 40*(I*a*b*c^2 + I*b^2*c)*(d*\sqrt{x} + c))*\cos(2*d*\sqrt{x} + 2*c) - (32*(d*\sqrt{x} + c)^3*a*b - 10*a*b*c^3 - 15*b^2*c^2 - 30*(2*a*b*c + b^2)*(d*\sqrt{x} + c)^2 + 40*(a*b*c^2 + b^2*c)*(d*\sqrt{x} + c))*\sin(2*d*\sqrt{x} + 2*c))*\operatorname{polylog}(3, -e^(2*I*d*\sqrt{x} + 2*I*c)) - 5*((2*I*a*b - b^2)*(d*\sqrt{x} + c)^6 + 6*(-2*I*b^2 + (-2*I*a*b + b^2)
\end{aligned}$$

$$2)c)(d\sqrt{x} + c)^5 + 15(4Ib^2c + (2Iab - b^2)c^2)(d\sqrt{x} + c)^4 + 20(-6Ib^2c^2 + (-2Iab + b^2)c^3)(d\sqrt{x} + c)^3 + 15(8Ib^2c^3 + (2Iab - b^2)c^4)(d\sqrt{x} + c)^2 + 6(b^2c^5 - 10Ib^2c^4)(d\sqrt{x} + c)\sin(2d\sqrt{x} + 2c))/(-30I\cos(2d\sqrt{x} + 2c) + 30\sin(2d\sqrt{x} + 2c) - 30I)/d^6$$

Giac [F]

$$\int x^2(a + b \tan(c + d\sqrt{x}))^2 dx = \int (b \tan(d\sqrt{x} + c) + a)^2 x^2 dx$$

[In] integrate(x^2*(a+b*tan(c+d*x^(1/2)))^2,x, algorithm="giac")

[Out] integrate((b*tan(d*sqrt(x) + c) + a)^2*x^2, x)

Mupad [F(-1)]

Timed out.

$$\int x^2(a + b \tan(c + d\sqrt{x}))^2 dx = \int x^2(a + b \tan(c + d\sqrt{x}))^2 dx$$

[In] int(x^2*(a + b*tan(c + d*x^(1/2)))^2,x)

[Out] int(x^2*(a + b*tan(c + d*x^(1/2)))^2, x)

3.32 $\int x(a + b \tan(c + d\sqrt{x}))^2 dx$

Optimal result	185
Rubi [A] (verified)	186
Mathematica [A] (verified)	190
Maple [F]	191
Fricas [F]	191
Sympy [F]	191
Maxima [B] (verification not implemented)	191
Giac [F]	192
Mupad [F(-1)]	193

Optimal result

Integrand size = 18, antiderivative size = 274

$$\int x(a + b \tan(c + d\sqrt{x}))^2 dx = -\frac{2ib^2x^{3/2}}{d} + \frac{a^2x^2}{2} + iabx^2 - \frac{b^2x^2}{2}$$

$$+ \frac{6b^2x \log(1 + e^{2i(c+d\sqrt{x})})}{d^2} - \frac{4abx^{3/2} \log(1 + e^{2i(c+d\sqrt{x})})}{d}$$

$$- \frac{6ib^2\sqrt{x} \operatorname{PolyLog}(2, -e^{2i(c+d\sqrt{x})})}{d^3}$$

$$+ \frac{6iabx \operatorname{PolyLog}(2, -e^{2i(c+d\sqrt{x})})}{d^2}$$

$$+ \frac{3b^2 \operatorname{PolyLog}(3, -e^{2i(c+d\sqrt{x})})}{d^4}$$

$$- \frac{6ab\sqrt{x} \operatorname{PolyLog}(3, -e^{2i(c+d\sqrt{x})})}{d^3}$$

$$- \frac{3iab \operatorname{PolyLog}(4, -e^{2i(c+d\sqrt{x})})}{d^4} + \frac{2b^2x^{3/2} \tan(c + d\sqrt{x})}{d}$$

```
[Out] -2*I*b^2*x^(3/2)/d+1/2*a^2*x^2+I*a*b*x^2-1/2*b^2*x^2+6*b^2*x*ln(1+exp(2*I*(c+d*x^(1/2))))/d^2-4*a*b*x^(3/2)*ln(1+exp(2*I*(c+d*x^(1/2))))/d+6*I*a*b*x*polylog(2,-exp(2*I*(c+d*x^(1/2))))/d^2+3*b^2*polylog(3,-exp(2*I*(c+d*x^(1/2))))/d^4-3*I*a*b*polylog(4,-exp(2*I*(c+d*x^(1/2))))/d^4-6*I*b^2*polylog(2,-exp(2*I*(c+d*x^(1/2))))*x^(1/2)/d^3-6*a*b*polylog(3,-exp(2*I*(c+d*x^(1/2))))*x^(1/2)/d^3+2*b^2*x^(3/2)*tan(c+d*x^(1/2))/d
```

Rubi [A] (verified)

Time = 0.54 (sec) , antiderivative size = 274, normalized size of antiderivative = 1.00, number of steps used = 16, number of rules used = 10, $\frac{\text{number of rules}}{\text{integrand size}} = 0.556$, Rules used = {3832, 3803, 3800, 2221, 2611, 6744, 2320, 6724, 3801, 30}

$$\int x(a + b \tan(c + d\sqrt{x}))^2 dx = \frac{a^2 x^2}{2} - \frac{3iab \operatorname{PolyLog}\left(4, -e^{2i(c+d\sqrt{x})}\right)}{d^4} - \frac{6ab\sqrt{x} \operatorname{PolyLog}\left(3, -e^{2i(c+d\sqrt{x})}\right)}{d^3} + \frac{6iabx \operatorname{PolyLog}\left(2, -e^{2i(c+d\sqrt{x})}\right)}{d^2} - \frac{4abx^{3/2} \log\left(1 + e^{2i(c+d\sqrt{x})}\right)}{d} + iabx^2 + \frac{3b^2 \operatorname{PolyLog}\left(3, -e^{2i(c+d\sqrt{x})}\right)}{d^4} - \frac{6ib^2\sqrt{x} \operatorname{PolyLog}\left(2, -e^{2i(c+d\sqrt{x})}\right)}{d^3} + \frac{6b^2x \log\left(1 + e^{2i(c+d\sqrt{x})}\right)}{d^2} + \frac{2b^2x^{3/2} \tan(c + d\sqrt{x})}{d} - \frac{2ib^2x^{3/2}}{d} - \frac{1}{2}b^2x^2$$

[In] Int[x*(a + b*Tan[c + d*Sqrt[x]])^2,x]

[Out] ((-2*I)*b^2*x^(3/2))/d + (a^2*x^2)/2 + I*a*b*x^2 - (b^2*x^2)/2 + (6*b^2*x*Log[1 + E^((2*I)*(c + d*Sqrt[x]))])/d^2 - (4*a*b*x^(3/2)*Log[1 + E^((2*I)*(c + d*Sqrt[x]))])/d - ((6*I)*b^2*Sqrt[x]*PolyLog[2, -E^((2*I)*(c + d*Sqrt[x]))])/d^3 + ((6*I)*a*b*x*PolyLog[2, -E^((2*I)*(c + d*Sqrt[x]))])/d^2 + (3*b^2*PolyLog[3, -E^((2*I)*(c + d*Sqrt[x]))])/d^4 - (6*a*b*Sqrt[x]*PolyLog[3, -E^((2*I)*(c + d*Sqrt[x]))])/d^3 - ((3*I)*a*b*PolyLog[4, -E^((2*I)*(c + d*Sqrt[x]))])/d^4 + (2*b^2*x^(3/2)*Tan[c + d*Sqrt[x]])/d

Rule 30

Int[(x_)^(m_.), x_Symbol] := Simp[x^(m + 1)/(m + 1), x] /; FreeQ[m, x] && NeQ[m, -1]

Rule 2221

Int[(((F_)^(g_.)*((e_.) + (f_.)*(x_)))^(n_.)*((c_.) + (d_.)*(x_))^(m_.))/((a_.) + (b_.)*((F_)^(g_.)*((e_.) + (f_.)*(x_)))^(n_.)), x_Symbol] := Simp

```

[((c + d*x)^m/(b*f*g*n*Log[F]))*Log[1 + b*((F^(g*(e + f*x)))^n/a)], x] - Dist[d*(m/(b*f*g*n*Log[F])), Int[(c + d*x)^(m - 1)*Log[1 + b*((F^(g*(e + f*x)))^n/a)], x], x] /; FreeQ[{F, a, b, c, d, e, f, g, n}, x] && IGtQ[m, 0]

```

Rule 2320

```

Int[u_, x_Symbol] := With[{v = FunctionOfExponential[u, x]}, Dist[v/D[v, x], Subst[Int[FunctionOfExponentialFunction[u, x]/x, x], x, v], x] /; FunctionOfExponentialQ[u, x] && !MatchQ[u, (w_)*((a_)*(v_)^(n_))^(m_)] /; FreeQ[{a, m, n}, x] && IntegerQ[m*n] && !MatchQ[u, E^((c_)*((a_) + (b_)*x))*(F_)[v_] /; FreeQ[{a, b, c}, x] && InverseFunctionQ[F[x]]]

```

Rule 2611

```

Int[Log[1 + (e_)*((F_)^((c_)*((a_) + (b_)*(x_))))^(n_)]*(f_) + (g_)*(x_)^(m_), x_Symbol] := Simp[(-f + g*x)^m*(PolyLog[2, (-e)*(F^(c*(a + b*x)))^n]/(b*c*n*Log[F])), x] + Dist[g*(m/(b*c*n*Log[F])), Int[(f + g*x)^(m - 1)*PolyLog[2, (-e)*(F^(c*(a + b*x)))^n], x], x] /; FreeQ[{F, a, b, c, e, f, g, n}, x] && GtQ[m, 0]

```

Rule 3800

```

Int[((c_) + (d_)*(x_))^(m_)*tan[(e_) + (f_)*(x_)], x_Symbol] := Simp[I*((c + d*x)^(m + 1)/(d*(m + 1))), x] - Dist[2*I, Int[(c + d*x)^m*(E^(2*I*(e + f*x)))/(1 + E^(2*I*(e + f*x))), x], x] /; FreeQ[{c, d, e, f}, x] && IGtQ[m, 0]

```

Rule 3801

```

Int[((c_) + (d_)*(x_))^(m_)*((b_)*tan[(e_) + (f_)*(x_)])^(n_), x_Symbol] := Simp[b*(c + d*x)^m*((b*Tan[e + f*x])^(n - 1)/(f*(n - 1))), x] + (-Dist[b*d*(m/(f*(n - 1))), Int[(c + d*x)^(m - 1)*(b*Tan[e + f*x])^(n - 1), x], x] - Dist[b^2, Int[(c + d*x)^m*(b*Tan[e + f*x])^(n - 2), x], x]) /; FreeQ[{b, c, d, e, f}, x] && GtQ[n, 1] && GtQ[m, 0]

```

Rule 3803

```

Int[((c_) + (d_)*(x_))^(m_)*((a_) + (b_)*tan[(e_) + (f_)*(x_)])^(n_), x_Symbol] := Int[ExpandIntegrand[(c + d*x)^m, (a + b*Tan[e + f*x])^n, x], x] /; FreeQ[{a, b, c, d, e, f, m}, x] && IGtQ[m, 0] && IGtQ[n, 0]

```

Rule 3832

```

Int[(x_)^(m_)*((a_) + (b_)*Tan[(c_) + (d_)*(x_)^(n_)])^(p_), x_Symbol] := Dist[1/n, Subst[Int[x^(Simplify[(m + 1)/n] - 1)*(a + b*Tan[c + d*x])^p, x], x, x^n], x] /; FreeQ[{a, b, c, d, m, n, p}, x] && IGtQ[Simplify[(m +

```

1)/n], 0] && IntegerQ[p]

Rule 6724

Int[PolyLog[n_, (c_.)*((a_.) + (b_.)*(x_))^(p_.)]/((d_.) + (e_.)*(x_)), x_Symbol] :> Simp[PolyLog[n + 1, c*(a + b*x)^p]/(e*p), x] /; FreeQ[{a, b, c, d, e, n, p}, x] && EqQ[b*d, a*e]

Rule 6744

Int[((e_.) + (f_.)*(x_))^(m_.)*PolyLog[n_, (d_.)*((F_)^((c_.)*((a_.) + (b_.)*(x_))))^(p_.)], x_Symbol] :> Simp[(e + f*x)^m*(PolyLog[n + 1, d*(F^(c*(a + b*x)))^p]/(b*c*p*Log[F])), x] - Dist[f*(m/(b*c*p*Log[F])), Int[(e + f*x)^(m - 1)*PolyLog[n + 1, d*(F^(c*(a + b*x)))^p], x], x] /; FreeQ[{F, a, b, c, d, e, f, n, p}, x] && GtQ[m, 0]

Rubi steps

$$\begin{aligned}
 \text{integral} &= 2\text{Subst}\left(\int x^3(a + b \tan(c + dx))^2 dx, x, \sqrt{x}\right) \\
 &= 2\text{Subst}\left(\int (a^2x^3 + 2abx^3 \tan(c + dx) + b^2x^3 \tan^2(c + dx)) dx, x, \sqrt{x}\right) \\
 &= \frac{a^2x^2}{2} + (4ab)\text{Subst}\left(\int x^3 \tan(c + dx) dx, x, \sqrt{x}\right) \\
 &\quad + (2b^2)\text{Subst}\left(\int x^3 \tan^2(c + dx) dx, x, \sqrt{x}\right) \\
 &= \frac{a^2x^2}{2} + iabx^2 + \frac{2b^2x^{3/2} \tan(c + d\sqrt{x})}{d} - (8iab)\text{Subst}\left(\int \frac{e^{2i(c+dx)}x^3}{1 + e^{2i(c+dx)}} dx, x, \sqrt{x}\right) \\
 &\quad - (2b^2)\text{Subst}\left(\int x^3 dx, x, \sqrt{x}\right) - \frac{(6b^2)\text{Subst}\left(\int x^2 \tan(c + dx) dx, x, \sqrt{x}\right)}{d} \\
 &= -\frac{2ib^2x^{3/2}}{d} + \frac{a^2x^2}{2} + iabx^2 - \frac{b^2x^2}{2} - \frac{4abx^{3/2} \log(1 + e^{2i(c+d\sqrt{x})})}{d} + \frac{2b^2x^{3/2} \tan(c + d\sqrt{x})}{d} \\
 &\quad + \frac{(12ab)\text{Subst}\left(\int x^2 \log(1 + e^{2i(c+dx)}) dx, x, \sqrt{x}\right)}{d} + \frac{(12ib^2)\text{Subst}\left(\int \frac{e^{2i(c+dx)}x^2}{1 + e^{2i(c+dx)}} dx, x, \sqrt{x}\right)}{d}
 \end{aligned}$$

$$\begin{aligned}
&= -\frac{2ib^2x^{3/2}}{d} + \frac{a^2x^2}{2} + iabx^2 - \frac{b^2x^2}{2} + \frac{6b^2x \log\left(1 + e^{2i(c+d\sqrt{x})}\right)}{d^2} \\
&\quad - \frac{4abx^{3/2} \log\left(1 + e^{2i(c+d\sqrt{x})}\right)}{d} + \frac{6iabx \operatorname{PolyLog}\left(2, -e^{2i(c+d\sqrt{x})}\right)}{d^2} \\
&\quad + \frac{2b^2x^{3/2} \tan(c + d\sqrt{x})}{d} - \frac{(12iab) \operatorname{Subst}\left(\int x \operatorname{PolyLog}\left(2, -e^{2i(c+dx)}\right) dx, x, \sqrt{x}\right)}{d^2} \\
&\quad - \frac{(12b^2) \operatorname{Subst}\left(\int x \log\left(1 + e^{2i(c+dx)}\right) dx, x, \sqrt{x}\right)}{d^2} \\
&= -\frac{2ib^2x^{3/2}}{d} + \frac{a^2x^2}{2} + iabx^2 - \frac{b^2x^2}{2} + \frac{6b^2x \log\left(1 + e^{2i(c+d\sqrt{x})}\right)}{d^2} \\
&\quad - \frac{4abx^{3/2} \log\left(1 + e^{2i(c+d\sqrt{x})}\right)}{d} - \frac{6ib^2\sqrt{x} \operatorname{PolyLog}\left(2, -e^{2i(c+d\sqrt{x})}\right)}{d^3} \\
&\quad + \frac{6iabx \operatorname{PolyLog}\left(2, -e^{2i(c+d\sqrt{x})}\right)}{d^2} - \frac{6ab\sqrt{x} \operatorname{PolyLog}\left(3, -e^{2i(c+d\sqrt{x})}\right)}{d^3} \\
&\quad + \frac{2b^2x^{3/2} \tan(c + d\sqrt{x})}{d} + \frac{(6ab) \operatorname{Subst}\left(\int \operatorname{PolyLog}\left(3, -e^{2i(c+dx)}\right) dx, x, \sqrt{x}\right)}{d^3} \\
&\quad + \frac{(6ib^2) \operatorname{Subst}\left(\int \operatorname{PolyLog}\left(2, -e^{2i(c+dx)}\right) dx, x, \sqrt{x}\right)}{d^3} \\
&= -\frac{2ib^2x^{3/2}}{d} + \frac{a^2x^2}{2} + iabx^2 - \frac{b^2x^2}{2} + \frac{6b^2x \log\left(1 + e^{2i(c+d\sqrt{x})}\right)}{d^2} \\
&\quad - \frac{4abx^{3/2} \log\left(1 + e^{2i(c+d\sqrt{x})}\right)}{d} - \frac{6ib^2\sqrt{x} \operatorname{PolyLog}\left(2, -e^{2i(c+d\sqrt{x})}\right)}{d^3} \\
&\quad + \frac{6iabx \operatorname{PolyLog}\left(2, -e^{2i(c+d\sqrt{x})}\right)}{d^2} - \frac{6ab\sqrt{x} \operatorname{PolyLog}\left(3, -e^{2i(c+d\sqrt{x})}\right)}{d^3} \\
&\quad + \frac{2b^2x^{3/2} \tan(c + d\sqrt{x})}{d} - \frac{(3iab) \operatorname{Subst}\left(\int \frac{\operatorname{PolyLog}(3, -x)}{x} dx, x, e^{2i(c+d\sqrt{x})}\right)}{d^4} \\
&\quad + \frac{(3b^2) \operatorname{Subst}\left(\int \frac{\operatorname{PolyLog}(2, -x)}{x} dx, x, e^{2i(c+d\sqrt{x})}\right)}{d^4}
\end{aligned}$$

$$\begin{aligned}
&= -\frac{2ib^2x^{3/2}}{d} + \frac{a^2x^2}{2} + iabx^2 - \frac{b^2x^2}{2} + \frac{6b^2x \log\left(1 + e^{2i(c+d\sqrt{x})}\right)}{d^2} \\
&\quad - \frac{4abx^{3/2} \log\left(1 + e^{2i(c+d\sqrt{x})}\right)}{d} - \frac{6ib^2\sqrt{x} \operatorname{PolyLog}\left(2, -e^{2i(c+d\sqrt{x})}\right)}{d^3} \\
&\quad + \frac{6iabx \operatorname{PolyLog}\left(2, -e^{2i(c+d\sqrt{x})}\right)}{d^2} + \frac{3b^2 \operatorname{PolyLog}\left(3, -e^{2i(c+d\sqrt{x})}\right)}{d^4} \\
&\quad - \frac{6ab\sqrt{x} \operatorname{PolyLog}\left(3, -e^{2i(c+d\sqrt{x})}\right)}{d^3} \\
&\quad - \frac{3iab \operatorname{PolyLog}\left(4, -e^{2i(c+d\sqrt{x})}\right)}{d^4} + \frac{2b^2x^{3/2} \tan(c + d\sqrt{x})}{d}
\end{aligned}$$

Mathematica [A] (verified)

Time = 1.72 (sec) , antiderivative size = 365, normalized size of antiderivative = 1.33

$$\begin{aligned}
&\int x(a + b \tan(c + d\sqrt{x}))^2 dx \\
&= \frac{b\left(4ibd^3x^{3/2} - 2iad^4x^2 + 6bd^2x \log\left(1 + e^{-2i(c+d\sqrt{x})}\right) + 6bd^2e^{2ic}x \log\left(1 + e^{-2i(c+d\sqrt{x})}\right) - 4ad^3x^{3/2} \log\left(1 + e^{-2i(c+d\sqrt{x})}\right)\right)}{d^4} \\
&\quad + \frac{2b^2x^{3/2} \sec(c) \sec(c + d\sqrt{x}) \sin(d\sqrt{x})}{d} + \frac{1}{2}x^2(a^2 - b^2 + 2ab \tan(c))
\end{aligned}$$

[In] Integrate[x*(a + b*Tan[c + d*Sqrt[x]])^2,x]

[Out] (b*((4*I)*b*d^3*x^(3/2) - (2*I)*a*d^4*x^2 + 6*b*d^2*x*Log[1 + E^((-2*I)*(c + d*Sqrt[x]))] + 6*b*d^2*E^((2*I)*c)*x*Log[1 + E^((-2*I)*(c + d*Sqrt[x]))] - 4*a*d^3*x^(3/2)*Log[1 + E^((-2*I)*(c + d*Sqrt[x]))] - 4*a*d^3*E^((2*I)*c)*x^(3/2)*Log[1 + E^((-2*I)*(c + d*Sqrt[x]))] - (6*I)*d*(1 + E^((2*I)*c))*(-b + a*d*Sqrt[x])*Sqrt[x]*PolyLog[2, -E^((-2*I)*(c + d*Sqrt[x]))] + 3*(1 + E^((2*I)*c))*(b - 2*a*d*Sqrt[x])*PolyLog[3, -E^((-2*I)*(c + d*Sqrt[x]))] + (3*I)*a*PolyLog[4, -E^((-2*I)*(c + d*Sqrt[x]))] + (3*I)*a*E^((2*I)*c)*PolyLog[4, -E^((-2*I)*(c + d*Sqrt[x]))]))/(d^4*(1 + E^((2*I)*c))) + (2*b^2*x^(3/2)*Sec[c]*Sec[c + d*Sqrt[x]]*Sin[d*Sqrt[x]])/d + (x^2*(a^2 - b^2 + 2*a*b*Tan[c]))/2

Maple [F]

$$\int x(a + b \tan(c + d\sqrt{x}))^2 dx$$

```
[In] int(x*(a+b*tan(c+d*x^(1/2)))^2,x)
```

```
[Out] int(x*(a+b*tan(c+d*x^(1/2)))^2,x)
```

Fricas [F]

$$\int x(a + b \tan(c + d\sqrt{x}))^2 dx = \int (b \tan(d\sqrt{x} + c) + a)^2 x dx$$

```
[In] integrate(x*(a+b*tan(c+d*x^(1/2)))^2,x, algorithm="fricas")
```

```
[Out] integral(b^2*x*tan(d*sqrt(x) + c)^2 + 2*a*b*x*tan(d*sqrt(x) + c) + a^2*x, x
)
```

Sympy [F]

$$\int x(a + b \tan(c + d\sqrt{x}))^2 dx = \int x(a + b \tan(c + d\sqrt{x}))^2 dx$$

```
[In] integrate(x*(a+b*tan(c+d*x**(1/2)))**2,x)
```

```
[Out] Integral(x*(a + b*tan(c + d*sqrt(x)))**2, x)
```

Maxima [B] (verification not implemented)

Both result and optimal contain complex but leaf count of result is larger than twice the leaf count of optimal. 1290 vs. $2(218) = 436$.

Time = 0.51 (sec) , antiderivative size = 1290, normalized size of antiderivative = 4.71

$$\int x(a + b \tan(c + d\sqrt{x}))^2 dx = \text{Too large to display}$$

```
[In] integrate(x*(a+b*tan(c+d*x^(1/2)))^2,x, algorithm="maxima")
```

```
[Out] 1/2*((d*sqrt(x) + c)^4*a^2 - 4*(d*sqrt(x) + c)^3*a^2*c + 6*(d*sqrt(x) + c)^2*a^2*c^2 - 4*(d*sqrt(x) + c)*a^2*c^3 - 8*a*b*c^3*log(sec(d*sqrt(x) + c)) - 4*(12*I*(d*sqrt(x) + c)*b^2*c^3 - 3*(2*a*b + I*b^2)*(d*sqrt(x) + c)^4 + 12*(2*a*b + I*b^2)*(d*sqrt(x) + c)^3*c - 18*(2*a*b + I*b^2)*(d*sqrt(x) + c)^2*c^2 + 24*b^2*c^3 + 4*(8*(d*sqrt(x) + c)^3*a*b - 9*b^2*c^2 - 9*(2*a*b*c + b
```

```

^2)*(d*sqrt(x) + c)^2 + 18*(a*b*c^2 + b^2*c)*(d*sqrt(x) + c) + (8*(d*sqrt(x)
) + c)^3*a*b - 9*b^2*c^2 - 9*(2*a*b*c + b^2)*(d*sqrt(x) + c)^2 + 18*(a*b*c^
2 + b^2*c)*(d*sqrt(x) + c))*cos(2*d*sqrt(x) + 2*c) - (-8*I*(d*sqrt(x) + c)^
3*a*b + 9*I*b^2*c^2 + 9*(2*I*a*b*c + I*b^2)*(d*sqrt(x) + c)^2 + 18*(-I*a*b*
c^2 - I*b^2*c)*(d*sqrt(x) + c))*sin(2*d*sqrt(x) + 2*c))*arctan2(sin(2*d*sqr
t(x) + 2*c), cos(2*d*sqrt(x) + 2*c) + 1) - 3*((2*a*b + I*b^2)*(d*sqrt(x) +
c)^4 - 4*(2*b^2 + (2*a*b + I*b^2)*c)*(d*sqrt(x) + c)^3 + 6*(4*b^2*c + (2*a*
b + I*b^2)*c^2)*(d*sqrt(x) + c)^2 + 4*(-I*b^2*c^3 - 6*b^2*c^2)*(d*sqrt(x) +
c))*cos(2*d*sqrt(x) + 2*c) - 12*(4*(d*sqrt(x) + c)^2*a*b + 3*a*b*c^2 + 3*b
^2*c - 3*(2*a*b*c + b^2)*(d*sqrt(x) + c) + (4*(d*sqrt(x) + c)^2*a*b + 3*a*b
*c^2 + 3*b^2*c - 3*(2*a*b*c + b^2)*(d*sqrt(x) + c))*cos(2*d*sqrt(x) + 2*c)
+ (4*I*(d*sqrt(x) + c)^2*a*b + 3*I*a*b*c^2 + 3*I*b^2*c + 3*(-2*I*a*b*c - I*
b^2)*(d*sqrt(x) + c))*sin(2*d*sqrt(x) + 2*c))*dilog(-e^(2*I*d*sqrt(x) + 2*I
*c)) - 2*(8*I*(d*sqrt(x) + c)^3*a*b - 9*I*b^2*c^2 + 9*(-2*I*a*b*c - I*b^2)*
(d*sqrt(x) + c)^2 + 18*(I*a*b*c^2 + I*b^2*c)*(d*sqrt(x) + c) + (8*I*(d*sqrt
(x) + c)^3*a*b - 9*I*b^2*c^2 + 9*(-2*I*a*b*c - I*b^2)*(d*sqrt(x) + c)^2 + 1
8*(I*a*b*c^2 + I*b^2*c)*(d*sqrt(x) + c))*cos(2*d*sqrt(x) + 2*c) - (8*(d*sqr
t(x) + c)^3*a*b - 9*b^2*c^2 - 9*(2*a*b*c + b^2)*(d*sqrt(x) + c)^2 + 18*(a*b
*c^2 + b^2*c)*(d*sqrt(x) + c))*sin(2*d*sqrt(x) + 2*c))*log(cos(2*d*sqrt(x)
+ 2*c)^2 + sin(2*d*sqrt(x) + 2*c)^2 + 2*cos(2*d*sqrt(x) + 2*c) + 1) + 24*(a
*b*cos(2*d*sqrt(x) + 2*c) + I*a*b*sin(2*d*sqrt(x) + 2*c) + a*b)*polylog(4,
-e^(2*I*d*sqrt(x) + 2*I*c)) - 6*(8*I*(d*sqrt(x) + c)*a*b - 6*I*a*b*c - 3*I*
b^2 + (8*I*(d*sqrt(x) + c)*a*b - 6*I*a*b*c - 3*I*b^2)*cos(2*d*sqrt(x) + 2*c
) - (8*(d*sqrt(x) + c)*a*b - 6*a*b*c - 3*b^2)*sin(2*d*sqrt(x) + 2*c))*polyl
og(3, -e^(2*I*d*sqrt(x) + 2*I*c)) - 3*((2*I*a*b - b^2)*(d*sqrt(x) + c)^4 +
4*(-2*I*b^2 + (-2*I*a*b + b^2)*c)*(d*sqrt(x) + c)^3 + 6*(4*I*b^2*c + (2*I*a
*b - b^2)*c^2)*(d*sqrt(x) + c)^2 + 4*(b^2*c^3 - 6*I*b^2*c^2)*(d*sqrt(x) + c
))*sin(2*d*sqrt(x) + 2*c))/(-12*I*cos(2*d*sqrt(x) + 2*c) + 12*sin(2*d*sqrt(
x) + 2*c) - 12*I))/d^4

```

Giac [F]

$$\int x(a + b \tan(c + d\sqrt{x}))^2 dx = \int (b \tan(d\sqrt{x} + c) + a)^2 x dx$$

[In] integrate(x*(a+b*tan(c+d*x^(1/2)))^2,x, algorithm="giac")

[Out] integrate((b*tan(d*sqrt(x) + c) + a)^2*x, x)

Mupad [F(-1)]

Timed out.

$$\int x(a + b \tan(c + d\sqrt{x}))^2 dx = \int x(a + b \tan(c + d\sqrt{x}))^2 dx$$

```
[In] int(x*(a + b*tan(c + d*x^(1/2)))^2,x)
```

```
[Out] int(x*(a + b*tan(c + d*x^(1/2)))^2, x)
```

3.33 $\int (a + b \tan(c + d\sqrt{x}))^2 dx$

Optimal result	194
Rubi [A] (verified)	194
Mathematica [B] (verified)	197
Maple [F]	197
Fricas [A] (verification not implemented)	197
Sympy [F]	198
Maxima [B] (verification not implemented)	198
Giac [F]	199
Mupad [F(-1)]	199

Optimal result

Integrand size = 16, antiderivative size = 119

$$\int (a + b \tan(c + d\sqrt{x}))^2 dx = a^2x + 2iabx - b^2x - \frac{4ab\sqrt{x} \log(1 + e^{2i(c+d\sqrt{x})})}{d} + \frac{2b^2 \log(\cos(c + d\sqrt{x}))}{d^2} + \frac{2iab \operatorname{PolyLog}(2, -e^{2i(c+d\sqrt{x})})}{d^2} + \frac{2b^2\sqrt{x} \tan(c + d\sqrt{x})}{d}$$

[Out] $a^2x + 2Iabx - b^2x + \frac{2b^2 \ln(\cos(c + d\sqrt{x}))}{d^2} + \frac{2Iab \operatorname{polylog}(2, -\exp(2I(c + d\sqrt{x})))}{d^2} - \frac{4ab\sqrt{x} \ln(1 + \exp(2I(c + d\sqrt{x})))}{d} + \frac{2b^2\sqrt{x} \tan(c + d\sqrt{x})}{d}$

Rubi [A] (verified)

Time = 0.22 (sec) , antiderivative size = 119, normalized size of antiderivative = 1.00, number of steps used = 10, number of rules used = 9, $\frac{\text{number of rules}}{\text{integrand size}} = 0.562$, Rules used = {3824, 3803, 3800, 2221, 2317, 2438, 3801, 3556, 30}

$$\int (a + b \tan(c + d\sqrt{x}))^2 dx = a^2x + \frac{2iab \operatorname{PolyLog}(2, -e^{2i(c+d\sqrt{x})})}{d^2} - \frac{4ab\sqrt{x} \log(1 + e^{2i(c+d\sqrt{x})})}{d} + 2iabx + \frac{2b^2 \log(\cos(c + d\sqrt{x}))}{d^2} + \frac{2b^2\sqrt{x} \tan(c + d\sqrt{x})}{d} - b^2x$$

[In] $\operatorname{Int}[(a + b \operatorname{Tan}[c + d \operatorname{Sqrt}[x]])^2, x]$

[Out] $a^2x + (2I)abx - b^2x - (4ab\sqrt{x}\log[1 + E^{(2I)(c + d\sqrt{x})}])]/d + (2b^2\log[\cos[c + d\sqrt{x}]])/d^2 + ((2I)ab\text{PolyLog}[2, -E^{(2I)(c + d\sqrt{x})}])/d^2 + (2b^2\sqrt{x}\tan[c + d\sqrt{x}])/d$

Rule 30

$\text{Int}[(x_)^{(m_)}, x_Symbol] \rightarrow \text{Simp}[x^{(m+1)}/(m+1), x] \text{ ; FreeQ}[m, x] \ \&\& \ \text{NeQ}[m, -1]$

Rule 2221

$\text{Int}[(((F_)^{((g_)*(e_) + (f_)*(x_))})^{(n_)*((c_) + (d_)*(x_))^{(m_)}})/((a_) + (b_)*((F_)^{((g_)*(e_) + (f_)*(x_))})^{(n_)}), x_Symbol] \rightarrow \text{Simp}[(c + dx)^m/(bfgn\log[F])\log[1 + b((F^{(g(e + fx)))^n/a}], x] - \text{Dist}[d(m/(bfgn\log[F])), \text{Int}[(c + dx)^{(m-1)}\log[1 + b((F^{(g(e + fx)))^n/a}], x], x] \text{ ; FreeQ}[\{F, a, b, c, d, e, f, g, n\}, x] \ \&\& \ \text{IGtQ}[m, 0]$

Rule 2317

$\text{Int}[\log[(a_) + (b_)*((F_)^{((e_)*((c_) + (d_)*(x_))})^{(n_)}], x_Symbol] \rightarrow \text{Dist}[1/(d*e*n\log[F]), \text{Subst}[\text{Int}[\log[a + bx]/x, x], x, (F^{(e*(c + dx)))^n}], x] \text{ ; FreeQ}[\{F, a, b, c, d, e, n\}, x] \ \&\& \ \text{GtQ}[a, 0]$

Rule 2438

$\text{Int}[\log[(c_)*((d_) + (e_)*(x_)^{(n_)})]/(x_), x_Symbol] \rightarrow \text{Simp}[-\text{PolyLog}[2, (-c)*e*x^n]/n, x] \text{ ; FreeQ}[\{c, d, e, n\}, x] \ \&\& \ \text{EqQ}[c*d, 1]$

Rule 3556

$\text{Int}[\tan[(c_) + (d_)*(x_)], x_Symbol] \rightarrow \text{Simp}[-\log[\text{RemoveContent}[\cos[c + dx], x]]/d, x] \text{ ; FreeQ}[\{c, d\}, x]$

Rule 3800

$\text{Int}[(((c_) + (d_)*(x_))^{(m_)*\tan[(e_) + (f_)*(x_)]}, x_Symbol] \rightarrow \text{Simp}[I*((c + dx)^{(m+1)}/(d*(m+1))), x] - \text{Dist}[2I, \text{Int}[(c + dx)^m*(E^{(2I*(e + fx))}/(1 + E^{(2I*(e + fx))}))], x], x] \text{ ; FreeQ}[\{c, d, e, f\}, x] \ \&\& \ \text{IGtQ}[m, 0]$

Rule 3801

$\text{Int}[(((c_) + (d_)*(x_))^{(m_)*((b_)*\tan[(e_) + (f_)*(x_)]})^{(n_)}, x_Symbol] \rightarrow \text{Simp}[b*(c + dx)^m*((b*\tan[e + fx])^{(n-1)}/(f*(n-1))), x] + (-\text{Dist}[b*d*(m/(f*(n-1))), \text{Int}[(c + dx)^{(m-1)}*(b*\tan[e + fx])^{(n-1)}, x], x] - \text{Dist}[b^2, \text{Int}[(c + dx)^m*(b*\tan[e + fx])^{(n-2)}, x], x]) \text{ ; FreeQ}[\{b, c, d, e, f\}, x] \ \&\& \ \text{GtQ}[n, 1] \ \&\& \ \text{GtQ}[m, 0]$

Rule 3803

```
Int[((c_.) + (d_.)*(x_))^(m_.)*((a_.) + (b_.)*tan[(e_.) + (f_.)*(x_)])^(n_.)
, x_Symbol] := Int[ExpandIntegrand[(c + d*x)^m, (a + b*Tan[e + f*x])^n, x],
x] /; FreeQ[{a, b, c, d, e, f, m}, x] && IGtQ[m, 0] && IGtQ[n, 0]
```

Rule 3824

```
Int[((a_.) + (b_.)*Tan[(c_.) + (d_.)*(x_)^(n_)])^(p_.), x_Symbol] := Dist[1
/n, Subst[Int[x^(1/n - 1)*(a + b*Tan[c + d*x])^p, x], x, x^n], x] /; FreeQ[
{a, b, c, d, p}, x] && IGtQ[1/n, 0] && IntegerQ[p]
```

Rubi steps

$$\begin{aligned}
\text{integral} &= 2\text{Subst}\left(\int x(a + b \tan(c + dx))^2 dx, x, \sqrt{x}\right) \\
&= 2\text{Subst}\left(\int (a^2x + 2abx \tan(c + dx) + b^2x \tan^2(c + dx)) dx, x, \sqrt{x}\right) \\
&= a^2x + (4ab)\text{Subst}\left(\int x \tan(c + dx) dx, x, \sqrt{x}\right) + (2b^2)\text{Subst}\left(\int x \tan^2(c + dx) dx, x, \sqrt{x}\right) \\
&= a^2x + 2iabx + \frac{2b^2\sqrt{x} \tan(c + d\sqrt{x})}{d} - (8iab)\text{Subst}\left(\int \frac{e^{2i(c+dx)}x}{1 + e^{2i(c+dx)}} dx, x, \sqrt{x}\right) \\
&\quad - (2b^2)\text{Subst}\left(\int x dx, x, \sqrt{x}\right) - \frac{(2b^2)\text{Subst}\left(\int \tan(c + dx) dx, x, \sqrt{x}\right)}{d} \\
&= a^2x + 2iabx - b^2x - \frac{4ab\sqrt{x} \log(1 + e^{2i(c+d\sqrt{x})})}{d} + \frac{2b^2 \log(\cos(c + d\sqrt{x}))}{d^2} \\
&\quad + \frac{2b^2\sqrt{x} \tan(c + d\sqrt{x})}{d} + \frac{(4ab)\text{Subst}\left(\int \log(1 + e^{2i(c+dx)}) dx, x, \sqrt{x}\right)}{d} \\
&= a^2x + 2iabx - b^2x - \frac{4ab\sqrt{x} \log(1 + e^{2i(c+d\sqrt{x})})}{d} + \frac{2b^2 \log(\cos(c + d\sqrt{x}))}{d^2} \\
&\quad + \frac{2b^2\sqrt{x} \tan(c + d\sqrt{x})}{d} - \frac{(2iab)\text{Subst}\left(\int \frac{\log(1+x)}{x} dx, x, e^{2i(c+d\sqrt{x})}\right)}{d^2} \\
&= a^2x + 2iabx - b^2x - \frac{4ab\sqrt{x} \log(1 + e^{2i(c+d\sqrt{x})})}{d} + \frac{2b^2 \log(\cos(c + d\sqrt{x}))}{d^2} \\
&\quad + \frac{2iab \text{PolyLog}\left(2, -e^{2i(c+d\sqrt{x})}\right)}{d^2} + \frac{2b^2\sqrt{x} \tan(c + d\sqrt{x})}{d}
\end{aligned}$$

Mathematica [B] (verified)

Both result and optimal contain complex but leaf count is larger than twice the leaf count of optimal. 253 vs. $2(119) = 238$.

Time = 4.95 (sec) , antiderivative size = 253, normalized size of antiderivative = 2.13

$$\int (a + b \tan(c + d\sqrt{x}))^2 dx$$

$$= \frac{\sec(c) \left(-2ab \cos(c) \left(id\sqrt{x}(\pi + 2 \arctan(\cot(c))) + \pi \log(1 + e^{-2id\sqrt{x}}) + 2(d\sqrt{x} - \arctan(\cot(c))) \log(1 + e^{-2id\sqrt{x}}) \right) \right)}{d^2}$$

[In] Integrate[(a + b*Tan[c + d*Sqrt[x]])^2,x]

[Out] (Sec[c]*(-2*a*b*Cos[c]*(I*d*Sqrt[x]*(Pi + 2*ArcTan[Cot[c]]) + Pi*Log[1 + E^((-2*I)*d*Sqrt[x])]) + 2*(d*Sqrt[x] - ArcTan[Cot[c]])*Log[1 - E^((2*I)*(d*Sqrt[x] - ArcTan[Cot[c]])*)] - Pi*Log[Cos[d*Sqrt[x]]] + 2*ArcTan[Cot[c]]*Log[Sin[d*Sqrt[x] - ArcTan[Cot[c]]]) - I*PolyLog[2, E^((2*I)*(d*Sqrt[x] - ArcTan[Cot[c]])*)] - (2*a*b*d^2*x*Sqrt[Csc[c]^2]*Sin[c])/E^(I*ArcTan[Cot[c]]) + d^2*x*((a^2 - b^2)*Cos[c] + 2*a*b*Sin[c]) + 2*b^2*(Cos[c]*Log[Cos[c + d*Sqrt[x]]) + d*Sqrt[x]*Sin[c]) + 2*b^2*d*Sqrt[x]*Sec[c + d*Sqrt[x]]*Sin[d*Sqrt[x]])/d^2

Maple [F]

$$\int (a + b \tan(c + d\sqrt{x}))^2 dx$$

[In] int((a+b*tan(c+d*x^(1/2)))^2,x)

[Out] int((a+b*tan(c+d*x^(1/2)))^2,x)

Fricas [A] (verification not implemented)

none

Time = 0.26 (sec) , antiderivative size = 196, normalized size of antiderivative = 1.65

$$\int (a + b \tan(c + d\sqrt{x}))^2 dx$$

$$= \frac{2b^2d\sqrt{x} \tan(d\sqrt{x} + c) + (a^2 - b^2)d^2x - iab\text{Li}_2\left(\frac{2(i \tan(d\sqrt{x}+c)-1)}{\tan(d\sqrt{x}+c)^2+1} + 1\right) + iab\text{Li}_2\left(\frac{2(-i \tan(d\sqrt{x}+c)-1)}{\tan(d\sqrt{x}+c)^2+1} + 1\right)}{d^2}$$

[In] integrate((a+b*tan(c+d*x^(1/2)))^2,x, algorithm="fricas")

[Out] (2*b^2*d*sqrt(x)*tan(d*sqrt(x) + c) + (a^2 - b^2)*d^2*x - I*a*b*dilog(2*(I*tan(d*sqrt(x) + c) - 1)/(tan(d*sqrt(x) + c)^2 + 1) + 1) + I*a*b*dilog(2*(-I

```
*tan(d*sqrt(x) + c) - 1)/(tan(d*sqrt(x) + c)^2 + 1) + 1) - (2*a*b*d*sqrt(x)
- b^2)*log(-2*(I*tan(d*sqrt(x) + c) - 1)/(tan(d*sqrt(x) + c)^2 + 1)) - (2*
a*b*d*sqrt(x) - b^2)*log(-2*(-I*tan(d*sqrt(x) + c) - 1)/(tan(d*sqrt(x) + c)
^2 + 1)))/d^2
```

Sympy [F]

$$\int (a + b \tan(c + d\sqrt{x}))^2 dx = \int (a + b \tan(c + d\sqrt{x}))^2 dx$$

```
[In] integrate((a+b*tan(c+d*x**(1/2)))**2,x)
```

```
[Out] Integral((a + b*tan(c + d*sqrt(x)))**2, x)
```

Maxima [B] (verification not implemented)

Both result and optimal contain complex but leaf count of result is larger than twice the leaf count of optimal. 497 vs. 2(98) = 196.

Time = 0.54 (sec) , antiderivative size = 497, normalized size of antiderivative = 4.18

$$\int (a + b \tan(c + d\sqrt{x}))^2 dx = a^2x + \frac{4b^2d\sqrt{x} + 4(ab \cos(2d\sqrt{x} + 2c) + iab \sin(2d\sqrt{x} + 2c) + ab) \arctan(\sin(2d\sqrt{x} - 2c), \cos(2d\sqrt{x} - 2c))}{1}$$

```
[In] integrate((a+b*tan(c+d*x^(1/2)))^2,x, algorithm="maxima")
```

```
[Out] a^2*x + (4*b^2*d*sqrt(x) + 4*(a*b*cos(2*d*sqrt(x) + 2*c) + I*a*b*sin(2*d*sqrt(x) + 2*c) + a*b)*arctan2(sin(2*d*sqrt(x) - 2*c), cos(2*d*sqrt(x) - 2*c) + 1)*arctan2(sin(d*sqrt(x)), cos(d*sqrt(x))) - 2*(I*a*b*cos(2*d*sqrt(x) + 2*c) - a*b*sin(2*d*sqrt(x) + 2*c) + I*a*b)*arctan2(sin(d*sqrt(x)), cos(d*sqrt(x))))*log(cos(2*d*sqrt(x) - 2*c)^2 + sin(2*d*sqrt(x) - 2*c)^2 + 2*cos(2*d*sqrt(x) - 2*c) + 1) - ((2*a*b - I*b^2)*d^2*cos(2*d*sqrt(x) + 2*c) - (-2*I*a*b - b^2)*d^2*sin(2*d*sqrt(x) + 2*c) + (2*a*b - I*b^2)*d^2)*x + 2*(b^2*cos(2*d*sqrt(x) + 2*c) + I*b^2*sin(2*d*sqrt(x) + 2*c) + b^2)*arctan2(sin(2*d*sqrt(x)) + sin(2*c), cos(2*d*sqrt(x)) + cos(2*c)) - 2*(a*b*cos(2*d*sqrt(x) + 2*c) + I*a*b*sin(2*d*sqrt(x) + 2*c) + a*b)*dilog(-e^(2*I*d*sqrt(x) - 2*I*c)) + (-I*b^2*cos(2*d*sqrt(x) + 2*c) + b^2*sin(2*d*sqrt(x) + 2*c) - I*b^2)*log(cos(2*d*sqrt(x))^2 + 2*cos(2*d*sqrt(x))*cos(2*c) + cos(2*c)^2 + sin(2*d*sqrt(x))^2 + 2*sin(2*d*sqrt(x))*sin(2*c) + sin(2*c)^2)/(-I*d^2*cos(2*d*sqrt(x) + 2*c) + d^2*sin(2*d*sqrt(x) + 2*c) - I*d^2)
```

Giac [F]

$$\int (a + b \tan(c + d\sqrt{x}))^2 dx = \int (b \tan(d\sqrt{x} + c) + a)^2 dx$$

[In] integrate((a+b*tan(c+d*x^(1/2)))^2,x, algorithm="giac")

[Out] integrate((b*tan(d*sqrt(x) + c) + a)^2, x)

Mupad [F(-1)]

Timed out.

$$\int (a + b \tan(c + d\sqrt{x}))^2 dx = \int (a + b \tan(c + d\sqrt{x}))^2 dx$$

[In] int((a + b*tan(c + d*x^(1/2)))^2,x)

[Out] int((a + b*tan(c + d*x^(1/2)))^2, x)

$$3.34 \quad \int \frac{(a+b \tan(c+d\sqrt{x}))^2}{x} dx$$

Optimal result	200
Rubi [N/A]	200
Mathematica [N/A]	201
Maple [N/A] (verified)	201
Fricas [N/A]	201
Sympy [N/A]	201
Maxima [N/A]	202
Giac [N/A]	202
Mupad [N/A]	202

Optimal result

Integrand size = 20, antiderivative size = 20

$$\int \frac{(a+b \tan(c+d\sqrt{x}))^2}{x} dx = \text{Int}\left(\frac{(a+b \tan(c+d\sqrt{x}))^2}{x}, x\right)$$

[Out] Unintegrable((a+b*tan(c+d*x^(1/2)))^2/x,x)

Rubi [N/A]

Not integrable

Time = 0.03 (sec) , antiderivative size = 20, normalized size of antiderivative = 1.00, number of steps used = 0, number of rules used = 0, $\frac{\text{number of rules}}{\text{integrand size}} = 0.000$, Rules used = {}

$$\int \frac{(a+b \tan(c+d\sqrt{x}))^2}{x} dx = \int \frac{(a+b \tan(c+d\sqrt{x}))^2}{x} dx$$

[In] Int[(a + b*Tan[c + d*Sqrt[x]])^2/x,x]

[Out] Defer[Int][(a + b*Tan[c + d*Sqrt[x]])^2/x, x]

Rubi steps

$$\text{integral} = \int \frac{(a+b \tan(c+d\sqrt{x}))^2}{x} dx$$

Mathematica [N/A]

Not integrable

Time = 130.41 (sec) , antiderivative size = 22, normalized size of antiderivative = 1.10

$$\int \frac{(a + b \tan(c + d\sqrt{x}))^2}{x} dx = \int \frac{(a + b \tan(c + d\sqrt{x}))^2}{x} dx$$

[In] Integrate[(a + b*Tan[c + d*Sqrt[x]])^2/x,x]

[Out] Integrate[(a + b*Tan[c + d*Sqrt[x]])^2/x, x]

Maple [N/A] (verified)

Not integrable

Time = 0.97 (sec) , antiderivative size = 18, normalized size of antiderivative = 0.90

$$\int \frac{(a + b \tan(c + d\sqrt{x}))^2}{x} dx$$

[In] int((a+b*tan(c+d*x^(1/2)))^2/x,x)

[Out] int((a+b*tan(c+d*x^(1/2)))^2/x,x)

Fricas [N/A]

Not integrable

Time = 0.25 (sec) , antiderivative size = 36, normalized size of antiderivative = 1.80

$$\int \frac{(a + b \tan(c + d\sqrt{x}))^2}{x} dx = \int \frac{(b \tan(d\sqrt{x} + c) + a)^2}{x} dx$$

[In] integrate((a+b*tan(c+d*x^(1/2)))^2/x,x, algorithm="fricas")

[Out] integral((b^2*tan(d*sqrt(x) + c)^2 + 2*a*b*tan(d*sqrt(x) + c) + a^2)/x, x)

Sympy [N/A]

Not integrable

Time = 8.72 (sec) , antiderivative size = 17, normalized size of antiderivative = 0.85

$$\int \frac{(a + b \tan(c + d\sqrt{x}))^2}{x} dx = \int \frac{(a + b \tan(c + d\sqrt{x}))^2}{x} dx$$

[In] integrate((a+b*tan(c+d*x**(1/2)))**2/x,x)

[Out] Integral((a + b*tan(c + d*sqrt(x)))**2/x, x)

Maxima [N/A]

Not integrable

Time = 0.73 (sec) , antiderivative size = 298, normalized size of antiderivative = 14.90

$$\int \frac{(a + b \tan(c + d\sqrt{x}))^2}{x} dx = \int \frac{(b \tan(d\sqrt{x} + c) + a)^2}{x} dx$$

```
[In] integrate((a+b*tan(c+d*x^(1/2)))^2/x,x, algorithm="maxima")
```

```
[Out] (4*b^2*sqrt(x)*sin(2*d*sqrt(x) + 2*c) + (d*cos(2*d*sqrt(x) + 2*c)^2 + d*sin(2*d*sqrt(x) + 2*c)^2 + 2*d*cos(2*d*sqrt(x) + 2*c) + d)*x*integrate(2*(2*a*b*d*x*sin(2*d*sqrt(x) + 2*c) + b^2*sqrt(x)*sin(2*d*sqrt(x) + 2*c)))/((d*cos(2*d*sqrt(x) + 2*c)^2 + d*sin(2*d*sqrt(x) + 2*c)^2 + 2*d*cos(2*d*sqrt(x) + 2*c) + d)*x^2), x) + ((a^2 - b^2)*d*cos(2*d*sqrt(x) + 2*c)^2 + (a^2 - b^2)*d*sin(2*d*sqrt(x) + 2*c)^2 + 2*(a^2 - b^2)*d*cos(2*d*sqrt(x) + 2*c) + (a^2 - b^2)*d)*x*log(x))/((d*cos(2*d*sqrt(x) + 2*c)^2 + d*sin(2*d*sqrt(x) + 2*c)^2 + 2*d*cos(2*d*sqrt(x) + 2*c) + d)*x)
```

Giac [N/A]

Not integrable

Time = 0.85 (sec) , antiderivative size = 20, normalized size of antiderivative = 1.00

$$\int \frac{(a + b \tan(c + d\sqrt{x}))^2}{x} dx = \int \frac{(b \tan(d\sqrt{x} + c) + a)^2}{x} dx$$

```
[In] integrate((a+b*tan(c+d*x^(1/2)))^2/x,x, algorithm="giac")
```

```
[Out] integrate((b*tan(d*sqrt(x) + c) + a)^2/x, x)
```

Mupad [N/A]

Not integrable

Time = 4.03 (sec) , antiderivative size = 20, normalized size of antiderivative = 1.00

$$\int \frac{(a + b \tan(c + d\sqrt{x}))^2}{x} dx = \int \frac{(a + b \tan(c + d\sqrt{x}))^2}{x} dx$$

```
[In] int((a + b*tan(c + d*x^(1/2)))^2/x,x)
```

```
[Out] int((a + b*tan(c + d*x^(1/2)))^2/x, x)
```

$$3.35 \quad \int \frac{(a+b \tan(c+d\sqrt{x}))^2}{x^2} dx$$

Optimal result	203
Rubi [N/A]	203
Mathematica [N/A]	204
Maple [N/A] (verified)	204
Fricas [N/A]	204
Sympy [N/A]	205
Maxima [N/A]	205
Giac [N/A]	205
Mupad [N/A]	206

Optimal result

Integrand size = 20, antiderivative size = 20

$$\int \frac{(a+b \tan(c+d\sqrt{x}))^2}{x^2} dx = \text{Int}\left(\frac{(a+b \tan(c+d\sqrt{x}))^2}{x^2}, x\right)$$

[Out] Unintegrable((a+b*tan(c+d*x^(1/2)))^2/x^2,x)

Rubi [N/A]

Not integrable

Time = 0.02 (sec) , antiderivative size = 20, normalized size of antiderivative = 1.00, number of steps used = 0, number of rules used = 0, $\frac{\text{number of rules}}{\text{integrand size}} = 0.000$, Rules used = {}

$$\int \frac{(a+b \tan(c+d\sqrt{x}))^2}{x^2} dx = \int \frac{(a+b \tan(c+d\sqrt{x}))^2}{x^2} dx$$

[In] Int[(a + b*Tan[c + d*Sqrt[x]])^2/x^2,x]

[Out] Defer[Int] [(a + b*Tan[c + d*Sqrt[x]])^2/x^2, x]

Rubi steps

$$\text{integral} = \int \frac{(a+b \tan(c+d\sqrt{x}))^2}{x^2} dx$$

Mathematica [N/A]

Not integrable

Time = 19.32 (sec) , antiderivative size = 22, normalized size of antiderivative = 1.10

$$\int \frac{(a + b \tan(c + d\sqrt{x}))^2}{x^2} dx = \int \frac{(a + b \tan(c + d\sqrt{x}))^2}{x^2} dx$$

[In] Integrate[(a + b*Tan[c + d*Sqrt[x]])^2/x^2,x]

[Out] Integrate[(a + b*Tan[c + d*Sqrt[x]])^2/x^2, x]

Maple [N/A] (verified)

Not integrable

Time = 1.05 (sec) , antiderivative size = 18, normalized size of antiderivative = 0.90

$$\int \frac{(a + b \tan(c + d\sqrt{x}))^2}{x^2} dx$$

[In] int((a+b*tan(c+d*x^(1/2)))^2/x^2,x)

[Out] int((a+b*tan(c+d*x^(1/2)))^2/x^2,x)

Fricas [N/A]

Not integrable

Time = 0.25 (sec) , antiderivative size = 36, normalized size of antiderivative = 1.80

$$\int \frac{(a + b \tan(c + d\sqrt{x}))^2}{x^2} dx = \int \frac{(b \tan(d\sqrt{x} + c) + a)^2}{x^2} dx$$

[In] integrate((a+b*tan(c+d*x^(1/2)))^2/x^2,x, algorithm="fricas")

[Out] integral((b^2*tan(d*sqrt(x) + c)^2 + 2*a*b*tan(d*sqrt(x) + c) + a^2)/x^2, x)

Sympy [N/A]

Not integrable

Time = 1.79 (sec) , antiderivative size = 19, normalized size of antiderivative = 0.95

$$\int \frac{(a + b \tan(c + d\sqrt{x}))^2}{x^2} dx = \int \frac{(a + b \tan(c + d\sqrt{x}))^2}{x^2} dx$$

[In] integrate((a+b*tan(c+d*x**(1/2)))**2/x**2,x)

[Out] Integral((a + b*tan(c + d*sqrt(x)))**2/x**2, x)

Maxima [N/A]

Not integrable

Time = 1.00 (sec) , antiderivative size = 300, normalized size of antiderivative = 15.00

$$\int \frac{(a + b \tan(c + d\sqrt{x}))^2}{x^2} dx = \int \frac{(b \tan(d\sqrt{x} + c) + a)^2}{x^2} dx$$

[In] integrate((a+b*tan(c+d*x^(1/2)))^2/x^2,x, algorithm="maxima")

```
[Out] ((d*cos(2*d*sqrt(x) + 2*c)^2 + d*sin(2*d*sqrt(x) + 2*c)^2 + 2*d*cos(2*d*sqrt(x) + 2*c) + d)*x^2*integrate(2*(2*a*b*d*x*sin(2*d*sqrt(x) + 2*c) + 3*b^2*sqrt(x)*sin(2*d*sqrt(x) + 2*c))/((d*cos(2*d*sqrt(x) + 2*c)^2 + d*sin(2*d*sqrt(x) + 2*c)^2 + 2*d*cos(2*d*sqrt(x) + 2*c) + d)*x^3), x) + 4*b^2*sqrt(x)*sin(2*d*sqrt(x) + 2*c) - ((a^2 - b^2)*d*cos(2*d*sqrt(x) + 2*c)^2 + (a^2 - b^2)*d*sin(2*d*sqrt(x) + 2*c)^2 + 2*(a^2 - b^2)*d*cos(2*d*sqrt(x) + 2*c) + (a^2 - b^2)*d)*x)/((d*cos(2*d*sqrt(x) + 2*c)^2 + d*sin(2*d*sqrt(x) + 2*c)^2 + 2*d*cos(2*d*sqrt(x) + 2*c) + d)*x^2)
```

Giac [N/A]

Not integrable

Time = 0.89 (sec) , antiderivative size = 20, normalized size of antiderivative = 1.00

$$\int \frac{(a + b \tan(c + d\sqrt{x}))^2}{x^2} dx = \int \frac{(b \tan(d\sqrt{x} + c) + a)^2}{x^2} dx$$

[In] integrate((a+b*tan(c+d*x^(1/2)))^2/x^2,x, algorithm="giac")

[Out] integrate((b*tan(d*sqrt(x) + c) + a)^2/x^2, x)

Mupad [N/A]

Not integrable

Time = 4.84 (sec) , antiderivative size = 20, normalized size of antiderivative = 1.00

$$\int \frac{(a + b \tan(c + d\sqrt{x}))^2}{x^2} dx = \int \frac{(a + b \tan(c + d\sqrt{x}))^2}{x^2} dx$$

```
[In] int((a + b*tan(c + d*x^(1/2)))^2/x^2,x)
```

```
[Out] int((a + b*tan(c + d*x^(1/2)))^2/x^2, x)
```

3.36 $\int \frac{x^3}{a+b \tan(c+d\sqrt{x})} dx$

Optimal result	207
Rubi [A] (verified)	208
Mathematica [A] (verified)	213
Maple [F]	213
Fricas [F]	213
Sympy [F]	214
Maxima [B] (verification not implemented)	214
Giac [F]	215
Mupad [F(-1)]	215

Optimal result

Integrand size = 20, antiderivative size = 460

$$\int \frac{x^3}{a+b \tan(c+d\sqrt{x})} dx = \frac{x^4}{4(a+ib)} + \frac{2bx^{7/2} \log\left(1 + \frac{(a^2+b^2)e^{2i(c+d\sqrt{x})}}{(a+ib)^2}\right)}{(a^2+b^2)d} - \frac{7ibx^3 \text{PolyLog}\left(2, -\frac{(a^2+b^2)e^{2i(c+d\sqrt{x})}}{(a+ib)^2}\right)}{(a^2+b^2)d^2} + \frac{21bx^{5/2} \text{PolyLog}\left(3, -\frac{(a^2+b^2)e^{2i(c+d\sqrt{x})}}{(a+ib)^2}\right)}{(a^2+b^2)d^3} + \frac{105ibx^2 \text{PolyLog}\left(4, -\frac{(a^2+b^2)e^{2i(c+d\sqrt{x})}}{(a+ib)^2}\right)}{2(a^2+b^2)d^4} - \frac{105bx^{3/2} \text{PolyLog}\left(5, -\frac{(a^2+b^2)e^{2i(c+d\sqrt{x})}}{(a+ib)^2}\right)}{(a^2+b^2)d^5} - \frac{315ibx \text{PolyLog}\left(6, -\frac{(a^2+b^2)e^{2i(c+d\sqrt{x})}}{(a+ib)^2}\right)}{2(a^2+b^2)d^6} + \frac{315b\sqrt{x} \text{PolyLog}\left(7, -\frac{(a^2+b^2)e^{2i(c+d\sqrt{x})}}{(a+ib)^2}\right)}{2(a^2+b^2)d^7} + \frac{315ib \text{PolyLog}\left(8, -\frac{(a^2+b^2)e^{2i(c+d\sqrt{x})}}{(a+ib)^2}\right)}{4(a^2+b^2)d^8}$$

```
[Out] 1/4*x^4/(a+I*b)+2*b*x^(7/2)*ln(1+(a^2+b^2)*exp(2*I*(c+d*x^(1/2)))/(a+I*b)^2)/(a^2+b^2)/d-7*I*b*x^3*polylog(2,-(a^2+b^2)*exp(2*I*(c+d*x^(1/2)))/(a+I*b)^2)/(a^2+b^2)/d^2+21*b*x^(5/2)*polylog(3,-(a^2+b^2)*exp(2*I*(c+d*x^(1/2)))/
```

$$\begin{aligned} & (a+I*b)^2/(a^2+b^2)/d^3+105/2*I*b*x^2*polylog(4,-(a^2+b^2)*exp(2*I*(c+d*x^ \\ & (1/2)))/(a+I*b)^2)/(a^2+b^2)/d^4-105*b*x^(3/2)*polylog(5,-(a^2+b^2)*exp(2*I \\ & *(c+d*x^(1/2)))/(a+I*b)^2)/(a^2+b^2)/d^5-315/2*I*b*x*polylog(6,-(a^2+b^2)*e \\ & xp(2*I*(c+d*x^(1/2)))/(a+I*b)^2)/(a^2+b^2)/d^6+315/4*I*b*polylog(8,-(a^2+b^ \\ & 2)*exp(2*I*(c+d*x^(1/2)))/(a+I*b)^2)/(a^2+b^2)/d^8+315/2*b*polylog(7,-(a^2+ \\ & b^2)*exp(2*I*(c+d*x^(1/2)))/(a+I*b)^2)*x^(1/2)/(a^2+b^2)/d^7 \end{aligned}$$

Rubi [A] (verified)

Time = 0.65 (sec) , antiderivative size = 460, normalized size of antiderivative = 1.00, number of steps used = 11, number of rules used = 7, $\frac{\text{number of rules}}{\text{integrand size}} = 0.350$, Rules used = {3832, 3813, 2221, 2611, 6744, 2320, 6724}

$$\begin{aligned} \int \frac{x^3}{a + b \tan(c + d\sqrt{x})} dx = & \frac{315ib \operatorname{PolyLog}\left(8, -\frac{(a^2+b^2)e^{2i(c+d\sqrt{x})}}{(a+ib)^2}\right)}{4d^8(a^2+b^2)} \\ & + \frac{315b\sqrt{x} \operatorname{PolyLog}\left(7, -\frac{(a^2+b^2)e^{2i(c+d\sqrt{x})}}{(a+ib)^2}\right)}{2d^7(a^2+b^2)} \\ & - \frac{315ibx \operatorname{PolyLog}\left(6, -\frac{(a^2+b^2)e^{2i(c+d\sqrt{x})}}{(a+ib)^2}\right)}{2d^6(a^2+b^2)} \\ & - \frac{105bx^{3/2} \operatorname{PolyLog}\left(5, -\frac{(a^2+b^2)e^{2i(c+d\sqrt{x})}}{(a+ib)^2}\right)}{d^5(a^2+b^2)} \\ & + \frac{105ibx^2 \operatorname{PolyLog}\left(4, -\frac{(a^2+b^2)e^{2i(c+d\sqrt{x})}}{(a+ib)^2}\right)}{2d^4(a^2+b^2)} \\ & + \frac{21bx^{5/2} \operatorname{PolyLog}\left(3, -\frac{(a^2+b^2)e^{2i(c+d\sqrt{x})}}{(a+ib)^2}\right)}{d^3(a^2+b^2)} \\ & - \frac{7ibx^3 \operatorname{PolyLog}\left(2, -\frac{(a^2+b^2)e^{2i(c+d\sqrt{x})}}{(a+ib)^2}\right)}{d^2(a^2+b^2)} \\ & + \frac{2bx^{7/2} \log\left(1 + \frac{(a^2+b^2)e^{2i(c+d\sqrt{x})}}{(a+ib)^2}\right)}{d(a^2+b^2)} + \frac{x^4}{4(a+ib)} \end{aligned}$$

[In] Int[x^3/(a + b*Tan[c + d*Sqrt[x]]),x]

[Out] $x^4/(4*(a + I*b)) + (2*b*x^(7/2)*Log[1 + ((a^2 + b^2)*E^((2*I)*(c + d*Sqrt[x])))]/(a + I*b)^2)/((a^2 + b^2)*d) - ((7*I)*b*x^3*PolyLog[2, -(((a^2 + b^2)*E^((2*I)*(c + d*Sqrt[x])))/(a + I*b)^2)]/((a^2 + b^2)*d^2) + (21*b*x^(5/2)*PolyLog[3, -(((a^2 + b^2)*E^((2*I)*(c + d*Sqrt[x])))/(a + I*b)^2)]/((a^2 + b^2)*d^3) + (((105*I)/2)*b*x^2*PolyLog[4, -(((a^2 + b^2)*E^((2*I)*(c + d*Sqrt[x])))/(a + I*b)^2)]/((a^2 + b^2)*d^4) - (105*b*x^(3/2)*PolyLog[5, -$

$$\frac{((a^2 + b^2)E^{((2I)(c + d\sqrt{x}))})/(a + I*b)^2)}{(a^2 + b^2)d^5} - \frac{(((315I)/2)*b*x*PolyLog[6, -((a^2 + b^2)E^{((2I)(c + d\sqrt{x}))})/(a + I*b)^2])}{(a^2 + b^2)d^6} + \frac{(315*b*\sqrt{x}*PolyLog[7, -((a^2 + b^2)E^{((2I)(c + d\sqrt{x}))})/(a + I*b)^2])}{(2*(a^2 + b^2)d^7)} + \frac{(((315I)/4)*b*PolyLog[8, -((a^2 + b^2)E^{((2I)(c + d\sqrt{x}))})/(a + I*b)^2])}{(a^2 + b^2)d^8}$$

Rule 2221

```
Int[(((F_)^((g_)*((e_) + (f_)*(x_))))^(n_)*((c_) + (d_)*(x_))^(m_))/
((a_) + (b_)*((F_)^((g_)*((e_) + (f_)*(x_))))^(n_)), x_Symbol] := Simp
[((c + d*x)^m/(b*f*g*n*Log[F]))*Log[1 + b*((F^(g*(e + f*x)))^n/a)], x] - Di
st[d*(m/(b*f*g*n*Log[F])), Int[(c + d*x)^(m - 1)*Log[1 + b*((F^(g*(e + f*x)
))^n/a)], x], x] /; FreeQ[{F, a, b, c, d, e, f, g, n}, x] && IGtQ[m, 0]
```

Rule 2320

```
Int[u_, x_Symbol] := With[{v = FunctionOfExponential[u, x]}, Dist[v/D[v, x]
, Subst[Int[FunctionOfExponentialFunction[u, x]/x, x], x, v], x] /; Functi
onOfExponentialQ[u, x] && !MatchQ[u, (w_)*((a_)*(v_)^(n_))^(m_)] /; FreeQ[
{a, m, n}, x] && IntegerQ[m*n] && !MatchQ[u, E^((c_)*((a_) + (b_)*x))*
(F_) [v_] /; FreeQ[{a, b, c}, x] && InverseFunctionQ[F[x]]]
```

Rule 2611

```
Int[Log[1 + (e_)*((F_)^((c_)*((a_) + (b_)*(x_))))^(n_)]*((f_) + (g_)
*(x_))^(m_), x_Symbol] := Simp[(-f + g*x)^m*(PolyLog[2, (-e)*(F^(c*(a +
b*x)))^n]/(b*c*n*Log[F])), x] + Dist[g*(m/(b*c*n*Log[F])), Int[(f + g*x)^(m
- 1)*PolyLog[2, (-e)*(F^(c*(a + b*x)))^n], x], x] /; FreeQ[{F, a, b, c, e,
f, g, n}, x] && GtQ[m, 0]
```

Rule 3813

```
Int[(((c_) + (d_)*(x_))^(m_))/((a_) + (b_)*tan[(e_) + (f_)*(x_)]), x_Sy
mbol] := Simp[(c + d*x)^(m + 1)/(d*(m + 1)*(a + I*b)), x] + Dist[2*I*b, Int
[(c + d*x)^m*(E^Simp[2*I*(e + f*x), x])/((a + I*b)^2 + (a^2 + b^2)*E^Simp[2*
I*(e + f*x), x])], x], x] /; FreeQ[{a, b, c, d, e, f}, x] && NeQ[a^2 + b^2,
0] && IGtQ[m, 0]
```

Rule 3832

```
Int[(x_)^(m_)*((a_) + (b_)*Tan[(c_) + (d_)*(x_)^(n_)])^(p_), x_Symbol
] := Dist[1/n, Subst[Int[x^(Simplify[(m + 1)/n] - 1)*(a + b*Tan[c + d*x])^p
, x], x, x^n], x] /; FreeQ[{a, b, c, d, m, n, p}, x] && IGtQ[Simplify[(m +
1)/n], 0] && IntegerQ[p]
```

Rule 6724

Int[PolyLog[n_, (c_.)*((a_.) + (b_.)*(x_))^(p_.)]/((d_.) + (e_.)*(x_)), x_Symbol] :> Simp[PolyLog[n + 1, c*(a + b*x)^p]/(e*p), x] /; FreeQ[{a, b, c, d, e, n, p}, x] && EqQ[b*d, a*e]

Rule 6744

Int[((e_.) + (f_.)*(x_))^(m_.)*PolyLog[n_, (d_.)*((F_)^((c_.)*((a_.) + (b_.)*(x_))))^(p_.)], x_Symbol] :> Simp[(e + f*x)^m*(PolyLog[n + 1, d*(F^(c*(a + b*x)))^p]/(b*c*p*Log[F])), x] - Dist[f*(m/(b*c*p*Log[F])), Int[(e + f*x)^(m - 1)*PolyLog[n + 1, d*(F^(c*(a + b*x)))^p], x], x] /; FreeQ[{F, a, b, c, d, e, f, n, p}, x] && GtQ[m, 0]

Rubi steps

$$\begin{aligned}
 \text{integral} &= 2\text{Subst}\left(\int \frac{x^7}{a + b \tan(c + dx)} dx, x, \sqrt{x}\right) \\
 &= \frac{x^4}{4(a + ib)} + (4ib)\text{Subst}\left(\int \frac{e^{2i(c+dx)} x^7}{(a + ib)^2 + (a^2 + b^2) e^{2i(c+dx)}} dx, x, \sqrt{x}\right) \\
 &= \frac{x^4}{4(a + ib)} + \frac{2bx^{7/2} \log\left(1 + \frac{(a^2+b^2)e^{2i(c+d\sqrt{x})}}{(a+ib)^2}\right)}{(a^2 + b^2) d} \\
 &\quad - \frac{(14b)\text{Subst}\left(\int x^6 \log\left(1 + \frac{(a^2+b^2)e^{2i(c+dx)}}{(a+ib)^2}\right) dx, x, \sqrt{x}\right)}{(a^2 + b^2) d} \\
 &= \frac{x^4}{4(a + ib)} + \frac{2bx^{7/2} \log\left(1 + \frac{(a^2+b^2)e^{2i(c+d\sqrt{x})}}{(a+ib)^2}\right)}{(a^2 + b^2) d} - \frac{7ibx^3 \text{PolyLog}\left(2, -\frac{(a^2+b^2)e^{2i(c+d\sqrt{x})}}{(a+ib)^2}\right)}{(a^2 + b^2) d^2} \\
 &\quad + \frac{(42ib)\text{Subst}\left(\int x^5 \text{PolyLog}\left(2, -\frac{(a^2+b^2)e^{2i(c+dx)}}{(a+ib)^2}\right) dx, x, \sqrt{x}\right)}{(a^2 + b^2) d^2} \\
 &= \frac{x^4}{4(a + ib)} + \frac{2bx^{7/2} \log\left(1 + \frac{(a^2+b^2)e^{2i(c+d\sqrt{x})}}{(a+ib)^2}\right)}{(a^2 + b^2) d} \\
 &\quad - \frac{7ibx^3 \text{PolyLog}\left(2, -\frac{(a^2+b^2)e^{2i(c+d\sqrt{x})}}{(a+ib)^2}\right)}{(a^2 + b^2) d^2} + \frac{21bx^{5/2} \text{PolyLog}\left(3, -\frac{(a^2+b^2)e^{2i(c+d\sqrt{x})}}{(a+ib)^2}\right)}{(a^2 + b^2) d^3} \\
 &\quad - \frac{(105b)\text{Subst}\left(\int x^4 \text{PolyLog}\left(3, -\frac{(a^2+b^2)e^{2i(c+dx)}}{(a+ib)^2}\right) dx, x, \sqrt{x}\right)}{(a^2 + b^2) d^3}
 \end{aligned}$$

$$\begin{aligned}
&= \frac{x^4}{4(a+ib)} + \frac{2bx^{7/2} \log\left(1 + \frac{(a^2+b^2)e^{2i(c+d\sqrt{x})}}{(a+ib)^2}\right)}{(a^2+b^2)d} - \frac{7ibx^3 \operatorname{PolyLog}\left(2, -\frac{(a^2+b^2)e^{2i(c+d\sqrt{x})}}{(a+ib)^2}\right)}{(a^2+b^2)d^2} \\
&\quad + \frac{21bx^{5/2} \operatorname{PolyLog}\left(3, -\frac{(a^2+b^2)e^{2i(c+d\sqrt{x})}}{(a+ib)^2}\right)}{(a^2+b^2)d^3} + \frac{105ibx^2 \operatorname{PolyLog}\left(4, -\frac{(a^2+b^2)e^{2i(c+d\sqrt{x})}}{(a+ib)^2}\right)}{2(a^2+b^2)d^4} \\
&\quad - \frac{(210ib) \operatorname{Subst}\left(\int x^3 \operatorname{PolyLog}\left(4, -\frac{(a^2+b^2)e^{2i(c+dx)}}{(a+ib)^2}\right) dx, x, \sqrt{x}\right)}{(a^2+b^2)d^4} \\
&= \frac{x^4}{4(a+ib)} + \frac{2bx^{7/2} \log\left(1 + \frac{(a^2+b^2)e^{2i(c+d\sqrt{x})}}{(a+ib)^2}\right)}{(a^2+b^2)d} - \frac{7ibx^3 \operatorname{PolyLog}\left(2, -\frac{(a^2+b^2)e^{2i(c+d\sqrt{x})}}{(a+ib)^2}\right)}{(a^2+b^2)d^2} \\
&\quad + \frac{21bx^{5/2} \operatorname{PolyLog}\left(3, -\frac{(a^2+b^2)e^{2i(c+d\sqrt{x})}}{(a+ib)^2}\right)}{(a^2+b^2)d^3} + \frac{105ibx^2 \operatorname{PolyLog}\left(4, -\frac{(a^2+b^2)e^{2i(c+d\sqrt{x})}}{(a+ib)^2}\right)}{2(a^2+b^2)d^4} \\
&\quad - \frac{105bx^{3/2} \operatorname{PolyLog}\left(5, -\frac{(a^2+b^2)e^{2i(c+d\sqrt{x})}}{(a+ib)^2}\right)}{(a^2+b^2)d^5} \\
&\quad + \frac{(315b) \operatorname{Subst}\left(\int x^2 \operatorname{PolyLog}\left(5, -\frac{(a^2+b^2)e^{2i(c+dx)}}{(a+ib)^2}\right) dx, x, \sqrt{x}\right)}{(a^2+b^2)d^5} \\
&= \frac{x^4}{4(a+ib)} + \frac{2bx^{7/2} \log\left(1 + \frac{(a^2+b^2)e^{2i(c+d\sqrt{x})}}{(a+ib)^2}\right)}{(a^2+b^2)d} - \frac{7ibx^3 \operatorname{PolyLog}\left(2, -\frac{(a^2+b^2)e^{2i(c+d\sqrt{x})}}{(a+ib)^2}\right)}{(a^2+b^2)d^2} \\
&\quad + \frac{21bx^{5/2} \operatorname{PolyLog}\left(3, -\frac{(a^2+b^2)e^{2i(c+d\sqrt{x})}}{(a+ib)^2}\right)}{(a^2+b^2)d^3} + \frac{105ibx^2 \operatorname{PolyLog}\left(4, -\frac{(a^2+b^2)e^{2i(c+d\sqrt{x})}}{(a+ib)^2}\right)}{2(a^2+b^2)d^4} \\
&\quad - \frac{105bx^{3/2} \operatorname{PolyLog}\left(5, -\frac{(a^2+b^2)e^{2i(c+d\sqrt{x})}}{(a+ib)^2}\right)}{(a^2+b^2)d^5} - \frac{315ibx \operatorname{PolyLog}\left(6, -\frac{(a^2+b^2)e^{2i(c+d\sqrt{x})}}{(a+ib)^2}\right)}{2(a^2+b^2)d^6} \\
&\quad + \frac{(315ib) \operatorname{Subst}\left(\int x \operatorname{PolyLog}\left(6, -\frac{(a^2+b^2)e^{2i(c+dx)}}{(a+ib)^2}\right) dx, x, \sqrt{x}\right)}{(a^2+b^2)d^6}
\end{aligned}$$

$$\begin{aligned}
&= \frac{x^4}{4(a+ib)} + \frac{2bx^{7/2} \log\left(1 + \frac{(a^2+b^2)e^{2i(c+d\sqrt{x})}}{(a+ib)^2}\right)}{(a^2+b^2)d} - \frac{7ibx^3 \text{PolyLog}\left(2, -\frac{(a^2+b^2)e^{2i(c+d\sqrt{x})}}{(a+ib)^2}\right)}{(a^2+b^2)d^2} \\
&+ \frac{21bx^{5/2} \text{PolyLog}\left(3, -\frac{(a^2+b^2)e^{2i(c+d\sqrt{x})}}{(a+ib)^2}\right)}{(a^2+b^2)d^3} + \frac{105ibx^2 \text{PolyLog}\left(4, -\frac{(a^2+b^2)e^{2i(c+d\sqrt{x})}}{(a+ib)^2}\right)}{2(a^2+b^2)d^4} \\
&- \frac{105bx^{3/2} \text{PolyLog}\left(5, -\frac{(a^2+b^2)e^{2i(c+d\sqrt{x})}}{(a+ib)^2}\right)}{(a^2+b^2)d^5} \\
&- \frac{315ibx \text{PolyLog}\left(6, -\frac{(a^2+b^2)e^{2i(c+d\sqrt{x})}}{(a+ib)^2}\right)}{2(a^2+b^2)d^6} + \frac{315b\sqrt{x} \text{PolyLog}\left(7, -\frac{(a^2+b^2)e^{2i(c+d\sqrt{x})}}{(a+ib)^2}\right)}{2(a^2+b^2)d^7} \\
&- \frac{(315b)\text{Subst}\left(\int \text{PolyLog}\left(7, -\frac{(a^2+b^2)e^{2i(c+dx)}}{(a+ib)^2}\right) dx, x, \sqrt{x}\right)}{2(a^2+b^2)d^7} \\
&= \frac{x^4}{4(a+ib)} + \frac{2bx^{7/2} \log\left(1 + \frac{(a^2+b^2)e^{2i(c+d\sqrt{x})}}{(a+ib)^2}\right)}{(a^2+b^2)d} - \frac{7ibx^3 \text{PolyLog}\left(2, -\frac{(a^2+b^2)e^{2i(c+d\sqrt{x})}}{(a+ib)^2}\right)}{(a^2+b^2)d^2} \\
&+ \frac{21bx^{5/2} \text{PolyLog}\left(3, -\frac{(a^2+b^2)e^{2i(c+d\sqrt{x})}}{(a+ib)^2}\right)}{(a^2+b^2)d^3} + \frac{105ibx^2 \text{PolyLog}\left(4, -\frac{(a^2+b^2)e^{2i(c+d\sqrt{x})}}{(a+ib)^2}\right)}{2(a^2+b^2)d^4} \\
&- \frac{105bx^{3/2} \text{PolyLog}\left(5, -\frac{(a^2+b^2)e^{2i(c+d\sqrt{x})}}{(a+ib)^2}\right)}{(a^2+b^2)d^5} \\
&- \frac{315ibx \text{PolyLog}\left(6, -\frac{(a^2+b^2)e^{2i(c+d\sqrt{x})}}{(a+ib)^2}\right)}{2(a^2+b^2)d^6} + \frac{315b\sqrt{x} \text{PolyLog}\left(7, -\frac{(a^2+b^2)e^{2i(c+d\sqrt{x})}}{(a+ib)^2}\right)}{2(a^2+b^2)d^7} \\
&+ \frac{(315ib)\text{Subst}\left(\int \frac{\text{PolyLog}\left(7, -\frac{(a^2+b^2)x}{(a+ib)^2}\right)}{x} dx, x, e^{2i(c+d\sqrt{x})}\right)}{4(a^2+b^2)d^8} \\
&= \frac{x^4}{4(a+ib)} + \frac{2bx^{7/2} \log\left(1 + \frac{(a^2+b^2)e^{2i(c+d\sqrt{x})}}{(a+ib)^2}\right)}{(a^2+b^2)d} - \frac{7ibx^3 \text{PolyLog}\left(2, -\frac{(a^2+b^2)e^{2i(c+d\sqrt{x})}}{(a+ib)^2}\right)}{(a^2+b^2)d^2} \\
&+ \frac{21bx^{5/2} \text{PolyLog}\left(3, -\frac{(a^2+b^2)e^{2i(c+d\sqrt{x})}}{(a+ib)^2}\right)}{(a^2+b^2)d^3} + \frac{105ibx^2 \text{PolyLog}\left(4, -\frac{(a^2+b^2)e^{2i(c+d\sqrt{x})}}{(a+ib)^2}\right)}{2(a^2+b^2)d^4} \\
&- \frac{105bx^{3/2} \text{PolyLog}\left(5, -\frac{(a^2+b^2)e^{2i(c+d\sqrt{x})}}{(a+ib)^2}\right)}{(a^2+b^2)d^5} - \frac{315ibx \text{PolyLog}\left(6, -\frac{(a^2+b^2)e^{2i(c+d\sqrt{x})}}{(a+ib)^2}\right)}{2(a^2+b^2)d^6} \\
&+ \frac{315b\sqrt{x} \text{PolyLog}\left(7, -\frac{(a^2+b^2)e^{2i(c+d\sqrt{x})}}{(a+ib)^2}\right)}{2(a^2+b^2)d^7} + \frac{315ib \text{PolyLog}\left(8, -\frac{(a^2+b^2)e^{2i(c+d\sqrt{x})}}{(a+ib)^2}\right)}{4(a^2+b^2)d^8}
\end{aligned}$$

Mathematica [A] (verified)

Time = 1.50 (sec) , antiderivative size = 401, normalized size of antiderivative = 0.87

$$\int \frac{x^3}{a + b \tan(c + d\sqrt{x})} dx$$

$$= \frac{ad^8 x^4 + ibd^8 x^4 + 8bd^7 x^{7/2} \log\left(1 + \frac{(a+ib)e^{-2i(c+d\sqrt{x})}}{a-ib}\right) + 28ibd^6 x^3 \operatorname{PolyLog}\left(2, \frac{(-a-ib)e^{-2i(c+d\sqrt{x})}}{a-ib}\right) + 84bd^5 x^5/2}{}$$

[In] Integrate[x^3/(a + b*Tan[c + d*Sqrt[x]]),x]

[Out] (a*d^8*x^4 + I*b*d^8*x^4 + 8*b*d^7*x^(7/2)*Log[1 + (a + I*b)/((a - I*b)*E^((2*I)*(c + d*Sqrt[x])))] + (28*I)*b*d^6*x^3*PolyLog[2, (-a - I*b)/((a - I*b)*E^((2*I)*(c + d*Sqrt[x])))] + 84*b*d^5*x^(5/2)*PolyLog[3, (-a - I*b)/((a - I*b)*E^((2*I)*(c + d*Sqrt[x])))] - (210*I)*b*d^4*x^2*PolyLog[4, (-a - I*b)/((a - I*b)*E^((2*I)*(c + d*Sqrt[x])))] - 420*b*d^3*x^(3/2)*PolyLog[5, (-a - I*b)/((a - I*b)*E^((2*I)*(c + d*Sqrt[x])))] + (630*I)*b*d^2*x*PolyLog[6, (-a - I*b)/((a - I*b)*E^((2*I)*(c + d*Sqrt[x])))] + 630*b*d*Sqrt[x]*PolyLog[7, (-a - I*b)/((a - I*b)*E^((2*I)*(c + d*Sqrt[x])))] - (315*I)*b*PolyLog[8, (-a - I*b)/((a - I*b)*E^((2*I)*(c + d*Sqrt[x])))]/(4*(a^2 + b^2)*d^8)

Maple [F]

$$\int \frac{x^3}{a + b \tan(c + d\sqrt{x})} dx$$

[In] int(x^3/(a+b*tan(c+d*x^(1/2))),x)

[Out] int(x^3/(a+b*tan(c+d*x^(1/2))),x)

Fricas [F]

$$\int \frac{x^3}{a + b \tan(c + d\sqrt{x})} dx = \int \frac{x^3}{b \tan(d\sqrt{x} + c) + a} dx$$

[In] integrate(x^3/(a+b*tan(c+d*x^(1/2))),x, algorithm="fricas")

[Out] integral(x^3/(b*tan(d*sqrt(x) + c) + a), x)

SymPy [F]

$$\int \frac{x^3}{a + b \tan(c + d\sqrt{x})} dx = \int \frac{x^3}{a + b \tan(c + d\sqrt{x})} dx$$

```
[In] integrate(x**3/(a+b*tan(c+d*x**(1/2))),x)
```

```
[Out] Integral(x**3/(a + b*tan(c + d*sqrt(x))), x)
```

Maxima [B] (verification not implemented)

Both result and optimal contain complex but leaf count of result is larger than twice the leaf count of optimal. 1133 vs. $2(383) = 766$.

Time = 0.59 (sec) , antiderivative size = 1133, normalized size of antiderivative = 2.46

$$\int \frac{x^3}{a + b \tan(c + d\sqrt{x})} dx = \text{Too large to display}$$

```
[In] integrate(x^3/(a+b*tan(c+d*x^(1/2))),x, algorithm="maxima")
```

```
[Out] -1/420*(420*(2*(d*sqrt(x) + c)*a/(a^2 + b^2) + 2*b*log(b*tan(d*sqrt(x) + c) + a)/(a^2 + b^2) - b*log(tan(d*sqrt(x) + c)^2 + 1)/(a^2 + b^2))*c^7 - (105*(d*sqrt(x) + c)^8*(a - I*b) - 840*(d*sqrt(x) + c)^7*(a - I*b)*c + 2940*(d*sqrt(x) + c)^6*(a - I*b)*c^2 - 5880*(d*sqrt(x) + c)^5*(a - I*b)*c^3 + 7350*(d*sqrt(x) + c)^4*(a - I*b)*c^4 - 5880*(d*sqrt(x) + c)^3*(a - I*b)*c^5 + 2940*(d*sqrt(x) + c)^2*(a - I*b)*c^6 - 8*(960*I*(d*sqrt(x) + c)^7*b - 3920*I*(d*sqrt(x) + c)^6*b*c + 7056*I*(d*sqrt(x) + c)^5*b*c^2 - 7350*I*(d*sqrt(x) + c)^4*b*c^3 + 4900*I*(d*sqrt(x) + c)^3*b*c^4 - 2205*I*(d*sqrt(x) + c)^2*b*c^5 + 735*I*(d*sqrt(x) + c)*b*c^6)*arctan2((2*a*b*cos(2*d*sqrt(x) + 2*c) - (a^2 - b^2)*sin(2*d*sqrt(x) + 2*c))/(a^2 + b^2), (2*a*b*sin(2*d*sqrt(x) + 2*c) + a^2 + b^2 + (a^2 - b^2)*cos(2*d*sqrt(x) + 2*c))/(a^2 + b^2)) - 420*(64*I*(d*sqrt(x) + c)^6*b - 224*I*(d*sqrt(x) + c)^5*b*c + 336*I*(d*sqrt(x) + c)^4*b*c^2 - 280*I*(d*sqrt(x) + c)^3*b*c^3 + 140*I*(d*sqrt(x) + c)^2*b*c^4 - 42*I*(d*sqrt(x) + c)*b*c^5 + 7*I*b*c^6)*dilog((I*a + b)*e^(2*I*d*sqrt(x) + 2*I*c)/(-I*a + b)) + 4*(960*(d*sqrt(x) + c)^7*b - 3920*(d*sqrt(x) + c)^6*b*c + 7056*(d*sqrt(x) + c)^5*b*c^2 - 7350*(d*sqrt(x) + c)^4*b*c^3 + 4900*(d*sqrt(x) + c)^3*b*c^4 - 2205*(d*sqrt(x) + c)^2*b*c^5 + 735*(d*sqrt(x) + c)*b*c^6)*log(((a^2 + b^2)*cos(2*d*sqrt(x) + 2*c)^2 + 4*a*b*sin(2*d*sqrt(x) + 2*c) + (a^2 + b^2)*sin(2*d*sqrt(x) + 2*c)^2 + a^2 + b^2 + 2*(a^2 - b^2)*cos(2*d*sqrt(x) + 2*c))/(a^2 + b^2)) + 302400*I*b*polylog(8, (I*a + b)*e^(2*I*d*sqrt(x) + 2*I*c)/(-I*a + b)) + 50400*(12*(d*sqrt(x) + c)*b - 7*b*c)*polylog(7, (I*a + b)*e^(2*I*d*sqrt(x) + 2*I*c)/(-I*a + b)) - 10080*(60*I*(d*sqrt(x) + c)^2*b - 70*I*(d*sqrt(x) + c)*b*c + 21*I*b*c^2)*polylog(6, (I*a + b)*
```

$$e^{(2I*d*\sqrt{x} + 2I*c)/(-I*a + b)} - 2520*(160*(d*\sqrt{x} + c)^3*b - 280*(d*\sqrt{x} + c)^2*b*c + 168*(d*\sqrt{x} + c)*b*c^2 - 35*b*c^3)*\text{polylog}(5, (I*a + b)*e^{(2I*d*\sqrt{x} + 2I*c)/(-I*a + b)}) - 840*(-240*I*(d*\sqrt{x} + c)^4*b + 560*I*(d*\sqrt{x} + c)^3*b*c - 504*I*(d*\sqrt{x} + c)^2*b*c^2 + 210*I*(d*\sqrt{x} + c)*b*c^3 - 35*I*b*c^4)*\text{polylog}(4, (I*a + b)*e^{(2I*d*\sqrt{x} + 2I*c)/(-I*a + b)}) + 420*(192*(d*\sqrt{x} + c)^5*b - 560*(d*\sqrt{x} + c)^4*b*c + 672*(d*\sqrt{x} + c)^3*b*c^2 - 420*(d*\sqrt{x} + c)^2*b*c^3 + 140*(d*\sqrt{x} + c)*b*c^4 - 21*b*c^5)*\text{polylog}(3, (I*a + b)*e^{(2I*d*\sqrt{x} + 2I*c)/(-I*a + b)})/(a^2 + b^2))/d^8$$

Giac [F]

$$\int \frac{x^3}{a + b \tan(c + d\sqrt{x})} dx = \int \frac{x^3}{b \tan(d\sqrt{x} + c) + a} dx$$

[In] integrate(x^3/(a+b*tan(c+d*x^(1/2))),x, algorithm="giac")

[Out] integrate(x^3/(b*tan(d*sqrt(x) + c) + a), x)

Mupad [F(-1)]

Timed out.

$$\int \frac{x^3}{a + b \tan(c + d\sqrt{x})} dx = \int \frac{x^3}{a + b \tan(c + d\sqrt{x})} dx$$

[In] int(x^3/(a + b*tan(c + d*x^(1/2))),x)

[Out] int(x^3/(a + b*tan(c + d*x^(1/2))), x)

3.37 $\int \frac{x^2}{a+b \tan(c+d\sqrt{x})} dx$

Optimal result	216
Rubi [A] (verified)	217
Mathematica [A] (verified)	220
Maple [F]	221
Fricas [F]	221
Sympy [F]	221
Maxima [B] (verification not implemented)	222
Giac [F]	222
Mupad [F(-1)]	223

Optimal result

Integrand size = 20, antiderivative size = 344

$$\int \frac{x^2}{a+b \tan(c+d\sqrt{x})} dx = \frac{x^3}{3(a+ib)} + \frac{2bx^{5/2} \log\left(1 + \frac{(a^2+b^2)e^{2i(c+d\sqrt{x})}}{(a+ib)^2}\right)}{(a^2+b^2)d}$$

$$- \frac{5ibx^2 \operatorname{PolyLog}\left(2, -\frac{(a^2+b^2)e^{2i(c+d\sqrt{x})}}{(a+ib)^2}\right)}{(a^2+b^2)d^2}$$

$$+ \frac{10bx^{3/2} \operatorname{PolyLog}\left(3, -\frac{(a^2+b^2)e^{2i(c+d\sqrt{x})}}{(a+ib)^2}\right)}{(a^2+b^2)d^3}$$

$$+ \frac{15ibx \operatorname{PolyLog}\left(4, -\frac{(a^2+b^2)e^{2i(c+d\sqrt{x})}}{(a+ib)^2}\right)}{(a^2+b^2)d^4}$$

$$- \frac{15b\sqrt{x} \operatorname{PolyLog}\left(5, -\frac{(a^2+b^2)e^{2i(c+d\sqrt{x})}}{(a+ib)^2}\right)}{(a^2+b^2)d^5}$$

$$- \frac{15ib \operatorname{PolyLog}\left(6, -\frac{(a^2+b^2)e^{2i(c+d\sqrt{x})}}{(a+ib)^2}\right)}{2(a^2+b^2)d^6}$$

```
[Out] 1/3*x^3/(a+I*b)+2*b*x^(5/2)*ln(1+(a^2+b^2)*exp(2*I*(c+d*x^(1/2)))/(a+I*b)^2)/(a^2+b^2)/d-5*I*b*x^2*polylog(2,-(a^2+b^2)*exp(2*I*(c+d*x^(1/2)))/(a+I*b)^2)/(a^2+b^2)/d^2+10*b*x^(3/2)*polylog(3,-(a^2+b^2)*exp(2*I*(c+d*x^(1/2)))/(a+I*b)^2)/(a^2+b^2)/d^3+15*I*b*x*polylog(4,-(a^2+b^2)*exp(2*I*(c+d*x^(1/2)))/(a+I*b)^2)/(a^2+b^2)/d^4-15/2*I*b*polylog(6,-(a^2+b^2)*exp(2*I*(c+d*x^(1/2)))/(a+I*b)^2)/(a^2+b^2)/d^6-15*b*polylog(5,-(a^2+b^2)*exp(2*I*(c+d*x^(1/2)))/(a+I*b)^2)*x^(1/2)/(a^2+b^2)/d^5
```


Rubi [A] (verified)

Time = 0.51 (sec) , antiderivative size = 344, normalized size of antiderivative = 1.00, number of steps used = 9, number of rules used = 7, $\frac{\text{number of rules}}{\text{integrand size}} = 0.350$, Rules used = {3832, 3813, 2221, 2611, 6744, 2320, 6724}

$$\int \frac{x^2}{a + b \tan(c + d\sqrt{x})} dx = -\frac{15ib \operatorname{PolyLog}\left(6, -\frac{(a^2+b^2)e^{2i(c+d\sqrt{x})}}{(a+ib)^2}\right)}{2d^6(a^2+b^2)} - \frac{15b\sqrt{x} \operatorname{PolyLog}\left(5, -\frac{(a^2+b^2)e^{2i(c+d\sqrt{x})}}{(a+ib)^2}\right)}{d^5(a^2+b^2)} + \frac{15ibx \operatorname{PolyLog}\left(4, -\frac{(a^2+b^2)e^{2i(c+d\sqrt{x})}}{(a+ib)^2}\right)}{d^4(a^2+b^2)} + \frac{10bx^{3/2} \operatorname{PolyLog}\left(3, -\frac{(a^2+b^2)e^{2i(c+d\sqrt{x})}}{(a+ib)^2}\right)}{d^3(a^2+b^2)} - \frac{5ibx^2 \operatorname{PolyLog}\left(2, -\frac{(a^2+b^2)e^{2i(c+d\sqrt{x})}}{(a+ib)^2}\right)}{d^2(a^2+b^2)} + \frac{2bx^{5/2} \log\left(1 + \frac{(a^2+b^2)e^{2i(c+d\sqrt{x})}}{(a+ib)^2}\right)}{d(a^2+b^2)} + \frac{x^3}{3(a+ib)}$$

[In] Int[x^2/(a + b*Tan[c + d*Sqrt[x]]),x]

[Out] x^3/(3*(a + I*b)) + (2*b*x^(5/2)*Log[1 + ((a^2 + b^2)*E^((2*I)*(c + d*Sqrt[x])))/(a + I*b)^2])/((a^2 + b^2)*d) - ((5*I)*b*x^2*PolyLog[2, -((a^2 + b^2)*E^((2*I)*(c + d*Sqrt[x])))/(a + I*b)^2])/((a^2 + b^2)*d^2) + (10*b*x^(3/2)*PolyLog[3, -((a^2 + b^2)*E^((2*I)*(c + d*Sqrt[x])))/(a + I*b)^2])/((a^2 + b^2)*d^3) + ((15*I)*b*x*PolyLog[4, -((a^2 + b^2)*E^((2*I)*(c + d*Sqrt[x])))/(a + I*b)^2])/((a^2 + b^2)*d^4) - (15*b*Sqrt[x]*PolyLog[5, -((a^2 + b^2)*E^((2*I)*(c + d*Sqrt[x])))/(a + I*b)^2])/((a^2 + b^2)*d^5) - ((15*I)/2)*b*PolyLog[6, -((a^2 + b^2)*E^((2*I)*(c + d*Sqrt[x])))/(a + I*b)^2])/((a^2 + b^2)*d^6)

Rule 2221

Int[(((F_)^((g_)*(e_) + (f_)*(x_)))^(n_))*((c_) + (d_)*(x_))^(m_))/((a_) + (b_)*((F_)^((g_)*(e_) + (f_)*(x_)))^(n_)), x_Symbol] :> Simp[(((c + d*x)^m/(b*f*g*n*Log[F]))*Log[1 + b*((F^(g*(e + f*x)))^n/a)], x] - Dist[d*(m/(b*f*g*n*Log[F])), Int[(c + d*x)^(m - 1)*Log[1 + b*((F^(g*(e + f*x)))^n/a)], x], x] /; FreeQ[{F, a, b, c, d, e, f, g, n}, x] && IGtQ[m, 0]

Rule 2320

```
Int[u_, x_Symbol] := With[{v = FunctionOfExponential[u, x]}, Dist[v/D[v, x]
, Subst[Int[FunctionOfExponentialFunction[u, x]/x, x], x, v], x]] /; Functi
onOfExponentialQ[u, x] && !MatchQ[u, (w_)*((a_.)*(v_)^(n_))^(m_)] /; FreeQ[
{a, m, n}, x] && IntegerQ[m*n] && !MatchQ[u, E^((c_.)*((a_.) + (b_.)*x))*
(F_) [v_] /; FreeQ[{a, b, c}, x] && InverseFunctionQ[F[x]]]
```

Rule 2611

```
Int[Log[1 + (e_.)*((F_)^((c_.)*((a_.) + (b_.)*(x_))))^(n_.)]*((f_.) + (g_.)
*(x_))^(m_.), x_Symbol] := Simp[(-f + g*x)^m*(PolyLog[2, (-e)*(F^(c*(a +
b*x)))^n]/(b*c*n*Log[F])), x] + Dist[g*(m/(b*c*n*Log[F])), Int[(f + g*x)^(m
- 1)*PolyLog[2, (-e)*(F^(c*(a + b*x)))^n], x], x] /; FreeQ[{F, a, b, c, e,
f, g, n}, x] && GtQ[m, 0]
```

Rule 3813

```
Int[((c_.) + (d_.)*(x_))^(m_.)/((a_.) + (b_.)*tan[(e_.) + (f_.)*(x_)]), x_Sy
mbol] := Simp[(c + d*x)^(m + 1)/(d*(m + 1)*(a + I*b)), x] + Dist[2*I*b, Int
[(c + d*x)^m*(E^Simp[2*I*(e + f*x), x]/((a + I*b)^2 + (a^2 + b^2)*E^Simp[2*
I*(e + f*x), x])), x], x] /; FreeQ[{a, b, c, d, e, f}, x] && NeQ[a^2 + b^2,
0] && IGtQ[m, 0]
```

Rule 3832

```
Int[(x_)^(m_.)*((a_.) + (b_.)*Tan[(c_.) + (d_.)*(x_)^(n_)])^(p_.), x_Symbol
] := Dist[1/n, Subst[Int[x^(Simplify[(m + 1)/n] - 1)*(a + b*Tan[c + d*x])^p
, x], x, x^n], x] /; FreeQ[{a, b, c, d, m, n, p}, x] && IGtQ[Simplify[(m +
1)/n], 0] && IntegerQ[p]
```

Rule 6724

```
Int[PolyLog[n_, (c_.)*((a_.) + (b_.)*(x_))^(p_.)]/((d_.) + (e_.)*(x_)), x_S
ymbol] := Simp[PolyLog[n + 1, c*(a + b*x)^p]/(e*p), x] /; FreeQ[{a, b, c, d
, e, n, p}, x] && EqQ[b*d, a*e]
```

Rule 6744

```
Int[((e_.) + (f_.)*(x_))^(m_.)*PolyLog[n_, (d_.)*((F_)^((c_.)*((a_.) + (b_.)
*(x_)))]^(p_.), x_Symbol] := Simp[(e + f*x)^m*(PolyLog[n + 1, d*(F^(c*(a
+ b*x)))^p]/(b*c*p*Log[F])), x] - Dist[f*(m/(b*c*p*Log[F])), Int[(e + f*x)^(
m - 1)*PolyLog[n + 1, d*(F^(c*(a + b*x)))^p], x], x] /; FreeQ[{F, a, b, c,
d, e, f, n, p}, x] && GtQ[m, 0]
```

Rubi steps

$$\begin{aligned}
\text{integral} &= 2\text{Subst}\left(\int \frac{x^5}{a + b \tan(c + dx)} dx, x, \sqrt{x}\right) \\
&= \frac{x^3}{3(a + ib)} + (4ib)\text{Subst}\left(\int \frac{e^{2i(c+dx)}x^5}{(a + ib)^2 + (a^2 + b^2)e^{2i(c+dx)}} dx, x, \sqrt{x}\right) \\
&= \frac{x^3}{3(a + ib)} + \frac{2bx^{5/2} \log\left(1 + \frac{(a^2+b^2)e^{2i(c+d\sqrt{x})}}{(a+ib)^2}\right)}{(a^2 + b^2) d} \\
&\quad - \frac{(10b)\text{Subst}\left(\int x^4 \log\left(1 + \frac{(a^2+b^2)e^{2i(c+dx)}}{(a+ib)^2}\right) dx, x, \sqrt{x}\right)}{(a^2 + b^2) d} \\
&= \frac{x^3}{3(a + ib)} + \frac{2bx^{5/2} \log\left(1 + \frac{(a^2+b^2)e^{2i(c+d\sqrt{x})}}{(a+ib)^2}\right)}{(a^2 + b^2) d} - \frac{5ibx^2 \text{PolyLog}\left(2, -\frac{(a^2+b^2)e^{2i(c+d\sqrt{x})}}{(a+ib)^2}\right)}{(a^2 + b^2) d^2} \\
&\quad + \frac{(20ib)\text{Subst}\left(\int x^3 \text{PolyLog}\left(2, -\frac{(a^2+b^2)e^{2i(c+dx)}}{(a+ib)^2}\right) dx, x, \sqrt{x}\right)}{(a^2 + b^2) d^2} \\
&= \frac{x^3}{3(a + ib)} + \frac{2bx^{5/2} \log\left(1 + \frac{(a^2+b^2)e^{2i(c+d\sqrt{x})}}{(a+ib)^2}\right)}{(a^2 + b^2) d} \\
&\quad - \frac{5ibx^2 \text{PolyLog}\left(2, -\frac{(a^2+b^2)e^{2i(c+d\sqrt{x})}}{(a+ib)^2}\right)}{(a^2 + b^2) d^2} + \frac{10bx^{3/2} \text{PolyLog}\left(3, -\frac{(a^2+b^2)e^{2i(c+d\sqrt{x})}}{(a+ib)^2}\right)}{(a^2 + b^2) d^3} \\
&\quad - \frac{(30b)\text{Subst}\left(\int x^2 \text{PolyLog}\left(3, -\frac{(a^2+b^2)e^{2i(c+dx)}}{(a+ib)^2}\right) dx, x, \sqrt{x}\right)}{(a^2 + b^2) d^3} \\
&= \frac{x^3}{3(a + ib)} + \frac{2bx^{5/2} \log\left(1 + \frac{(a^2+b^2)e^{2i(c+d\sqrt{x})}}{(a+ib)^2}\right)}{(a^2 + b^2) d} - \frac{5ibx^2 \text{PolyLog}\left(2, -\frac{(a^2+b^2)e^{2i(c+d\sqrt{x})}}{(a+ib)^2}\right)}{(a^2 + b^2) d^2} \\
&\quad + \frac{10bx^{3/2} \text{PolyLog}\left(3, -\frac{(a^2+b^2)e^{2i(c+d\sqrt{x})}}{(a+ib)^2}\right)}{(a^2 + b^2) d^3} + \frac{15ibx \text{PolyLog}\left(4, -\frac{(a^2+b^2)e^{2i(c+d\sqrt{x})}}{(a+ib)^2}\right)}{(a^2 + b^2) d^4} \\
&\quad - \frac{(30ib)\text{Subst}\left(\int x \text{PolyLog}\left(4, -\frac{(a^2+b^2)e^{2i(c+dx)}}{(a+ib)^2}\right) dx, x, \sqrt{x}\right)}{(a^2 + b^2) d^4}
\end{aligned}$$

$$\begin{aligned}
&= \frac{x^3}{3(a+ib)} + \frac{2bx^{5/2} \log\left(1 + \frac{(a^2+b^2)e^{2i(c+d\sqrt{x})}}{(a+ib)^2}\right)}{(a^2+b^2)d} \\
&\quad - \frac{5ibx^2 \operatorname{PolyLog}\left(2, -\frac{(a^2+b^2)e^{2i(c+d\sqrt{x})}}{(a+ib)^2}\right)}{(a^2+b^2)d^2} + \frac{10bx^{3/2} \operatorname{PolyLog}\left(3, -\frac{(a^2+b^2)e^{2i(c+d\sqrt{x})}}{(a+ib)^2}\right)}{(a^2+b^2)d^3} \\
&\quad + \frac{15ibx \operatorname{PolyLog}\left(4, -\frac{(a^2+b^2)e^{2i(c+d\sqrt{x})}}{(a+ib)^2}\right)}{(a^2+b^2)d^4} - \frac{15b\sqrt{x} \operatorname{PolyLog}\left(5, -\frac{(a^2+b^2)e^{2i(c+d\sqrt{x})}}{(a+ib)^2}\right)}{(a^2+b^2)d^5} \\
&\quad + \frac{(15b)\operatorname{Subst}\left(\int \operatorname{PolyLog}\left(5, -\frac{(a^2+b^2)e^{2i(c+d\sqrt{x})}}{(a+ib)^2}\right) dx, x, \sqrt{x}\right)}{(a^2+b^2)d^5} \\
&= \frac{x^3}{3(a+ib)} + \frac{2bx^{5/2} \log\left(1 + \frac{(a^2+b^2)e^{2i(c+d\sqrt{x})}}{(a+ib)^2}\right)}{(a^2+b^2)d} \\
&\quad - \frac{5ibx^2 \operatorname{PolyLog}\left(2, -\frac{(a^2+b^2)e^{2i(c+d\sqrt{x})}}{(a+ib)^2}\right)}{(a^2+b^2)d^2} + \frac{10bx^{3/2} \operatorname{PolyLog}\left(3, -\frac{(a^2+b^2)e^{2i(c+d\sqrt{x})}}{(a+ib)^2}\right)}{(a^2+b^2)d^3} \\
&\quad + \frac{15ibx \operatorname{PolyLog}\left(4, -\frac{(a^2+b^2)e^{2i(c+d\sqrt{x})}}{(a+ib)^2}\right)}{(a^2+b^2)d^4} - \frac{15b\sqrt{x} \operatorname{PolyLog}\left(5, -\frac{(a^2+b^2)e^{2i(c+d\sqrt{x})}}{(a+ib)^2}\right)}{(a^2+b^2)d^5} \\
&\quad - \frac{(15ib)\operatorname{Subst}\left(\int \frac{\operatorname{PolyLog}\left(5, -\frac{(a^2+b^2)x}{(a+ib)^2}\right)}{x} dx, x, e^{2i(c+d\sqrt{x})}\right)}{2(a^2+b^2)d^6} \\
&= \frac{x^3}{3(a+ib)} + \frac{2bx^{5/2} \log\left(1 + \frac{(a^2+b^2)e^{2i(c+d\sqrt{x})}}{(a+ib)^2}\right)}{(a^2+b^2)d} - \frac{5ibx^2 \operatorname{PolyLog}\left(2, -\frac{(a^2+b^2)e^{2i(c+d\sqrt{x})}}{(a+ib)^2}\right)}{(a^2+b^2)d^2} \\
&\quad + \frac{10bx^{3/2} \operatorname{PolyLog}\left(3, -\frac{(a^2+b^2)e^{2i(c+d\sqrt{x})}}{(a+ib)^2}\right)}{(a^2+b^2)d^3} + \frac{15ibx \operatorname{PolyLog}\left(4, -\frac{(a^2+b^2)e^{2i(c+d\sqrt{x})}}{(a+ib)^2}\right)}{(a^2+b^2)d^4} \\
&\quad - \frac{15b\sqrt{x} \operatorname{PolyLog}\left(5, -\frac{(a^2+b^2)e^{2i(c+d\sqrt{x})}}{(a+ib)^2}\right)}{(a^2+b^2)d^5} - \frac{15ib \operatorname{PolyLog}\left(6, -\frac{(a^2+b^2)e^{2i(c+d\sqrt{x})}}{(a+ib)^2}\right)}{2(a^2+b^2)d^6}
\end{aligned}$$

Mathematica [A] (verified)

Time = 1.16 (sec) , antiderivative size = 308, normalized size of antiderivative = 0.90

$$\begin{aligned}
&\int \frac{x^2}{a + b \tan(c + d\sqrt{x})} dx \\
&= \frac{2ad^6x^3 + 2ibd^6x^3 + 12bd^5x^{5/2} \log\left(1 + \frac{(a+ib)e^{-2i(c+d\sqrt{x})}}{a-ib}\right) + 30ibd^4x^2 \operatorname{PolyLog}\left(2, \frac{(-a-ib)e^{-2i(c+d\sqrt{x})}}{a-ib}\right) + 60bd^3x}{2(a^2+b^2)d^6}
\end{aligned}$$

[In] Integrate[x^2/(a + b*Tan[c + d*Sqrt[x]]),x]

[Out] $(2*a*d^6*x^3 + (2*I)*b*d^6*x^3 + 12*b*d^5*x^{(5/2)}*\text{Log}[1 + (a + I*b)/((a - I*b)*E^{((2*I)*(c + d*\text{Sqrt}[x])})])] + (30*I)*b*d^4*x^2*\text{PolyLog}[2, (-a - I*b)/((a - I*b)*E^{((2*I)*(c + d*\text{Sqrt}[x])})})] + 60*b*d^3*x^{(3/2)}*\text{PolyLog}[3, (-a - I*b)/((a - I*b)*E^{((2*I)*(c + d*\text{Sqrt}[x])})})] - (90*I)*b*d^2*x*\text{PolyLog}[4, (-a - I*b)/((a - I*b)*E^{((2*I)*(c + d*\text{Sqrt}[x])})})] - 90*b*d*\text{Sqrt}[x]*\text{PolyLog}[5, (-a - I*b)/((a - I*b)*E^{((2*I)*(c + d*\text{Sqrt}[x])})})] + (45*I)*b*\text{PolyLog}[6, (-a - I*b)/((a - I*b)*E^{((2*I)*(c + d*\text{Sqrt}[x])})})]/(6*(a^2 + b^2)*d^6)$

Maple [F]

$$\int \frac{x^2}{a + b \tan(c + d\sqrt{x})} dx$$

[In] int(x^2/(a+b*tan(c+d*x^(1/2))),x)

[Out] int(x^2/(a+b*tan(c+d*x^(1/2))),x)

Fricas [F]

$$\int \frac{x^2}{a + b \tan(c + d\sqrt{x})} dx = \int \frac{x^2}{b \tan(d\sqrt{x} + c) + a} dx$$

[In] integrate(x^2/(a+b*tan(c+d*x^(1/2))),x, algorithm="fricas")

[Out] integral(x^2/(b*tan(d*sqrt(x) + c) + a), x)

Sympy [F]

$$\int \frac{x^2}{a + b \tan(c + d\sqrt{x})} dx = \int \frac{x^2}{a + b \tan(c + d\sqrt{x})} dx$$

[In] integrate(x**2/(a+b*tan(c+d*x**(1/2))),x)

[Out] Integral(x**2/(a + b*tan(c + d*sqrt(x))), x)

Maxima [B] (verification not implemented)

Both result and optimal contain complex but leaf count of result is larger than twice the leaf count of optimal. 813 vs. $2(289) = 578$.

Time = 0.53 (sec) , antiderivative size = 813, normalized size of antiderivative = 2.36

$$\int \frac{x^2}{a + b \tan(c + d\sqrt{x})} dx = \text{Too large to display}$$

[In] integrate(x^2/(a+b*tan(c+d*x^(1/2))),x, algorithm="maxima")

[Out]
$$-1/15*(15*(2*(d*\text{sqrt}(x) + c)*a/(a^2 + b^2) + 2*b*\log(b*\text{tan}(d*\text{sqrt}(x) + c) + a)/(a^2 + b^2) - b*\log(\text{tan}(d*\text{sqrt}(x) + c)^2 + 1)/(a^2 + b^2))*c^5 - (5*(d*\text{sqrt}(x) + c)^6*(a - I*b) - 30*(d*\text{sqrt}(x) + c)^5*(a - I*b)*c + 75*(d*\text{sqrt}(x) + c)^4*(a - I*b)*c^2 - 100*(d*\text{sqrt}(x) + c)^3*(a - I*b)*c^3 + 75*(d*\text{sqrt}(x) + c)^2*(a - I*b)*c^4 - 2*(48*I*(d*\text{sqrt}(x) + c)^5*b - 150*I*(d*\text{sqrt}(x) + c)^4*b*c + 200*I*(d*\text{sqrt}(x) + c)^3*b*c^2 - 150*I*(d*\text{sqrt}(x) + c)^2*b*c^3 + 75*I*(d*\text{sqrt}(x) + c)*b*c^4)*\arctan2((2*a*b*\cos(2*d*\text{sqrt}(x) + 2*c) - (a^2 - b^2)*\sin(2*d*\text{sqrt}(x) + 2*c))/(a^2 + b^2), (2*a*b*\sin(2*d*\text{sqrt}(x) + 2*c) + a^2 + b^2 + (a^2 - b^2)*\cos(2*d*\text{sqrt}(x) + 2*c))/(a^2 + b^2)) - 15*(16*I*(d*\text{sqrt}(x) + c)^4*b - 40*I*(d*\text{sqrt}(x) + c)^3*b*c + 40*I*(d*\text{sqrt}(x) + c)^2*b*c^2 - 20*I*(d*\text{sqrt}(x) + c)*b*c^3 + 5*I*b*c^4)*\text{dilog}((I*a + b)*e^(2*I*d*\text{sqrt}(x) + 2*I*c)/(-I*a + b)) + (48*(d*\text{sqrt}(x) + c)^5*b - 150*(d*\text{sqrt}(x) + c)^4*b*c + 200*(d*\text{sqrt}(x) + c)^3*b*c^2 - 150*(d*\text{sqrt}(x) + c)^2*b*c^3 + 75*(d*\text{sqrt}(x) + c)*b*c^4)*\log(((a^2 + b^2)*\cos(2*d*\text{sqrt}(x) + 2*c))^2 + 4*a*b*\sin(2*d*\text{sqrt}(x) + 2*c) + (a^2 + b^2)*\sin(2*d*\text{sqrt}(x) + 2*c))^2 + a^2 + b^2 + 2*(a^2 - b^2)*\cos(2*d*\text{sqrt}(x) + 2*c))/(a^2 + b^2)) - 360*I*b*\text{polylog}(6, (I*a + b)*e^(2*I*d*\text{sqrt}(x) + 2*I*c)/(-I*a + b)) - 90*(8*(d*\text{sqrt}(x) + c)*b - 5*b*c)*\text{polylog}(5, (I*a + b)*e^(2*I*d*\text{sqrt}(x) + 2*I*c)/(-I*a + b)) - 60*(-12*I*(d*\text{sqrt}(x) + c)^2*b + 15*I*(d*\text{sqrt}(x) + c)*b*c - 5*I*b*c^2)*\text{polylog}(4, (I*a + b)*e^(2*I*d*\text{sqrt}(x) + 2*I*c)/(-I*a + b)) + 30*(16*(d*\text{sqrt}(x) + c)^3*b - 30*(d*\text{sqrt}(x) + c)^2*b*c + 20*(d*\text{sqrt}(x) + c)*b*c^2 - 5*b*c^3)*\text{polylog}(3, (I*a + b)*e^(2*I*d*\text{sqrt}(x) + 2*I*c)/(-I*a + b)))/(a^2 + b^2))/d^6$$

Giac [F]

$$\int \frac{x^2}{a + b \tan(c + d\sqrt{x})} dx = \int \frac{x^2}{b \tan(d\sqrt{x} + c) + a} dx$$

[In] integrate(x^2/(a+b*tan(c+d*x^(1/2))),x, algorithm="giac")

[Out] integrate(x^2/(b*tan(d*sqrt(x) + c) + a), x)

Mupad [F(-1)]

Timed out.

$$\int \frac{x^2}{a + b \tan(c + d\sqrt{x})} dx = \int \frac{x^2}{a + b \tan(c + d \sqrt{x})} dx$$

```
[In] int(x^2/(a + b*tan(c + d*x^(1/2))),x)
```

```
[Out] int(x^2/(a + b*tan(c + d*x^(1/2))), x)
```

3.38 $\int \frac{x}{a+b \tan(c+d\sqrt{x})} dx$

Optimal result	224
Rubi [A] (verified)	225
Mathematica [A] (verified)	227
Maple [F]	228
Fricas [F]	228
Sympy [F]	228
Maxima [B] (verification not implemented)	228
Giac [F]	229
Mupad [F(-1)]	229

Optimal result

Integrand size = 18, antiderivative size = 234

$$\int \frac{x}{a+b \tan(c+d\sqrt{x})} dx = \frac{x^2}{2(a+ib)} + \frac{2bx^{3/2} \log\left(1 + \frac{(a^2+b^2)e^{2i(c+d\sqrt{x})}}{(a+ib)^2}\right)}{(a^2+b^2)d}$$

$$- \frac{3ibx \operatorname{PolyLog}\left(2, -\frac{(a^2+b^2)e^{2i(c+d\sqrt{x})}}{(a+ib)^2}\right)}{(a^2+b^2)d^2}$$

$$+ \frac{3b\sqrt{x} \operatorname{PolyLog}\left(3, -\frac{(a^2+b^2)e^{2i(c+d\sqrt{x})}}{(a+ib)^2}\right)}{(a^2+b^2)d^3}$$

$$+ \frac{3ib \operatorname{PolyLog}\left(4, -\frac{(a^2+b^2)e^{2i(c+d\sqrt{x})}}{(a+ib)^2}\right)}{2(a^2+b^2)d^4}$$

```
[Out] 1/2*x^2/(a+I*b)+2*b*x^(3/2)*ln(1+(a^2+b^2)*exp(2*I*(c+d*x^(1/2)))/(a+I*b)^2
)/(a^2+b^2)/d-3*I*b*x*polylog(2,-(a^2+b^2)*exp(2*I*(c+d*x^(1/2)))/(a+I*b)^2
)/(a^2+b^2)/d^2+3/2*I*b*polylog(4,-(a^2+b^2)*exp(2*I*(c+d*x^(1/2)))/(a+I*b)
^2)/(a^2+b^2)/d^4+3*b*polylog(3,-(a^2+b^2)*exp(2*I*(c+d*x^(1/2)))/(a+I*b)^2
)*x^(1/2)/(a^2+b^2)/d^3
```


Rubi [A] (verified)

Time = 0.36 (sec) , antiderivative size = 234, normalized size of antiderivative = 1.00, number of steps used = 7, number of rules used = 7, $\frac{\text{number of rules}}{\text{integrand size}} = 0.389$, Rules used = {3832, 3813, 2221, 2611, 6744, 2320, 6724}

$$\int \frac{x}{a + b \tan(c + d\sqrt{x})} dx = \frac{3ib \operatorname{PolyLog}\left(4, -\frac{(a^2+b^2)e^{2i(c+d\sqrt{x})}}{(a+ib)^2}\right)}{2d^4(a^2+b^2)} + \frac{3b\sqrt{x} \operatorname{PolyLog}\left(3, -\frac{(a^2+b^2)e^{2i(c+d\sqrt{x})}}{(a+ib)^2}\right)}{d^3(a^2+b^2)} - \frac{3ibx \operatorname{PolyLog}\left(2, -\frac{(a^2+b^2)e^{2i(c+d\sqrt{x})}}{(a+ib)^2}\right)}{d^2(a^2+b^2)} + \frac{2bx^{3/2} \log\left(1 + \frac{(a^2+b^2)e^{2i(c+d\sqrt{x})}}{(a+ib)^2}\right)}{d(a^2+b^2)} + \frac{x^2}{2(a+ib)}$$

[In] Int[x/(a + b*Tan[c + d*Sqrt[x]]),x]

[Out] $x^2/(2*(a + I*b)) + (2*b*x^{(3/2)}*Log[1 + ((a^2 + b^2)*E^{((2*I)*(c + d*Sqrt[x]))})/(a + I*b)^2])/(a + I*b)^2)/((a^2 + b^2)*d) - ((3*I)*b*x*PolyLog[2, -(((a^2 + b^2)*E^{((2*I)*(c + d*Sqrt[x]))})/(a + I*b)^2)])/(a + I*b)^2)/((a^2 + b^2)*d^2) + (3*b*Sqrt[x]*PolyLog[3, -(((a^2 + b^2)*E^{((2*I)*(c + d*Sqrt[x]))})/(a + I*b)^2)])/(a^2 + b^2)*d^3 + (((3*I)/2)*b*PolyLog[4, -(((a^2 + b^2)*E^{((2*I)*(c + d*Sqrt[x]))})/(a + I*b)^2)])/(a + I*b)^2)/((a^2 + b^2)*d^4)$

Rule 2221

Int[(((F_)^((g_)*(e_) + (f_)*(x_)))^(n_))*((c_) + (d_)*(x_))^(m_)]/((a_) + (b_)*((F_)^((g_)*(e_) + (f_)*(x_)))^(n_)), x_Symbol] :> Simp[((c + d*x)^m/(b*f*g*n*Log[F]))*Log[1 + b*((F^(g*(e + f*x)))^n/a)], x] - Dist[d*(m/(b*f*g*n*Log[F])), Int[(c + d*x)^(m - 1)*Log[1 + b*((F^(g*(e + f*x)))^n/a)], x], x] /; FreeQ[{F, a, b, c, d, e, f, g, n}, x] && IGtQ[m, 0]

Rule 2320

Int[u_, x_Symbol] :> With[{v = FunctionOfExponential[u, x]}, Dist[v/D[v, x], Subst[Int[FunctionOfExponentialFunction[u, x]/x, x], x, v], x] /; FunctionOfExponentialQ[u, x] && !MatchQ[u, (w_)*((a_)*(v_)^(n_))^(m_)] /; FreeQ[{a, m, n}, x] && IntegerQ[m*n] && !MatchQ[u, E^((c_)*((a_) + (b_)*x))* (F_)[v_] /; FreeQ[{a, b, c}, x] && InverseFunctionQ[F[x]]]

Rule 2611

Int[Log[1 + (e_)*((F_)^((c_)*((a_) + (b_)*(x_)))^(n_))]*((f_) + (g_)*(x_))^(m_), x_Symbol] :> Simp[(-(f + g*x)^m)*(PolyLog[2, (-e)*(F^(c*(a +

$b*x)))^n]/(b*c*n*\text{Log}[F]), x] + \text{Dist}[g*(m/(b*c*n*\text{Log}[F])), \text{Int}[(f + g*x)^{(m-1)}*\text{PolyLog}[2, (-e)*(F^{(c*(a + b*x)))^n}], x], x] /; \text{FreeQ}\{F, a, b, c, e, f, g, n\}, x] \&\& \text{GtQ}[m, 0]$

Rule 3813

$\text{Int}[(c + d*x)^{(m+1)}/(d*(m+1)*(a + I*b)), x] + \text{Dist}[2*I*b, \text{Int}[(c + d*x)^m*(E^{\text{Simp}[2*I*(e + f*x), x]}/((a + I*b)^2 + (a^2 + b^2)*E^{\text{Simp}[2*I*(e + f*x), x]})), x], x] /; \text{FreeQ}\{a, b, c, d, e, f\}, x] \&\& \text{NeQ}[a^2 + b^2, 0] \&\& \text{IGtQ}[m, 0]$

Rule 3832

$\text{Int}[(x)^{(m+1)}*((a + b*\text{Tan}[c + d*x])^n)]^{(p)}, x_Symbol] := \text{Dist}[1/n, \text{Subst}[\text{Int}[x^{(\text{Simplify}[(m+1)/n] - 1)*(a + b*\text{Tan}[c + d*x])^p}], x, x^n], x] /; \text{FreeQ}\{a, b, c, d, m, n, p\}, x] \&\& \text{IGtQ}[\text{Simplify}[(m+1)/n], 0] \&\& \text{IntegerQ}[p]$

Rule 6724

$\text{Int}[\text{PolyLog}[n, (c + d*x)^{(a + b*x)^p}]/(d + e*x), x_Symbol] := \text{Simp}[\text{PolyLog}[n + 1, c*(a + b*x)^p]/(e*p), x] /; \text{FreeQ}\{a, b, c, d, e, n, p\}, x] \&\& \text{EqQ}[b*d, a*e]$

Rule 6744

$\text{Int}[(e + f*x)^{(m+1)}*\text{PolyLog}[n, (d + e*x)^{(c + d*x)^{(a + b*x)^p}}], x_Symbol] := \text{Simp}[(e + f*x)^m*(\text{PolyLog}[n + 1, d*(F^{(c*(a + b*x)^p})]/(b*c*p*\text{Log}[F])), x] - \text{Dist}[f*(m/(b*c*p*\text{Log}[F])), \text{Int}[(e + f*x)^{(m-1)}*\text{PolyLog}[n + 1, d*(F^{(c*(a + b*x)^p})], x], x] /; \text{FreeQ}\{F, a, b, c, d, e, f, n, p\}, x] \&\& \text{GtQ}[m, 0]$

Rubi steps

$$\begin{aligned} \text{integral} &= 2\text{Subst}\left(\int \frac{x^3}{a + b \tan(c + dx)} dx, x, \sqrt{x}\right) \\ &= \frac{x^2}{2(a + ib)} + (4ib)\text{Subst}\left(\int \frac{e^{2i(c+dx)} x^3}{(a + ib)^2 + (a^2 + b^2) e^{2i(c+dx)}} dx, x, \sqrt{x}\right) \\ &= \frac{x^2}{2(a + ib)} + \frac{2bx^{3/2} \log\left(1 + \frac{(a^2+b^2)e^{2i(c+d\sqrt{x})}}{(a+ib)^2}\right)}{(a^2 + b^2) d} \\ &\quad - \frac{(6b)\text{Subst}\left(\int x^2 \log\left(1 + \frac{(a^2+b^2)e^{2i(c+dx)}}{(a+ib)^2}\right) dx, x, \sqrt{x}\right)}{(a^2 + b^2) d} \end{aligned}$$

$$\begin{aligned}
&= \frac{x^2}{2(a+ib)} + \frac{2bx^{3/2} \log\left(1 + \frac{(a^2+b^2)e^{2i(c+d\sqrt{x})}}{(a+ib)^2}\right)}{(a^2+b^2)d} - \frac{3ibx \operatorname{PolyLog}\left(2, -\frac{(a^2+b^2)e^{2i(c+d\sqrt{x})}}{(a+ib)^2}\right)}{(a^2+b^2)d^2} \\
&\quad + \frac{(3ib)\operatorname{Subst}\left(\int x \operatorname{PolyLog}\left(2, -\frac{(a^2+b^2)e^{2i(c+d\sqrt{x})}}{(a+ib)^2}\right) dx, x, \sqrt{x}\right)}{(a^2+b^2)d^2} \\
&= \frac{x^2}{2(a+ib)} + \frac{2bx^{3/2} \log\left(1 + \frac{(a^2+b^2)e^{2i(c+d\sqrt{x})}}{(a+ib)^2}\right)}{(a^2+b^2)d} \\
&\quad - \frac{3ibx \operatorname{PolyLog}\left(2, -\frac{(a^2+b^2)e^{2i(c+d\sqrt{x})}}{(a+ib)^2}\right)}{(a^2+b^2)d^2} + \frac{3b\sqrt{x} \operatorname{PolyLog}\left(3, -\frac{(a^2+b^2)e^{2i(c+d\sqrt{x})}}{(a+ib)^2}\right)}{(a^2+b^2)d^3} \\
&\quad - \frac{(3b)\operatorname{Subst}\left(\int \operatorname{PolyLog}\left(3, -\frac{(a^2+b^2)e^{2i(c+d\sqrt{x})}}{(a+ib)^2}\right) dx, x, \sqrt{x}\right)}{(a^2+b^2)d^3} \\
&= \frac{x^2}{2(a+ib)} + \frac{2bx^{3/2} \log\left(1 + \frac{(a^2+b^2)e^{2i(c+d\sqrt{x})}}{(a+ib)^2}\right)}{(a^2+b^2)d} \\
&\quad - \frac{3ibx \operatorname{PolyLog}\left(2, -\frac{(a^2+b^2)e^{2i(c+d\sqrt{x})}}{(a+ib)^2}\right)}{(a^2+b^2)d^2} + \frac{3b\sqrt{x} \operatorname{PolyLog}\left(3, -\frac{(a^2+b^2)e^{2i(c+d\sqrt{x})}}{(a+ib)^2}\right)}{(a^2+b^2)d^3} \\
&\quad + \frac{(3ib)\operatorname{Subst}\left(\int \frac{\operatorname{PolyLog}\left(3, -\frac{(a^2+b^2)x}{(a+ib)^2}\right)}{x} dx, x, e^{2i(c+d\sqrt{x})}\right)}{2(a^2+b^2)d^4} \\
&= \frac{x^2}{2(a+ib)} + \frac{2bx^{3/2} \log\left(1 + \frac{(a^2+b^2)e^{2i(c+d\sqrt{x})}}{(a+ib)^2}\right)}{(a^2+b^2)d} - \frac{3ibx \operatorname{PolyLog}\left(2, -\frac{(a^2+b^2)e^{2i(c+d\sqrt{x})}}{(a+ib)^2}\right)}{(a^2+b^2)d^2} \\
&\quad + \frac{3b\sqrt{x} \operatorname{PolyLog}\left(3, -\frac{(a^2+b^2)e^{2i(c+d\sqrt{x})}}{(a+ib)^2}\right)}{(a^2+b^2)d^3} + \frac{3ib \operatorname{PolyLog}\left(4, -\frac{(a^2+b^2)e^{2i(c+d\sqrt{x})}}{(a+ib)^2}\right)}{2(a^2+b^2)d^4}
\end{aligned}$$

Mathematica [A] (verified)

Time = 1.01 (sec) , antiderivative size = 213, normalized size of antiderivative = 0.91

$$\begin{aligned}
&\int \frac{x}{a + b \tan(c + d\sqrt{x})} dx \\
&= \frac{ad^4x^2 + ibd^4x^2 + 4bd^3x^{3/2} \log\left(1 + \frac{(a+ib)e^{-2i(c+d\sqrt{x})}}{a-ib}\right) + 6ibd^2x \operatorname{PolyLog}\left(2, \frac{(-a-ib)e^{-2i(c+d\sqrt{x})}}{a-ib}\right) + 6bd\sqrt{x} \operatorname{PolyLog}\left(3, \frac{(-a-ib)e^{-2i(c+d\sqrt{x})}}{a-ib}\right)}{2(a^2+b^2)d^4}
\end{aligned}$$

[In] Integrate[x/(a + b*Tan[c + d*Sqrt[x]]), x]

```
[Out] (a*d^4*x^2 + I*b*d^4*x^2 + 4*b*d^3*x^(3/2)*Log[1 + (a + I*b)/((a - I*b)*E^((2*I)*(c + d*Sqrt[x])))] + (6*I)*b*d^2*x*PolyLog[2, (-a - I*b)/((a - I*b)*E^((2*I)*(c + d*Sqrt[x])))] + 6*b*d*Sqrt[x]*PolyLog[3, (-a - I*b)/((a - I*b)*E^((2*I)*(c + d*Sqrt[x])))] - (3*I)*b*PolyLog[4, (-a - I*b)/((a - I*b)*E^((2*I)*(c + d*Sqrt[x])))])/(2*(a^2 + b^2)*d^4)
```

Maple [F]

$$\int \frac{x}{a + b \tan(c + d\sqrt{x})} dx$$

```
[In] int(x/(a+b*tan(c+d*x^(1/2))),x)
```

```
[Out] int(x/(a+b*tan(c+d*x^(1/2))),x)
```

Fricas [F]

$$\int \frac{x}{a + b \tan(c + d\sqrt{x})} dx = \int \frac{x}{b \tan(d\sqrt{x} + c) + a} dx$$

```
[In] integrate(x/(a+b*tan(c+d*x^(1/2))),x, algorithm="fricas")
```

```
[Out] integral(x/(b*tan(d*sqrt(x) + c) + a), x)
```

Sympy [F]

$$\int \frac{x}{a + b \tan(c + d\sqrt{x})} dx = \int \frac{x}{a + b \tan(c + d\sqrt{x})} dx$$

```
[In] integrate(x/(a+b*tan(c+d*x**(1/2))),x)
```

```
[Out] Integral(x/(a + b*tan(c + d*sqrt(x))), x)
```

Maxima [B] (verification not implemented)

Both result and optimal contain complex but leaf count of result is larger than twice the leaf count of optimal. 555 vs. $2(195) = 390$.

Time = 0.50 (sec) , antiderivative size = 555, normalized size of antiderivative = 2.37

$$\int \frac{x}{a + b \tan(c + d\sqrt{x})} dx =$$

$$6 \left(\frac{2(d\sqrt{x}+c)a}{a^2+b^2} + \frac{2b \log(b \tan(d\sqrt{x}+c)+a)}{a^2+b^2} - \frac{b \log(\tan(d\sqrt{x}+c)^2+1)}{a^2+b^2} \right) c^3 - \frac{3(d\sqrt{x}+c)^4(a-ib) - 12(d\sqrt{x}+c)^3(a-ib)c + 18(d\sqrt{x}+c)^2(a-ib)c^2 - 6(d\sqrt{x}+c)(a-ib)c^3 + 6(a-ib)c^4}{a^2+b^2}$$

[In] integrate(x/(a+b*tan(c+d*x^(1/2))),x, algorithm="maxima")

[Out]
$$-1/6*(6*(2*(d*\text{sqrt}(x) + c)*a/(a^2 + b^2) + 2*b*\log(b*\text{tan}(d*\text{sqrt}(x) + c) + a)/(a^2 + b^2) - b*\log(\text{tan}(d*\text{sqrt}(x) + c)^2 + 1)/(a^2 + b^2))*c^3 - (3*(d*\text{sqrt}(x) + c)^4*(a - I*b) - 12*(d*\text{sqrt}(x) + c)^3*(a - I*b)*c + 18*(d*\text{sqrt}(x) + c)^2*(a - I*b)*c^2 - 4*(4*I*(d*\text{sqrt}(x) + c)^3*b - 9*I*(d*\text{sqrt}(x) + c)^2*b*c + 9*I*(d*\text{sqrt}(x) + c)*b*c^2)*\arctan2((2*a*b*\cos(2*d*\text{sqrt}(x) + 2*c) - (a^2 - b^2)*\sin(2*d*\text{sqrt}(x) + 2*c))/(a^2 + b^2), (2*a*b*\sin(2*d*\text{sqrt}(x) + 2*c) + a^2 + b^2 + (a^2 - b^2)*\cos(2*d*\text{sqrt}(x) + 2*c))/(a^2 + b^2)) - 6*(4*I*(d*\text{sqrt}(x) + c)^2*b - 6*I*(d*\text{sqrt}(x) + c)*b*c + 3*I*b*c^2)*\text{dilog}((I*a + b)*e^(2*I*d*\text{sqrt}(x) + 2*I*c)/(-I*a + b)) + 2*(4*(d*\text{sqrt}(x) + c)^3*b - 9*(d*\text{sqrt}(x) + c)^2*b*c + 9*(d*\text{sqrt}(x) + c)*b*c^2)*\log(((a^2 + b^2)*\cos(2*d*\text{sqrt}(x) + 2*c)^2 + 4*a*b*\sin(2*d*\text{sqrt}(x) + 2*c) + (a^2 + b^2)*\sin(2*d*\text{sqrt}(x) + 2*c)^2 + a^2 + b^2 + 2*(a^2 - b^2)*\cos(2*d*\text{sqrt}(x) + 2*c))/(a^2 + b^2)) + 12*I*b*\text{polylog}(4, (I*a + b)*e^(2*I*d*\text{sqrt}(x) + 2*I*c)/(-I*a + b)) + 6*(4*(d*\text{sqrt}(x) + c)*b - 3*b*c)*\text{polylog}(3, (I*a + b)*e^(2*I*d*\text{sqrt}(x) + 2*I*c)/(-I*a + b)))/(a^2 + b^2))/d^4$$

Giac [F]

$$\int \frac{x}{a + b \tan(c + d\sqrt{x})} dx = \int \frac{x}{b \tan(d\sqrt{x} + c) + a} dx$$

[In] integrate(x/(a+b*tan(c+d*x^(1/2))),x, algorithm="giac")

[Out] integrate(x/(b*tan(d*sqrt(x) + c) + a), x)

Mupad [F(-1)]

Timed out.

$$\int \frac{x}{a + b \tan(c + d\sqrt{x})} dx = \int \frac{x}{a + b \tan(c + d\sqrt{x})} dx$$

[In] int(x/(a + b*tan(c + d*x^(1/2))),x)

[Out] int(x/(a + b*tan(c + d*x^(1/2))), x)

3.39 $\int \frac{1}{a+b \tan(c+d\sqrt{x})} dx$

Optimal result	230
Rubi [A] (verified)	230
Mathematica [A] (verified)	232
Maple [F]	232
Fricas [B] (verification not implemented)	232
Sympy [F]	233
Maxima [B] (verification not implemented)	233
Giac [F]	234
Mupad [F(-1)]	234

Optimal result

Integrand size = 16, antiderivative size = 119

$$\int \frac{1}{a+b \tan(c+d\sqrt{x})} dx = \frac{x}{a+ib} + \frac{2b\sqrt{x} \log\left(1 + \frac{(a^2+b^2)e^{2i(c+d\sqrt{x})}}{(a+ib)^2}\right)}{(a^2+b^2)d} - \frac{ib \operatorname{PolyLog}\left(2, -\frac{(a^2+b^2)e^{2i(c+d\sqrt{x})}}{(a+ib)^2}\right)}{(a^2+b^2)d^2}$$

[Out] $x/(a+I*b) - I*b*\operatorname{polylog}(2, -(a^2+b^2)*\exp(2*I*(c+d*\sqrt{x}))) / (a+I*b)^2 / (a^2+b^2) / d^2 + 2*b*\ln(1+(a^2+b^2)*\exp(2*I*(c+d*\sqrt{x}))) / (a+I*b)^2 * x^{1/2} / (a^2+b^2) / d$

Rubi [A] (verified)

Time = 0.20 (sec) , antiderivative size = 119, normalized size of antiderivative = 1.00, number of steps used = 5, number of rules used = 5, $\frac{\text{number of rules}}{\text{integrand size}} = 0.312$, Rules used = {3824, 3813, 2221, 2317, 2438}

$$\int \frac{1}{a+b \tan(c+d\sqrt{x})} dx = -\frac{ib \operatorname{PolyLog}\left(2, -\frac{(a^2+b^2)e^{2i(c+d\sqrt{x})}}{(a+ib)^2}\right)}{d^2(a^2+b^2)} + \frac{2b\sqrt{x} \log\left(1 + \frac{(a^2+b^2)e^{2i(c+d\sqrt{x})}}{(a+ib)^2}\right)}{d(a^2+b^2)} + \frac{x}{a+ib}$$

[In] $\operatorname{Int}[(a + b*\operatorname{Tan}[c + d*\operatorname{Sqrt}[x]])^{-1}, x]$

[Out] $x/(a + I*b) + (2*b*\operatorname{Sqrt}[x]*\operatorname{Log}[1 + ((a^2 + b^2)*E^{((2*I)*(c + d*\operatorname{Sqrt}[x]))}) / (a + I*b)^2]) / ((a^2 + b^2)*d) - (I*b*\operatorname{PolyLog}[2, -(((a^2 + b^2)*E^{((2*I)*(c + d*\operatorname{Sqrt}[x]))}) / (a + I*b)^2)]) / ((a^2 + b^2)*d^2)$

Rule 2221

```
Int[(((F_)^((g_)*((e_) + (f_)*(x_))))^(n_))*((c_) + (d_)*(x_))^(m_)]/
((a_) + (b_)*((F_)^((g_)*((e_) + (f_)*(x_))))^(n_)), x_Symbol] := Simp
[((c + d*x)^m/(b*f*g*n*Log[F]))*Log[1 + b*((F^(g*(e + f*x)))^n/a)], x] - Di
st[d*(m/(b*f*g*n*Log[F])), Int[(c + d*x)^(m - 1)*Log[1 + b*((F^(g*(e + f*x)
))^n/a)], x], x] /; FreeQ[{F, a, b, c, d, e, f, g, n}, x] && IGtQ[m, 0]
```

Rule 2317

```
Int[Log[(a_) + (b_)*((F_)^((e_)*((c_) + (d_)*(x_))))^(n_)], x_Symbol]
:= Dist[1/(d*e*n*Log[F]), Subst[Int[Log[a + b*x]/x, x], x, (F^(e*(c + d*x))
)^n], x] /; FreeQ[{F, a, b, c, d, e, n}, x] && GtQ[a, 0]
```

Rule 2438

```
Int[Log[(c_) * ((d_) + (e_)*(x_)^(n_))]/(x_), x_Symbol] := Simp[-PolyLog[2
, (-c)*e*x^n]/n, x] /; FreeQ[{c, d, e, n}, x] && EqQ[c*d, 1]
```

Rule 3813

```
Int[((c_) + (d_)*(x_))^(m_)/((a_) + (b_)*tan[(e_) + (f_)*(x_)]), x_Sy
mbol] := Simp[(c + d*x)^(m + 1)/(d*(m + 1)*(a + I*b)), x] + Dist[2*I*b, Int
[(c + d*x)^m*(E^Simp[2*I*(e + f*x), x])/((a + I*b)^2 + (a^2 + b^2)*E^Simp[2*
I*(e + f*x), x]), x], x] /; FreeQ[{a, b, c, d, e, f}, x] && NeQ[a^2 + b^2,
0] && IGtQ[m, 0]
```

Rule 3824

```
Int[((a_) + (b_)*Tan[(c_) + (d_)*(x_)^(n_)])^(p_), x_Symbol] := Dist[1
/n, Subst[Int[x^(1/n - 1)*(a + b*Tan[c + d*x])^p, x], x, x^n], x] /; FreeQ[
{a, b, c, d, p}, x] && IGtQ[1/n, 0] && IntegerQ[p]
```

Rubi steps

$$\begin{aligned}
\text{integral} &= 2\text{Subst}\left(\int \frac{x}{a + b \tan(c + dx)} dx, x, \sqrt{x}\right) \\
&= \frac{x}{a + ib} + (4ib)\text{Subst}\left(\int \frac{e^{2i(c+dx)}x}{(a + ib)^2 + (a^2 + b^2)e^{2i(c+dx)}} dx, x, \sqrt{x}\right) \\
&= \frac{x}{a + ib} + \frac{2b\sqrt{x} \log\left(1 + \frac{(a^2+b^2)e^{2i(c+d\sqrt{x})}}{(a+ib)^2}\right)}{(a^2 + b^2)d} - \frac{(2b)\text{Subst}\left(\int \log\left(1 + \frac{(a^2+b^2)e^{2i(c+d\sqrt{x})}}{(a+ib)^2}\right) dx, x, \sqrt{x}\right)}{(a^2 + b^2)d} \\
&= \frac{x}{a + ib} + \frac{2b\sqrt{x} \log\left(1 + \frac{(a^2+b^2)e^{2i(c+d\sqrt{x})}}{(a+ib)^2}\right)}{(a^2 + b^2)d} + \frac{(ib)\text{Subst}\left(\int \frac{\log\left(1 + \frac{(a^2+b^2)x}{(a+ib)^2}\right)}{x} dx, x, e^{2i(c+d\sqrt{x})}\right)}{(a^2 + b^2)d^2}
\end{aligned}$$

$$= \frac{x}{a+ib} + \frac{2b\sqrt{x} \log\left(1 + \frac{(a^2+b^2)e^{2i(c+d\sqrt{x})}}{(a+ib)^2}\right)}{(a^2+b^2)d} - \frac{ib \operatorname{PolyLog}\left(2, -\frac{(a^2+b^2)e^{2i(c+d\sqrt{x})}}{(a+ib)^2}\right)}{(a^2+b^2)d^2}$$

Mathematica [A] (verified)

Time = 0.18 (sec) , antiderivative size = 111, normalized size of antiderivative = 0.93

$$\int \frac{1}{a+b \tan(c+d\sqrt{x})} dx$$

$$= \frac{(a+ib)d^2x + 2bd\sqrt{x} \log\left(1 + \frac{(a+ib)e^{-2i(c+d\sqrt{x})}}{a-ib}\right) + ib \operatorname{PolyLog}\left(2, \frac{(-a-ib)e^{-2i(c+d\sqrt{x})}}{a-ib}\right)}{(a^2+b^2)d^2}$$

[In] Integrate[(a + b*Tan[c + d*Sqrt[x]])^(-1),x]

[Out] ((a + I*b)*d^2*x + 2*b*d*Sqrt[x]*Log[1 + (a + I*b)/((a - I*b)*E^((2*I)*(c + d*Sqrt[x])))] + I*b*PolyLog[2, (-a - I*b)/((a - I*b)*E^((2*I)*(c + d*Sqrt[x])))])/(a^2 + b^2)*d^2)

Maple [F]

$$\int \frac{1}{a+b \tan(c+d\sqrt{x})} dx$$

[In] int(1/(a+b*tan(c+d*x^(1/2))),x)

[Out] int(1/(a+b*tan(c+d*x^(1/2))),x)

Fricas [B] (verification not implemented)

Both result and optimal contain complex but leaf count of result is larger than twice the leaf count of optimal. 534 vs. 2(100) = 200.

Time = 0.27 (sec) , antiderivative size = 534, normalized size of antiderivative = 4.49

$$\int \frac{1}{a+b \tan(c+d\sqrt{x})} dx$$

$$= \frac{2ad^2x - 2bc \log\left(\frac{(iab+b^2) \tan(d\sqrt{x}+c)^2 - a^2 + iab + (ia^2+ib^2) \tan(d\sqrt{x}+c)}{\tan(d\sqrt{x}+c)^2 + 1}\right) - 2bc \log\left(\frac{(iab-b^2) \tan(d\sqrt{x}+c)^2 + a^2 + iab + (ia^2+ib^2) \tan(d\sqrt{x}+c)}{\tan(d\sqrt{x}+c)^2 + 1}\right)}{(a^2+b^2)d^2}$$

[In] integrate(1/(a+b*tan(c+d*x^(1/2))),x, algorithm="fricas")

[Out] 1/2*(2*a*d^2*x - 2*b*c*log(((I*a*b + b^2)*tan(d*sqrt(x) + c)^2 - a^2 + I*a*b + (I*a^2 + I*b^2)*tan(d*sqrt(x) + c))/(tan(d*sqrt(x) + c)^2 + 1)) - 2*b*c


```
*log(((I*a*b - b^2)*tan(d*sqrt(x) + c)^2 + a^2 + I*a*b + (I*a^2 + I*b^2)*tan(d*sqrt(x) + c))/(tan(d*sqrt(x) + c)^2 + 1)) + I*b*dilog(2*((I*a*b - b^2)*tan(d*sqrt(x) + c)^2 - a^2 - I*a*b + (I*a^2 - 2*a*b - I*b^2)*tan(d*sqrt(x) + c))/((a^2 + b^2)*tan(d*sqrt(x) + c)^2 + a^2 + b^2) + 1) - I*b*dilog(2*((-I*a*b - b^2)*tan(d*sqrt(x) + c)^2 - a^2 + I*a*b + (-I*a^2 - 2*a*b + I*b^2)*tan(d*sqrt(x) + c))/((a^2 + b^2)*tan(d*sqrt(x) + c)^2 + a^2 + b^2) + 1) + 2*(b*d*sqrt(x) + b*c)*log(-2*((I*a*b - b^2)*tan(d*sqrt(x) + c)^2 - a^2 - I*a*b + (I*a^2 - 2*a*b - I*b^2)*tan(d*sqrt(x) + c))/((a^2 + b^2)*tan(d*sqrt(x) + c)^2 + a^2 + b^2)) + 2*(b*d*sqrt(x) + b*c)*log(-2*((-I*a*b - b^2)*tan(d*sqrt(x) + c)^2 - a^2 + I*a*b + (-I*a^2 - 2*a*b + I*b^2)*tan(d*sqrt(x) + c))/((a^2 + b^2)*tan(d*sqrt(x) + c)^2 + a^2 + b^2)))/((a^2 + b^2)*d^2)
```

Sympy [F]

$$\int \frac{1}{a + b \tan(c + d\sqrt{x})} dx = \int \frac{1}{a + b \tan(c + d\sqrt{x})} dx$$

```
[In] integrate(1/(a+b*tan(c+d*x**(1/2))),x)
```

```
[Out] Integral(1/(a + b*tan(c + d*sqrt(x))), x)
```

Maxima [B] (verification not implemented)

Both result and optimal contain complex but leaf count of result is larger than twice the leaf count of optimal. 264 vs. 2(100) = 200.

Time = 0.45 (sec) , antiderivative size = 264, normalized size of antiderivative = 2.22

$$\int \frac{1}{a + b \tan(c + d\sqrt{x})} dx$$

$$= \frac{(a - ib)d^2x - 2ibd\sqrt{x} \arctan\left(\frac{2ab \cos(2d\sqrt{x}+2c) - (a^2 - b^2) \sin(2d\sqrt{x}+2c)}{a^2 + b^2}, \frac{2ab \sin(2d\sqrt{x}+2c) + a^2 + b^2 + (a^2 - b^2) \cos(2d\sqrt{x}+2c)}{a^2 + b^2}\right)}{}$$

```
[In] integrate(1/(a+b*tan(c+d*x^(1/2))),x, algorithm="maxima")
```

```
[Out] ((a - I*b)*d^2*x - 2*I*b*d*sqrt(x)*arctan2((2*a*b*cos(2*d*sqrt(x) + 2*c) - (a^2 - b^2)*sin(2*d*sqrt(x) + 2*c))/(a^2 + b^2), (2*a*b*sin(2*d*sqrt(x) + 2*c) + a^2 + b^2 + (a^2 - b^2)*cos(2*d*sqrt(x) + 2*c))/(a^2 + b^2)) + b*d*sqrt(x)*log(((a^2 + b^2)*cos(2*d*sqrt(x) + 2*c)^2 + 4*a*b*sin(2*d*sqrt(x) + 2*c) + (a^2 + b^2)*sin(2*d*sqrt(x) + 2*c)^2 + a^2 + b^2 + 2*(a^2 - b^2)*cos(2*d*sqrt(x) + 2*c))/(a^2 + b^2)) - I*b*dilog((I*a + b)*e^(2*I*d*sqrt(x) + 2*I*c)/(-I*a + b)))/((a^2 + b^2)*d^2)
```

Giac [F]

$$\int \frac{1}{a + b \tan(c + d\sqrt{x})} dx = \int \frac{1}{b \tan(d\sqrt{x} + c) + a} dx$$

[In] integrate(1/(a+b*tan(c+d*x^(1/2))),x, algorithm="giac")

[Out] integrate(1/(b*tan(d*sqrt(x) + c) + a), x)

Mupad [F(-1)]

Timed out.

$$\int \frac{1}{a + b \tan(c + d\sqrt{x})} dx = \int \frac{1}{a + b \tan(c + d\sqrt{x})} dx$$

[In] int(1/(a + b*tan(c + d*x^(1/2))),x)

[Out] int(1/(a + b*tan(c + d*x^(1/2))), x)

$$3.40 \quad \int \frac{1}{x(a+b \tan(c+d\sqrt{x}))} dx$$

Optimal result	235
Rubi [N/A]	235
Mathematica [N/A]	236
Maple [N/A] (verified)	236
Fricas [N/A]	236
Sympy [N/A]	236
Maxima [N/A]	237
Giac [N/A]	237
Mupad [N/A]	237

Optimal result

Integrand size = 20, antiderivative size = 20

$$\int \frac{1}{x(a+b \tan(c+d\sqrt{x}))} dx = \text{Int}\left(\frac{1}{x(a+b \tan(c+d\sqrt{x}))}, x\right)$$

[Out] Unintegrable(1/x/(a+b*tan(c+d*x^(1/2))), x)

Rubi [N/A]

Not integrable

Time = 0.03 (sec) , antiderivative size = 20, normalized size of antiderivative = 1.00, number of steps used = 0, number of rules used = 0, $\frac{\text{number of rules}}{\text{integrand size}} = 0.000$, Rules used = {}

$$\int \frac{1}{x(a+b \tan(c+d\sqrt{x}))} dx = \int \frac{1}{x(a+b \tan(c+d\sqrt{x}))} dx$$

[In] Int[1/(x*(a + b*Tan[c + d*Sqrt[x]])), x]

[Out] Defer[Int][1/(x*(a + b*Tan[c + d*Sqrt[x]])), x]

Rubi steps

$$\text{integral} = \int \frac{1}{x(a+b \tan(c+d\sqrt{x}))} dx$$

Mathematica [N/A]

Not integrable

Time = 4.45 (sec) , antiderivative size = 22, normalized size of antiderivative = 1.10

$$\int \frac{1}{x(a + b \tan(c + d\sqrt{x}))} dx = \int \frac{1}{x(a + b \tan(c + d\sqrt{x}))} dx$$

[In] Integrate[1/(x*(a + b*Tan[c + d*Sqrt[x]])),x]

[Out] Integrate[1/(x*(a + b*Tan[c + d*Sqrt[x]])), x]

Maple [N/A] (verified)

Not integrable

Time = 0.39 (sec) , antiderivative size = 18, normalized size of antiderivative = 0.90

$$\int \frac{1}{x(a + b \tan(c + d\sqrt{x}))} dx$$

[In] int(1/x/(a+b*tan(c+d*x^(1/2))),x)

[Out] int(1/x/(a+b*tan(c+d*x^(1/2))),x)

Fricas [N/A]

Not integrable

Time = 0.25 (sec) , antiderivative size = 19, normalized size of antiderivative = 0.95

$$\int \frac{1}{x(a + b \tan(c + d\sqrt{x}))} dx = \int \frac{1}{(b \tan(d\sqrt{x} + c) + a)x} dx$$

[In] integrate(1/x/(a+b*tan(c+d*x^(1/2))),x, algorithm="fricas")

[Out] integral(1/(b*x*tan(d*sqrt(x) + c) + a*x), x)

Sympy [N/A]

Not integrable

Time = 2.10 (sec) , antiderivative size = 17, normalized size of antiderivative = 0.85

$$\int \frac{1}{x(a + b \tan(c + d\sqrt{x}))} dx = \int \frac{1}{x(a + b \tan(c + d\sqrt{x}))} dx$$

[In] integrate(1/x/(a+b*tan(c+d*x**(1/2))),x)

[Out] Integral(1/(x*(a + b*tan(c + d*sqrt(x)))), x)

Maxima [N/A]

Not integrable

Time = 1.09 (sec) , antiderivative size = 496, normalized size of antiderivative = 24.80

$$\int \frac{1}{x(a + b \tan(c + d\sqrt{x}))} dx = \int \frac{1}{(b \tan(d\sqrt{x} + c) + a)x} dx$$

[In] integrate(1/x/(a+b*tan(c+d*x^(1/2))),x, algorithm="maxima")

```
[Out] -(2*(a^2*b + b^3)*integrate((a^2*sin(2*d*sqrt(x) + 2*c) - (2*a*b*cos(2*c) +
b^2*sin(2*c))*cos(2*d*sqrt(x)) - (b^2*cos(2*c) - 2*a*b*sin(2*c))*sin(2*d*sqrt(x)))/((a^4*cos(2*d*sqrt(x) + 2*c)^2 + a^4*sin(2*d*sqrt(x) + 2*c)^2 + a^4 + 2*a^2*b^2 + b^4 + ((4*a^2*b^2 + b^4)*cos(2*c)^2 + (4*a^2*b^2 + b^4)*sin(2*c)^2)*cos(2*d*sqrt(x))^2 + ((4*a^2*b^2 + b^4)*cos(2*c)^2 + (4*a^2*b^2 + b^4)*sin(2*c)^2)*sin(2*d*sqrt(x))^2 - 2*((a^2*b^2 + b^4)*cos(2*c) - 2*(a^3*b + a*b^3)*sin(2*c))*cos(2*d*sqrt(x)) + 2*(a^4 + a^2*b^2 - (a^2*b^2*cos(2*c) - 2*a^3*b*sin(2*c))*cos(2*d*sqrt(x)) + (2*a^3*b*cos(2*c) + a^2*b^2*sin(2*c))*sin(2*d*sqrt(x)))*cos(2*d*sqrt(x) + 2*c) + 2*(2*(a^3*b + a*b^3)*cos(2*c) + (a^2*b^2 + b^4)*sin(2*c))*sin(2*d*sqrt(x)) - 2*((2*a^3*b*cos(2*c) + a^2*b^2*sin(2*c))*cos(2*d*sqrt(x)) + (a^2*b^2*cos(2*c) - 2*a^3*b*sin(2*c))*sin(2*d*sqrt(x)))*sin(2*d*sqrt(x) + 2*c))*x, x) - a*log(x))/(a^2 + b^2)
```

Giac [N/A]

Not integrable

Time = 0.61 (sec) , antiderivative size = 20, normalized size of antiderivative = 1.00

$$\int \frac{1}{x(a + b \tan(c + d\sqrt{x}))} dx = \int \frac{1}{(b \tan(d\sqrt{x} + c) + a)x} dx$$

[In] integrate(1/x/(a+b*tan(c+d*x^(1/2))),x, algorithm="giac")

[Out] integrate(1/((b*tan(d*sqrt(x) + c) + a)*x), x)

Mupad [N/A]

Not integrable

Time = 4.07 (sec) , antiderivative size = 20, normalized size of antiderivative = 1.00

$$\int \frac{1}{x(a + b \tan(c + d\sqrt{x}))} dx = \int \frac{1}{x(a + b \tan(c + d\sqrt{x}))} dx$$

[In] int(1/(x*(a + b*tan(c + d*x^(1/2))))),x)

[Out] int(1/(x*(a + b*tan(c + d*x^(1/2))))), x)

$$3.41 \quad \int \frac{1}{x^2(a+b \tan(c+d\sqrt{x}))} dx$$

Optimal result	238
Rubi [N/A]	238
Mathematica [N/A]	239
Maple [N/A] (verified)	239
Fricas [N/A]	239
Sympy [N/A]	239
Maxima [N/A]	240
Giac [N/A]	240
Mupad [N/A]	240

Optimal result

Integrand size = 20, antiderivative size = 20

$$\int \frac{1}{x^2(a+b \tan(c+d\sqrt{x}))} dx = \text{Int}\left(\frac{1}{x^2(a+b \tan(c+d\sqrt{x}))}, x\right)$$

[Out] Unintegrable(1/x^2/(a+b*tan(c+d*x^(1/2))),x)

Rubi [N/A]

Not integrable

Time = 0.03 (sec) , antiderivative size = 20, normalized size of antiderivative = 1.00, number of steps used = 0, number of rules used = 0, $\frac{\text{number of rules}}{\text{integrand size}} = 0.000$, Rules used = {}

$$\int \frac{1}{x^2(a+b \tan(c+d\sqrt{x}))} dx = \int \frac{1}{x^2(a+b \tan(c+d\sqrt{x}))} dx$$

[In] Int[1/(x^2*(a + b*Tan[c + d*Sqrt[x]])),x]

[Out] Defer[Int][1/(x^2*(a + b*Tan[c + d*Sqrt[x]])), x]

Rubi steps

$$\text{integral} = \int \frac{1}{x^2(a+b \tan(c+d\sqrt{x}))} dx$$

Mathematica [N/A]

Not integrable

Time = 5.36 (sec) , antiderivative size = 22, normalized size of antiderivative = 1.10

$$\int \frac{1}{x^2 (a + b \tan (c + d\sqrt{x}))} dx = \int \frac{1}{x^2 (a + b \tan (c + d\sqrt{x}))} dx$$

[In] Integrate[1/(x^2*(a + b*Tan[c + d*Sqrt[x]])),x]

[Out] Integrate[1/(x^2*(a + b*Tan[c + d*Sqrt[x]])), x]

Maple [N/A] (verified)

Not integrable

Time = 0.46 (sec) , antiderivative size = 18, normalized size of antiderivative = 0.90

$$\int \frac{1}{x^2 (a + b \tan (c + d\sqrt{x}))} dx$$

[In] int(1/x^2/(a+b*tan(c+d*x^(1/2))),x)

[Out] int(1/x^2/(a+b*tan(c+d*x^(1/2))),x)

Fricas [N/A]

Not integrable

Time = 0.25 (sec) , antiderivative size = 23, normalized size of antiderivative = 1.15

$$\int \frac{1}{x^2 (a + b \tan (c + d\sqrt{x}))} dx = \int \frac{1}{(b \tan (d\sqrt{x} + c) + a)x^2} dx$$

[In] integrate(1/x^2/(a+b*tan(c+d*x^(1/2))),x, algorithm="fricas")

[Out] integral(1/(b*x^2*tan(d*sqrt(x) + c) + a*x^2), x)

Sympy [N/A]

Not integrable

Time = 2.04 (sec) , antiderivative size = 19, normalized size of antiderivative = 0.95

$$\int \frac{1}{x^2 (a + b \tan (c + d\sqrt{x}))} dx = \int \frac{1}{x^2 (a + b \tan (c + d\sqrt{x}))} dx$$

[In] integrate(1/x**2/(a+b*tan(c+d*x**(1/2))),x)

[Out] Integral(1/(x**2*(a + b*tan(c + d*sqrt(x)))), x)

Maxima [N/A]

Not integrable

Time = 1.27 (sec) , antiderivative size = 496, normalized size of antiderivative = 24.80

$$\int \frac{1}{x^2 (a + b \tan (c + d\sqrt{x}))} dx = \int \frac{1}{(b \tan (d\sqrt{x} + c) + a)x^2} dx$$

[In] integrate(1/x^2/(a+b*tan(c+d*x^(1/2))),x, algorithm="maxima")

```
[Out] -(2*(a^2*b + b^3)*x*integrate((a^2*sin(2*d*sqrt(x) + 2*c) - (2*a*b*cos(2*c)
+ b^2*sin(2*c))*cos(2*d*sqrt(x)) - (b^2*cos(2*c) - 2*a*b*sin(2*c))*sin(2*d
*sqrt(x)))/((a^4*cos(2*d*sqrt(x) + 2*c)^2 + a^4*sin(2*d*sqrt(x) + 2*c)^2 +
a^4 + 2*a^2*b^2 + b^4 + ((4*a^2*b^2 + b^4)*cos(2*c)^2 + (4*a^2*b^2 + b^4)*s
in(2*c)^2)*cos(2*d*sqrt(x))^2 + ((4*a^2*b^2 + b^4)*cos(2*c)^2 + (4*a^2*b^2
+ b^4)*sin(2*c)^2)*sin(2*d*sqrt(x))^2 - 2*((a^2*b^2 + b^4)*cos(2*c) - 2*(a^
3*b + a*b^3)*sin(2*c))*cos(2*d*sqrt(x)) + 2*(a^4 + a^2*b^2 - (a^2*b^2*cos(2
*c) - 2*a^3*b*sin(2*c))*cos(2*d*sqrt(x)) + (2*a^3*b*cos(2*c) + a^2*b^2*sin(
2*c))*sin(2*d*sqrt(x)))*cos(2*d*sqrt(x) + 2*c) + 2*(2*(a^3*b + a*b^3)*cos(2
*c) + (a^2*b^2 + b^4)*sin(2*c))*sin(2*d*sqrt(x)) - 2*((2*a^3*b*cos(2*c) + a
^2*b^2*sin(2*c))*cos(2*d*sqrt(x)) + (a^2*b^2*cos(2*c) - 2*a^3*b*sin(2*c))*s
in(2*d*sqrt(x)))*sin(2*d*sqrt(x) + 2*c))*x^2), x) + a)/((a^2 + b^2)*x)
```

Giac [N/A]

Not integrable

Time = 0.68 (sec) , antiderivative size = 20, normalized size of antiderivative = 1.00

$$\int \frac{1}{x^2 (a + b \tan (c + d\sqrt{x}))} dx = \int \frac{1}{(b \tan (d\sqrt{x} + c) + a)x^2} dx$$

[In] integrate(1/x^2/(a+b*tan(c+d*x^(1/2))),x, algorithm="giac")

[Out] integrate(1/((b*tan(d*sqrt(x) + c) + a)*x^2), x)

Mupad [N/A]

Not integrable

Time = 3.66 (sec) , antiderivative size = 20, normalized size of antiderivative = 1.00

$$\int \frac{1}{x^2 (a + b \tan (c + d\sqrt{x}))} dx = \int \frac{1}{x^2 (a + b \tan (c + d\sqrt{x}))} dx$$

[In] int(1/(x^2*(a + b*tan(c + d*x^(1/2))))),x)

[Out] int(1/(x^2*(a + b*tan(c + d*x^(1/2))))), x)

$$3.42 \quad \int \frac{x^2}{(a+b \tan(c+d\sqrt{x}))^2} dx$$

Optimal result	242
Rubi [A] (verified)	243
Mathematica [A] (verified)	254
Maple [F]	255
Fricas [F]	255
Sympy [F]	256
Maxima [B] (verification not implemented)	256
Giac [F]	258
Mupad [F(-1)]	259

Optimal result

Integrand size = 20, antiderivative size = 1147

$$\begin{aligned}
 \int \frac{x^2}{(a + b \tan(c + d\sqrt{x}))^2} dx = & -\frac{4ib^2x^{5/2}}{(a^2 + b^2)^2 d} \\
 & + \frac{4b^2x^{5/2}}{(a + ib)(ia + b)^2 d (ia - b + (ia + b)e^{2i(c+d\sqrt{x})})} \\
 & + \frac{x^3}{3(a - ib)^2} + \frac{4bx^3}{3(ia - b)(a - ib)^2} \\
 & - \frac{4b^2x^3}{3(a^2 + b^2)^2} + \frac{10b^2x^2 \log\left(1 + \frac{(a-ib)e^{2i(c+d\sqrt{x})}}{a+ib}\right)}{(a^2 + b^2)^2 d^2} \\
 & + \frac{4bx^{5/2} \log\left(1 + \frac{(a-ib)e^{2i(c+d\sqrt{x})}}{a+ib}\right)}{(a - ib)^2(a + ib)d} \\
 & - \frac{4ib^2x^{5/2} \log\left(1 + \frac{(a-ib)e^{2i(c+d\sqrt{x})}}{a+ib}\right)}{(a^2 + b^2)^2 d} \\
 & - \frac{20ib^2x^{3/2} \text{PolyLog}\left(2, -\frac{(a-ib)e^{2i(c+d\sqrt{x})}}{a+ib}\right)}{(a^2 + b^2)^2 d^3} \\
 & + \frac{10bx^2 \text{PolyLog}\left(2, -\frac{(a-ib)e^{2i(c+d\sqrt{x})}}{a+ib}\right)}{(ia - b)(a - ib)^2 d^2} \\
 & - \frac{10b^2x^2 \text{PolyLog}\left(2, -\frac{(a-ib)e^{2i(c+d\sqrt{x})}}{a+ib}\right)}{(a^2 + b^2)^2 d^2} \\
 & + \frac{30b^2x \text{PolyLog}\left(3, -\frac{(a-ib)e^{2i(c+d\sqrt{x})}}{a+ib}\right)}{(a^2 + b^2)^2 d^4} \\
 & + \frac{20bx^{3/2} \text{PolyLog}\left(3, -\frac{(a-ib)e^{2i(c+d\sqrt{x})}}{a+ib}\right)}{(a - ib)^2(a + ib)d^3} \\
 & - \frac{20ib^2x^{3/2} \text{PolyLog}\left(3, -\frac{(a-ib)e^{2i(c+d\sqrt{x})}}{a+ib}\right)}{(a^2 + b^2)^2 d^3} \\
 & + \frac{30ib^2\sqrt{x} \text{PolyLog}\left(4, -\frac{(a-ib)e^{2i(c+d\sqrt{x})}}{a+ib}\right)}{(a^2 + b^2)^2 d^5} \\
 & - \frac{30bx \text{PolyLog}\left(4, -\frac{(a-ib)e^{2i(c+d\sqrt{x})}}{a+ib}\right)}{(ia - b)(a - ib)^2 d^4} \\
 & + \frac{30b^2x \text{PolyLog}\left(4, -\frac{(a-ib)e^{2i(c+d\sqrt{x})}}{a+ib}\right)}{(a^2 + b^2)^2 d^4} \\
 & - \frac{15b^2 \text{PolyLog}\left(5, -\frac{(a-ib)e^{2i(c+d\sqrt{x})}}{a+ib}\right)}{(a^2 + b^2)^2 d^6} \\
 & - \frac{30b\sqrt{x} \text{PolyLog}\left(5, -\frac{(a-ib)e^{2i(c+d\sqrt{x})}}{a+ib}\right)}{(a - ib)^2(a + ib)d^5}
 \end{aligned}$$

```
[Out] -20*I*b^2*x^(3/2)*polylog(3,-(a-I*b)*exp(2*I*(c+d*x^(1/2)))/(a+I*b))/(a^2+b
^2)^2/d^3+4*b^2*x^(5/2)/(a+I*b)/(I*a+b)^2/d/(I*a-b+(I*a+b)*exp(2*I*(c+d*x^(
1/2))))+1/3*x^3/(a-I*b)^2+4/3*b*x^3/(I*a-b)/(a-I*b)^2-4/3*b^2*x^3/(a^2+b^2)
^2+10*b^2*x^2*ln(1+(a-I*b)*exp(2*I*(c+d*x^(1/2)))/(a+I*b))/(a^2+b^2)^2/d^2+
4*b*x^(5/2)*ln(1+(a-I*b)*exp(2*I*(c+d*x^(1/2)))/(a+I*b))/(a-I*b)^2/(a+I*b)/
d-4*I*b^2*x^(5/2)/(a^2+b^2)^2/d+30*I*b^2*polylog(4,-(a-I*b)*exp(2*I*(c+d*x^(
1/2)))/(a+I*b))*x^(1/2)/(a^2+b^2)^2/d^5+10*b*x^2*polylog(2,-(a-I*b)*exp(2*
I*(c+d*x^(1/2)))/(a+I*b))/(I*a-b)/(a-I*b)^2/d^2-10*b^2*x^2*polylog(2,-(a-I*
b)*exp(2*I*(c+d*x^(1/2)))/(a+I*b))/(a^2+b^2)^2/d^2+30*b^2*x*polylog(3,-(a-I
*b)*exp(2*I*(c+d*x^(1/2)))/(a+I*b))/(a^2+b^2)^2/d^4+20*b*x^(3/2)*polylog(3,
-(a-I*b)*exp(2*I*(c+d*x^(1/2)))/(a+I*b))/(a-I*b)^2/(a+I*b)/d^3+30*I*b^2*pol
ylog(5,-(a-I*b)*exp(2*I*(c+d*x^(1/2)))/(a+I*b))*x^(1/2)/(a^2+b^2)^2/d^5-30*
b*x*polylog(4,-(a-I*b)*exp(2*I*(c+d*x^(1/2)))/(a+I*b))/(I*a-b)/(a-I*b)^2/d^
4+30*b^2*x*polylog(4,-(a-I*b)*exp(2*I*(c+d*x^(1/2)))/(a+I*b))/(a^2+b^2)^2/d
^4-15*b^2*polylog(5,-(a-I*b)*exp(2*I*(c+d*x^(1/2)))/(a+I*b))/(a^2+b^2)^2/d^
6+15*b*polylog(6,-(a-I*b)*exp(2*I*(c+d*x^(1/2)))/(a+I*b))/(I*a-b)/(a-I*b)^2
/d^6-15*b^2*polylog(6,-(a-I*b)*exp(2*I*(c+d*x^(1/2)))/(a+I*b))/(a^2+b^2)^2/
d^6-4*I*b^2*x^(5/2)*ln(1+(a-I*b)*exp(2*I*(c+d*x^(1/2)))/(a+I*b))/(a^2+b^2)^
2/d-30*b*polylog(5,-(a-I*b)*exp(2*I*(c+d*x^(1/2)))/(a+I*b))*x^(1/2)/(a-I*b)
^2/(a+I*b)/d^5-20*I*b^2*x^(3/2)*polylog(2,-(a-I*b)*exp(2*I*(c+d*x^(1/2)))/(
a+I*b))/(a^2+b^2)^2/d^3
```

Rubi [A] (verified)

Time = 2.72 (sec) , antiderivative size = 1147, normalized size of antiderivative = 1.00, number of steps used = 28, number of rules used = 10, $\frac{\text{number of rules}}{\text{integrand size}} = 0.500$, Rules

used = {3832, 3815, 2216, 2215, 2221, 2611, 6744, 2320, 6724, 2222}

$$\begin{aligned}
\int \frac{x^2}{(a + b \tan(c + d\sqrt{x}))^2} dx = & \frac{4bx^3}{3(ia - b)(a - ib)^2} + \frac{x^3}{3(a - ib)^2} - \frac{4b^2x^3}{3(a^2 + b^2)^2} \\
& + \frac{4b \log\left(\frac{e^{2i(c+d\sqrt{x})(a-ib)}}{a+ib} + 1\right) x^{5/2}}{(a - ib)^2(a + ib)d} \\
& - \frac{4ib^2 \log\left(\frac{e^{2i(c+d\sqrt{x})(a-ib)}}{a+ib} + 1\right) x^{5/2}}{(a^2 + b^2)^2 d} - \frac{4ib^2x^{5/2}}{(a^2 + b^2)^2 d} \\
& + \frac{4b^2x^{5/2}}{(a + ib)(ia + b)^2d (ia + (ia + b)e^{2i(c+d\sqrt{x})} - b)} \\
& + \frac{10b^2 \log\left(\frac{e^{2i(c+d\sqrt{x})(a-ib)}}{a+ib} + 1\right) x^2}{(a^2 + b^2)^2 d^2} \\
& + \frac{10b \text{PolyLog}\left(2, -\frac{(a-ib)e^{2i(c+d\sqrt{x})}}{a+ib}\right) x^2}{(ia - b)(a - ib)^2d^2} \\
& - \frac{10b^2 \text{PolyLog}\left(2, -\frac{(a-ib)e^{2i(c+d\sqrt{x})}}{a+ib}\right) x^2}{(a^2 + b^2)^2 d^2} \\
& - \frac{20ib^2 \text{PolyLog}\left(2, -\frac{(a-ib)e^{2i(c+d\sqrt{x})}}{a+ib}\right) x^{3/2}}{(a^2 + b^2)^2 d^3} \\
& + \frac{20b \text{PolyLog}\left(3, -\frac{(a-ib)e^{2i(c+d\sqrt{x})}}{a+ib}\right) x^{3/2}}{(a - ib)^2(a + ib)d^3} \\
& - \frac{20ib^2 \text{PolyLog}\left(3, -\frac{(a-ib)e^{2i(c+d\sqrt{x})}}{a+ib}\right) x^{3/2}}{(a^2 + b^2)^2 d^3} \\
& + \frac{30b^2 \text{PolyLog}\left(3, -\frac{(a-ib)e^{2i(c+d\sqrt{x})}}{a+ib}\right) x}{(a^2 + b^2)^2 d^4} \\
& - \frac{30b \text{PolyLog}\left(4, -\frac{(a-ib)e^{2i(c+d\sqrt{x})}}{a+ib}\right) x}{(ia - b)(a - ib)^2d^4} \\
& + \frac{30b^2 \text{PolyLog}\left(4, -\frac{(a-ib)e^{2i(c+d\sqrt{x})}}{a+ib}\right) x}{(a^2 + b^2)^2 d^4} \\
& + \frac{30ib^2 \text{PolyLog}\left(4, -\frac{(a-ib)e^{2i(c+d\sqrt{x})}}{a+ib}\right) \sqrt{x}}{(a^2 + b^2)^2 d^5} \\
& - \frac{30b \text{PolyLog}\left(5, -\frac{(a-ib)e^{2i(c+d\sqrt{x})}}{a+ib}\right) \sqrt{x}}{(a - ib)^2(a + ib)d^5} \\
& + \frac{30ib^2 \text{PolyLog}\left(5, -\frac{(a-ib)e^{2i(c+d\sqrt{x})}}{a+ib}\right) \sqrt{x}}{(a^2 + b^2)^2 d^5} \\
& - \frac{15b^2 \text{PolyLog}\left(5, -\frac{(a-ib)e^{2i(c+d\sqrt{x})}}{a+ib}\right)}{(a^2 + b^2)^2 d^6}
\end{aligned}$$

[In] Int[x^2/(a + b*Tan[c + d*Sqrt[x]])^2,x]

[Out]
$$\begin{aligned} &((-4*I)*b^2*x^{(5/2)})/((a^2 + b^2)^2*d) + (4*b^2*x^{(5/2)})/((a + I*b)*(I*a + b)^2*d*(I*a - b + (I*a + b)*E^{((2*I)*(c + d*Sqrt[x]))})) + x^3/(3*(a - I*b)^2) \\ &+ (4*b*x^3)/(3*(I*a - b)*(a - I*b)^2) - (4*b^2*x^3)/(3*(a^2 + b^2)^2) + (10*b^2*x^2*Log[1 + ((a - I*b)*E^{((2*I)*(c + d*Sqrt[x]))})/(a + I*b)])/((a^2 + b^2)^2*d^2) \\ &+ (4*b*x^{(5/2)}*Log[1 + ((a - I*b)*E^{((2*I)*(c + d*Sqrt[x]))})/(a + I*b)])/((a - I*b)^2*(a + I*b)*d) - ((4*I)*b^2*x^{(5/2)}*Log[1 + ((a - I*b)*E^{((2*I)*(c + d*Sqrt[x]))})/(a + I*b)])/((a^2 + b^2)^2*d) \\ &- ((20*I)*b^2*x^{(3/2)}*PolyLog[2, -(((a - I*b)*E^{((2*I)*(c + d*Sqrt[x]))})/(a + I*b))])/((a^2 + b^2)^2*d^3) + (10*b*x^2*PolyLog[2, -(((a - I*b)*E^{((2*I)*(c + d*Sqrt[x]))})/(a + I*b))])/((I*a - b)*(a - I*b)^2*d^2) \\ &- (10*b^2*x^2*PolyLog[2, -(((a - I*b)*E^{((2*I)*(c + d*Sqrt[x]))})/(a + I*b))])/((a^2 + b^2)^2*d^2) + (30*b^2*x*PolyLog[3, -(((a - I*b)*E^{((2*I)*(c + d*Sqrt[x]))})/(a + I*b))])/((a^2 + b^2)^2*d^4) \\ &+ (20*b*x^{(3/2)}*PolyLog[3, -(((a - I*b)*E^{((2*I)*(c + d*Sqrt[x]))})/(a + I*b))])/((a - I*b)^2*(a + I*b)*d^3) - ((20*I)*b^2*x^{(3/2)}*PolyLog[3, -(((a - I*b)*E^{((2*I)*(c + d*Sqrt[x]))})/(a + I*b))])/((a^2 + b^2)^2*d^3) \\ &+ ((30*I)*b^2*Sqrt[x]*PolyLog[4, -(((a - I*b)*E^{((2*I)*(c + d*Sqrt[x]))})/(a + I*b))])/((a^2 + b^2)^2*d^5) - (30*b*x*PolyLog[4, -(((a - I*b)*E^{((2*I)*(c + d*Sqrt[x]))})/(a + I*b))])/((I*a - b)*(a - I*b)^2*d^4) \\ &+ (30*b^2*x*PolyLog[4, -(((a - I*b)*E^{((2*I)*(c + d*Sqrt[x]))})/(a + I*b))])/((a^2 + b^2)^2*d^4) - (15*b^2*PolyLog[5, -(((a - I*b)*E^{((2*I)*(c + d*Sqrt[x]))})/(a + I*b))])/((a^2 + b^2)^2*d^6) \\ &- (30*b*Sqrt[x]*PolyLog[5, -(((a - I*b)*E^{((2*I)*(c + d*Sqrt[x]))})/(a + I*b))])/((a - I*b)^2*(a + I*b)*d^5) + ((30*I)*b^2*Sqrt[x]*PolyLog[5, -(((a - I*b)*E^{((2*I)*(c + d*Sqrt[x]))})/(a + I*b))])/((a^2 + b^2)^2*d^5) \\ &+ (15*b*PolyLog[6, -(((a - I*b)*E^{((2*I)*(c + d*Sqrt[x]))})/(a + I*b))])/((I*a - b)*(a - I*b)^2*d^6) - (15*b^2*PolyLog[6, -(((a - I*b)*E^{((2*I)*(c + d*Sqrt[x]))})/(a + I*b))])/((a^2 + b^2)^2*d^6) \end{aligned}$$

Rule 2215

Int[((c_) + (d_)*(x_))^(m_)/((a_) + (b_)*((F_)^((g_)*((e_) + (f_)*(x_))))^(n_)), x_Symbol] := Simp[(c + d*x)^(m + 1)/(a*d*(m + 1)), x] - Dist[b/a, Int[(c + d*x)^m*((F)^(g*(e + f*x)))^n/(a + b*(F)^(g*(e + f*x)))^n], x] /; FreeQ[{F, a, b, c, d, e, f, g, n}, x] && IGtQ[m, 0]

Rule 2216

Int[((a_) + (b_)*((F_)^((g_)*((e_) + (f_)*(x_))))^(n_))^(p_)*((c_) + (d_)*(x_))^(m_), x_Symbol] := Dist[1/a, Int[(c + d*x)^m*(a + b*(F)^(g*(e + f*x)))^n]^(p + 1), x] - Dist[b/a, Int[(c + d*x)^m*(F)^(g*(e + f*x))^n*(a + b*(F)^(g*(e + f*x)))^n]^p, x] /; FreeQ[{F, a, b, c, d, e, f, g, n}, x] && ILtQ[p, 0] && IGtQ[m, 0]

Rule 2221

Int[(((F_)^((g_)*((e_) + (f_)*(x_))))^(n_)*((c_) + (d_)*(x_))^(m_))/((a_) + (b_)*((F_)^((g_)*((e_) + (f_)*(x_))))^(n_)), x_Symbol] := Simp

```

[((c + d*x)^m/(b*f*g*n*Log[F]))*Log[1 + b*((F^(g*(e + f*x)))^n/a)], x] - Dist[d*(m/(b*f*g*n*Log[F])), Int[(c + d*x)^(m - 1)*Log[1 + b*((F^(g*(e + f*x)))^n/a)], x], x] /; FreeQ[{F, a, b, c, d, e, f, g, n}, x] && IGtQ[m, 0]

```

Rule 2222

```

Int[((F_)^((g_)*(e_) + (f_)*(x_)))^(n_)*((a_) + (b_)*((F_)^((g_)*(e_) + (f_)*(x_)))^(n_))^(p_)*((c_) + (d_)*(x_)^(m_)), x_Symbol] :>
Simp[(c + d*x)^m*((a + b*(F^(g*(e + f*x)))^n)^(p + 1)/(b*f*g*n*(p + 1)*Log[F])), x] - Dist[d*(m/(b*f*g*n*(p + 1)*Log[F])), Int[(c + d*x)^(m - 1)*(a + b*(F^(g*(e + f*x)))^n)^(p + 1), x], x] /; FreeQ[{F, a, b, c, d, e, f, g, m, n, p}, x] && NeQ[p, -1]

```

Rule 2320

```

Int[u_, x_Symbol] :> With[{v = FunctionOfExponential[u, x]}, Dist[v/D[v, x], Subst[Int[FunctionOfExponentialFunction[u, x]/x, x], x, v], x] /; FunctionOfExponentialQ[u, x] && !MatchQ[u, (w_)*((a_)*(v_)^(n_))^(m_)] /; FreeQ[{a, m, n}, x] && IntegerQ[m*n] && !MatchQ[u, E^((c_)*((a_) + (b_)*x))*(F_)[v_] /; FreeQ[{a, b, c}, x] && InverseFunctionQ[F[x]]]

```

Rule 2611

```

Int[Log[1 + (e_)*((F_)^((c_)*((a_) + (b_)*(x_)))^(n_))]*((f_) + (g_)*(x_))^(m_), x_Symbol] :> Simp[(-f + g*x)^m*(PolyLog[2, (-e)*(F^(c*(a + b*x)))^n]/(b*c*n*Log[F])), x] + Dist[g*(m/(b*c*n*Log[F])), Int[(f + g*x)^(m - 1)*PolyLog[2, (-e)*(F^(c*(a + b*x)))^n], x], x] /; FreeQ[{F, a, b, c, e, f, g, n}, x] && GtQ[m, 0]

```

Rule 3815

```

Int[((c_) + (d_)*(x_))^(m_)*((a_) + (b_)*tan[(e_) + (f_)*(x_)])^(n_), x_Symbol] :> Int[ExpandIntegrand[(c + d*x)^m, (1/(a - I*b) - 2*I*(b/(a^2 + b^2 + (a - I*b)^2*E^(2*I*(e + f*x))))^(-n), x], x] /; FreeQ[{a, b, c, d, e, f}, x] && NeQ[a^2 + b^2, 0] && ILtQ[n, 0] && IGtQ[m, 0]

```

Rule 3832

```

Int[(x_)^(m_)*((a_) + (b_)*Tan[(c_) + (d_)*(x_)^(n_)])^(p_), x_Symbol] :> Dist[1/n, Subst[Int[x^(Simplify[(m + 1)/n] - 1)*(a + b*Tan[c + d*x])^p, x], x, x^n], x] /; FreeQ[{a, b, c, d, m, n, p}, x] && IGtQ[Simplify[(m + 1)/n], 0] && IntegerQ[p]

```

Rule 6724

```

Int[PolyLog[n_, (c_)*((a_) + (b_)*(x_))^(p_)]/((d_) + (e_)*(x_)), x_Symbol] :> Simp[PolyLog[n + 1, c*(a + b*x)^p]/(e*p), x] /; FreeQ[{a, b, c, d}

```

, e, n, p], x] && EqQ[b*d, a*e]

Rule 6744

Int[((e_.) + (f_.)*(x_))^(m_.)*PolyLog[n_, (d_.)*((F_)^((c_.)*((a_.) + (b_.)*(x_)))^(p_.)], x_Symbol] := Simp[(e + f*x)^m*(PolyLog[n + 1, d*(F^(c*(a + b*x)))^p]/(b*c*p*Log[F])), x] - Dist[f*(m/(b*c*p*Log[F])), Int[(e + f*x)^(m - 1)*PolyLog[n + 1, d*(F^(c*(a + b*x)))^p], x], x] /; FreeQ[{F, a, b, c, d, e, f, n, p], x] && GtQ[m, 0]

Rubi steps

$$\begin{aligned}
 \text{integral} &= 2\text{Subst}\left(\int \frac{x^5}{(a + b \tan(c + dx))^2} dx, x, \sqrt{x}\right) \\
 &= 2\text{Subst}\left(\int \left(\frac{x^5}{(a - ib)^2} - \frac{4b^2 x^5}{(ia + b)^2 \left(ia \left(1 + \frac{ib}{a}\right) + ia \left(1 - \frac{ib}{a}\right) e^{2ic+2idx}\right)^2} \right. \right. \\
 &\quad \left. \left. + \frac{4bx^5}{(a - ib)^2 \left(ia \left(1 + \frac{ib}{a}\right) + ia \left(1 - \frac{ib}{a}\right) e^{2ic+2idx}\right)}\right) dx, x, \sqrt{x}\right) \\
 &= \frac{x^3}{3(a - ib)^2} + \frac{(8b)\text{Subst}\left(\int \frac{x^5}{ia \left(1 + \frac{ib}{a}\right) + ia \left(1 - \frac{ib}{a}\right) e^{2ic+2idx}} dx, x, \sqrt{x}\right)}{(a - ib)^2} \\
 &\quad - \frac{(8b^2)\text{Subst}\left(\int \frac{x^5}{\left(ia \left(1 + \frac{ib}{a}\right) + ia \left(1 - \frac{ib}{a}\right) e^{2ic+2idx}\right)^2} dx, x, \sqrt{x}\right)}{(ia + b)^2} \\
 &= \frac{x^3}{3(a - ib)^2} + \frac{4bx^3}{3(ia - b)(a - ib)^2} + \frac{(8b^2)\text{Subst}\left(\int \frac{x^5}{ia \left(1 + \frac{ib}{a}\right) + ia \left(1 - \frac{ib}{a}\right) e^{2ic+2idx}} dx, x, \sqrt{x}\right)}{(ia - b)(a - ib)^2} \\
 &\quad - \frac{(8b)\text{Subst}\left(\int \frac{e^{2ic+2idx} x^5}{ia \left(1 + \frac{ib}{a}\right) + ia \left(1 - \frac{ib}{a}\right) e^{2ic+2idx}} dx, x, \sqrt{x}\right)}{a^2 + b^2} \\
 &\quad - \frac{(8b^2)\text{Subst}\left(\int \frac{e^{2ic+2idx} x^5}{\left(ia \left(1 + \frac{ib}{a}\right) + ia \left(1 - \frac{ib}{a}\right) e^{2ic+2idx}\right)^2} dx, x, \sqrt{x}\right)}{a^2 + b^2}
 \end{aligned}$$

$$\begin{aligned}
&= -\frac{4b^2x^{5/2}}{(a-ib)^2(a+ib)d} \frac{ia-b+(ia+b)e^{2i(c+d\sqrt{x})}}{(a-ib)^2} + \frac{x^3}{3(a-ib)^2} \\
&+ \frac{4bx^3}{3(ia-b)(a-ib)^2} - \frac{4b^2x^3}{3(a^2+b^2)^2} + \frac{4bx^{5/2} \log\left(1 + \frac{(a-ib)e^{2i(c+d\sqrt{x})}}{a+ib}\right)}{(a-ib)^2(a+ib)d} \\
&- \frac{(8b^2) \text{Subst}\left(\int \frac{e^{2ic+2idx}x^5}{ia(1+\frac{ib}{a})+ia(1-\frac{ib}{a})e^{2ic+2idx}} dx, x, \sqrt{x}\right)}{(a+ib)^2(ia+b)} \\
&- \frac{(20b) \text{Subst}\left(\int x^4 \log\left(1 + \frac{(1-\frac{ib}{a})e^{2ic+2idx}}{1+\frac{ib}{a}}\right) dx, x, \sqrt{x}\right)}{(a-ib)^2(a+ib)d} \\
&+ \frac{(20b^2) \text{Subst}\left(\int \frac{x^4}{ia(1+\frac{ib}{a})+ia(1-\frac{ib}{a})e^{2ic+2idx}} dx, x, \sqrt{x}\right)}{(a-ib)^2(a+ib)d} \\
&= -\frac{4ib^2x^{5/2}}{(a^2+b^2)^2d} - \frac{4b^2x^{5/2}}{(a-ib)^2(a+ib)d} \frac{ia-b+(ia+b)e^{2i(c+d\sqrt{x})}}{(a-ib)^2} + \frac{x^3}{3(a-ib)^2} \\
&+ \frac{4bx^3}{3(ia-b)(a-ib)^2} - \frac{4b^2x^3}{3(a^2+b^2)^2} + \frac{4bx^{5/2} \log\left(1 + \frac{(a-ib)e^{2i(c+d\sqrt{x})}}{a+ib}\right)}{(a-ib)^2(a+ib)d} \\
&- \frac{4ib^2x^{5/2} \log\left(1 + \frac{(a-ib)e^{2i(c+d\sqrt{x})}}{a+ib}\right)}{(a^2+b^2)^2d} + \frac{10bx^2 \text{PolyLog}\left(2, -\frac{(a-ib)e^{2i(c+d\sqrt{x})}}{a+ib}\right)}{(ia-b)(a-ib)^2d^2} \\
&- \frac{(40b) \text{Subst}\left(\int x^3 \text{PolyLog}\left(2, -\frac{(1-\frac{ib}{a})e^{2ic+2idx}}{1+\frac{ib}{a}}\right) dx, x, \sqrt{x}\right)}{(ia-b)(a-ib)^2d^2} \\
&- \frac{(20b^2) \text{Subst}\left(\int \frac{e^{2ic+2idx}x^4}{ia(1+\frac{ib}{a})+ia(1-\frac{ib}{a})e^{2ic+2idx}} dx, x, \sqrt{x}\right)}{(a-ib)(a+ib)^2d} \\
&+ \frac{(20ib^2) \text{Subst}\left(\int x^4 \log\left(1 + \frac{(1-\frac{ib}{a})e^{2ic+2idx}}{1+\frac{ib}{a}}\right) dx, x, \sqrt{x}\right)}{(a^2+b^2)^2d}
\end{aligned}$$

$$\begin{aligned}
&= -\frac{4ib^2x^{5/2}}{(a^2+b^2)^2d} - \frac{4b^2x^{5/2}}{(a-ib)^2(a+ib)d} \frac{(ia-b+(ia+b)e^{2i(c+d\sqrt{x})})}{(a-ib)^2(a+ib)d} \\
&+ \frac{x^3}{3(a-ib)^2} + \frac{4bx^3}{3(ia-b)(a-ib)^2} - \frac{4b^2x^3}{3(a^2+b^2)^2} \\
&+ \frac{10b^2x^2 \log\left(1 + \frac{(a-ib)e^{2i(c+d\sqrt{x})}}{a+ib}\right)}{(a^2+b^2)^2d^2} + \frac{4bx^{5/2} \log\left(1 + \frac{(a-ib)e^{2i(c+d\sqrt{x})}}{a+ib}\right)}{(a-ib)^2(a+ib)d} \\
&- \frac{4ib^2x^{5/2} \log\left(1 + \frac{(a-ib)e^{2i(c+d\sqrt{x})}}{a+ib}\right)}{(a^2+b^2)^2d} + \frac{10bx^2 \text{PolyLog}\left(2, -\frac{(a-ib)e^{2i(c+d\sqrt{x})}}{a+ib}\right)}{(ia-b)(a-ib)^2d^2} \\
&- \frac{10b^2x^2 \text{PolyLog}\left(2, -\frac{(a-ib)e^{2i(c+d\sqrt{x})}}{a+ib}\right)}{(a^2+b^2)^2d^2} + \frac{20bx^{3/2} \text{PolyLog}\left(3, -\frac{(a-ib)e^{2i(c+d\sqrt{x})}}{a+ib}\right)}{(a-ib)^2(a+ib)d^3} \\
&- \frac{(60b) \text{Subst}\left(\int x^2 \text{PolyLog}\left(3, -\frac{\left(1-\frac{ib}{a}\right)e^{2ic+2idx}}{1+\frac{ib}{a}}\right) dx, x, \sqrt{x}\right)}{(a-ib)^2(a+ib)d^3} \\
&- \frac{(40b^2) \text{Subst}\left(\int x^3 \log\left(1 + \frac{\left(1-\frac{ib}{a}\right)e^{2ic+2idx}}{1+\frac{ib}{a}}\right) dx, x, \sqrt{x}\right)}{(a^2+b^2)^2d^2} \\
&+ \frac{(40b^2) \text{Subst}\left(\int x^3 \text{PolyLog}\left(2, -\frac{\left(1-\frac{ib}{a}\right)e^{2ic+2idx}}{1+\frac{ib}{a}}\right) dx, x, \sqrt{x}\right)}{(a^2+b^2)^2d^2}
\end{aligned}$$

$$\begin{aligned}
&= -\frac{4ib^2x^{5/2}}{(a^2+b^2)^2d} - \frac{4b^2x^{5/2}}{(a-ib)^2(a+ib)d} \frac{ia-b+(ia+b)e^{2i(c+d\sqrt{x})}}{(a^2+b^2)^2d^2} + \frac{x^3}{3(a-ib)^2} \\
&+ \frac{4bx^3}{3(ia-b)(a-ib)^2} - \frac{4b^2x^3}{3(a^2+b^2)^2} + \frac{10b^2x^2 \log\left(1 + \frac{(a-ib)e^{2i(c+d\sqrt{x})}}{a+ib}\right)}{(a^2+b^2)^2d^2} \\
&+ \frac{4bx^{5/2} \log\left(1 + \frac{(a-ib)e^{2i(c+d\sqrt{x})}}{a+ib}\right)}{(a-ib)^2(a+ib)d} - \frac{4ib^2x^{5/2} \log\left(1 + \frac{(a-ib)e^{2i(c+d\sqrt{x})}}{a+ib}\right)}{(a^2+b^2)^2d} \\
&- \frac{20ib^2x^{3/2} \text{PolyLog}\left(2, -\frac{(a-ib)e^{2i(c+d\sqrt{x})}}{a+ib}\right)}{(a^2+b^2)^2d^3} + \frac{10bx^2 \text{PolyLog}\left(2, -\frac{(a-ib)e^{2i(c+d\sqrt{x})}}{a+ib}\right)}{(ia-b)(a-ib)^2d^2} \\
&- \frac{10b^2x^2 \text{PolyLog}\left(2, -\frac{(a-ib)e^{2i(c+d\sqrt{x})}}{a+ib}\right)}{(a^2+b^2)^2d^2} + \frac{20bx^{3/2} \text{PolyLog}\left(3, -\frac{(a-ib)e^{2i(c+d\sqrt{x})}}{a+ib}\right)}{(a-ib)^2(a+ib)d^3} \\
&- \frac{20ib^2x^{3/2} \text{PolyLog}\left(3, -\frac{(a-ib)e^{2i(c+d\sqrt{x})}}{a+ib}\right)}{(a^2+b^2)^2d^3} - \frac{30bx \text{PolyLog}\left(4, -\frac{(a-ib)e^{2i(c+d\sqrt{x})}}{a+ib}\right)}{(ia-b)(a-ib)^2d^4} \\
&+ \frac{(60b) \text{Subst}\left(\int x \text{PolyLog}\left(4, -\frac{\left(1-\frac{ib}{a}\right)e^{2ic+2idx}}{1+\frac{ib}{a}}\right) dx, x, \sqrt{x}\right)}{(ia-b)(a-ib)^2d^4} \\
&+ \frac{(60ib^2) \text{Subst}\left(\int x^2 \text{PolyLog}\left(2, -\frac{\left(1-\frac{ib}{a}\right)e^{2ic+2idx}}{1+\frac{ib}{a}}\right) dx, x, \sqrt{x}\right)}{(a^2+b^2)^2d^3} \\
&+ \frac{(60ib^2) \text{Subst}\left(\int x^2 \text{PolyLog}\left(3, -\frac{\left(1-\frac{ib}{a}\right)e^{2ic+2idx}}{1+\frac{ib}{a}}\right) dx, x, \sqrt{x}\right)}{(a^2+b^2)^2d^3}
\end{aligned}$$

$$\begin{aligned}
&= -\frac{4ib^2x^{5/2}}{(a^2+b^2)^2d} - \frac{4b^2x^{5/2}}{(a-ib)^2(a+ib)d} \frac{(ia-b+(ia+b)e^{2i(c+d\sqrt{x})})}{x^3} \\
&+ \frac{4bx^3}{3(a-ib)^2} + \frac{4b^2x^3}{3(ia-b)(a-ib)^2} - \frac{4b^2x^3}{3(a^2+b^2)^2} \\
&+ \frac{10b^2x^2 \log\left(1 + \frac{(a-ib)e^{2i(c+d\sqrt{x})}}{a+ib}\right)}{(a^2+b^2)^2d^2} + \frac{4bx^{5/2} \log\left(1 + \frac{(a-ib)e^{2i(c+d\sqrt{x})}}{a+ib}\right)}{(a-ib)^2(a+ib)d} \\
&- \frac{4ib^2x^{5/2} \log\left(1 + \frac{(a-ib)e^{2i(c+d\sqrt{x})}}{a+ib}\right)}{(a^2+b^2)^2d} - \frac{20ib^2x^{3/2} \text{PolyLog}\left(2, -\frac{(a-ib)e^{2i(c+d\sqrt{x})}}{a+ib}\right)}{(a^2+b^2)^2d^3} \\
&+ \frac{10bx^2 \text{PolyLog}\left(2, -\frac{(a-ib)e^{2i(c+d\sqrt{x})}}{a+ib}\right)}{(ia-b)(a-ib)^2d^2} - \frac{10b^2x^2 \text{PolyLog}\left(2, -\frac{(a-ib)e^{2i(c+d\sqrt{x})}}{a+ib}\right)}{(a^2+b^2)^2d^2} \\
&+ \frac{30b^2x \text{PolyLog}\left(3, -\frac{(a-ib)e^{2i(c+d\sqrt{x})}}{a+ib}\right)}{(a^2+b^2)^2d^4} + \frac{20bx^{3/2} \text{PolyLog}\left(3, -\frac{(a-ib)e^{2i(c+d\sqrt{x})}}{a+ib}\right)}{(a-ib)^2(a+ib)d^3} \\
&- \frac{20ib^2x^{3/2} \text{PolyLog}\left(3, -\frac{(a-ib)e^{2i(c+d\sqrt{x})}}{a+ib}\right)}{(a^2+b^2)^2d^3} - \frac{30bx \text{PolyLog}\left(4, -\frac{(a-ib)e^{2i(c+d\sqrt{x})}}{a+ib}\right)}{(ia-b)(a-ib)^2d^4} \\
&+ \frac{30b^2x \text{PolyLog}\left(4, -\frac{(a-ib)e^{2i(c+d\sqrt{x})}}{a+ib}\right)}{(a^2+b^2)^2d^4} - \frac{30b\sqrt{x} \text{PolyLog}\left(5, -\frac{(a-ib)e^{2i(c+d\sqrt{x})}}{a+ib}\right)}{(a-ib)^2(a+ib)d^5} \\
&+ \frac{(30b) \text{Subst}\left(\int \text{PolyLog}\left(5, -\frac{(1-\frac{ib}{a})e^{2ic+2idx}}{1+\frac{ib}{a}}\right) dx, x, \sqrt{x}\right)}{(a-ib)^2(a+ib)d^5} \\
&- \frac{(60b^2) \text{Subst}\left(\int x \text{PolyLog}\left(3, -\frac{(1-\frac{ib}{a})e^{2ic+2idx}}{1+\frac{ib}{a}}\right) dx, x, \sqrt{x}\right)}{(a^2+b^2)^2d^4} \\
&- \frac{(60b^2) \text{Subst}\left(\int x \text{PolyLog}\left(4, -\frac{(1-\frac{ib}{a})e^{2ic+2idx}}{1+\frac{ib}{a}}\right) dx, x, \sqrt{x}\right)}{(a^2+b^2)^2d^4}
\end{aligned}$$

$$\begin{aligned}
&= -\frac{4ib^2x^{5/2}}{(a^2+b^2)^2d} - \frac{4b^2x^{5/2}}{(a-ib)^2(a+ib)d} \frac{(ia-b+(ia+b)e^{2i(c+d\sqrt{x})})}{(a-b+(ia+b)e^{2i(c+d\sqrt{x})})} \\
&+ \frac{x^3}{3(a-ib)^2} + \frac{4bx^3}{3(ia-b)(a-ib)^2} - \frac{4b^2x^3}{3(a^2+b^2)^2} \\
&+ \frac{10b^2x^2 \log\left(1 + \frac{(a-ib)e^{2i(c+d\sqrt{x})}}{a+ib}\right)}{(a^2+b^2)^2d^2} + \frac{4bx^{5/2} \log\left(1 + \frac{(a-ib)e^{2i(c+d\sqrt{x})}}{a+ib}\right)}{(a-ib)^2(a+ib)d} \\
&- \frac{4ib^2x^{5/2} \log\left(1 + \frac{(a-ib)e^{2i(c+d\sqrt{x})}}{a+ib}\right)}{(a^2+b^2)^2d} - \frac{20ib^2x^{3/2} \text{PolyLog}\left(2, -\frac{(a-ib)e^{2i(c+d\sqrt{x})}}{a+ib}\right)}{(a^2+b^2)^2d^3} \\
&+ \frac{10bx^2 \text{PolyLog}\left(2, -\frac{(a-ib)e^{2i(c+d\sqrt{x})}}{a+ib}\right)}{(ia-b)(a-ib)^2d^2} - \frac{10b^2x^2 \text{PolyLog}\left(2, -\frac{(a-ib)e^{2i(c+d\sqrt{x})}}{a+ib}\right)}{(a^2+b^2)^2d^2} \\
&+ \frac{30b^2x \text{PolyLog}\left(3, -\frac{(a-ib)e^{2i(c+d\sqrt{x})}}{a+ib}\right)}{(a^2+b^2)^2d^4} + \frac{20bx^{3/2} \text{PolyLog}\left(3, -\frac{(a-ib)e^{2i(c+d\sqrt{x})}}{a+ib}\right)}{(a-ib)^2(a+ib)d^3} \\
&- \frac{20ib^2x^{3/2} \text{PolyLog}\left(3, -\frac{(a-ib)e^{2i(c+d\sqrt{x})}}{a+ib}\right)}{(a^2+b^2)^2d^3} + \frac{30ib^2\sqrt{x} \text{PolyLog}\left(4, -\frac{(a-ib)e^{2i(c+d\sqrt{x})}}{a+ib}\right)}{(a^2+b^2)^2d^5} \\
&- \frac{30bx \text{PolyLog}\left(4, -\frac{(a-ib)e^{2i(c+d\sqrt{x})}}{a+ib}\right)}{(ia-b)(a-ib)^2d^4} + \frac{30b^2x \text{PolyLog}\left(4, -\frac{(a-ib)e^{2i(c+d\sqrt{x})}}{a+ib}\right)}{(a^2+b^2)^2d^4} \\
&- \frac{30b\sqrt{x} \text{PolyLog}\left(5, -\frac{(a-ib)e^{2i(c+d\sqrt{x})}}{a+ib}\right)}{(a-ib)^2(a+ib)d^5} + \frac{30ib^2\sqrt{x} \text{PolyLog}\left(5, -\frac{(a-ib)e^{2i(c+d\sqrt{x})}}{a+ib}\right)}{(a^2+b^2)^2d^5} \\
&+ \frac{(15b) \text{Subst}\left(\int \frac{\text{PolyLog}\left(5, -\frac{(a-ib)x}{a+ib}\right)}{x} dx, x, e^{2i(c+d\sqrt{x})}\right)}{(ia-b)(a-ib)^2d^6} \\
&- \frac{(30ib^2) \text{Subst}\left(\int \text{PolyLog}\left(4, -\frac{\left(1-\frac{ib}{a}\right)e^{2ic+2idx}}{1+\frac{ib}{a}}\right) dx, x, \sqrt{x}\right)}{(a^2+b^2)^2d^5} \\
&- \frac{(30ib^2) \text{Subst}\left(\int \text{PolyLog}\left(5, -\frac{\left(1-\frac{ib}{a}\right)e^{2ic+2idx}}{1+\frac{ib}{a}}\right) dx, x, \sqrt{x}\right)}{(a^2+b^2)^2d^5}
\end{aligned}$$

$$\begin{aligned}
&= -\frac{4ib^2x^{5/2}}{(a^2+b^2)^2d} - \frac{4b^2x^{5/2}}{(a-ib)^2(a+ib)d} \frac{ia-b+(ia+b)e^{2i(c+d\sqrt{x})}}{(a^2+b^2)^2d} + \frac{x^3}{3(a-ib)^2} \\
&+ \frac{4bx^3}{3(ia-b)(a-ib)^2} - \frac{4b^2x^3}{3(a^2+b^2)^2} + \frac{10b^2x^2 \log\left(1 + \frac{(a-ib)e^{2i(c+d\sqrt{x})}}{a+ib}\right)}{(a^2+b^2)^2d^2} \\
&+ \frac{4bx^{5/2} \log\left(1 + \frac{(a-ib)e^{2i(c+d\sqrt{x})}}{a+ib}\right)}{(a-ib)^2(a+ib)d} - \frac{4ib^2x^{5/2} \log\left(1 + \frac{(a-ib)e^{2i(c+d\sqrt{x})}}{a+ib}\right)}{(a^2+b^2)^2d} \\
&- \frac{20ib^2x^{3/2} \text{PolyLog}\left(2, -\frac{(a-ib)e^{2i(c+d\sqrt{x})}}{a+ib}\right)}{(a^2+b^2)^2d^3} + \frac{10bx^2 \text{PolyLog}\left(2, -\frac{(a-ib)e^{2i(c+d\sqrt{x})}}{a+ib}\right)}{(ia-b)(a-ib)^2d^2} \\
&- \frac{10b^2x^2 \text{PolyLog}\left(2, -\frac{(a-ib)e^{2i(c+d\sqrt{x})}}{a+ib}\right)}{(a^2+b^2)^2d^2} + \frac{30b^2x \text{PolyLog}\left(3, -\frac{(a-ib)e^{2i(c+d\sqrt{x})}}{a+ib}\right)}{(a^2+b^2)^2d^4} \\
&+ \frac{20bx^{3/2} \text{PolyLog}\left(3, -\frac{(a-ib)e^{2i(c+d\sqrt{x})}}{a+ib}\right)}{(a-ib)^2(a+ib)d^3} - \frac{20ib^2x^{3/2} \text{PolyLog}\left(3, -\frac{(a-ib)e^{2i(c+d\sqrt{x})}}{a+ib}\right)}{(a^2+b^2)^2d^3} \\
&+ \frac{30ib^2\sqrt{x} \text{PolyLog}\left(4, -\frac{(a-ib)e^{2i(c+d\sqrt{x})}}{a+ib}\right)}{(a^2+b^2)^2d^5} - \frac{30bx \text{PolyLog}\left(4, -\frac{(a-ib)e^{2i(c+d\sqrt{x})}}{a+ib}\right)}{(ia-b)(a-ib)^2d^4} \\
&+ \frac{30b^2x \text{PolyLog}\left(4, -\frac{(a-ib)e^{2i(c+d\sqrt{x})}}{a+ib}\right)}{(a^2+b^2)^2d^4} - \frac{30b\sqrt{x} \text{PolyLog}\left(5, -\frac{(a-ib)e^{2i(c+d\sqrt{x})}}{a+ib}\right)}{(a-ib)^2(a+ib)d^5} \\
&+ \frac{30ib^2\sqrt{x} \text{PolyLog}\left(5, -\frac{(a-ib)e^{2i(c+d\sqrt{x})}}{a+ib}\right)}{(a^2+b^2)^2d^5} + \frac{15b \text{PolyLog}\left(6, -\frac{(a-ib)e^{2i(c+d\sqrt{x})}}{a+ib}\right)}{(ia-b)(a-ib)^2d^6} \\
&- \frac{(15b^2) \text{Subst}\left(\int \frac{\text{PolyLog}\left(4, -\frac{(a-ib)x}{a+ib}\right)}{x} dx, x, e^{2i(c+d\sqrt{x})}\right)}{(a^2+b^2)^2d^6} \\
&- \frac{(15b^2) \text{Subst}\left(\int \frac{\text{PolyLog}\left(5, -\frac{(a-ib)x}{a+ib}\right)}{x} dx, x, e^{2i(c+d\sqrt{x})}\right)}{(a^2+b^2)^2d^6}
\end{aligned}$$

$$\begin{aligned}
&= -\frac{4ib^2x^{5/2}}{(a^2+b^2)^2d} - \frac{4b^2x^{5/2}}{(a-ib)^2(a+ib)d} \frac{1}{(ia-b+(a+b)e^{2i(c+d\sqrt{x})})} + \frac{x^3}{3(a-ib)^2} \\
&+ \frac{4bx^3}{3(ia-b)(a-ib)^2} - \frac{4b^2x^3}{3(a^2+b^2)^2} + \frac{10b^2x^2 \log\left(1 + \frac{(a-ib)e^{2i(c+d\sqrt{x})}}{a+ib}\right)}{(a^2+b^2)^2d^2} \\
&+ \frac{4bx^{5/2} \log\left(1 + \frac{(a-ib)e^{2i(c+d\sqrt{x})}}{a+ib}\right)}{(a-ib)^2(a+ib)d} - \frac{4ib^2x^{5/2} \log\left(1 + \frac{(a-ib)e^{2i(c+d\sqrt{x})}}{a+ib}\right)}{(a^2+b^2)^2d} \\
&- \frac{20ib^2x^{3/2} \text{PolyLog}\left(2, -\frac{(a-ib)e^{2i(c+d\sqrt{x})}}{a+ib}\right)}{(a^2+b^2)^2d^3} + \frac{10bx^2 \text{PolyLog}\left(2, -\frac{(a-ib)e^{2i(c+d\sqrt{x})}}{a+ib}\right)}{(ia-b)(a-ib)^2d^2} \\
&- \frac{10b^2x^2 \text{PolyLog}\left(2, -\frac{(a-ib)e^{2i(c+d\sqrt{x})}}{a+ib}\right)}{(a^2+b^2)^2d^2} + \frac{30b^2x \text{PolyLog}\left(3, -\frac{(a-ib)e^{2i(c+d\sqrt{x})}}{a+ib}\right)}{(a^2+b^2)^2d^4} \\
&+ \frac{20bx^{3/2} \text{PolyLog}\left(3, -\frac{(a-ib)e^{2i(c+d\sqrt{x})}}{a+ib}\right)}{(a-ib)^2(a+ib)d^3} - \frac{20ib^2x^{3/2} \text{PolyLog}\left(3, -\frac{(a-ib)e^{2i(c+d\sqrt{x})}}{a+ib}\right)}{(a^2+b^2)^2d^3} \\
&+ \frac{30ib^2\sqrt{x} \text{PolyLog}\left(4, -\frac{(a-ib)e^{2i(c+d\sqrt{x})}}{a+ib}\right)}{(a^2+b^2)^2d^5} - \frac{30bx \text{PolyLog}\left(4, -\frac{(a-ib)e^{2i(c+d\sqrt{x})}}{a+ib}\right)}{(ia-b)(a-ib)^2d^4} \\
&+ \frac{30b^2x \text{PolyLog}\left(4, -\frac{(a-ib)e^{2i(c+d\sqrt{x})}}{a+ib}\right)}{(a^2+b^2)^2d^4} - \frac{15b^2 \text{PolyLog}\left(5, -\frac{(a-ib)e^{2i(c+d\sqrt{x})}}{a+ib}\right)}{(a^2+b^2)^2d^6} \\
&- \frac{30b\sqrt{x} \text{PolyLog}\left(5, -\frac{(a-ib)e^{2i(c+d\sqrt{x})}}{a+ib}\right)}{(a-ib)^2(a+ib)d^5} + \frac{30ib^2\sqrt{x} \text{PolyLog}\left(5, -\frac{(a-ib)e^{2i(c+d\sqrt{x})}}{a+ib}\right)}{(a^2+b^2)^2d^5} \\
&+ \frac{15b \text{PolyLog}\left(6, -\frac{(a-ib)e^{2i(c+d\sqrt{x})}}{a+ib}\right)}{(ia-b)(a-ib)^2d^6} - \frac{15b^2 \text{PolyLog}\left(6, -\frac{(a-ib)e^{2i(c+d\sqrt{x})}}{a+ib}\right)}{(a^2+b^2)^2d^6}
\end{aligned}$$

Mathematica [A] (verified)

Time = 3.26 (sec) , antiderivative size = 848, normalized size of antiderivative = 0.74

$$\int \frac{x^2}{(a+b \tan(c+d\sqrt{x}))^2} dx$$

$$\frac{ib \left(12(a+ib)b(ia+b)d^5x^{5/2} + 4a(a+ib)(ia+b)d^6x^3 + 30(a-ib)bd^4(-ib(-1+e^{2ic})+a(1+e^{2ic}))x^2 \log\left(1 + \frac{(a+ib)e^{-2i(c+d\sqrt{x})}}{a-ib}\right) + 12a(a-ib)d^5(-ib) \right)}{(a^2+b^2)^2d^6}$$

[In] Integrate[x^2/(a + b*Tan[c + d*Sqrt[x]])^2,x]

[Out] (((-I)*b*(12*(a + I*b)*b*(I*a + b)*d^5*x^(5/2) + 4*a*(a + I*b)*(I*a + b)*d^6*x^3 + 30*(a - I*b)*b*d^4*((-I)*b*(-1 + E^((2*I)*c)) + a*(1 + E^((2*I)*c)))*x^2*Log[1 + (a + I*b)/((a - I*b)*E^((2*I)*(c + d*Sqrt[x])))] + 12*a*(a -

$$\begin{aligned}
& I*b*d^5*((-I)*b*(-1 + E^{((2*I)*c)}) + a*(1 + E^{((2*I)*c)}))*x^{(5/2)}*\text{Log}[1 + \\
& (a + I*b)/((a - I*b)*E^{((2*I)*(c + d*\text{Sqrt}[x]))})] + 15*(a - I*b)*b*((-I)*b*(\\
& -1 + E^{((2*I)*c)}) + a*(1 + E^{((2*I)*c)}))*((4*I)*d^3*x^{(3/2)}*\text{PolyLog}[2, (-a \\
& - I*b)/((a - I*b)*E^{((2*I)*(c + d*\text{Sqrt}[x]))})] + 6*d^2*x*\text{PolyLog}[3, (-a - I* \\
& b)/((a - I*b)*E^{((2*I)*(c + d*\text{Sqrt}[x]))})] - (6*I)*d*\text{Sqrt}[x]*\text{PolyLog}[4, (-a \\
& - I*b)/((a - I*b)*E^{((2*I)*(c + d*\text{Sqrt}[x]))})] - 3*\text{PolyLog}[5, (-a - I*b)/((a \\
& - I*b)*E^{((2*I)*(c + d*\text{Sqrt}[x]))})] + 15*a*(a - I*b)*((-I)*b*(-1 + E^{((2*I) \\
&)*c}) + a*(1 + E^{((2*I)*c)}))*((2*I)*d^4*x^2*\text{PolyLog}[2, (-a - I*b)/((a - I*b) \\
&)*E^{((2*I)*(c + d*\text{Sqrt}[x]))})] + 4*d^3*x^{(3/2)}*\text{PolyLog}[3, (-a - I*b)/((a - I \\
& *b)*E^{((2*I)*(c + d*\text{Sqrt}[x]))})] - (6*I)*d^2*x*\text{PolyLog}[4, (-a - I*b)/((a - I \\
& *b)*E^{((2*I)*(c + d*\text{Sqrt}[x]))})] - 6*d*\text{Sqrt}[x]*\text{PolyLog}[5, (-a - I*b)/((a - I \\
& *b)*E^{((2*I)*(c + d*\text{Sqrt}[x]))})] + (3*I)*\text{PolyLog}[6, (-a - I*b)/((a - I*b)*E^{ \\
& ((2*I)*(c + d*\text{Sqrt}[x]))})])]/(d^6*(b - b*E^{((2*I)*c)} - I*a*(1 + E^{((2*I)*c) \\
&))) + ((a - I*b)^2*(a + I*b)*x^3*(a*\text{Cos}[c] - b*\text{Sin}[c]))/(a*\text{Cos}[c] + b*\text{Sin}[c \\
&]) + (6*(a - I*b)^2*(a + I*b)*b^2*x^{(5/2)}*\text{Sin}[d*\text{Sqrt}[x]])/(d*(a*\text{Cos}[c] + b* \\
& \text{Sin}[c])*(a*\text{Cos}[c + d*\text{Sqrt}[x]] + b*\text{Sin}[c + d*\text{Sqrt}[x]]))/(3*(a - I*b)^3*(a + \\
& I*b)^2)
\end{aligned}$$

Maple [F]

$$\int \frac{x^2}{(a + b \tan(c + d\sqrt{x}))^2} dx$$

[In] int(x^2/(a+b*tan(c+d*x^(1/2)))^2,x)

[Out] int(x^2/(a+b*tan(c+d*x^(1/2)))^2,x)

Fricas [F]

$$\int \frac{x^2}{(a + b \tan(c + d\sqrt{x}))^2} dx = \int \frac{x^2}{(b \tan(d\sqrt{x} + c) + a)^2} dx$$

[In] integrate(x^2/(a+b*tan(c+d*x^(1/2)))^2,x, algorithm="fricas")

[Out] integral(x^2/(b^2*tan(d*sqrt(x) + c)^2 + 2*a*b*tan(d*sqrt(x) + c) + a^2), x)

SymPy [F]

$$\int \frac{x^2}{(a + b \tan(c + d\sqrt{x}))^2} dx = \int \frac{x^2}{(a + b \tan(c + d\sqrt{x}))^2} dx$$

```
[In] integrate(x**2/(a+b*tan(c+d*x**(1/2)))**2,x)
```

```
[Out] Integral(x**2/(a + b*tan(c + d*sqrt(x)))**2, x)
```

Maxima [B] (verification not implemented)

Both result and optimal contain complex but leaf count of result is larger than twice the leaf count of optimal. 4345 vs. $2(928) = 1856$.

Time = 1.39 (sec) , antiderivative size = 4345, normalized size of antiderivative = 3.79

$$\int \frac{x^2}{(a + b \tan(c + d\sqrt{x}))^2} dx = \text{Too large to display}$$

```
[In] integrate(x^2/(a+b*tan(c+d*x^(1/2)))^2,x, algorithm="maxima")
```

```
[Out] -1/15*(30*(2*a*b*log(b*tan(d*sqrt(x) + c) + a)/(a^4 + 2*a^2*b^2 + b^4) - a*
b*log(tan(d*sqrt(x) + c)^2 + 1)/(a^4 + 2*a^2*b^2 + b^4) + (a^2 - b^2)*(d*sq
rt(x) + c)/(a^4 + 2*a^2*b^2 + b^4) - b/(a^3 + a*b^2 + (a^2*b + b^3)*tan(d*s
qrt(x) + c)))*c^5 - (5*(a^3 - I*a^2*b + a*b^2 - I*b^3)*(d*sqrt(x) + c)^6 -
30*(a^3 - I*a^2*b + a*b^2 - I*b^3)*(d*sqrt(x) + c)^5*c + 75*(a^3 - I*a^2*b
+ a*b^2 - I*b^3)*(d*sqrt(x) + c)^4*c^2 - 100*(a^3 - I*a^2*b + a*b^2 - I*b^3
)*(d*sqrt(x) + c)^3*c^3 + 75*(a^3 - I*a^2*b + a*b^2 - I*b^3)*(d*sqrt(x) + c
)^2*c^4 - 150*((-I*a*b^2 - b^3)*c^4*cos(2*d*sqrt(x) + 2*c) + (a*b^2 - I*b^3
)*c^4*sin(2*d*sqrt(x) + 2*c) + (-I*a*b^2 + b^3)*c^4)*arctan2(-b*cos(2*d*sq
rt(x) + 2*c) + a*sin(2*d*sqrt(x) + 2*c) + b, a*cos(2*d*sqrt(x) + 2*c) + b*si
n(2*d*sqrt(x) + 2*c) + a) - 4*(48*(I*a^2*b - a*b^2)*(d*sqrt(x) + c)^5 + 75*
(I*a*b^2 - b^3 + 2*(-I*a^2*b + a*b^2)*c)*(d*sqrt(x) + c)^4 + 200*((I*a^2*b
- a*b^2)*c^2 + (-I*a*b^2 + b^3)*c)*(d*sqrt(x) + c)^3 + 75*(2*(-I*a^2*b + a
b^2)*c^3 + 3*(I*a*b^2 - b^3)*c^2)*(d*sqrt(x) + c)^2 + 75*((I*a^2*b - a*b^2)
*c^4 + 2*(-I*a*b^2 + b^3)*c^3)*(d*sqrt(x) + c) + (48*(I*a^2*b + a*b^2)*(d*s
qrt(x) + c)^5 + 75*(I*a*b^2 + b^3 + 2*(-I*a^2*b - a*b^2)*c)*(d*sqrt(x) + c)
^4 + 200*((I*a^2*b + a*b^2)*c^2 + (-I*a*b^2 - b^3)*c)*(d*sqrt(x) + c)^3 + 7
5*(2*(-I*a^2*b - a*b^2)*c^3 + 3*(I*a*b^2 + b^3)*c^2)*(d*sqrt(x) + c)^2 + 75
*((I*a^2*b + a*b^2)*c^4 + 2*(-I*a*b^2 - b^3)*c^3)*(d*sqrt(x) + c))*cos(2*d*
sqrt(x) + 2*c) - (48*(a^2*b - I*a*b^2)*(d*sqrt(x) + c)^5 + 75*(a*b^2 - I*b^
3 - 2*(a^2*b - I*a*b^2)*c)*(d*sqrt(x) + c)^4 + 200*((a^2*b - I*a*b^2)*c^2 -
(a*b^2 - I*b^3)*c)*(d*sqrt(x) + c)^3 - 75*(2*(a^2*b - I*a*b^2)*c^3 - 3*(a
b^2 - I*b^3)*c^2)*(d*sqrt(x) + c)^2 + 75*((a^2*b - I*a*b^2)*c^4 - 2*(a*b^2
```


$$\begin{aligned}
& - I*b^3*c^3*(d*\sqrt{x} + c))*\sin(2*d*\sqrt{x} + 2*c))*\arctan2((2*a*b*\cos(2 \\
& *d*\sqrt{x} + 2*c) - (a^2 - b^2)*\sin(2*d*\sqrt{x} + 2*c))/(a^2 + b^2), (2*a*b \\
& *sin(2*d*\sqrt{x} + 2*c) + a^2 + b^2 + (a^2 - b^2)*\cos(2*d*\sqrt{x} + 2*c))/(\\
& a^2 + b^2)) + 5*((a^3 - 3*I*a^2*b - 3*a*b^2 + I*b^3)*(d*\sqrt{x} + c)^6 - 6* \\
& (2*I*a*b^2 + 2*b^3 + (a^3 - 3*I*a^2*b - 3*a*b^2 + I*b^3)*c)*(d*\sqrt{x} + c) \\
& ^5 - 60*(I*a*b^2 + b^3)*(d*\sqrt{x} + c)*c^4 + 15*((a^3 - 3*I*a^2*b - 3*a*b^2 \\
& + I*b^3)*c^2 - 4*(-I*a*b^2 - b^3)*c)*(d*\sqrt{x} + c)^4 - 20*((a^3 - 3*I*a \\
& ^2*b - 3*a*b^2 + I*b^3)*c^3 + 6*(I*a*b^2 + b^3)*c^2)*(d*\sqrt{x} + c)^3 + 15 \\
& *((a^3 - 3*I*a^2*b - 3*a*b^2 + I*b^3)*c^4 - 8*(-I*a*b^2 - b^3)*c^3)*(d*\sqrt{x} \\
& (x) + c)^2)*\cos(2*d*\sqrt{x} + 2*c) - 30*(16*(I*a^2*b - a*b^2)*(d*\sqrt{x} + \\
& c)^4 + 5*(I*a^2*b - a*b^2)*c^4 + 20*(I*a*b^2 - b^3 + 2*(-I*a^2*b + a*b^2)*c \\
&)*(d*\sqrt{x} + c)^3 + 10*(-I*a*b^2 + b^3)*c^3 + 40*((I*a^2*b - a*b^2)*c^2 + \\
& (-I*a*b^2 + b^3)*c)*(d*\sqrt{x} + c)^2 + 10*(2*(-I*a^2*b + a*b^2)*c^3 + 3*(\\
& I*a*b^2 - b^3)*c^2)*(d*\sqrt{x} + c) + (16*(I*a^2*b + a*b^2)*(d*\sqrt{x} + c) \\
& ^4 + 5*(I*a^2*b + a*b^2)*c^4 + 20*(I*a*b^2 + b^3 + 2*(-I*a^2*b - a*b^2)*c)* \\
& (d*\sqrt{x} + c)^3 + 10*(-I*a*b^2 - b^3)*c^3 + 40*((I*a^2*b + a*b^2)*c^2 + (\\
& -I*a*b^2 - b^3)*c)*(d*\sqrt{x} + c)^2 + 10*(2*(-I*a^2*b - a*b^2)*c^3 + 3*(I* \\
& a*b^2 + b^3)*c^2)*(d*\sqrt{x} + c))*\cos(2*d*\sqrt{x} + 2*c) - (16*(a^2*b - I* \\
& a*b^2)*(d*\sqrt{x} + c)^4 + 5*(a^2*b - I*a*b^2)*c^4 + 20*(a*b^2 - I*b^3 - 2* \\
& (a^2*b - I*a*b^2)*c)*(d*\sqrt{x} + c)^3 - 10*(a*b^2 - I*b^3)*c^3 + 40*((a^2*b \\
& b - I*a*b^2)*c^2 - (a*b^2 - I*b^3)*c)*(d*\sqrt{x} + c)^2 - 10*(2*(a^2*b - I* \\
& a*b^2)*c^3 - 3*(a*b^2 - I*b^3)*c^2)*(d*\sqrt{x} + c))*\sin(2*d*\sqrt{x} + 2*c) \\
&)*\operatorname{dilog}((I*a + b)*e^{(2*I*d*\sqrt{x} + 2*I*c)/(-I*a + b)}) + 75*((a*b^2 - I*b^ \\
& 3)*c^4*\cos(2*d*\sqrt{x} + 2*c) - (-I*a*b^2 - b^3)*c^4*\sin(2*d*\sqrt{x} + 2*c) \\
& + (a*b^2 + I*b^3)*c^4)*\log((a^2 + b^2)*\cos(2*d*\sqrt{x} + 2*c)^2 + 4*a*b*\sin \\
& (2*d*\sqrt{x} + 2*c) + (a^2 + b^2)*\sin(2*d*\sqrt{x} + 2*c)^2 + a^2 + b^2 + 2 \\
& *(a^2 - b^2)*\cos(2*d*\sqrt{x} + 2*c)) + 2*(48*(a^2*b + I*a*b^2)*(d*\sqrt{x} + \\
& c)^5 + 75*(a*b^2 + I*b^3 - 2*(a^2*b + I*a*b^2)*c)*(d*\sqrt{x} + c)^4 + 200* \\
& ((a^2*b + I*a*b^2)*c^2 - (a*b^2 + I*b^3)*c)*(d*\sqrt{x} + c)^3 - 75*(2*(a^2*b \\
& b + I*a*b^2)*c^3 - 3*(a*b^2 + I*b^3)*c^2)*(d*\sqrt{x} + c)^2 + 75*((a^2*b + \\
& I*a*b^2)*c^4 - 2*(a*b^2 + I*b^3)*c^3)*(d*\sqrt{x} + c) + (48*(a^2*b - I*a*b^ \\
& 2)*(d*\sqrt{x} + c)^5 + 75*(a*b^2 - I*b^3 - 2*(a^2*b - I*a*b^2)*c)*(d*\sqrt{x} \\
&) + c)^4 + 200*((a^2*b - I*a*b^2)*c^2 - (a*b^2 - I*b^3)*c)*(d*\sqrt{x} + c)^ \\
& 3 - 75*(2*(a^2*b - I*a*b^2)*c^3 - 3*(a*b^2 - I*b^3)*c^2)*(d*\sqrt{x} + c)^2 \\
& + 75*((a^2*b - I*a*b^2)*c^4 - 2*(a*b^2 - I*b^3)*c^3)*(d*\sqrt{x} + c))*\cos(2 \\
& *d*\sqrt{x} + 2*c) - (48*(-I*a^2*b - a*b^2)*(d*\sqrt{x} + c)^5 + 75*(-I*a*b^2 \\
& - b^3 + 2*(I*a^2*b + a*b^2)*c)*(d*\sqrt{x} + c)^4 + 200*((-I*a^2*b - a*b^2) \\
& *c^2 + (I*a*b^2 + b^3)*c)*(d*\sqrt{x} + c)^3 + 75*(2*(I*a^2*b + a*b^2)*c^3 + \\
& 3*(-I*a*b^2 - b^3)*c^2)*(d*\sqrt{x} + c)^2 + 75*((-I*a^2*b - a*b^2)*c^4 + 2 \\
& *(I*a*b^2 + b^3)*c^3)*(d*\sqrt{x} + c))*\sin(2*d*\sqrt{x} + 2*c))*\log(((a^2 + \\
& b^2)*\cos(2*d*\sqrt{x} + 2*c)^2 + 4*a*b*\sin(2*d*\sqrt{x} + 2*c) + (a^2 + b^2)* \\
& \sin(2*d*\sqrt{x} + 2*c)^2 + a^2 + b^2 + 2*(a^2 - b^2)*\cos(2*d*\sqrt{x} + 2*c) \\
&))/(a^2 + b^2)) - 720*(I*a^2*b - a*b^2 + (I*a^2*b + a*b^2)*\cos(2*d*\sqrt{x} + \\
& 2*c) - (a^2*b - I*a*b^2)*\sin(2*d*\sqrt{x} + 2*c))*\operatorname{polylog}(6, (I*a + b)*e^{(2 \\
& *I*d*\sqrt{x} + 2*I*c)/(-I*a + b)}) - 90*(5*a*b^2 + 5*I*b^3 + 16*(a^2*b + I*a
\end{aligned}$$

```

*b^2)*(d*sqrt(x) + c) - 10*(a^2*b + I*a*b^2)*c + (5*a*b^2 - 5*I*b^3 + 16*(a
^2*b - I*a*b^2)*(d*sqrt(x) + c) - 10*(a^2*b - I*a*b^2)*c)*cos(2*d*sqrt(x) +
2*c) + (5*I*a*b^2 + 5*b^3 + 16*(I*a^2*b + a*b^2)*(d*sqrt(x) + c) + 10*(-I*
a^2*b - a*b^2)*c)*sin(2*d*sqrt(x) + 2*c))*polylog(5, (I*a + b)*e^(2*I*d*sqrt
(x) + 2*I*c)/(-I*a + b)) - 60*(24*(-I*a^2*b + a*b^2)*(d*sqrt(x) + c)^2 + 1
0*(-I*a^2*b + a*b^2)*c^2 + 15*(-I*a*b^2 + b^3 + 2*(I*a^2*b - a*b^2)*c)*(d*s
qrt(x) + c) + 10*(I*a*b^2 - b^3)*c + (24*(-I*a^2*b - a*b^2)*(d*sqrt(x) + c)
^2 + 10*(-I*a^2*b - a*b^2)*c^2 + 15*(-I*a*b^2 - b^3 + 2*(I*a^2*b + a*b^2)*c
)*(d*sqrt(x) + c) + 10*(I*a*b^2 + b^3)*c)*cos(2*d*sqrt(x) + 2*c) + (24*(a^2
*b - I*a*b^2)*(d*sqrt(x) + c)^2 + 10*(a^2*b - I*a*b^2)*c^2 + 15*(a*b^2 - I*
b^3 - 2*(a^2*b - I*a*b^2)*c)*(d*sqrt(x) + c) - 10*(a*b^2 - I*b^3)*c)*sin(2*
d*sqrt(x) + 2*c))*polylog(4, (I*a + b)*e^(2*I*d*sqrt(x) + 2*I*c)/(-I*a + b
) + 30*(32*(a^2*b + I*a*b^2)*(d*sqrt(x) + c)^3 - 10*(a^2*b + I*a*b^2)*c^3 +
30*(a*b^2 + I*b^3 - 2*(a^2*b + I*a*b^2)*c)*(d*sqrt(x) + c)^2 + 15*(a*b^2 +
I*b^3)*c^2 + 40*((a^2*b + I*a*b^2)*c^2 - (a*b^2 + I*b^3)*c)*(d*sqrt(x) + c
) + (32*(a^2*b - I*a*b^2)*(d*sqrt(x) + c)^3 - 10*(a^2*b - I*a*b^2)*c^3 + 30
*(a*b^2 - I*b^3 - 2*(a^2*b - I*a*b^2)*c)*(d*sqrt(x) + c)^2 + 15*(a*b^2 - I*
b^3)*c^2 + 40*((a^2*b - I*a*b^2)*c^2 - (a*b^2 - I*b^3)*c)*(d*sqrt(x) + c))*
cos(2*d*sqrt(x) + 2*c) - (32*(-I*a^2*b - a*b^2)*(d*sqrt(x) + c)^3 + 10*(I*a
^2*b + a*b^2)*c^3 + 30*(-I*a*b^2 - b^3 + 2*(I*a^2*b + a*b^2)*c)*(d*sqrt(x)
+ c)^2 + 15*(-I*a*b^2 - b^3)*c^2 + 40*((-I*a^2*b - a*b^2)*c^2 + (I*a*b^2 +
b^3)*c)*(d*sqrt(x) + c))*sin(2*d*sqrt(x) + 2*c))*polylog(3, (I*a + b)*e^(2*
I*d*sqrt(x) + 2*I*c)/(-I*a + b)) - 5*((-I*a^3 - 3*a^2*b + 3*I*a*b^2 + b^3)*
(d*sqrt(x) + c)^6 - 6*(2*a*b^2 - 2*I*b^3 - (I*a^3 + 3*a^2*b - 3*I*a*b^2 - b
^3)*c)*(d*sqrt(x) + c)^5 - 60*(a*b^2 - I*b^3)*(d*sqrt(x) + c)*c^4 + 15*((-I
*a^3 - 3*a^2*b + 3*I*a*b^2 + b^3)*c^2 + 4*(a*b^2 - I*b^3)*c)*(d*sqrt(x) + c
)^4 + 20*((I*a^3 + 3*a^2*b - 3*I*a*b^2 - b^3)*c^3 - 6*(a*b^2 - I*b^3)*c^2)*
(d*sqrt(x) + c)^3 + 15*((-I*a^3 - 3*a^2*b + 3*I*a*b^2 + b^3)*c^4 + 8*(a*b^2
- I*b^3)*c^3)*(d*sqrt(x) + c)^2)*sin(2*d*sqrt(x) + 2*c))/(a^5 + I*a^4*b +
2*a^3*b^2 + 2*I*a^2*b^3 + a*b^4 + I*b^5 + (a^5 - I*a^4*b + 2*a^3*b^2 - 2*I*
a^2*b^3 + a*b^4 - I*b^5)*cos(2*d*sqrt(x) + 2*c) - (-I*a^5 - a^4*b - 2*I*a^3
*b^2 - 2*a^2*b^3 - I*a*b^4 - b^5)*sin(2*d*sqrt(x) + 2*c))/d^6

```

Giac [F]

$$\int \frac{x^2}{(a + b \tan(c + d\sqrt{x}))^2} dx = \int \frac{x^2}{(b \tan(d\sqrt{x} + c) + a)^2} dx$$

[In] integrate(x^2/(a+b*tan(c+d*x^(1/2)))^2,x, algorithm="giac")

[Out] integrate(x^2/(b*tan(d*sqrt(x) + c) + a)^2, x)

Mupad [F(-1)]

Timed out.

$$\int \frac{x^2}{(a + b \tan(c + d\sqrt{x}))^2} dx = \int \frac{x^2}{(a + b \tan(c + d\sqrt{x}))^2} dx$$

```
[In] int(x^2/(a + b*tan(c + d*x^(1/2)))^2,x)
```

```
[Out] int(x^2/(a + b*tan(c + d*x^(1/2)))^2, x)
```

3.43 $\int \frac{x}{(a+b \tan(c+d\sqrt{x}))^2} dx$

Optimal result	261
Rubi [A] (verified)	262
Mathematica [A] (verified)	270
Maple [F]	270
Fricas [F]	271
Sympy [F]	271
Maxima [B] (verification not implemented)	271
Giac [F]	273
Mupad [F(-1)]	273

Optimal result

Integrand size = 18, antiderivative size = 787

$$\begin{aligned}
 \int \frac{x}{(a + b \tan(c + d\sqrt{x}))^2} dx = & -\frac{4ib^2x^{3/2}}{(a^2 + b^2)^2 d} \\
 & + \frac{4b^2x^{3/2}}{(a + ib)(ia + b)^2 d (ia - b + (ia + b)e^{2i(c+d\sqrt{x})})} \\
 & + \frac{x^2}{2(a - ib)^2} + \frac{2bx^2}{(ia - b)(a - ib)^2} \\
 & - \frac{2b^2x^2}{(a^2 + b^2)^2} + \frac{6b^2x \log\left(1 + \frac{(a-ib)e^{2i(c+d\sqrt{x})}}{a+ib}\right)}{(a^2 + b^2)^2 d^2} \\
 & + \frac{4bx^{3/2} \log\left(1 + \frac{(a-ib)e^{2i(c+d\sqrt{x})}}{a+ib}\right)}{(a - ib)^2(a + ib)d} \\
 & - \frac{4ib^2x^{3/2} \log\left(1 + \frac{(a-ib)e^{2i(c+d\sqrt{x})}}{a+ib}\right)}{(a^2 + b^2)^2 d} \\
 & - \frac{6ib^2\sqrt{x} \operatorname{PolyLog}\left(2, -\frac{(a-ib)e^{2i(c+d\sqrt{x})}}{a+ib}\right)}{(a^2 + b^2)^2 d^3} \\
 & + \frac{6bx \operatorname{PolyLog}\left(2, -\frac{(a-ib)e^{2i(c+d\sqrt{x})}}{a+ib}\right)}{(ia - b)(a - ib)^2 d^2} \\
 & - \frac{6b^2x \operatorname{PolyLog}\left(2, -\frac{(a-ib)e^{2i(c+d\sqrt{x})}}{a+ib}\right)}{(a^2 + b^2)^2 d^2} \\
 & + \frac{3b^2 \operatorname{PolyLog}\left(3, -\frac{(a-ib)e^{2i(c+d\sqrt{x})}}{a+ib}\right)}{(a^2 + b^2)^2 d^4} \\
 & + \frac{6b\sqrt{x} \operatorname{PolyLog}\left(3, -\frac{(a-ib)e^{2i(c+d\sqrt{x})}}{a+ib}\right)}{(a - ib)^2(a + ib)d^3} \\
 & - \frac{6ib^2\sqrt{x} \operatorname{PolyLog}\left(3, -\frac{(a-ib)e^{2i(c+d\sqrt{x})}}{a+ib}\right)}{(a^2 + b^2)^2 d^3} \\
 & - \frac{3b \operatorname{PolyLog}\left(4, -\frac{(a-ib)e^{2i(c+d\sqrt{x})}}{a+ib}\right)}{(ia - b)(a - ib)^2 d^4} \\
 & + \frac{3b^2 \operatorname{PolyLog}\left(4, -\frac{(a-ib)e^{2i(c+d\sqrt{x})}}{a+ib}\right)}{(a^2 + b^2)^2 d^4}
 \end{aligned}$$

[Out] $-6*I*b^2*polylog(2, -(a-I*b)*exp(2*I*(c+d*x^(1/2)))/(a+I*b))*x^(1/2)/(a^2+b^2)^2/d^3+4*b^2*x^(3/2)/(a+I*b)/(I*a+b)^2/d/(I*a-b+(I*a+b)*exp(2*I*(c+d*x^(1$

$$\begin{aligned}
& /2))) + 1/2 * x^2 / (a - I * b)^2 + 2 * b * x^2 / (I * a - b) / (a - I * b)^2 - 2 * b^2 * x^2 / (a^2 + b^2)^2 + 6 * \\
& b^2 * x * \ln(1 + (a - I * b) * \exp(2 * I * (c + d * x^{1/2}))) / (a + I * b) / (a^2 + b^2)^2 / d^2 + 4 * b * x^{3/2} * \ln(1 + (a - I * b) * \exp(2 * I * (c + d * x^{1/2}))) / (a + I * b) / (a - I * b)^2 / (a + I * b) / d - 6 * I * b^2 * \text{polylog}(3, -(a - I * b) * \exp(2 * I * (c + d * x^{1/2}))) / (a + I * b) * x^{1/2} / (a^2 + b^2)^2 / d^3 + 6 * b * x * \text{polylog}(2, -(a - I * b) * \exp(2 * I * (c + d * x^{1/2}))) / (a + I * b) / (I * a - b) / (a - I * b)^2 / d^2 - 6 * b^2 * x * \text{polylog}(2, -(a - I * b) * \exp(2 * I * (c + d * x^{1/2}))) / (a + I * b) / (a^2 + b^2)^2 / d^2 + 3 * b^2 * \text{polylog}(3, -(a - I * b) * \exp(2 * I * (c + d * x^{1/2}))) / (a + I * b) / (a^2 + b^2)^2 / d^4 - 3 * b * \text{polylog}(4, -(a - I * b) * \exp(2 * I * (c + d * x^{1/2}))) / (a + I * b) / (I * a - b) / (a - I * b)^2 / d^4 + 3 * b^2 * \text{polylog}(4, -(a - I * b) * \exp(2 * I * (c + d * x^{1/2}))) / (a + I * b) / (a^2 + b^2)^2 / d^4 - 4 * I * b^2 * x^{3/2} / (a^2 + b^2)^2 / d + 6 * b * \text{polylog}(3, -(a - I * b) * \exp(2 * I * (c + d * x^{1/2}))) / (a + I * b) * x^{1/2} / (a - I * b)^2 / (a + I * b) / d^3 - 4 * I * b^2 * x^{3/2} * \ln(1 + (a - I * b) * \exp(2 * I * (c + d * x^{1/2}))) / (a + I * b) / (a^2 + b^2)^2 / d
\end{aligned}$$

Rubi [A] (verified)

Time = 1.90 (sec) , antiderivative size = 787, normalized size of antiderivative = 1.00, number of steps used = 22, number of rules used = 10, $\frac{\text{number of rules}}{\text{integrand size}} = 0.556$, Rules

used = {3832, 3815, 2216, 2215, 2221, 2611, 6744, 2320, 6724, 2222}

$$\begin{aligned}
 \int \frac{x}{(a + b \tan(c + d\sqrt{x}))^2} dx = & \frac{3b^2 \operatorname{PolyLog}\left(3, -\frac{(a-ib)e^{2i(c+d\sqrt{x})}}{a+ib}\right)}{d^4(a^2 + b^2)^2} \\
 & + \frac{3b^2 \operatorname{PolyLog}\left(4, -\frac{(a-ib)e^{2i(c+d\sqrt{x})}}{a+ib}\right)}{d^4(a^2 + b^2)^2} \\
 & - \frac{6ib^2\sqrt{x} \operatorname{PolyLog}\left(2, -\frac{(a-ib)e^{2i(c+d\sqrt{x})}}{a+ib}\right)}{d^3(a^2 + b^2)^2} \\
 & - \frac{6ib^2\sqrt{x} \operatorname{PolyLog}\left(3, -\frac{(a-ib)e^{2i(c+d\sqrt{x})}}{a+ib}\right)}{d^3(a^2 + b^2)^2} \\
 & - \frac{6b^2x \operatorname{PolyLog}\left(2, -\frac{(a-ib)e^{2i(c+d\sqrt{x})}}{a+ib}\right)}{d^2(a^2 + b^2)^2} \\
 & + \frac{6b^2x \log\left(1 + \frac{(a-ib)e^{2i(c+d\sqrt{x})}}{a+ib}\right)}{d^2(a^2 + b^2)^2} \\
 & - \frac{4ib^2x^{3/2} \log\left(1 + \frac{(a-ib)e^{2i(c+d\sqrt{x})}}{a+ib}\right)}{d(a^2 + b^2)^2} \\
 & - \frac{4ib^2x^{3/2}}{d(a^2 + b^2)^2} - \frac{2b^2x^2}{(a^2 + b^2)^2} \\
 & + \frac{4b^2x^{3/2}}{d(a+ib)(b+ia)^2((b+ia)e^{2i(c+d\sqrt{x})} + ia - b)} \\
 & - \frac{3b \operatorname{PolyLog}\left(4, -\frac{(a-ib)e^{2i(c+d\sqrt{x})}}{a+ib}\right)}{d^4(-b+ia)(a-ib)^2} \\
 & + \frac{6b\sqrt{x} \operatorname{PolyLog}\left(3, -\frac{(a-ib)e^{2i(c+d\sqrt{x})}}{a+ib}\right)}{d^3(a-ib)^2(a+ib)} \\
 & + \frac{6bx \operatorname{PolyLog}\left(2, -\frac{(a-ib)e^{2i(c+d\sqrt{x})}}{a+ib}\right)}{d^2(-b+ia)(a-ib)^2} \\
 & + \frac{4bx^{3/2} \log\left(1 + \frac{(a-ib)e^{2i(c+d\sqrt{x})}}{a+ib}\right)}{d(a-ib)^2(a+ib)} \\
 & + \frac{2bx^2}{(-b+ia)(a-ib)^2} + \frac{x^2}{2(a-ib)^2}
 \end{aligned}$$

[In] Int[x/(a + b*Tan[c + d*Sqrt[x]])^2,x]

[Out] ((-4*I)*b^2*x^(3/2))/((a^2 + b^2)^2*d) + (4*b^2*x^(3/2))/((a + I*b)*(I*a + b)^2*d*(I*a - b + (I*a + b)*E^((2*I)*(c + d*Sqrt[x])))) + x^2/(2*(a - I*b)^2)

$$\begin{aligned}
& 2) + (2*b*x^2)/((I*a - b)*(a - I*b)^2) - (2*b^2*x^2)/(a^2 + b^2)^2 + (6*b^2 \\
& *x*\text{Log}[1 + ((a - I*b)*E^{(2*I)*(c + d*\text{Sqrt}[x])})]/(a + I*b)]/((a^2 + b^2)^2 \\
& *d^2) + (4*b*x^{(3/2)}*\text{Log}[1 + ((a - I*b)*E^{(2*I)*(c + d*\text{Sqrt}[x])})]/(a + I*b \\
&)]/((a - I*b)^2*(a + I*b)*d) - ((4*I)*b^2*x^{(3/2)}*\text{Log}[1 + ((a - I*b)*E^{(2 \\
& *I)*(c + d*\text{Sqrt}[x])})]/(a + I*b)]/((a^2 + b^2)^2*d) - ((6*I)*b^2*\text{Sqrt}[x]*\text{Po \\
& lyLog}[2, -((a - I*b)*E^{(2*I)*(c + d*\text{Sqrt}[x])})]/(a + I*b)]/((a^2 + b^2)^ \\
& 2*d^3) + (6*b*x*\text{PolyLog}[2, -((a - I*b)*E^{(2*I)*(c + d*\text{Sqrt}[x])})]/(a + I*b \\
&))]/((I*a - b)*(a - I*b)^2*d^2) - (6*b^2*x*\text{PolyLog}[2, -((a - I*b)*E^{(2*I \\
&)*(c + d*\text{Sqrt}[x])})]/(a + I*b)]/((a^2 + b^2)^2*d^2) + (3*b^2*\text{PolyLog}[3, -(\\
& ((a - I*b)*E^{(2*I)*(c + d*\text{Sqrt}[x])})]/(a + I*b)]/((a^2 + b^2)^2*d^4) + (6 \\
& *b*\text{Sqrt}[x]*\text{PolyLog}[3, -((a - I*b)*E^{(2*I)*(c + d*\text{Sqrt}[x])})]/(a + I*b)]/ \\
& ((a - I*b)^2*(a + I*b)*d^3) - ((6*I)*b^2*\text{Sqrt}[x]*\text{PolyLog}[3, -((a - I*b)*E^{ \\
& (2*I)*(c + d*\text{Sqrt}[x])})]/(a + I*b)]/((a^2 + b^2)^2*d^3) - (3*b*\text{PolyLog}[4, \\
& -((a - I*b)*E^{(2*I)*(c + d*\text{Sqrt}[x])})]/(a + I*b)]/((I*a - b)*(a - I*b)^ \\
& 2*d^4) + (3*b^2*\text{PolyLog}[4, -((a - I*b)*E^{(2*I)*(c + d*\text{Sqrt}[x])})]/(a + I*b \\
&))]/((a^2 + b^2)^2*d^4)
\end{aligned}$$

Rule 2215

$$\text{Int}[\{(c_.) + (d_.)*(x_)\}^{(m_)} / \{(a_.) + (b_.)*((F_)^{(g_.)*((e_.) + (f_.)*(x_)\}))^{(n_)}\}, x_Symbol] \rightarrow \text{Simp}[(c + d*x)^{(m + 1)} / (a*d*(m + 1)), x] - \text{Dist}[b/a, \text{Int}[(c + d*x)^m * (F^{(g*(e + f*x))})^n / (a + b*(F^{(g*(e + f*x))})^n), x], x] /; \text{FreeQ}\{F, a, b, c, d, e, f, g, n\}, x\} \&\& \text{IGtQ}[m, 0]$$

Rule 2216

$$\text{Int}[\{(a_.) + (b_.)*((F_)^{(g_.)*((e_.) + (f_.)*(x_)\}))^{(n_)}\}^{(p_)} * \{(c_.) + (d_.)*(x_)\}^{(m_)}, x_Symbol] \rightarrow \text{Dist}[1/a, \text{Int}[(c + d*x)^m * (a + b*(F^{(g*(e + f*x))})^n)^{(p + 1)}, x], x] - \text{Dist}[b/a, \text{Int}[(c + d*x)^m * (F^{(g*(e + f*x))})^n * (a + b*(F^{(g*(e + f*x))})^n)^p, x], x] /; \text{FreeQ}\{F, a, b, c, d, e, f, g, n\}, x\} \&\& \text{ILtQ}[p, 0] \&\& \text{IGtQ}[m, 0]$$

Rule 2221

$$\text{Int}[\{(F_)^{(g_.)*((e_.) + (f_.)*(x_)\}))^{(n_)} * \{(c_.) + (d_.)*(x_)\}^{(m_)}\} / \{(a_.) + (b_.)*((F_)^{(g_.)*((e_.) + (f_.)*(x_)\}))^{(n_)}\}, x_Symbol] \rightarrow \text{Simp}[\{(c + d*x)^m / (b*f*g*n*\text{Log}[F])\} * \text{Log}[1 + b*((F^{(g*(e + f*x))})^n/a)], x] - \text{Dist}[d*(m/(b*f*g*n*\text{Log}[F])), \text{Int}[(c + d*x)^{(m - 1)} * \text{Log}[1 + b*((F^{(g*(e + f*x))})^n/a)], x], x] /; \text{FreeQ}\{F, a, b, c, d, e, f, g, n\}, x\} \&\& \text{IGtQ}[m, 0]$$

Rule 2222

$$\text{Int}[\{(F_)^{(g_.)*((e_.) + (f_.)*(x_)\}))^{(n_)} * \{(a_.) + (b_.)*((F_)^{(g_.)*((e_.) + (f_.)*(x_)\}))^{(n_)}\}^{(p_)} * \{(c_.) + (d_.)*(x_)\}^{(m_)}, x_Symbol] \rightarrow \text{Simp}[(c + d*x)^m * (a + b*(F^{(g*(e + f*x))})^n)^{(p + 1)} / (b*f*g*n*(p + 1)*\text{Log}[F]), x] - \text{Dist}[d*(m/(b*f*g*n*(p + 1)*\text{Log}[F])), \text{Int}[(c + d*x)^{(m - 1)} * (a + b*(F^{(g*(e + f*x))})^n)^{(p + 1)}, x], x] /; \text{FreeQ}\{F, a, b, c, d, e, f, g, m$$

, n, p}, x] && NeQ[p, -1]

Rule 2320

```
Int[u_, x_Symbol] := With[{v = FunctionOfExponential[u, x]}, Dist[v/D[v, x]
, Subst[Int[FunctionOfExponentialFunction[u, x]/x, x], x, v], x] /; Functi
onOfExponentialQ[u, x] && !MatchQ[u, (w_)*((a_.)*(v_)^(n_))^(m_)] /; FreeQ[
{a, m, n}, x] && IntegerQ[m*n] && !MatchQ[u, E^((c_.)*((a_.) + (b_.)*x))*
(F_) [v_] /; FreeQ[{a, b, c}, x] && InverseFunctionQ[F[x]]]
```

Rule 2611

```
Int[Log[1 + (e_.)*((F_)^((c_.)*((a_.) + (b_.)*(x_))))^(n_.)]*((f_.) + (g_.)
*(x_)^(m_.), x_Symbol] := Simp[(-f + g*x)^m*(PolyLog[2, (-e)*(F^(c*(a +
b*x)))^n]/(b*c*n*Log[F])), x] + Dist[g*(m/(b*c*n*Log[F])), Int[(f + g*x)^(m
- 1)*PolyLog[2, (-e)*(F^(c*(a + b*x)))^n], x], x] /; FreeQ[{F, a, b, c, e,
f, g, n}, x] && GtQ[m, 0]
```

Rule 3815

```
Int[((c_.) + (d_.)*(x_))^(m_.)*((a_) + (b_.)*tan[(e_.) + (f_.)*(x_)])^(n_),
x_Symbol] := Int[ExpandIntegrand[(c + d*x)^m, (1/(a - I*b) - 2*I*(b/(a^2 +
b^2 + (a - I*b)^2*E^(2*I*(e + f*x))))^(-n), x], x] /; FreeQ[{a, b, c, d,
e, f}, x] && NeQ[a^2 + b^2, 0] && ILtQ[n, 0] && IGtQ[m, 0]
```

Rule 3832

```
Int[(x_)^(m_.)*((a_.) + (b_.)*Tan[(c_.) + (d_.)*(x_)^(n_)])^(p_.), x_Symbol
] := Dist[1/n, Subst[Int[x^(Simplify[(m + 1)/n] - 1)*(a + b*Tan[c + d*x])^p
, x], x, x^n], x] /; FreeQ[{a, b, c, d, m, n, p}, x] && IGtQ[Simplify[(m +
1)/n], 0] && IntegerQ[p]
```

Rule 6724

```
Int[PolyLog[n_, (c_.)*((a_.) + (b_.)*(x_))^(p_.)]/((d_.) + (e_.)*(x_)), x_S
ymbol] := Simp[PolyLog[n + 1, c*(a + b*x)^p]/(e*p), x] /; FreeQ[{a, b, c, d
, e, n, p}, x] && EqQ[b*d, a*e]
```

Rule 6744

```
Int[((e_.) + (f_.)*(x_))^(m_.)*PolyLog[n_, (d_.)*((F_)^((c_.)*((a_.) + (b_.)
*(x_))))^(p_.)], x_Symbol] := Simp[(e + f*x)^m*(PolyLog[n + 1, d*(F^(c*(a
+ b*x)))^p]/(b*c*p*Log[F])), x] - Dist[f*(m/(b*c*p*Log[F])), Int[(e + f*x)^(
m - 1)*PolyLog[n + 1, d*(F^(c*(a + b*x)))^p], x], x] /; FreeQ[{F, a, b, c,
d, e, f, n, p}, x] && GtQ[m, 0]
```

Rubi steps

$$\begin{aligned}
\text{integral} &= 2\text{Subst}\left(\int \frac{x^3}{(a + b \tan(c + dx))^2} dx, x, \sqrt{x}\right) \\
&= 2\text{Subst}\left(\int \left(\frac{x^3}{(a - ib)^2} - \frac{4b^2x^3}{(ia + b)^2 (ia(1 + \frac{ib}{a}) + ia(1 - \frac{ib}{a})e^{2ic+2idx})^2}\right.\right. \\
&\quad \left.\left. + \frac{4bx^3}{(a - ib)^2 (ia(1 + \frac{ib}{a}) + ia(1 - \frac{ib}{a})e^{2ic+2idx})}\right) dx, x, \sqrt{x}\right) \\
&= \frac{x^2}{2(a - ib)^2} + \frac{(8b)\text{Subst}\left(\int \frac{x^3}{ia(1 + \frac{ib}{a}) + ia(1 - \frac{ib}{a})e^{2ic+2idx}} dx, x, \sqrt{x}\right)}{(a - ib)^2} \\
&\quad - \frac{(8b^2)\text{Subst}\left(\int \frac{x^3}{(ia(1 + \frac{ib}{a}) + ia(1 - \frac{ib}{a})e^{2ic+2idx})^2} dx, x, \sqrt{x}\right)}{(ia + b)^2} \\
&= \frac{x^2}{2(a - ib)^2} + \frac{2bx^2}{(ia - b)(a - ib)^2} + \frac{(8b^2)\text{Subst}\left(\int \frac{x^3}{ia(1 + \frac{ib}{a}) + ia(1 - \frac{ib}{a})e^{2ic+2idx}} dx, x, \sqrt{x}\right)}{(ia - b)(a - ib)^2} \\
&\quad - \frac{(8b)\text{Subst}\left(\int \frac{e^{2ic+2idx}x^3}{ia(1 + \frac{ib}{a}) + ia(1 - \frac{ib}{a})e^{2ic+2idx}} dx, x, \sqrt{x}\right)}{a^2 + b^2} \\
&\quad - \frac{(8b^2)\text{Subst}\left(\int \frac{e^{2ic+2idx}x^3}{(ia(1 + \frac{ib}{a}) + ia(1 - \frac{ib}{a})e^{2ic+2idx})^2} dx, x, \sqrt{x}\right)}{a^2 + b^2} \\
&= -\frac{4b^2x^{3/2}}{(a - ib)^2(a + ib)d(ia - b + (ia + b)e^{2i(c+d\sqrt{x})})} + \frac{x^2}{2(a - ib)^2} \\
&\quad + \frac{2bx^2}{(ia - b)(a - ib)^2} - \frac{2b^2x^2}{(a^2 + b^2)^2} + \frac{4bx^{3/2} \log\left(1 + \frac{(a-ib)e^{2i(c+d\sqrt{x})}}{a+ib}\right)}{(a - ib)^2(a + ib)d} \\
&\quad - \frac{(8b^2)\text{Subst}\left(\int \frac{e^{2ic+2idx}x^3}{ia(1 + \frac{ib}{a}) + ia(1 - \frac{ib}{a})e^{2ic+2idx}} dx, x, \sqrt{x}\right)}{(a + ib)^2(ia + b)} \\
&\quad - \frac{(12b)\text{Subst}\left(\int x^2 \log\left(1 + \frac{(1 - \frac{ib}{a})e^{2ic+2idx}}{1 + \frac{ib}{a}}\right) dx, x, \sqrt{x}\right)}{(a - ib)^2(a + ib)d} \\
&\quad + \frac{(12b^2)\text{Subst}\left(\int \frac{x^2}{ia(1 + \frac{ib}{a}) + ia(1 - \frac{ib}{a})e^{2ic+2idx}} dx, x, \sqrt{x}\right)}{(a - ib)^2(a + ib)d}
\end{aligned}$$

$$\begin{aligned}
&= -\frac{4ib^2x^{3/2}}{(a^2+b^2)^2d} - \frac{4b^2x^{3/2}}{(a-ib)^2(a+ib)d} \frac{e^{2i(c+d\sqrt{x})}}{(ia-b+(ia+b)e^{2i(c+d\sqrt{x})})} + \frac{x^2}{2(a-ib)^2} \\
&+ \frac{2bx^2}{(ia-b)(a-ib)^2} - \frac{2b^2x^2}{(a^2+b^2)^2} + \frac{4bx^{3/2} \log\left(1 + \frac{(a-ib)e^{2i(c+d\sqrt{x})}}{a+ib}\right)}{(a-ib)^2(a+ib)d} \\
&- \frac{4ib^2x^{3/2} \log\left(1 + \frac{(a-ib)e^{2i(c+d\sqrt{x})}}{a+ib}\right)}{(a^2+b^2)^2d} + \frac{6bx \operatorname{PolyLog}\left(2, -\frac{(a-ib)e^{2i(c+d\sqrt{x})}}{a+ib}\right)}{(ia-b)(a-ib)^2d^2} \\
&- \frac{(12b) \operatorname{Subst}\left(\int x \operatorname{PolyLog}\left(2, -\frac{\left(1-\frac{ib}{a}\right)e^{2ic+2idx}}{1+\frac{ib}{a}}\right) dx, x, \sqrt{x}\right)}{(ia-b)(a-ib)^2d^2} \\
&- \frac{(12b^2) \operatorname{Subst}\left(\int \frac{e^{2ic+2idx}x^2}{ia\left(1+\frac{ib}{a}\right)+ia\left(1-\frac{ib}{a}\right)e^{2ic+2idx}} dx, x, \sqrt{x}\right)}{(a-ib)(a+ib)^2d} \\
&+ \frac{(12ib^2) \operatorname{Subst}\left(\int x^2 \log\left(1 + \frac{\left(1-\frac{ib}{a}\right)e^{2ic+2idx}}{1+\frac{ib}{a}}\right) dx, x, \sqrt{x}\right)}{(a^2+b^2)^2d} \\
&= -\frac{4ib^2x^{3/2}}{(a^2+b^2)^2d} - \frac{4b^2x^{3/2}}{(a-ib)^2(a+ib)d} \frac{e^{2i(c+d\sqrt{x})}}{(ia-b+(ia+b)e^{2i(c+d\sqrt{x})})} \\
&+ \frac{x^2}{2(a-ib)^2} + \frac{2bx^2}{(ia-b)(a-ib)^2} - \frac{2b^2x^2}{(a^2+b^2)^2} \\
&+ \frac{6b^2x \log\left(1 + \frac{(a-ib)e^{2i(c+d\sqrt{x})}}{a+ib}\right)}{(a^2+b^2)^2d^2} + \frac{4bx^{3/2} \log\left(1 + \frac{(a-ib)e^{2i(c+d\sqrt{x})}}{a+ib}\right)}{(a-ib)^2(a+ib)d} \\
&- \frac{4ib^2x^{3/2} \log\left(1 + \frac{(a-ib)e^{2i(c+d\sqrt{x})}}{a+ib}\right)}{(a^2+b^2)^2d} + \frac{6bx \operatorname{PolyLog}\left(2, -\frac{(a-ib)e^{2i(c+d\sqrt{x})}}{a+ib}\right)}{(ia-b)(a-ib)^2d^2} \\
&- \frac{6b^2x \operatorname{PolyLog}\left(2, -\frac{(a-ib)e^{2i(c+d\sqrt{x})}}{a+ib}\right)}{(a^2+b^2)^2d^2} + \frac{6b\sqrt{x} \operatorname{PolyLog}\left(3, -\frac{(a-ib)e^{2i(c+d\sqrt{x})}}{a+ib}\right)}{(a-ib)^2(a+ib)d^3} \\
&- \frac{(6b) \operatorname{Subst}\left(\int \operatorname{PolyLog}\left(3, -\frac{\left(1-\frac{ib}{a}\right)e^{2ic+2idx}}{1+\frac{ib}{a}}\right) dx, x, \sqrt{x}\right)}{(a-ib)^2(a+ib)d^3} \\
&- \frac{(12b^2) \operatorname{Subst}\left(\int x \log\left(1 + \frac{\left(1-\frac{ib}{a}\right)e^{2ic+2idx}}{1+\frac{ib}{a}}\right) dx, x, \sqrt{x}\right)}{(a^2+b^2)^2d^2} \\
&+ \frac{(12b^2) \operatorname{Subst}\left(\int x \operatorname{PolyLog}\left(2, -\frac{\left(1-\frac{ib}{a}\right)e^{2ic+2idx}}{1+\frac{ib}{a}}\right) dx, x, \sqrt{x}\right)}{(a^2+b^2)^2d^2}
\end{aligned}$$

$$\begin{aligned}
&= -\frac{4ib^2x^{3/2}}{(a^2+b^2)^2d} - \frac{4b^2x^{3/2}}{(a-ib)^2(a+ib)d(ia-b+(ia+b)e^{2i(c+d\sqrt{x})})} \\
&+ \frac{x^2}{2(a-ib)^2} + \frac{2bx^2}{(ia-b)(a-ib)^2} - \frac{2b^2x^2}{(a^2+b^2)^2} \\
&+ \frac{6b^2x \log\left(1 + \frac{(a-ib)e^{2i(c+d\sqrt{x})}}{a+ib}\right)}{(a^2+b^2)^2d^2} + \frac{4bx^{3/2} \log\left(1 + \frac{(a-ib)e^{2i(c+d\sqrt{x})}}{a+ib}\right)}{(a-ib)^2(a+ib)d} \\
&- \frac{4ib^2x^{3/2} \log\left(1 + \frac{(a-ib)e^{2i(c+d\sqrt{x})}}{a+ib}\right)}{(a^2+b^2)^2d} - \frac{6ib^2\sqrt{x} \operatorname{PolyLog}\left(2, -\frac{(a-ib)e^{2i(c+d\sqrt{x})}}{a+ib}\right)}{(a^2+b^2)^2d^3} \\
&+ \frac{6bx \operatorname{PolyLog}\left(2, -\frac{(a-ib)e^{2i(c+d\sqrt{x})}}{a+ib}\right)}{(ia-b)(a-ib)^2d^2} - \frac{6b^2x \operatorname{PolyLog}\left(2, -\frac{(a-ib)e^{2i(c+d\sqrt{x})}}{a+ib}\right)}{(a^2+b^2)^2d^2} \\
&+ \frac{6b\sqrt{x} \operatorname{PolyLog}\left(3, -\frac{(a-ib)e^{2i(c+d\sqrt{x})}}{a+ib}\right)}{(a-ib)^2(a+ib)d^3} - \frac{6ib^2\sqrt{x} \operatorname{PolyLog}\left(3, -\frac{(a-ib)e^{2i(c+d\sqrt{x})}}{a+ib}\right)}{(a^2+b^2)^2d^3} \\
&- \frac{(3b) \operatorname{Subst}\left(\int \frac{\operatorname{PolyLog}\left(3, -\frac{(a-ib)x}{a+ib}\right)}{x} dx, x, e^{2i(c+d\sqrt{x})}\right)}{(ia-b)(a-ib)^2d^4} \\
&+ \frac{(6ib^2) \operatorname{Subst}\left(\int \operatorname{PolyLog}\left(2, -\frac{\left(1-\frac{ib}{a}\right)e^{2ic+2idx}}{1+\frac{ib}{a}}\right) dx, x, \sqrt{x}\right)}{(a^2+b^2)^2d^3} \\
&+ \frac{(6ib^2) \operatorname{Subst}\left(\int \operatorname{PolyLog}\left(3, -\frac{\left(1-\frac{ib}{a}\right)e^{2ic+2idx}}{1+\frac{ib}{a}}\right) dx, x, \sqrt{x}\right)}{(a^2+b^2)^2d^3}
\end{aligned}$$

$$\begin{aligned}
&= -\frac{4ib^2x^{3/2}}{(a^2+b^2)^2d} - \frac{4b^2x^{3/2}}{(a-ib)^2(a+ib)d} \frac{ia-b+(ia+b)e^{2i(c+d\sqrt{x})}}{(a^2+b^2)^2d^2} + \frac{x^2}{2(a-ib)^2} \\
&+ \frac{2bx^2}{(ia-b)(a-ib)^2} - \frac{2b^2x^2}{(a^2+b^2)^2} + \frac{6b^2x \log\left(1 + \frac{(a-ib)e^{2i(c+d\sqrt{x})}}{a+ib}\right)}{(a^2+b^2)^2d^2} \\
&+ \frac{4bx^{3/2} \log\left(1 + \frac{(a-ib)e^{2i(c+d\sqrt{x})}}{a+ib}\right)}{(a-ib)^2(a+ib)d} - \frac{4ib^2x^{3/2} \log\left(1 + \frac{(a-ib)e^{2i(c+d\sqrt{x})}}{a+ib}\right)}{(a^2+b^2)^2d} \\
&- \frac{6ib^2\sqrt{x} \operatorname{PolyLog}\left(2, -\frac{(a-ib)e^{2i(c+d\sqrt{x})}}{a+ib}\right)}{(a^2+b^2)^2d^3} + \frac{6bx \operatorname{PolyLog}\left(2, -\frac{(a-ib)e^{2i(c+d\sqrt{x})}}{a+ib}\right)}{(ia-b)(a-ib)^2d^2} \\
&- \frac{6b^2x \operatorname{PolyLog}\left(2, -\frac{(a-ib)e^{2i(c+d\sqrt{x})}}{a+ib}\right)}{(a^2+b^2)^2d^2} + \frac{6b\sqrt{x} \operatorname{PolyLog}\left(3, -\frac{(a-ib)e^{2i(c+d\sqrt{x})}}{a+ib}\right)}{(a-ib)^2(a+ib)d^3} \\
&- \frac{6ib^2\sqrt{x} \operatorname{PolyLog}\left(3, -\frac{(a-ib)e^{2i(c+d\sqrt{x})}}{a+ib}\right)}{(a^2+b^2)^2d^3} - \frac{3b \operatorname{PolyLog}\left(4, -\frac{(a-ib)e^{2i(c+d\sqrt{x})}}{a+ib}\right)}{(ia-b)(a-ib)^2d^4} \\
&+ \frac{(3b^2) \operatorname{Subst}\left(\int \frac{\operatorname{PolyLog}\left(2, -\frac{(a-ib)x}{a+ib}\right)}{x} dx, x, e^{2i(c+d\sqrt{x})}\right)}{(a^2+b^2)^2d^4} \\
&+ \frac{(3b^2) \operatorname{Subst}\left(\int \frac{\operatorname{PolyLog}\left(3, -\frac{(a-ib)x}{a+ib}\right)}{x} dx, x, e^{2i(c+d\sqrt{x})}\right)}{(a^2+b^2)^2d^4} \\
&= -\frac{4ib^2x^{3/2}}{(a^2+b^2)^2d} - \frac{4b^2x^{3/2}}{(a-ib)^2(a+ib)d} \frac{ia-b+(ia+b)e^{2i(c+d\sqrt{x})}}{(a^2+b^2)^2d^2} + \frac{x^2}{2(a-ib)^2} \\
&+ \frac{2bx^2}{(ia-b)(a-ib)^2} - \frac{2b^2x^2}{(a^2+b^2)^2} + \frac{6b^2x \log\left(1 + \frac{(a-ib)e^{2i(c+d\sqrt{x})}}{a+ib}\right)}{(a^2+b^2)^2d^2} \\
&+ \frac{4bx^{3/2} \log\left(1 + \frac{(a-ib)e^{2i(c+d\sqrt{x})}}{a+ib}\right)}{(a-ib)^2(a+ib)d} - \frac{4ib^2x^{3/2} \log\left(1 + \frac{(a-ib)e^{2i(c+d\sqrt{x})}}{a+ib}\right)}{(a^2+b^2)^2d} \\
&- \frac{6ib^2\sqrt{x} \operatorname{PolyLog}\left(2, -\frac{(a-ib)e^{2i(c+d\sqrt{x})}}{a+ib}\right)}{(a^2+b^2)^2d^3} + \frac{6bx \operatorname{PolyLog}\left(2, -\frac{(a-ib)e^{2i(c+d\sqrt{x})}}{a+ib}\right)}{(ia-b)(a-ib)^2d^2} \\
&- \frac{6b^2x \operatorname{PolyLog}\left(2, -\frac{(a-ib)e^{2i(c+d\sqrt{x})}}{a+ib}\right)}{(a^2+b^2)^2d^2} + \frac{3b^2 \operatorname{PolyLog}\left(3, -\frac{(a-ib)e^{2i(c+d\sqrt{x})}}{a+ib}\right)}{(a^2+b^2)^2d^4} \\
&+ \frac{6b\sqrt{x} \operatorname{PolyLog}\left(3, -\frac{(a-ib)e^{2i(c+d\sqrt{x})}}{a+ib}\right)}{(a-ib)^2(a+ib)d^3} - \frac{6ib^2\sqrt{x} \operatorname{PolyLog}\left(3, -\frac{(a-ib)e^{2i(c+d\sqrt{x})}}{a+ib}\right)}{(a^2+b^2)^2d^3} \\
&- \frac{3b \operatorname{PolyLog}\left(4, -\frac{(a-ib)e^{2i(c+d\sqrt{x})}}{a+ib}\right)}{(ia-b)(a-ib)^2d^4} + \frac{3b^2 \operatorname{PolyLog}\left(4, -\frac{(a-ib)e^{2i(c+d\sqrt{x})}}{a+ib}\right)}{(a^2+b^2)^2d^4}
\end{aligned}$$

Mathematica [A] (verified)

Time = 2.62 (sec) , antiderivative size = 662, normalized size of antiderivative = 0.84

$$\int \frac{x}{(a + b \tan(c + d\sqrt{x}))^2} dx$$

$$= \frac{2ib \left(4(a+ib)b(ia+b)d^3 x^{3/2} + 2a(a+ib)(ia+b)d^4 x^2 + 6(a-ib)bd^2 (-ib(-1+e^{2ic}) + a(1+e^{2ic}))x \log \left(1 + \frac{(a+ib)e^{-2i(c+d\sqrt{x})}}{a-ib} \right) + 4a(a-ib)d^3 (-ib(-1+e^{2ic}) + a(1+e^{2ic})) \right)}{(a+ib)^2 (a-ib)^2}$$

[In] Integrate[x/(a + b*Tan[c + d*Sqrt[x]])^2,x]

```
[Out] (((-2*I)*b*(4*(a + I*b)*b*(I*a + b)*d^3*x^(3/2) + 2*a*(a + I*b)*(I*a + b)*d^4*x^2 + 6*(a - I*b)*b*d^2*((-I)*b*(-1 + E^((2*I)*c)) + a*(1 + E^((2*I)*c))) *x*Log[1 + (a + I*b)/((a - I*b)*E^((2*I)*(c + d*Sqrt[x])))] + 4*a*(a - I*b)*d^3*((-I)*b*(-1 + E^((2*I)*c)) + a*(1 + E^((2*I)*c))) *x^(3/2)*Log[1 + (a + I*b)/((a - I*b)*E^((2*I)*(c + d*Sqrt[x])))] + 3*(a - I*b)*b*((-I)*b*(-1 + E^((2*I)*c)) + a*(1 + E^((2*I)*c))) *((2*I)*d*Sqrt[x]*PolyLog[2, (-a - I*b)/((a - I*b)*E^((2*I)*(c + d*Sqrt[x])))] + PolyLog[3, (-a - I*b)/((a - I*b)*E^((2*I)*(c + d*Sqrt[x])))] + 3*a*(a - I*b)*((-I)*b*(-1 + E^((2*I)*c)) + a*(1 + E^((2*I)*c))) *((2*I)*d^2*x*PolyLog[2, (-a - I*b)/((a - I*b)*E^((2*I)*(c + d*Sqrt[x])))] + 2*d*Sqrt[x]*PolyLog[3, (-a - I*b)/((a - I*b)*E^((2*I)*(c + d*Sqrt[x])))] - I*PolyLog[4, (-a - I*b)/((a - I*b)*E^((2*I)*(c + d*Sqrt[x])))])))/(d^4*(b - b*E^((2*I)*c) - I*a*(1 + E^((2*I)*c))) + ((a - I*b)^2*(a + I*b)*x^2*(a*Cos[c] - b*Sin[c])/(a*Cos[c] + b*Sin[c]) + (4*(a - I*b)^2*(a + I*b)*b^2*x^(3/2)*Sin[d*Sqrt[x]])/(d*(a*Cos[c] + b*Sin[c])*(a*Cos[c + d*Sqrt[x]] + b*Sin[c + d*Sqrt[x])))/(2*(a - I*b)^3*(a + I*b)^2)
```

Maple [F]

$$\int \frac{x}{(a + b \tan(c + d\sqrt{x}))^2} dx$$

[In] int(x/(a+b*tan(c+d*x^(1/2)))^2,x)

[Out] int(x/(a+b*tan(c+d*x^(1/2)))^2,x)

$$\begin{aligned}
& 3)*c)*(d*\sqrt{x} + c))*\cos(2*d*\sqrt{x} + 2*c) - (8*(a^2*b - I*a*b^2)*(d*\sqrt{x} + c)^3 + 9*(a*b^2 - I*b^3 - 2*(a^2*b - I*a*b^2)*c)*(d*\sqrt{x} + c)^2 + \\
& 18*((a^2*b - I*a*b^2)*c^2 - (a*b^2 - I*b^3)*c)*(d*\sqrt{x} + c))*\sin(2*d*\sqrt{x} + 2*c))*\arctan2((2*a*b*\cos(2*d*\sqrt{x} + 2*c) - (a^2 - b^2)*\sin(2*d*\sqrt{x} + 2*c))/(a^2 + b^2), (2*a*b*\sin(2*d*\sqrt{x} + 2*c) + a^2 + b^2 + (a^2 - b^2)*\cos(2*d*\sqrt{x} + 2*c))/(a^2 + b^2)) + 3*((a^3 - 3*I*a^2*b - 3*a*b^2 + I*b^3)*(d*\sqrt{x} + c)^4 - 4*(2*I*a*b^2 + 2*b^3 + (a^3 - 3*I*a^2*b - 3*a*b^2 + I*b^3)*c)*(d*\sqrt{x} + c)^3 - 24*(I*a*b^2 + b^3)*(d*\sqrt{x} + c)*c^2 + 6*((a^3 - 3*I*a^2*b - 3*a*b^2 + I*b^3)*c^2 - 4*(-I*a*b^2 - b^3)*c)*(d*\sqrt{x} + c)^2)*\cos(2*d*\sqrt{x} + 2*c) - 12*(4*(I*a^2*b - a*b^2)*(d*\sqrt{x} + c)^2 + 3*(I*a^2*b - a*b^2)*c^2 + 3*(I*a*b^2 - b^3 + 2*(-I*a^2*b + a*b^2)*c)*(d*\sqrt{x} + c) + 3*(-I*a*b^2 + b^3)*c + (4*(I*a^2*b + a*b^2)*(d*\sqrt{x} + c)^2 + 3*(I*a^2*b + a*b^2)*c^2 + 3*(I*a*b^2 + b^3 + 2*(-I*a^2*b - a*b^2)*c)*(d*\sqrt{x} + c) + 3*(-I*a*b^2 - b^3)*c)*\cos(2*d*\sqrt{x} + 2*c) - (4*(a^2*b - I*a*b^2)*(d*\sqrt{x} + c)^2 + 3*(a^2*b - I*a*b^2)*c^2 + 3*(a*b^2 - I*b^3 - 2*(a^2*b - I*a*b^2)*c)*(d*\sqrt{x} + c) - 3*(a*b^2 - I*b^3)*c)*\sin(2*d*\sqrt{x} + 2*c))*\operatorname{dilog}((I*a + b)*e^{(2*I*d*\sqrt{x} + 2*I*c)/(-I*a + b)}) + 18*((a*b^2 - I*b^3)*c^2*\cos(2*d*\sqrt{x} + 2*c) - (-I*a*b^2 - b^3)*c^2*\sin(2*d*\sqrt{x} + 2*c) + (a*b^2 + I*b^3)*c^2)*\log((a^2 + b^2)*\cos(2*d*\sqrt{x} + 2*c)^2 + 4*a*b*\sin(2*d*\sqrt{x} + 2*c) + (a^2 + b^2)*\sin(2*d*\sqrt{x} + 2*c)^2 + a^2 + b^2 + 2*(a^2 - b^2)*\cos(2*d*\sqrt{x} + 2*c)) + 2*(8*(a^2*b + I*a*b^2)*(d*\sqrt{x} + c)^3 + 9*(a*b^2 + I*b^3 - 2*(a^2*b + I*a*b^2)*c)*(d*\sqrt{x} + c)^2 + 18*((a^2*b + I*a*b^2)*c^2 - (a*b^2 + I*b^3)*c)*(d*\sqrt{x} + c) + (8*(a^2*b - I*a*b^2)*(d*\sqrt{x} + c)^3 + 9*(a*b^2 - I*b^3 - 2*(a^2*b - I*a*b^2)*c)*(d*\sqrt{x} + c)^2 + 18*((a^2*b - I*a*b^2)*c^2 - (a*b^2 - I*b^3)*c)*(d*\sqrt{x} + c))*\cos(2*d*\sqrt{x} + 2*c) - (8*(-I*a^2*b - a*b^2)*(d*\sqrt{x} + c)^3 + 9*(-I*a*b^2 - b^3 + 2*(I*a^2*b + a*b^2)*c)*(d*\sqrt{x} + c)^2 + 18*((-I*a^2*b - a*b^2)*c^2 + (I*a*b^2 + b^3)*c)*(d*\sqrt{x} + c))*\sin(2*d*\sqrt{x} + 2*c))*\log(((a^2 + b^2)*\cos(2*d*\sqrt{x} + 2*c)^2 + 4*a*b*\sin(2*d*\sqrt{x} + 2*c) + (a^2 + b^2)*\sin(2*d*\sqrt{x} + 2*c)^2 + a^2 + b^2 + 2*(a^2 - b^2)*\cos(2*d*\sqrt{x} + 2*c))/(a^2 + b^2)) - 24*(-I*a^2*b + a*b^2 + (-I*a^2*b - a*b^2)*\cos(2*d*\sqrt{x} + 2*c) + (a^2*b - I*a*b^2)*\sin(2*d*\sqrt{x} + 2*c))*\operatorname{polylog}(4, (I*a + b)*e^{(2*I*d*\sqrt{x} + 2*I*c)/(-I*a + b)}) + 6*(3*a*b^2 + 3*I*b^3 + 8*(a^2*b + I*a*b^2)*(d*\sqrt{x} + c) - 6*(a^2*b + I*a*b^2)*c + (3*a*b^2 - 3*I*b^3 + 8*(a^2*b - I*a*b^2)*(d*\sqrt{x} + c) - 6*(a^2*b - I*a*b^2)*c)*\cos(2*d*\sqrt{x} + 2*c) - (-3*I*a*b^2 - 3*b^3 + 8*(-I*a^2*b - a*b^2)*(d*\sqrt{x} + c) + 6*(I*a^2*b + a*b^2)*c)*\sin(2*d*\sqrt{x} + 2*c))*\operatorname{polylog}(3, (I*a + b)*e^{(2*I*d*\sqrt{x} + 2*I*c)/(-I*a + b)}) - 3*((-I*a^3 - 3*a^2*b + 3*I*a*b^2 + b^3)*(d*\sqrt{x} + c)^4 - 4*(2*a*b^2 - 2*I*b^3 - (I*a^3 + 3*a^2*b - 3*I*a*b^2 - b^3)*c)*(d*\sqrt{x} + c)^3 - 24*(a*b^2 - I*b^3)*(d*\sqrt{x} + c)*c^2 + 6*((-I*a^3 - 3*a^2*b + 3*I*a*b^2 + b^3)*c^2 + 4*(a*b^2 - I*b^3)*c)*(d*\sqrt{x} + c)^2)*\sin(2*d*\sqrt{x} + 2*c))/(a^5 + I*a^4*b + 2*a^3*b^2 + 2*I*a^2*b^3 + a*b^4 + I*b^5 + (a^5 - I*a^4*b + 2*a^3*b^2 - 2*I*a^2*b^3 + a*b^4 - I*b^5)*\cos(2*d*\sqrt{x} + 2*c) - (-I*a^5 - a^4*b - 2*I*a^3*b^2 - 2*a^2*b^3 - I*a*b^4 - b^5)*\sin(2*d*\sqrt{x} + 2*c))/d^4
\end{aligned}$$

Giac [F]

$$\int \frac{x}{(a + b \tan(c + d\sqrt{x}))^2} dx = \int \frac{x}{(b \tan(d\sqrt{x} + c) + a)^2} dx$$

[In] integrate(x/(a+b*tan(c+d*x^(1/2)))^2,x, algorithm="giac")

[Out] integrate(x/(b*tan(d*sqrt(x) + c) + a)^2, x)

Mupad [F(-1)]

Timed out.

$$\int \frac{x}{(a + b \tan(c + d\sqrt{x}))^2} dx = \int \frac{x}{(a + b \tan(c + d\sqrt{x}))^2} dx$$

[In] int(x/(a + b*tan(c + d*x^(1/2)))^2,x)

[Out] int(x/(a + b*tan(c + d*x^(1/2)))^2, x)

3.44 $\int \frac{1}{(a+b \tan(c+d\sqrt{x}))^2} dx$

Optimal result	274
Rubi [A] (verified)	274
Mathematica [B] (verified)	277
Maple [F]	277
Fricas [B] (verification not implemented)	278
Sympy [F]	278
Maxima [B] (verification not implemented)	279
Giac [F]	279
Mupad [F(-1)]	280

Optimal result

Integrand size = 16, antiderivative size = 204

$$\int \frac{1}{(a+b \tan(c+d\sqrt{x}))^2} dx = \frac{(b+2ad\sqrt{x})^2}{2a(a+ib)(a^2+b^2)d^2} - \frac{x}{a^2+b^2} + \frac{2b(b+2ad\sqrt{x}) \log\left(1 + \frac{(a^2+b^2)e^{2i(c+d\sqrt{x})}}{(a+ib)^2}\right)}{(a^2+b^2)^2 d^2} - \frac{2iab \operatorname{PolyLog}\left(2, -\frac{(a^2+b^2)e^{2i(c+d\sqrt{x})}}{(a+ib)^2}\right)}{(a^2+b^2)^2 d^2} - \frac{2b\sqrt{x}}{(a^2+b^2)d(a+b \tan(c+d\sqrt{x}))}$$

```
[Out] -x/(a^2+b^2)-2*I*a*b*polylog(2,-(a^2+b^2)*exp(2*I*(c+d*x^(1/2)))/(a+I*b)^2)
/(a^2+b^2)^2/d^2+2*b*ln(1+(a^2+b^2)*exp(2*I*(c+d*x^(1/2)))/(a+I*b)^2)*(b+2*
a*d*x^(1/2))/(a^2+b^2)^2/d^2+1/2*(b+2*a*d*x^(1/2))^2/a/(a+I*b)/(a^2+b^2)/d^
2-2*b*x^(1/2)/(a^2+b^2)/d/(a+b*tan(c+d*x^(1/2)))
```

Rubi [A] (verified)

Time = 0.32 (sec) , antiderivative size = 204, normalized size of antiderivative = 1.00, number of steps used = 6, number of rules used = 6, $\frac{\text{number of rules}}{\text{integrand size}} = 0.375$, Rules used

= {3824, 3814, 3813, 2221, 2317, 2438}

$$\int \frac{1}{(a + b \tan(c + d\sqrt{x}))^2} dx = -\frac{2iab \operatorname{PolyLog}\left(2, -\frac{(a^2+b^2)e^{2i(c+d\sqrt{x})}}{(a+ib)^2}\right)}{d^2(a^2+b^2)^2} + \frac{2b(2ad\sqrt{x} + b) \log\left(1 + \frac{(a^2+b^2)e^{2i(c+d\sqrt{x})}}{(a+ib)^2}\right)}{d^2(a^2+b^2)^2} - \frac{2b\sqrt{x}}{d(a^2+b^2)(a+b\tan(c+d\sqrt{x}))} + \frac{(2ad\sqrt{x} + b)^2}{2ad^2(a+ib)(a^2+b^2)} - \frac{x}{a^2+b^2}$$

[In] Int[(a + b*Tan[c + d*Sqrt[x]])^(-2), x]

[Out] (b + 2*a*d*Sqrt[x])^2/(2*a*(a + I*b)*(a^2 + b^2)*d^2) - x/(a^2 + b^2) + (2*b*(b + 2*a*d*Sqrt[x])*Log[1 + ((a^2 + b^2)*E^((2*I)*(c + d*Sqrt[x])))]/(a + I*b)^2)/((a^2 + b^2)^2*d^2) - ((2*I)*a*b*PolyLog[2, -(((a^2 + b^2)*E^((2*I)*(c + d*Sqrt[x])))]/(a + I*b)^2)]/((a^2 + b^2)^2*d^2) - (2*b*Sqrt[x])/((a^2 + b^2)*d*(a + b*Tan[c + d*Sqrt[x]]))

Rule 2221

Int[(((F_)^(g_)*((e_) + (f_)*(x_)))^(n_)*((c_) + (d_)*(x_))^(m_))/((a_) + (b_)*((F_)^(g_)*((e_) + (f_)*(x_)))^(n_)), x_Symbol] := Simp[((c + d*x)^m/(b*f*g*n*Log[F]))*Log[1 + b*((F^(g*(e + f*x)))^n/a)], x] - Dist[d*(m/(b*f*g*n*Log[F])), Int[(c + d*x)^(m-1)*Log[1 + b*((F^(g*(e + f*x)))^n/a)], x], x] /; FreeQ[{F, a, b, c, d, e, f, g, n}, x] && IGtQ[m, 0]

Rule 2317

Int[Log[(a_) + (b_)*((F_)^(e_)*((c_) + (d_)*(x_)))^(n_)], x_Symbol] := Dist[1/(d*e*n*Log[F]), Subst[Int[Log[a + b*x]/x, x], x, (F^(e*(c + d*x)))^n], x] /; FreeQ[{F, a, b, c, d, e, n}, x] && GtQ[a, 0]

Rule 2438

Int[Log[(c_)*((d_) + (e_)*(x_)^(n_))]/(x_), x_Symbol] := Simp[-PolyLog[2, (-c)*e*x^n]/n, x] /; FreeQ[{c, d, e, n}, x] && EqQ[c*d, 1]

Rule 3813

Int[(((c_) + (d_)*(x_))^(m_))/((a_) + (b_)*tan[(e_) + (f_)*(x_)]), x_Symbol] := Simp[(c + d*x)^(m+1)/(d*(m+1)*(a + I*b)), x] + Dist[2*I*b, Int[(c + d*x)^m*(E^Simp[2*I*(e + f*x), x])/((a + I*b)^2 + (a^2 + b^2)*E^Simp[2*I*(e + f*x), x]), x], x] /; FreeQ[{a, b, c, d, e, f}, x] && NeQ[a^2 + b^2,

0] && IGtQ[m, 0]

Rule 3814

```
Int[((c_.) + (d_.)*(x_))/((a_.) + (b_.)*tan[(e_.) + (f_.)*(x_)])^2, x_Symbol]
:= Simp[-(c + d*x)^2/(2*d*(a^2 + b^2)), x] + (Dist[1/(f*(a^2 + b^2)), Int
[(b*d + 2*a*c*f + 2*a*d*f*x)/(a + b*Tan[e + f*x]), x], x] - Simp[b*((c + d*
x)/(f*(a^2 + b^2)*(a + b*Tan[e + f*x]))), x]) /; FreeQ[{a, b, c, d, e, f},
x] && NeQ[a^2 + b^2, 0]
```

Rule 3824

```
Int[((a_.) + (b_.)*Tan[(c_.) + (d_.)*(x_)^(n_)])^(p_.), x_Symbol] := Dist[1
/n, Subst[Int[x^(1/n - 1)*(a + b*Tan[c + d*x])^p, x], x, x^n], x] /; FreeQ[
{a, b, c, d, p}, x] && IGtQ[1/n, 0] && IntegerQ[p]
```

Rubi steps

$$\begin{aligned}
\text{integral} &= 2\text{Subst}\left(\int \frac{x}{(a + b \tan(c + dx))^2} dx, x, \sqrt{x}\right) \\
&= -\frac{x}{a^2 + b^2} - \frac{2b\sqrt{x}}{(a^2 + b^2)d(a + b \tan(c + d\sqrt{x}))} + \frac{2\text{Subst}\left(\int \frac{b+2adx}{a+b \tan(c+dx)} dx, x, \sqrt{x}\right)}{(a^2 + b^2)d} \\
&= \frac{(b + 2ad\sqrt{x})^2}{2a(a + ib)(a^2 + b^2)d^2} - \frac{x}{a^2 + b^2} - \frac{2b\sqrt{x}}{(a^2 + b^2)d(a + b \tan(c + d\sqrt{x}))} \\
&\quad + \frac{(4ib)\text{Subst}\left(\int \frac{e^{2i(c+dx)}(b+2adx)}{(a+ib)^2 + (a^2+b^2)e^{2i(c+dx)}} dx, x, \sqrt{x}\right)}{(a^2 + b^2)d} \\
&= \frac{(b + 2ad\sqrt{x})^2}{2a(a + ib)(a^2 + b^2)d^2} - \frac{x}{a^2 + b^2} + \frac{2b(b + 2ad\sqrt{x}) \log\left(1 + \frac{(a^2+b^2)e^{2i(c+d\sqrt{x})}}{(a+ib)^2}\right)}{(a^2 + b^2)^2 d^2} \\
&\quad - \frac{2b\sqrt{x}}{(a^2 + b^2)d(a + b \tan(c + d\sqrt{x}))} - \frac{(4ab)\text{Subst}\left(\int \log\left(1 + \frac{(a^2+b^2)e^{2i(c+dx)}}{(a+ib)^2}\right) dx, x, \sqrt{x}\right)}{(a^2 + b^2)^2 d} \\
&= \frac{(b + 2ad\sqrt{x})^2}{2a(a + ib)(a^2 + b^2)d^2} - \frac{x}{a^2 + b^2} + \frac{2b(b + 2ad\sqrt{x}) \log\left(1 + \frac{(a^2+b^2)e^{2i(c+d\sqrt{x})}}{(a+ib)^2}\right)}{(a^2 + b^2)^2 d^2} \\
&\quad - \frac{2b\sqrt{x}}{(a^2 + b^2)d(a + b \tan(c + d\sqrt{x}))} + \frac{(2iab)\text{Subst}\left(\int \frac{\log\left(1 + \frac{(a^2+b^2)x}{(a+ib)^2}\right)}{x} dx, x, e^{2i(c+d\sqrt{x})}\right)}{(a^2 + b^2)^2 d^2}
\end{aligned}$$

$$= \frac{(b + 2ad\sqrt{x})^2}{2a(a + ib)(a^2 + b^2)d^2} - \frac{x}{a^2 + b^2} + \frac{2b(b + 2ad\sqrt{x}) \log\left(1 + \frac{(a^2 + b^2)e^{2i(c + d\sqrt{x})}}{(a + ib)^2}\right)}{(a^2 + b^2)^2 d^2}$$

$$- \frac{2iab \operatorname{PolyLog}\left(2, -\frac{(a^2 + b^2)e^{2i(c + d\sqrt{x})}}{(a + ib)^2}\right)}{(a^2 + b^2)^2 d^2} - \frac{2b\sqrt{x}}{(a^2 + b^2)d(a + b \tan(c + d\sqrt{x}))}$$

Mathematica [B] (verified)

Both result and optimal contain complex but leaf count is larger than twice the leaf count of optimal. 517 vs. $2(204) = 408$.

Time = 5.67 (sec) , antiderivative size = 517, normalized size of antiderivative = 2.53

$$\int \frac{1}{(a + b \tan(c + d\sqrt{x}))^2} dx$$

$$= \frac{\sec^2(c + d\sqrt{x})(a \cos(c + d\sqrt{x}) + b \sin(c + d\sqrt{x})) \left(2b^2(a^2 + b^2)d\sqrt{x} \sin(c + d\sqrt{x}) - a(a^2 + b^2)(c - d\sqrt{x})\right)}{(a^2 + b^2)^2 d^2}$$

```
[In] Integrate[(a + b*Tan[c + d*Sqrt[x]])^(-2), x]
```

```
[Out] (Sec[c + d*Sqrt[x]]^2*(a*Cos[c + d*Sqrt[x]] + b*Sin[c + d*Sqrt[x]])*(2*b^2*(a^2 + b^2)*d*Sqrt[x]*Sin[c + d*Sqrt[x]] - a*(a^2 + b^2)*(c - d*Sqrt[x])*(c + d*Sqrt[x])*(a*Cos[c + d*Sqrt[x]] + b*Sin[c + d*Sqrt[x]]) - 2*b^2*(b*(c + d*Sqrt[x]) - a*Log[a*Cos[c + d*Sqrt[x]] + b*Sin[c + d*Sqrt[x]]])*(a*Cos[c + d*Sqrt[x]] + b*Sin[c + d*Sqrt[x]]) + 4*a*b*c*(b*(c + d*Sqrt[x]) - a*Log[a*Cos[c + d*Sqrt[x]] + b*Sin[c + d*Sqrt[x]]])*(a*Cos[c + d*Sqrt[x]] + b*Sin[c + d*Sqrt[x]]) - 2*a*b*(Sqrt[1 + a^2/b^2]*b*E^(I*ArcTan[a/b])*(c + d*Sqrt[x])^2 + a*((-I)*(c + d*Sqrt[x])*(Pi - 2*ArcTan[a/b]) - Pi*Log[1 + E^((-2*I)*(c + d*Sqrt[x]))]) - 2*(c + d*Sqrt[x] + ArcTan[a/b])*Log[1 - E^((2*I)*(c + d*Sqrt[x] + ArcTan[a/b]))]) + Pi*Log[Cos[c + d*Sqrt[x]]] + 2*ArcTan[a/b]*Log[Sin[c + d*Sqrt[x] + ArcTan[a/b]]) + I*PolyLog[2, E^((2*I)*(c + d*Sqrt[x] + ArcTan[a/b]))])*(a*Cos[c + d*Sqrt[x]] + b*Sin[c + d*Sqrt[x]])))/(a*(a^2 + b^2)^2*d^2*(a + b*Tan[c + d*Sqrt[x]])^2)
```

Maple [F]

$$\int \frac{1}{(a + b \tan(c + d\sqrt{x}))^2} dx$$

```
[In] int(1/(a+b*tan(c+d*x^(1/2)))^2,x)
```

```
[Out] int(1/(a+b*tan(c+d*x^(1/2)))^2,x)
```

Fricas [B] (verification not implemented)

Both result and optimal contain complex but leaf count of result is larger than twice the leaf count of optimal. 828 vs. $2(177) = 354$.

Time = 0.28 (sec) , antiderivative size = 828, normalized size of antiderivative = 4.06

$$\int \frac{1}{(a + b \tan(c + d\sqrt{x}))^2} dx = \frac{2b^3 d\sqrt{x} - (a^3 - ab^2)d^2 x + (a^3 - ab^2)d^2 - (iab^2 \tan(d\sqrt{x} + c) + ia^2 b) \operatorname{Li}_2\left(\frac{2((iab - b^2) \tan(d\sqrt{x} + c)^2 - a^2 - iab)}{(a^2 + b^2) \tan(d\sqrt{x} + c)}\right)}{}$$

[In] integrate(1/(a+b*tan(c+d*x^(1/2)))^2,x, algorithm="fricas")

[Out] $-(2*b^3*d*\sqrt{x} - (a^3 - a*b^2)*d^2*x + (a^3 - a*b^2)*d^2 - (I*a*b^2*\tan(d*\sqrt{x} + c) + I*a^2*b)*\operatorname{dilog}(2*((I*a*b - b^2)*\tan(d*\sqrt{x} + c))^2 - a^2 - I*a*b + (I*a^2 - 2*a*b - I*b^2)*\tan(d*\sqrt{x} + c))/((a^2 + b^2)*\tan(d*\sqrt{x} + c))^2 + a^2 + b^2) + 1 - (-I*a*b^2*\tan(d*\sqrt{x} + c) - I*a^2*b)*\operatorname{dilog}(2*((-I*a*b - b^2)*\tan(d*\sqrt{x} + c))^2 - a^2 + I*a*b + (-I*a^2 - 2*a*b + I*b^2)*\tan(d*\sqrt{x} + c))/((a^2 + b^2)*\tan(d*\sqrt{x} + c))^2 + a^2 + b^2) + 1 - 2*(a^2*b*d*\sqrt{x} + a^2*b*c + (a*b^2*d*\sqrt{x} + a*b^2*c)*\tan(d*\sqrt{x} + c))*\log(-2*((I*a*b - b^2)*\tan(d*\sqrt{x} + c))^2 - a^2 - I*a*b + (I*a^2 - 2*a*b - I*b^2)*\tan(d*\sqrt{x} + c))/((a^2 + b^2)*\tan(d*\sqrt{x} + c))^2 + a^2 + b^2) - 2*(a^2*b*d*\sqrt{x} + a^2*b*c + (a*b^2*d*\sqrt{x} + a*b^2*c)*\tan(d*\sqrt{x} + c))*\log(-2*((-I*a*b - b^2)*\tan(d*\sqrt{x} + c))^2 - a^2 + I*a*b + (-I*a^2 - 2*a*b + I*b^2)*\tan(d*\sqrt{x} + c))/((a^2 + b^2)*\tan(d*\sqrt{x} + c))^2 + a^2 + b^2) + (2*a^2*b*c - a*b^2 + (2*a*b^2*c - b^3)*\tan(d*\sqrt{x} + c))*\log(((I*a*b + b^2)*\tan(d*\sqrt{x} + c))^2 - a^2 + I*a*b + (I*a^2 + I*b^2)*\tan(d*\sqrt{x} + c))/(tan(d*\sqrt{x} + c))^2 + 1) + (2*a^2*b*c - a*b^2 + (2*a*b^2*c - b^3)*\tan(d*\sqrt{x} + c))*\log(((I*a*b - b^2)*\tan(d*\sqrt{x} + c))^2 + a^2 + I*a*b + (I*a^2 + I*b^2)*\tan(d*\sqrt{x} + c))/(tan(d*\sqrt{x} + c))^2 + 1) - (2*a*b^2*d*\sqrt{x} + (a^2*b - b^3)*d^2*x - (a^2*b - b^3)*d^2)*\tan(d*\sqrt{x} + c))/((a^4*b + 2*a^2*b^3 + b^5)*d^2*\tan(d*\sqrt{x} + c) + (a^5 + 2*a^3*b^2 + a*b^4)*d^2)$

Sympy [F]

$$\int \frac{1}{(a + b \tan(c + d\sqrt{x}))^2} dx = \int \frac{1}{(a + b \tan(c + d\sqrt{x}))^2} dx$$

[In] integrate(1/(a+b*tan(c+d*x**(1/2)))**2,x)

[Out] Integral((a + b*tan(c + d*sqrt(x)))**(-2), x)

Maxima [B] (verification not implemented)

Both result and optimal contain complex but leaf count of result is larger than twice the leaf count of optimal. 994 vs. $2(177) = 354$.

Time = 0.60 (sec) , antiderivative size = 994, normalized size of antiderivative = 4.87

$$\int \frac{1}{(a + b \tan(c + d\sqrt{x}))^2} dx = \text{Too large to display}$$

[In] integrate(1/(a+b*tan(c+d*x^(1/2)))^2,x, algorithm="maxima")

[Out] $((a^3 - I*a^2*b + a*b^2 - I*b^3)*d^2*x - 2*(-I*a*b^2 + b^3 + (-I*a*b^2 - b^3)*\cos(2*d*\sqrt{x} + 2*c) + (a*b^2 - I*b^3)*\sin(2*d*\sqrt{x} + 2*c))*\arctan2(-b*\cos(2*d*\sqrt{x} + 2*c) + a*\sin(2*d*\sqrt{x} + 2*c) + b, a*\cos(2*d*\sqrt{x} + 2*c) + b*\sin(2*d*\sqrt{x} + 2*c) + a) - 4*((I*a^2*b + a*b^2)*d*\sqrt{x}*\cos(2*d*\sqrt{x} + 2*c) - (a^2*b - I*a*b^2)*d*\sqrt{x}*\sin(2*d*\sqrt{x} + 2*c) + (I*a^2*b - a*b^2)*d*\sqrt{x})*\arctan2((2*a*b*\cos(2*d*\sqrt{x} + 2*c) - (a^2 - b^2)*\sin(2*d*\sqrt{x} + 2*c))/(a^2 + b^2), (2*a*b*\sin(2*d*\sqrt{x} + 2*c) + a^2 + b^2 + (a^2 - b^2)*\cos(2*d*\sqrt{x} + 2*c))/(a^2 + b^2)) + ((a^3 - 3*I*a^2*b - 3*a*b^2 + I*b^3)*d^2*x - 4*(I*a*b^2 + b^3)*d*\sqrt{x})*\cos(2*d*\sqrt{x} + 2*c) - 2*(I*a^2*b - a*b^2 + (I*a^2*b + a*b^2)*\cos(2*d*\sqrt{x} + 2*c) - (a^2*b - I*a*b^2)*\sin(2*d*\sqrt{x} + 2*c))*\operatorname{dilog}((I*a + b)*e^{(2*I*d*\sqrt{x} + 2*I*c)/(-I*a + b)}) + (a*b^2 + I*b^3 + (a*b^2 - I*b^3)*\cos(2*d*\sqrt{x} + 2*c) + (I*a*b^2 + b^3)*\sin(2*d*\sqrt{x} + 2*c))*\log((a^2 + b^2)*\cos(2*d*\sqrt{x} + 2*c)^2 + 4*a*b*\sin(2*d*\sqrt{x} + 2*c) + (a^2 + b^2)*\sin(2*d*\sqrt{x} + 2*c)^2 + a^2 + b^2 + 2*(a^2 - b^2)*\cos(2*d*\sqrt{x} + 2*c)) + 2*((a^2*b - I*a*b^2)*d*\sqrt{x}*\cos(2*d*\sqrt{x} + 2*c) - (-I*a^2*b - a*b^2)*d*\sqrt{x}*\sin(2*d*\sqrt{x} + 2*c) + (a^2*b + I*a*b^2)*d*\sqrt{x})*\log(((a^2 + b^2)*\cos(2*d*\sqrt{x} + 2*c)^2 + 4*a*b*\sin(2*d*\sqrt{x} + 2*c) + (a^2 + b^2)*\sin(2*d*\sqrt{x} + 2*c)^2 + a^2 + b^2 + 2*(a^2 - b^2)*\cos(2*d*\sqrt{x} + 2*c))/(a^2 + b^2)) + ((I*a^3 + 3*a^2*b - 3*I*a*b^2 - b^3)*d^2*x + 4*(a*b^2 - I*b^3)*d*\sqrt{x})*\sin(2*d*\sqrt{x} + 2*c))/((a^5 - I*a^4*b + 2*a^3*b^2 - 2*I*a^2*b^3 + a*b^4 - I*b^5)*d^2*\cos(2*d*\sqrt{x} + 2*c) - (-I*a^5 - a^4*b - 2*I*a^3*b^2 - 2*a^2*b^3 - I*a*b^4 - b^5)*d^2*\sin(2*d*\sqrt{x} + 2*c) + (a^5 + I*a^4*b + 2*a^3*b^2 + 2*I*a^2*b^3 + a*b^4 + I*b^5)*d^2)$

Giac [F]

$$\int \frac{1}{(a + b \tan(c + d\sqrt{x}))^2} dx = \int \frac{1}{(b \tan(d\sqrt{x} + c) + a)^2} dx$$

[In] integrate(1/(a+b*tan(c+d*x^(1/2)))^2,x, algorithm="giac")

[Out] integrate((b*tan(d*sqrt(x) + c) + a)^(-2), x)

Mupad [F(-1)]

Timed out.

$$\int \frac{1}{(a + b \tan(c + d\sqrt{x}))^2} dx = \int \frac{1}{(a + b \tan(c + d\sqrt{x}))^2} dx$$

```
[In] int(1/(a + b*tan(c + d*x^(1/2)))^2,x)
```

```
[Out] int(1/(a + b*tan(c + d*x^(1/2)))^2, x)
```


$$3.45 \quad \int \frac{1}{x(a+b \tan(c+d\sqrt{x}))^2} dx$$

Optimal result	281
Rubi [N/A]	281
Mathematica [N/A]	282
Maple [N/A] (verified)	282
Fricas [N/A]	282
Sympy [N/A]	283
Maxima [N/A]	283
Giac [N/A]	285
Mupad [N/A]	285

Optimal result

Integrand size = 20, antiderivative size = 20

$$\int \frac{1}{x(a+b \tan(c+d\sqrt{x}))^2} dx = \text{Int}\left(\frac{1}{x(a+b \tan(c+d\sqrt{x}))^2}, x\right)$$

[Out] Unintegrable(1/x/(a+b*tan(c+d*x^(1/2)))^2,x)

Rubi [N/A]

Not integrable

Time = 0.02 (sec) , antiderivative size = 20, normalized size of antiderivative = 1.00, number of steps used = 0, number of rules used = 0, $\frac{\text{number of rules}}{\text{integrand size}} = 0.000$, Rules used = {}

$$\int \frac{1}{x(a+b \tan(c+d\sqrt{x}))^2} dx = \int \frac{1}{x(a+b \tan(c+d\sqrt{x}))^2} dx$$

[In] Int[1/(x*(a + b*Tan[c + d*Sqrt[x]]))^2,x]

[Out] Defer[Int][1/(x*(a + b*Tan[c + d*Sqrt[x]]))^2), x]

Rubi steps

$$\text{integral} = \int \frac{1}{x(a+b \tan(c+d\sqrt{x}))^2} dx$$

Mathematica [N/A]

Not integrable

Time = 168.73 (sec) , antiderivative size = 22, normalized size of antiderivative = 1.10

$$\int \frac{1}{x (a + b \tan (c + d \sqrt{x}))^2} dx = \int \frac{1}{x (a + b \tan (c + d \sqrt{x}))^2} dx$$

[In] Integrate[1/(x*(a + b*Tan[c + d*Sqrt[x]]))^2,x]

[Out] Integrate[1/(x*(a + b*Tan[c + d*Sqrt[x]]))^2, x]

Maple [N/A] (verified)

Not integrable

Time = 0.65 (sec) , antiderivative size = 18, normalized size of antiderivative = 0.90

$$\int \frac{1}{x (a + b \tan (c + d \sqrt{x}))^2} dx$$

[In] int(1/x/(a+b*tan(c+d*x^(1/2)))^2,x)

[Out] int(1/x/(a+b*tan(c+d*x^(1/2)))^2,x)

Fricas [N/A]

Not integrable

Time = 0.25 (sec) , antiderivative size = 38, normalized size of antiderivative = 1.90

$$\int \frac{1}{x (a + b \tan (c + d \sqrt{x}))^2} dx = \int \frac{1}{(b \tan (d \sqrt{x} + c) + a)^2 x} dx$$

[In] integrate(1/x/(a+b*tan(c+d*x^(1/2)))^2,x, algorithm="fricas")

[Out] integral(1/(b^2*x*tan(d*sqrt(x) + c)^2 + 2*a*b*x*tan(d*sqrt(x) + c) + a^2*x), x)

Sympy [N/A]

Not integrable

Time = 3.46 (sec) , antiderivative size = 19, normalized size of antiderivative = 0.95

$$\int \frac{1}{x (a + b \tan (c + d \sqrt{x}))^2} dx = \int \frac{1}{x (a + b \tan (c + d \sqrt{x}))^2} dx$$

`[In] integrate(1/x/(a+b*tan(c+d*x**(1/2))))**2,x)``[Out] Integral(1/(x*(a + b*tan(c + d*sqrt(x))))**2), x)`**Maxima [N/A]**

Not integrable

Time = 3.51 (sec) , antiderivative size = 3514, normalized size of antiderivative = 175.70

$$\int \frac{1}{x (a + b \tan (c + d \sqrt{x}))^2} dx = \int \frac{1}{(b \tan (d \sqrt{x} + c) + a)^2} dx$$

`[In] integrate(1/x/(a+b*tan(c+d*x^(1/2)))^2,x, algorithm="maxima")`

```
[Out] (((4*a^10*b^2 + 16*a^8*b^4 + 24*a^6*b^6 + 17*a^4*b^8 + 6*a^2*b^10 + b^12)*
cos(2*c)^2 + (4*a^10*b^2 + 16*a^8*b^4 + 24*a^6*b^6 + 17*a^4*b^8 + 6*a^2*b^10
+ b^12)*sin(2*c)^2)*d*cos(2*d*sqrt(x))^2 + (a^12 + 2*a^10*b^2 + a^8*b^4)*
d*cos(2*d*sqrt(x) + 2*c)^2 + ((4*a^10*b^2 + 16*a^8*b^4 + 24*a^6*b^6 + 17*a^
4*b^8 + 6*a^2*b^10 + b^12)*cos(2*c)^2 + (4*a^10*b^2 + 16*a^8*b^4 + 24*a^6*b
^6 + 17*a^4*b^8 + 6*a^2*b^10 + b^12)*sin(2*c)^2)*d*sin(2*d*sqrt(x))^2 + (a^
12 + 2*a^10*b^2 + a^8*b^4)*d*sin(2*d*sqrt(x) + 2*c)^2 - 2*((a^8*b^4 + 4*a^6
*b^6 + 6*a^4*b^8 + 4*a^2*b^10 + b^12)*cos(2*c) - 2*(a^11*b + 5*a^9*b^3 + 10
*a^7*b^5 + 10*a^5*b^7 + 5*a^3*b^9 + a*b^11)*sin(2*c))*d*cos(2*d*sqrt(x)) +
2*(2*(a^11*b + 5*a^9*b^3 + 10*a^7*b^5 + 10*a^5*b^7 + 5*a^3*b^9 + a*b^11)*co
s(2*c) + (a^8*b^4 + 4*a^6*b^6 + 6*a^4*b^8 + 4*a^2*b^10 + b^12)*sin(2*c))*d*
sin(2*d*sqrt(x)) + (a^12 + 6*a^10*b^2 + 15*a^8*b^4 + 20*a^6*b^6 + 15*a^4*b^
8 + 6*a^2*b^10 + b^12)*d - 2*((a^8*b^4 + 2*a^6*b^6 + a^4*b^8)*cos(2*c) - 2
*(a^11*b + 3*a^9*b^3 + 3*a^7*b^5 + a^5*b^7)*sin(2*c))*d*cos(2*d*sqrt(x)) -
(2*(a^11*b + 3*a^9*b^3 + 3*a^7*b^5 + a^5*b^7)*cos(2*c) + (a^8*b^4 + 2*a^6*b
^6 + a^4*b^8)*sin(2*c))*d*sin(2*d*sqrt(x)) - (a^12 + 4*a^10*b^2 + 6*a^8*b^4
+ 4*a^6*b^6 + a^4*b^8)*d*cos(2*d*sqrt(x) + 2*c) - 2*((2*(a^11*b + 3*a^9*b
^3 + 3*a^7*b^5 + a^5*b^7)*cos(2*c) + (a^8*b^4 + 2*a^6*b^6 + a^4*b^8)*sin(2*
c))*d*cos(2*d*sqrt(x)) + ((a^8*b^4 + 2*a^6*b^6 + a^4*b^8)*cos(2*c) - 2*(a^1
1*b + 3*a^9*b^3 + 3*a^7*b^5 + a^5*b^7)*sin(2*c))*d*sin(2*d*sqrt(x)))*sin(2*
d*sqrt(x) + 2*c))*x*integrate(-2*(2*(a^5*b*d*sin(2*d*sqrt(x) + 2*c) - (a*b^
5*sin(2*c) + 2*(a^4*b^2 + a^2*b^4)*cos(2*c))*d*cos(2*d*sqrt(x)) - (a*b^5*co
```

$$\begin{aligned}
& s(2*c) - 2*(a^4*b^2 + a^2*b^4)*\sin(2*c))*d*\sin(2*d*\sqrt{x})) * x - (a^4*b^2*\sin(2*d*\sqrt{x} + 2*c) - (b^6*\sin(2*c) + 2*(a^3*b^3 + a*b^5)*\cos(2*c))*\cos(2*d*\sqrt{x}) - (b^6*\cos(2*c) - 2*(a^3*b^3 + a*b^5)*\sin(2*c))*\sin(2*d*\sqrt{x}))*\sqrt{x}) / ((a^8*d*\cos(2*d*\sqrt{x} + 2*c)^2 + a^8*d*\sin(2*d*\sqrt{x} + 2*c)^2 + ((4*a^6*b^2 + 8*a^4*b^4 + 4*a^2*b^6 + b^8)*\cos(2*c)^2 + (4*a^6*b^2 + 8*a^4*b^4 + 4*a^2*b^6 + b^8)*\sin(2*c)^2)*d*\cos(2*d*\sqrt{x})^2 + ((4*a^6*b^2 + 8*a^4*b^4 + 4*a^2*b^6 + b^8)*\cos(2*c)^2 + (4*a^6*b^2 + 8*a^4*b^4 + 4*a^2*b^6 + b^8)*\sin(2*c)^2)*d*\sin(2*d*\sqrt{x})^2 - 2*((a^4*b^4 + 2*a^2*b^6 + b^8)*\cos(2*c) - 2*(a^7*b + 3*a^5*b^3 + 3*a^3*b^5 + a*b^7)*\sin(2*c))*d*\cos(2*d*\sqrt{x}) + 2*(2*(a^7*b + 3*a^5*b^3 + 3*a^3*b^5 + a*b^7)*\cos(2*c) + (a^4*b^4 + 2*a^2*b^6 + b^8)*\sin(2*c))*d*\sin(2*d*\sqrt{x}) + (a^8 + 4*a^6*b^2 + 6*a^4*b^4 + 4*a^2*b^6 + b^8)*d - 2*((a^4*b^4*\cos(2*c) - 2*(a^7*b + a^5*b^3)*\sin(2*c))*d*\cos(2*d*\sqrt{x}) - (a^4*b^4*\sin(2*c) + 2*(a^7*b + a^5*b^3)*\cos(2*c))*d*\sin(2*d*\sqrt{x}) - (a^8 + 2*a^6*b^2 + a^4*b^4)*d)*\cos(2*d*\sqrt{x} + 2*c) - 2*((a^4*b^4*\sin(2*c) + 2*(a^7*b + a^5*b^3)*\cos(2*c))*d*\cos(2*d*\sqrt{x}) + (a^4*b^4*\cos(2*c) - 2*(a^7*b + a^5*b^3)*\sin(2*c))*d*\sin(2*d*\sqrt{x}))*\sin(2*d*\sqrt{x} + 2*c))*x^2), x) + (((4*a^8*b^2 + 4*a^6*b^4 - 4*a^4*b^6 - 3*a^2*b^8 - b^10)*\cos(2*c)^2 + (4*a^8*b^2 + 4*a^6*b^4 - 4*a^4*b^6 - 3*a^2*b^8 - b^10)*\sin(2*c)^2)*d*\cos(2*d*\sqrt{x})^2 + (a^10 - a^8*b^2)*d*\cos(2*d*\sqrt{x} + 2*c)^2 + ((4*a^8*b^2 + 4*a^6*b^4 - 4*a^4*b^6 - 3*a^2*b^8 - b^10)*\cos(2*c)^2 + (4*a^8*b^2 + 4*a^6*b^4 - 4*a^4*b^6 - 3*a^2*b^8 - b^10)*\sin(2*c)^2)*d*\sin(2*d*\sqrt{x})^2 + (a^10 - a^8*b^2)*d*\sin(2*d*\sqrt{x} + 2*c)^2 - 2*((a^6*b^4 + a^4*b^6 - a^2*b^8 - b^10)*\cos(2*c) - 2*(a^9*b + 2*a^7*b^3 - 2*a^3*b^7 - a*b^9)*\sin(2*c))*d*\cos(2*d*\sqrt{x}) + 2*(2*(a^9*b + 2*a^7*b^3 - 2*a^3*b^7 - a*b^9)*\cos(2*c) + (a^6*b^4 + a^4*b^6 - a^2*b^8 - b^10)*\sin(2*c))*d*\sin(2*d*\sqrt{x}) + (a^10 + 3*a^8*b^2 + 2*a^6*b^4 - 2*a^4*b^6 - 3*a^2*b^8 - b^10)*d - 2*((a^6*b^4 - a^4*b^6)*\cos(2*c) - 2*(a^9*b - a^5*b^5)*\sin(2*c))*d*\cos(2*d*\sqrt{x}) - (2*(a^9*b - a^5*b^5)*\cos(2*c) + (a^6*b^4 - a^4*b^6)*\sin(2*c))*d*\sin(2*d*\sqrt{x}) - (a^10 + a^8*b^2 - a^6*b^4 - a^4*b^6)*d)*\cos(2*d*\sqrt{x} + 2*c) - 2*((2*(a^9*b - a^5*b^5)*\cos(2*c) + (a^6*b^4 - a^4*b^6)*\sin(2*c))*d*\cos(2*d*\sqrt{x}) + ((a^6*b^4 - a^4*b^6)*\cos(2*c) - 2*(a^9*b - a^5*b^5)*\sin(2*c))*d*\sin(2*d*\sqrt{x}))*\sin(2*d*\sqrt{x} + 2*c))*x*\log(x) - 4*((2*(a^7*b^3 + 3*a^5*b^5 + 3*a^3*b^7 + a*b^9)*\cos(2*c) + (a^4*b^6 + 2*a^2*b^8 + b^10)*\sin(2*c))*\cos(2*d*\sqrt{x}) + ((a^4*b^6 + 2*a^2*b^8 + b^10)*\cos(2*c) - 2*(a^7*b^3 + 3*a^5*b^5 + 3*a^3*b^7 + a*b^9)*\sin(2*c))*\sin(2*d*\sqrt{x}) - (a^8*b^2 + 2*a^6*b^4 + a^4*b^6)*\sin(2*d*\sqrt{x} + 2*c))*\sqrt{x}) / (((4*a^10*b^2 + 16*a^8*b^4 + 24*a^6*b^6 + 17*a^4*b^8 + 6*a^2*b^10 + b^12)*\cos(2*c)^2 + (4*a^10*b^2 + 16*a^8*b^4 + 24*a^6*b^6 + 17*a^4*b^8 + 6*a^2*b^10 + b^12)*\sin(2*c)^2)*d*\cos(2*d*\sqrt{x})^2 + (a^12 + 2*a^10*b^2 + a^8*b^4)*d*\cos(2*d*\sqrt{x} + 2*c)^2 + ((4*a^10*b^2 + 16*a^8*b^4 + 24*a^6*b^6 + 17*a^4*b^8 + 6*a^2*b^10 + b^12)*\cos(2*c)^2 + (4*a^10*b^2 + 16*a^8*b^4 + 24*a^6*b^6 + 17*a^4*b^8 + 6*a^2*b^10 + b^12)*\sin(2*c)^2)*d*\sin(2*d*\sqrt{x})^2 + (a^12 + 2*a^10*b^2 + a^8*b^4)*d*\sin(2*d*\sqrt{x} + 2*c)^2 - 2*((a^8*b^4 + 4*a^6*b^6 + 6*a^4*b^8 + 4*a^2*b^10 + b^12)*\cos(2*c) - 2*(a^11*b + 5*a^9*b^3 + 10*a^7*b^5 + 10*a^5*b^7 + 5*a^3*b^9 + a*b^11)*\sin(2*c))*d*\cos(2*d*\sqrt{x}) + 2*(2*(a^11*b + 5*a^9*b^3 + 10*a^7*b^5 + 10*a^5*b^7 + 5*a^3*b^9 + a*b^11)*\sin(2*c))*d*\sin(2*d*\sqrt{x} + 2*c))
\end{aligned}$$

$1*b + 5*a^9*b^3 + 10*a^7*b^5 + 10*a^5*b^7 + 5*a^3*b^9 + a*b^{11})*\cos(2*c) +$
 $(a^8*b^4 + 4*a^6*b^6 + 6*a^4*b^8 + 4*a^2*b^{10} + b^{12})*\sin(2*c))*d*\sin(2*d*\sqrt{x}) +$
 $(a^{12} + 6*a^{10}*b^2 + 15*a^8*b^4 + 20*a^6*b^6 + 15*a^4*b^8 + 6*a^2*b^{10} + b^{12})*d -$
 $2*((a^8*b^4 + 2*a^6*b^6 + a^4*b^8)*\cos(2*c) - 2*(a^{11}*b + 3*a^9*b^3 +$
 $3*a^7*b^5 + a^5*b^7)*\sin(2*c))*d*\cos(2*d*\sqrt{x}) - (2*(a^{11}*b + 3*a^9*b^3 +$
 $3*a^7*b^5 + a^5*b^7)*\cos(2*c) + (a^8*b^4 + 2*a^6*b^6 + a^4*b^8)*\sin(2*c))*d*\sin(2*d*\sqrt{x}) -$
 $(a^{12} + 4*a^{10}*b^2 + 6*a^8*b^4 + 4*a^6*b^6 + a^4*b^8)*d)*\cos(2*d*\sqrt{x} + 2*c) -$
 $2*((2*(a^{11}*b + 3*a^9*b^3 + 3*a^7*b^5 + a^5*b^7)*\cos(2*c) + (a^8*b^4 + 2*a^6*b^6 + a^4*b^8)*\sin(2*c))*d*\cos(2*d*\sqrt{x}) +$
 $((a^8*b^4 + 2*a^6*b^6 + a^4*b^8)*\cos(2*c) - 2*(a^{11}*b + 3*a^9*b^3 + 3*a^7*b^5 + a^5*b^7)*\sin(2*c))*d*\sin(2*d*\sqrt{x}))*\sin(2*d*\sqrt{x} + 2*c))*x$

Giac [N/A]

Not integrable

Time = 1.12 (sec) , antiderivative size = 20, normalized size of antiderivative = 1.00

$$\int \frac{1}{x (a + b \tan (c + d \sqrt{x}))^2} dx = \int \frac{1}{(b \tan (d \sqrt{x} + c) + a)^2 x} dx$$

[In] integrate(1/x/(a+b*tan(c+d*x^(1/2)))^2,x, algorithm="giac")

[Out] integrate(1/((b*tan(d*sqrt(x) + c) + a)^2*x), x)

Mupad [N/A]

Not integrable

Time = 4.73 (sec) , antiderivative size = 20, normalized size of antiderivative = 1.00

$$\int \frac{1}{x (a + b \tan (c + d \sqrt{x}))^2} dx = \int \frac{1}{x (a + b \tan (c + d \sqrt{x}))^2} dx$$

[In] int(1/(x*(a + b*tan(c + d*x^(1/2)))^2),x)

[Out] int(1/(x*(a + b*tan(c + d*x^(1/2)))^2), x)

$$3.46 \quad \int \frac{1}{x^2 (a + b \tan(c + d\sqrt{x}))^2} dx$$

Optimal result	286
Rubi [N/A]	286
Mathematica [N/A]	287
Maple [N/A] (verified)	287
Fricas [N/A]	287
Sympy [N/A]	288
Maxima [F(-2)]	288
Giac [N/A]	288
Mupad [N/A]	289

Optimal result

Integrand size = 20, antiderivative size = 20

$$\int \frac{1}{x^2 (a + b \tan(c + d\sqrt{x}))^2} dx = \text{Int}\left(\frac{1}{x^2 (a + b \tan(c + d\sqrt{x}))^2}, x\right)$$

[Out] Unintegrable(1/x^2/(a+b*tan(c+d*x^(1/2)))^2,x)

Rubi [N/A]

Not integrable

Time = 0.03 (sec) , antiderivative size = 20, normalized size of antiderivative = 1.00, number of steps used = 0, number of rules used = 0, $\frac{\text{number of rules}}{\text{integrand size}} = 0.000$, Rules used = {}

$$\int \frac{1}{x^2 (a + b \tan(c + d\sqrt{x}))^2} dx = \int \frac{1}{x^2 (a + b \tan(c + d\sqrt{x}))^2} dx$$

[In] Int[1/(x^2*(a + b*Tan[c + d*Sqrt[x]]))^2],x]

[Out] Defer[Int][1/(x^2*(a + b*Tan[c + d*Sqrt[x]]))^2], x]

Rubi steps

$$\text{integral} = \int \frac{1}{x^2 (a + b \tan(c + d\sqrt{x}))^2} dx$$

Mathematica [N/A]

Not integrable

Time = 33.61 (sec) , antiderivative size = 22, normalized size of antiderivative = 1.10

$$\int \frac{1}{x^2 (a + b \tan (c + d\sqrt{x}))^2} dx = \int \frac{1}{x^2 (a + b \tan (c + d\sqrt{x}))^2} dx$$

[In] Integrate[1/(x^2*(a + b*Tan[c + d*Sqrt[x]]))^2, x]

[Out] Integrate[1/(x^2*(a + b*Tan[c + d*Sqrt[x]]))^2, x]

Maple [N/A] (verified)

Not integrable

Time = 0.72 (sec) , antiderivative size = 18, normalized size of antiderivative = 0.90

$$\int \frac{1}{x^2 (a + b \tan (c + d\sqrt{x}))^2} dx$$

[In] int(1/x^2/(a+b*tan(c+d*x^(1/2)))^2,x)

[Out] int(1/x^2/(a+b*tan(c+d*x^(1/2)))^2,x)

Fricas [N/A]

Not integrable

Time = 0.25 (sec) , antiderivative size = 44, normalized size of antiderivative = 2.20

$$\int \frac{1}{x^2 (a + b \tan (c + d\sqrt{x}))^2} dx = \int \frac{1}{(b \tan (d\sqrt{x} + c) + a)^2 x^2} dx$$

[In] integrate(1/x^2/(a+b*tan(c+d*x^(1/2)))^2,x, algorithm="fricas")

[Out] integral(1/(b^2*x^2*tan(d*sqrt(x) + c)^2 + 2*a*b*x^2*tan(d*sqrt(x) + c) + a^2*x^2), x)

Sympy [N/A]

Not integrable

Time = 3.43 (sec) , antiderivative size = 20, normalized size of antiderivative = 1.00

$$\int \frac{1}{x^2 (a + b \tan (c + d\sqrt{x}))^2} dx = \int \frac{1}{x^2 (a + b \tan (c + d\sqrt{x}))^2} dx$$

[In] integrate(1/x**2/(a+b*tan(c+d*x**(1/2)))**2,x)

[Out] Integral(1/(x**2*(a + b*tan(c + d*sqrt(x)))**2), x)

Maxima [F(-2)]

Exception generated.

$$\int \frac{1}{x^2 (a + b \tan (c + d\sqrt{x}))^2} dx = \text{Exception raised: RuntimeError}$$

[In] integrate(1/x^2/(a+b*tan(c+d*x^(1/2)))^2,x, algorithm="maxima")

[Out] Exception raised: RuntimeError >> ECL says: THROW: The catch RAT-ERR is undefined.

Giac [N/A]

Not integrable

Time = 1.11 (sec) , antiderivative size = 20, normalized size of antiderivative = 1.00

$$\int \frac{1}{x^2 (a + b \tan (c + d\sqrt{x}))^2} dx = \int \frac{1}{(b \tan (d\sqrt{x} + c) + a)^2 x^2} dx$$

[In] integrate(1/x^2/(a+b*tan(c+d*x^(1/2)))^2,x, algorithm="giac")

[Out] integrate(1/((b*tan(d*sqrt(x) + c) + a)^2*x^2), x)

Mupad [N/A]

Not integrable

Time = 4.12 (sec) , antiderivative size = 20, normalized size of antiderivative = 1.00

$$\int \frac{1}{x^2 (a + b \tan (c + d \sqrt{x}))^2} dx = \int \frac{1}{x^2 (a + b \tan (c + d \sqrt{x}))^2} dx$$

```
[In] int(1/(x^2*(a + b*tan(c + d*x^(1/2)))^2), x)
```

```
[Out] int(1/(x^2*(a + b*tan(c + d*x^(1/2)))^2), x)
```

3.47 $\int x^2 (a + b \tan (c + d \sqrt[3]{x})) dx$

Optimal result	290
Rubi [A] (verified)	291
Mathematica [A] (verified)	296
Maple [F]	297
Fricas [F]	297
Sympy [F]	297
Maxima [B] (verification not implemented)	297
Giac [F]	298
Mupad [F(-1)]	299

Optimal result

Integrand size = 18, antiderivative size = 287

$$\begin{aligned}
 \int x^2 (a + b \tan (c + d \sqrt[3]{x})) dx = & \frac{ax^3}{3} + \frac{1}{3} ibx^3 - \frac{3bx^{8/3} \log \left(1 + e^{2i(c+d\sqrt[3]{x})} \right)}{d} \\
 & + \frac{12ibx^{7/3} \text{PolyLog} \left(2, -e^{2i(c+d\sqrt[3]{x})} \right)}{d^2} \\
 & - \frac{42bx^2 \text{PolyLog} \left(3, -e^{2i(c+d\sqrt[3]{x})} \right)}{d^3} \\
 & - \frac{126ibx^{5/3} \text{PolyLog} \left(4, -e^{2i(c+d\sqrt[3]{x})} \right)}{d^4} \\
 & + \frac{315bx^{4/3} \text{PolyLog} \left(5, -e^{2i(c+d\sqrt[3]{x})} \right)}{d^5} \\
 & + \frac{630ibx \text{PolyLog} \left(6, -e^{2i(c+d\sqrt[3]{x})} \right)}{d^6} \\
 & - \frac{945bx^{2/3} \text{PolyLog} \left(7, -e^{2i(c+d\sqrt[3]{x})} \right)}{d^7} \\
 & - \frac{945ib\sqrt[3]{x} \text{PolyLog} \left(8, -e^{2i(c+d\sqrt[3]{x})} \right)}{d^8} \\
 & + \frac{945b \text{PolyLog} \left(9, -e^{2i(c+d\sqrt[3]{x})} \right)}{2d^9}
 \end{aligned}$$

```
[Out] 1/3*a*x^3+1/3*I*b*x^3-3*b*x^(8/3)*ln(1+exp(2*I*(c+d*x^(1/3))))/d+12*I*b*x^(7/3)*polylog(2,-exp(2*I*(c+d*x^(1/3))))/d^2-42*b*x^2*polylog(3,-exp(2*I*(c+d*x^(1/3))))/d^3-126*I*b*x^(5/3)*polylog(4,-exp(2*I*(c+d*x^(1/3))))/d^4+315
```

$*b*x^{(4/3)}*polylog(5,-exp(2*I*(c+d*x^{(1/3)})))/d^5+630*I*b*x*polylog(6,-exp(2*I*(c+d*x^{(1/3)})))/d^6-945*b*x^{(2/3)}*polylog(7,-exp(2*I*(c+d*x^{(1/3)})))/d^7-945*I*b*x^{(1/3)}*polylog(8,-exp(2*I*(c+d*x^{(1/3)})))/d^8+945/2*b*polylog(9,-exp(2*I*(c+d*x^{(1/3)})))/d^9$

Rubi [A] (verified)

Time = 0.50 (sec) , antiderivative size = 287, normalized size of antiderivative = 1.00, number of steps used = 14, number of rules used = 8, $\frac{\text{number of rules}}{\text{integrand size}} = 0.444$, Rules used = {14, 3832, 3800, 2221, 2611, 6744, 2320, 6724}

$$\int x^2(a + b \tan(c + d\sqrt[3]{x})) dx = \frac{ax^3}{3} + \frac{945b \text{PolyLog}\left(9, -e^{2i(c+d\sqrt[3]{x})}\right)}{2d^9} - \frac{945ib\sqrt[3]{x} \text{PolyLog}\left(8, -e^{2i(c+d\sqrt[3]{x})}\right)}{d^8} - \frac{945bx^{2/3} \text{PolyLog}\left(7, -e^{2i(c+d\sqrt[3]{x})}\right)}{d^7} + \frac{630ibx \text{PolyLog}\left(6, -e^{2i(c+d\sqrt[3]{x})}\right)}{d^6} + \frac{315bx^{4/3} \text{PolyLog}\left(5, -e^{2i(c+d\sqrt[3]{x})}\right)}{d^5} - \frac{126ibx^{5/3} \text{PolyLog}\left(4, -e^{2i(c+d\sqrt[3]{x})}\right)}{d^4} - \frac{42bx^2 \text{PolyLog}\left(3, -e^{2i(c+d\sqrt[3]{x})}\right)}{d^3} + \frac{12ibx^{7/3} \text{PolyLog}\left(2, -e^{2i(c+d\sqrt[3]{x})}\right)}{d^2} - \frac{3bx^{8/3} \log\left(1 + e^{2i(c+d\sqrt[3]{x})}\right)}{d} + \frac{1}{3}ibx^3$$

[In] Int[x^2*(a + b*Tan[c + d*x^(1/3)]),x]

[Out] (a*x^3)/3 + (I/3)*b*x^3 - (3*b*x^(8/3)*Log[1 + E^((2*I)*(c + d*x^(1/3)))])/d + ((12*I)*b*x^(7/3)*PolyLog[2, -E^((2*I)*(c + d*x^(1/3)))]/d^2 - (42*b*x^2*PolyLog[3, -E^((2*I)*(c + d*x^(1/3)))]/d^3 - ((126*I)*b*x^(5/3)*PolyLog[4, -E^((2*I)*(c + d*x^(1/3)))]/d^4 + (315*b*x^(4/3)*PolyLog[5, -E^((2*I)*(c + d*x^(1/3)))]/d^5 + ((630*I)*b*x*PolyLog[6, -E^((2*I)*(c + d*x^(1/3)))]/d^6 - (945*b*x^(2/3)*PolyLog[7, -E^((2*I)*(c + d*x^(1/3)))]/d^7 - ((945*I)*b*x^(1/3)*PolyLog[8, -E^((2*I)*(c + d*x^(1/3)))]/d^8 + (945*b*PolyLog[9, -E^((2*I)*(c + d*x^(1/3)))]/(2*d^9)

Rule 14

```
Int[(u_)*((c_)*(x_)^(m_)), x_Symbol] := Int[ExpandIntegrand[(c*x)^m*u, x], x] /; FreeQ[{c, m}, x] && SumQ[u] && !LinearQ[u, x] && !MatchQ[u, (a_ + (b_)*(v_)) /; FreeQ[{a, b}, x] && InverseFunctionQ[v]]
```

Rule 2221

```
Int[(((F_)^((g_)*((e_) + (f_)*(x_))))^(n_)*((c_) + (d_)*(x_)^(m_)))/((a_) + (b_)*((F_)^((g_)*((e_) + (f_)*(x_))))^(n_)), x_Symbol] := Simp[((c + d*x)^m/(b*f*g*n*Log[F]))*Log[1 + b*((F^(g*(e + f*x)))^n/a)], x] - Dist[d*(m/(b*f*g*n*Log[F])), Int[(c + d*x)^(m - 1)*Log[1 + b*((F^(g*(e + f*x)))^n/a)], x], x] /; FreeQ[{F, a, b, c, d, e, f, g, n}, x] && IGtQ[m, 0]
```

Rule 2320

```
Int[u_, x_Symbol] := With[{v = FunctionOfExponential[u, x]}, Dist[v/D[v, x], Subst[Int[FunctionOfExponentialFunction[u, x]/x, x], x, v], x] /; FunctionOfExponentialQ[u, x] && !MatchQ[u, (w_)*((a_)*(v_)^(n_))^(m_)] /; FreeQ[{a, m, n}, x] && IntegerQ[m*n] && !MatchQ[u, E^((c_)*((a_) + (b_)*x))* (F_)[v_] /; FreeQ[{a, b, c}, x] && InverseFunctionQ[F[x]]]
```

Rule 2611

```
Int[Log[1 + (e_)*((F_)^((c_)*((a_) + (b_)*(x_))))^(n_)]*((f_) + (g_)*(x_)^(m_)), x_Symbol] := Simp[(-f + g*x)^m*(PolyLog[2, (-e)*(F^(c*(a + b*x)))^n]/(b*c*n*Log[F])), x] + Dist[g*(m/(b*c*n*Log[F])), Int[(f + g*x)^(m - 1)*PolyLog[2, (-e)*(F^(c*(a + b*x)))^n], x], x] /; FreeQ[{F, a, b, c, e, f, g, n}, x] && GtQ[m, 0]
```

Rule 3800

```
Int[((c_) + (d_)*(x_)^(m_))*tan[(e_) + (f_)*(x_)], x_Symbol] := Simp[I*((c + d*x)^(m + 1)/(d*(m + 1))), x] - Dist[2*I, Int[(c + d*x)^m*(E^(2*I*(e + f*x)))/(1 + E^(2*I*(e + f*x))), x], x] /; FreeQ[{c, d, e, f}, x] && IGtQ[m, 0]
```

Rule 3832

```
Int[(x_)^(m_)*((a_) + (b_)*Tan[(c_) + (d_)*(x_)^(n_)])^(p_), x_Symbol] := Dist[1/n, Subst[Int[x^(Simplify[(m + 1)/n] - 1)*(a + b*Tan[c + d*x])^p, x], x, x^n], x] /; FreeQ[{a, b, c, d, m, n, p}, x] && IGtQ[Simplify[(m + 1)/n], 0] && IntegerQ[p]
```

Rule 6724

Int[PolyLog[n_, (c_.)*(a_.) + (b_.)*(x_)]/((d_.) + (e_.)*(x_)), x_Symbol] := Simp[PolyLog[n + 1, c*(a + b*x)^p]/(e*p), x] /; FreeQ[{a, b, c, d, e, n, p}, x] && EqQ[b*d, a*e]

Rule 6744

Int[((e_.) + (f_.)*(x_))^(m_.)*PolyLog[n_, (d_.)*((F_)^((c_.)*(a_.) + (b_.)*(x_)))^(p_.)], x_Symbol] := Simp[(e + f*x)^m*(PolyLog[n + 1, d*(F^(c*(a + b*x)))^p]/(b*c*p*Log[F])), x] - Dist[f*(m/(b*c*p*Log[F])), Int[(e + f*x)^(m - 1)*PolyLog[n + 1, d*(F^(c*(a + b*x)))^p], x], x] /; FreeQ[{F, a, b, c, d, e, f, n, p}, x] && GtQ[m, 0]

Rubi steps

$$\begin{aligned}
 \text{integral} &= \int (ax^2 + bx^2 \tan(c + d\sqrt[3]{x})) dx \\
 &= \frac{ax^3}{3} + b \int x^2 \tan(c + d\sqrt[3]{x}) dx \\
 &= \frac{ax^3}{3} + (3b)\text{Subst}\left(\int x^8 \tan(c + dx) dx, x, \sqrt[3]{x}\right) \\
 &= \frac{ax^3}{3} + \frac{1}{3}ibx^3 - (6ib)\text{Subst}\left(\int \frac{e^{2i(c+dx)}x^8}{1 + e^{2i(c+dx)}} dx, x, \sqrt[3]{x}\right) \\
 &= \frac{ax^3}{3} + \frac{1}{3}ibx^3 - \frac{3bx^{8/3} \log\left(1 + e^{2i(c+d\sqrt[3]{x}})\right)}{d} + \frac{(24b)\text{Subst}\left(\int x^7 \log\left(1 + e^{2i(c+dx)}\right) dx, x, \sqrt[3]{x}\right)}{d} \\
 &= \frac{ax^3}{3} + \frac{1}{3}ibx^3 - \frac{3bx^{8/3} \log\left(1 + e^{2i(c+d\sqrt[3]{x}})\right)}{d} + \frac{12ibx^{7/3} \text{PolyLog}\left(2, -e^{2i(c+d\sqrt[3]{x}})\right)}{d^2} \\
 &\quad - \frac{(84ib)\text{Subst}\left(\int x^6 \text{PolyLog}\left(2, -e^{2i(c+dx)}\right) dx, x, \sqrt[3]{x}\right)}{d^2} \\
 &= \frac{ax^3}{3} + \frac{1}{3}ibx^3 - \frac{3bx^{8/3} \log\left(1 + e^{2i(c+d\sqrt[3]{x}})\right)}{d} + \frac{12ibx^{7/3} \text{PolyLog}\left(2, -e^{2i(c+d\sqrt[3]{x}})\right)}{d^2} \\
 &\quad - \frac{42bx^2 \text{PolyLog}\left(3, -e^{2i(c+d\sqrt[3]{x}})\right)}{d^3} + \frac{(252b)\text{Subst}\left(\int x^5 \text{PolyLog}\left(3, -e^{2i(c+dx)}\right) dx, x, \sqrt[3]{x}\right)}{d^3} \\
 &= \frac{ax^3}{3} + \frac{1}{3}ibx^3 - \frac{3bx^{8/3} \log\left(1 + e^{2i(c+d\sqrt[3]{x}})\right)}{d} + \frac{12ibx^{7/3} \text{PolyLog}\left(2, -e^{2i(c+d\sqrt[3]{x}})\right)}{d^2} \\
 &\quad - \frac{42bx^2 \text{PolyLog}\left(3, -e^{2i(c+d\sqrt[3]{x}})\right)}{d^3} - \frac{126ibx^{5/3} \text{PolyLog}\left(4, -e^{2i(c+d\sqrt[3]{x}})\right)}{d^4} \\
 &\quad + \frac{(630ib)\text{Subst}\left(\int x^4 \text{PolyLog}\left(4, -e^{2i(c+dx)}\right) dx, x, \sqrt[3]{x}\right)}{d^4}
 \end{aligned}$$

$$\begin{aligned}
&= \frac{ax^3}{3} + \frac{1}{3}ibx^3 - \frac{3bx^{8/3} \log\left(1 + e^{2i(c+d\sqrt[3]{x})}\right)}{d} \\
&+ \frac{12ibx^{7/3} \text{PolyLog}\left(2, -e^{2i(c+d\sqrt[3]{x})}\right)}{d^2} - \frac{42bx^2 \text{PolyLog}\left(3, -e^{2i(c+d\sqrt[3]{x})}\right)}{d^3} \\
&- \frac{126ibx^{5/3} \text{PolyLog}\left(4, -e^{2i(c+d\sqrt[3]{x})}\right)}{d^4} + \frac{315bx^{4/3} \text{PolyLog}\left(5, -e^{2i(c+d\sqrt[3]{x})}\right)}{d^5} \\
&- \frac{(1260b)\text{Subst}\left(\int x^3 \text{PolyLog}\left(5, -e^{2i(c+dx)}\right) dx, x, \sqrt[3]{x}\right)}{d^5} \\
&= \frac{ax^3}{3} + \frac{1}{3}ibx^3 - \frac{3bx^{8/3} \log\left(1 + e^{2i(c+d\sqrt[3]{x})}\right)}{d} + \frac{12ibx^{7/3} \text{PolyLog}\left(2, -e^{2i(c+d\sqrt[3]{x})}\right)}{d^2} \\
&- \frac{42bx^2 \text{PolyLog}\left(3, -e^{2i(c+d\sqrt[3]{x})}\right)}{d^3} - \frac{126ibx^{5/3} \text{PolyLog}\left(4, -e^{2i(c+d\sqrt[3]{x})}\right)}{d^4} \\
&+ \frac{315bx^{4/3} \text{PolyLog}\left(5, -e^{2i(c+d\sqrt[3]{x})}\right)}{d^5} + \frac{630ibx \text{PolyLog}\left(6, -e^{2i(c+d\sqrt[3]{x})}\right)}{d^6} \\
&- \frac{(1890ib)\text{Subst}\left(\int x^2 \text{PolyLog}\left(6, -e^{2i(c+dx)}\right) dx, x, \sqrt[3]{x}\right)}{d^6} \\
&= \frac{ax^3}{3} + \frac{1}{3}ibx^3 - \frac{3bx^{8/3} \log\left(1 + e^{2i(c+d\sqrt[3]{x})}\right)}{d} \\
&+ \frac{12ibx^{7/3} \text{PolyLog}\left(2, -e^{2i(c+d\sqrt[3]{x})}\right)}{d^2} - \frac{42bx^2 \text{PolyLog}\left(3, -e^{2i(c+d\sqrt[3]{x})}\right)}{d^3} \\
&- \frac{126ibx^{5/3} \text{PolyLog}\left(4, -e^{2i(c+d\sqrt[3]{x})}\right)}{d^4} + \frac{315bx^{4/3} \text{PolyLog}\left(5, -e^{2i(c+d\sqrt[3]{x})}\right)}{d^5} \\
&+ \frac{630ibx \text{PolyLog}\left(6, -e^{2i(c+d\sqrt[3]{x})}\right)}{d^6} - \frac{945bx^{2/3} \text{PolyLog}\left(7, -e^{2i(c+d\sqrt[3]{x})}\right)}{d^7} \\
&+ \frac{(1890b)\text{Subst}\left(\int x \text{PolyLog}\left(7, -e^{2i(c+dx)}\right) dx, x, \sqrt[3]{x}\right)}{d^7} \\
&= \frac{ax^3}{3} + \frac{1}{3}ibx^3 - \frac{3bx^{8/3} \log\left(1 + e^{2i(c+d\sqrt[3]{x})}\right)}{d} + \frac{12ibx^{7/3} \text{PolyLog}\left(2, -e^{2i(c+d\sqrt[3]{x})}\right)}{d^2} \\
&- \frac{42bx^2 \text{PolyLog}\left(3, -e^{2i(c+d\sqrt[3]{x})}\right)}{d^3} - \frac{126ibx^{5/3} \text{PolyLog}\left(4, -e^{2i(c+d\sqrt[3]{x})}\right)}{d^4} \\
&+ \frac{315bx^{4/3} \text{PolyLog}\left(5, -e^{2i(c+d\sqrt[3]{x})}\right)}{d^5} + \frac{630ibx \text{PolyLog}\left(6, -e^{2i(c+d\sqrt[3]{x})}\right)}{d^6} \\
&- \frac{945bx^{2/3} \text{PolyLog}\left(7, -e^{2i(c+d\sqrt[3]{x})}\right)}{d^7} - \frac{945ib\sqrt[3]{x} \text{PolyLog}\left(8, -e^{2i(c+d\sqrt[3]{x})}\right)}{d^8} \\
&+ \frac{(945ib)\text{Subst}\left(\int \text{PolyLog}\left(8, -e^{2i(c+dx)}\right) dx, x, \sqrt[3]{x}\right)}{d^8}
\end{aligned}$$

$$\begin{aligned}
&= \frac{ax^3}{3} + \frac{1}{3}ibx^3 - \frac{3bx^{8/3} \log\left(1 + e^{2i(c+d\sqrt[3]{x})}\right)}{d} + \frac{12ibx^{7/3} \text{PolyLog}\left(2, -e^{2i(c+d\sqrt[3]{x})}\right)}{d^2} \\
&\quad - \frac{42bx^2 \text{PolyLog}\left(3, -e^{2i(c+d\sqrt[3]{x})}\right)}{d^3} - \frac{126ibx^{5/3} \text{PolyLog}\left(4, -e^{2i(c+d\sqrt[3]{x})}\right)}{d^4} \\
&\quad + \frac{315bx^{4/3} \text{PolyLog}\left(5, -e^{2i(c+d\sqrt[3]{x})}\right)}{d^5} + \frac{630ibx \text{PolyLog}\left(6, -e^{2i(c+d\sqrt[3]{x})}\right)}{d^6} \\
&\quad - \frac{945bx^{2/3} \text{PolyLog}\left(7, -e^{2i(c+d\sqrt[3]{x})}\right)}{d^7} - \frac{945ib\sqrt[3]{x} \text{PolyLog}\left(8, -e^{2i(c+d\sqrt[3]{x})}\right)}{d^8} \\
&\quad + \frac{(945b)\text{Subst}\left(\int \frac{\text{PolyLog}(8, -x)}{x} dx, x, e^{2i(c+d\sqrt[3]{x})}\right)}{2d^9} \\
&= \frac{ax^3}{3} + \frac{1}{3}ibx^3 - \frac{3bx^{8/3} \log\left(1 + e^{2i(c+d\sqrt[3]{x})}\right)}{d} \\
&\quad + \frac{12ibx^{7/3} \text{PolyLog}\left(2, -e^{2i(c+d\sqrt[3]{x})}\right)}{d^2} - \frac{42bx^2 \text{PolyLog}\left(3, -e^{2i(c+d\sqrt[3]{x})}\right)}{d^3} \\
&\quad - \frac{126ibx^{5/3} \text{PolyLog}\left(4, -e^{2i(c+d\sqrt[3]{x})}\right)}{d^4} + \frac{315bx^{4/3} \text{PolyLog}\left(5, -e^{2i(c+d\sqrt[3]{x})}\right)}{d^5} \\
&\quad + \frac{630ibx \text{PolyLog}\left(6, -e^{2i(c+d\sqrt[3]{x})}\right)}{d^6} - \frac{945bx^{2/3} \text{PolyLog}\left(7, -e^{2i(c+d\sqrt[3]{x})}\right)}{d^7} \\
&\quad - \frac{945ib\sqrt[3]{x} \text{PolyLog}\left(8, -e^{2i(c+d\sqrt[3]{x})}\right)}{d^8} + \frac{945b \text{PolyLog}\left(9, -e^{2i(c+d\sqrt[3]{x})}\right)}{2d^9}
\end{aligned}$$

Mathematica [A] (verified)

Time = 0.10 (sec) , antiderivative size = 287, normalized size of antiderivative = 1.00

$$\begin{aligned}
\int x^2(a + b \tan(c + d\sqrt[3]{x})) dx &= \frac{ax^3}{3} + \frac{1}{3}ibx^3 - \frac{3bx^{8/3} \log\left(1 + e^{2i(c+d\sqrt[3]{x})}\right)}{d} \\
&+ \frac{12ibx^{7/3} \text{PolyLog}\left(2, -e^{2i(c+d\sqrt[3]{x})}\right)}{d^2} \\
&- \frac{42bx^2 \text{PolyLog}\left(3, -e^{2i(c+d\sqrt[3]{x})}\right)}{d^3} \\
&- \frac{126ibx^{5/3} \text{PolyLog}\left(4, -e^{2i(c+d\sqrt[3]{x})}\right)}{d^4} \\
&+ \frac{315bx^{4/3} \text{PolyLog}\left(5, -e^{2i(c+d\sqrt[3]{x})}\right)}{d^5} \\
&+ \frac{630ibx \text{PolyLog}\left(6, -e^{2i(c+d\sqrt[3]{x})}\right)}{d^6} \\
&- \frac{945bx^{2/3} \text{PolyLog}\left(7, -e^{2i(c+d\sqrt[3]{x})}\right)}{d^7} \\
&- \frac{945ib\sqrt[3]{x} \text{PolyLog}\left(8, -e^{2i(c+d\sqrt[3]{x})}\right)}{d^8} \\
&+ \frac{945b \text{PolyLog}\left(9, -e^{2i(c+d\sqrt[3]{x})}\right)}{2d^9}
\end{aligned}$$

```
[In] Integrate[x^2*(a + b*Tan[c + d*x^(1/3)]),x]
```

```
[Out] (a*x^3)/3 + (I/3)*b*x^3 - (3*b*x^(8/3)*Log[1 + E^((2*I)*(c + d*x^(1/3)))])/
d + ((12*I)*b*x^(7/3)*PolyLog[2, -E^((2*I)*(c + d*x^(1/3)))])/d^2 - (42*b*x
^2*PolyLog[3, -E^((2*I)*(c + d*x^(1/3)))])/d^3 - ((126*I)*b*x^(5/3)*PolyLog
[4, -E^((2*I)*(c + d*x^(1/3)))])/d^4 + (315*b*x^(4/3)*PolyLog[5, -E^((2*I)*
(c + d*x^(1/3)))])/d^5 + ((630*I)*b*x*PolyLog[6, -E^((2*I)*(c + d*x^(1/3))
)])/d^6 - (945*b*x^(2/3)*PolyLog[7, -E^((2*I)*(c + d*x^(1/3)))])/d^7 - ((945
*I)*b*x^(1/3)*PolyLog[8, -E^((2*I)*(c + d*x^(1/3)))])/d^8 + (945*b*PolyLog[
9, -E^((2*I)*(c + d*x^(1/3)))])/(2*d^9)
```


Maple [F]

$$\int x^2 \left(a + b \tan \left(c + d x^{\frac{1}{3}} \right) \right) dx$$

```
[In] int(x^2*(a+b*tan(c+d*x^(1/3))),x)
```

```
[Out] int(x^2*(a+b*tan(c+d*x^(1/3))),x)
```

Fricas [F]

$$\int x^2 (a + b \tan (c + d \sqrt[3]{x})) dx = \int (b \tan (dx^{\frac{1}{3}} + c) + a) x^2 dx$$

```
[In] integrate(x^2*(a+b*tan(c+d*x^(1/3))),x, algorithm="fricas")
```

```
[Out] integral(b*x^2*tan(d*x^(1/3) + c) + a*x^2, x)
```

Sympy [F]

$$\int x^2 (a + b \tan (c + d \sqrt[3]{x})) dx = \int x^2 (a + b \tan (c + d \sqrt[3]{x})) dx$$

```
[In] integrate(x**2*(a+b*tan(c+d*x**(1/3))),x)
```

```
[Out] Integral(x**2*(a + b*tan(c + d*x**(1/3))), x)
```

Maxima [B] (verification not implemented)

Both result and optimal contain complex but leaf count of result is larger than twice the leaf count of optimal. 1119 vs. $2(222) = 444$.

Time = 0.49 (sec) , antiderivative size = 1119, normalized size of antiderivative = 3.90

$$\int x^2 (a + b \tan (c + d \sqrt[3]{x})) dx = \text{Too large to display}$$

```
[In] integrate(x^2*(a+b*tan(c+d*x^(1/3))),x, algorithm="maxima")
```

```
[Out] 1/105*(35*(d*x^(1/3) + c)^9*a + 35*I*(d*x^(1/3) + c)^9*b - 315*(d*x^(1/3) + c)^8*a*c - 315*I*(d*x^(1/3) + c)^8*b*c + 1260*(d*x^(1/3) + c)^7*a*c^2 + 1260*I*(d*x^(1/3) + c)^7*b*c^2 - 2940*(d*x^(1/3) + c)^6*a*c^3 - 2940*I*(d*x^(1/3) + c)^6*b*c^3 + 4410*(d*x^(1/3) + c)^5*a*c^4 + 4410*I*(d*x^(1/3) + c)^5*b*c^4 - 4410*(d*x^(1/3) + c)^4*a*c^5 - 4410*I*(d*x^(1/3) + c)^4*b*c^5 + 2940*(d*x^(1/3) + c)^3*a*c^6 + 2940*I*(d*x^(1/3) + c)^3*b*c^6 - 1260*(d*x^(1/3) + c)^2*a*c^7 + 1260*I*(d*x^(1/3) + c)^2*b*c^7 - 315*(d*x^(1/3) + c)*a*c^8 - 315*I*(d*x^(1/3) + c)*b*c^8 + 35*a*c^9 + 35*I*b*c^9
```

$$\begin{aligned}
& 3) + c)^2 * a * c^7 - 1260 * I * (d * x^{1/3} + c)^2 * b * c^7 + 315 * (d * x^{1/3} + c) * a * c^8 \\
& + 315 * b * c^8 * \log(\sec(d * x^{1/3} + c)) + 12 * (-420 * I * (d * x^{1/3} + c)^8 * b + 19 \\
& 20 * I * (d * x^{1/3} + c)^7 * b * c - 3920 * I * (d * x^{1/3} + c)^6 * b * c^2 + 4704 * I * (d * x^{1/3} \\
& + c)^5 * b * c^3 - 3675 * I * (d * x^{1/3} + c)^4 * b * c^4 + 1960 * I * (d * x^{1/3} + c) \\
& ^3 * b * c^5 - 735 * I * (d * x^{1/3} + c)^2 * b * c^6 + 210 * I * (d * x^{1/3} + c) * b * c^7) * \arctan \\
& \tan 2(\sin(2 * d * x^{1/3} + 2 * c), \cos(2 * d * x^{1/3} + 2 * c) + 1) + 1260 * (16 * I * (d * x^{1/3} \\
& + c)^7 * b - 64 * I * (d * x^{1/3} + c)^6 * b * c + 112 * I * (d * x^{1/3} + c)^5 * b * c^2 \\
& - 112 * I * (d * x^{1/3} + c)^4 * b * c^3 + 70 * I * (d * x^{1/3} + c)^3 * b * c^4 - 28 * I * (d * x^{1/3} \\
& + c)^2 * b * c^5 + 7 * I * (d * x^{1/3} + c) * b * c^6 - I * b * c^7) * \operatorname{dilog}(-e^{(2 * I * d * x^{1/3} \\
& + 2 * I * c)}) - 6 * (420 * (d * x^{1/3} + c)^8 * b - 1920 * (d * x^{1/3} + c)^7 * b * c \\
& + 3920 * (d * x^{1/3} + c)^6 * b * c^2 - 4704 * (d * x^{1/3} + c)^5 * b * c^3 + 3675 * (d * x^{1/3} \\
& + c)^4 * b * c^4 - 1960 * (d * x^{1/3} + c)^3 * b * c^5 + 735 * (d * x^{1/3} + c)^2 * b * c^6 - 210 * (d * x^{1/3} \\
& + c) * b * c^7) * \log(\cos(2 * d * x^{1/3} + 2 * c)^2 + \sin(2 * d * x^{1/3} \\
& + 2 * c)^2 + 2 * \cos(2 * d * x^{1/3} + 2 * c) + 1) + 793800 * b * \operatorname{polylog}(9, -e^{(2 * I * d * x^{1/3} \\
& + 2 * I * c)}) + 226800 * (-7 * I * (d * x^{1/3} + c) * b + 4 * I * b * c) * \operatorname{polylog}(8 \\
& , -e^{(2 * I * d * x^{1/3} + 2 * I * c)}) - 75600 * (21 * (d * x^{1/3} + c)^2 * b - 24 * (d * x^{1/3} \\
& + c) * b * c + 7 * b * c^2) * \operatorname{polylog}(7, -e^{(2 * I * d * x^{1/3} + 2 * I * c)}) + 30240 * (35 * I \\
& * (d * x^{1/3} + c)^3 * b - 60 * I * (d * x^{1/3} + c)^2 * b * c + 35 * I * (d * x^{1/3} + c) * b * c^2 \\
& - 7 * I * b * c^3) * \operatorname{polylog}(6, -e^{(2 * I * d * x^{1/3} + 2 * I * c)}) + 1890 * (280 * (d * x^{1/3} \\
& + c)^4 * b - 640 * (d * x^{1/3} + c)^3 * b * c + 560 * (d * x^{1/3} + c)^2 * b * c^2 - 22 \\
& 4 * (d * x^{1/3} + c) * b * c^3 + 35 * b * c^4) * \operatorname{polylog}(5, -e^{(2 * I * d * x^{1/3} + 2 * I * c)}) \\
& + 1260 * (-168 * I * (d * x^{1/3} + c)^5 * b + 480 * I * (d * x^{1/3} + c)^4 * b * c - 560 * I * (d \\
& * x^{1/3} + c)^3 * b * c^2 + 336 * I * (d * x^{1/3} + c)^2 * b * c^3 - 105 * I * (d * x^{1/3} + c) * b * c^4 \\
& + 14 * I * b * c^5) * \operatorname{polylog}(4, -e^{(2 * I * d * x^{1/3} + 2 * I * c)}) - 630 * (112 * (d * x^{1/3} \\
& + c)^6 * b - 384 * (d * x^{1/3} + c)^5 * b * c + 560 * (d * x^{1/3} + c)^4 * b * c^2 - 448 * (d * x^{1/3} \\
& + c)^3 * b * c^3 + 210 * (d * x^{1/3} + c)^2 * b * c^4 - 56 * (d * x^{1/3} + c) * b * c^5 + 7 * b * c^6) * \operatorname{polylog}(3, -e^{(2 * I * d * x^{1/3} \\
& + 2 * I * c)})) / d^9
\end{aligned}$$

Giac [F]

$$\int x^2 (a + b \tan(c + d \sqrt[3]{x})) dx = \int (b \tan(dx^{1/3} + c) + a) x^2 dx$$

[In] integrate(x^2*(a+b*tan(c+d*x^(1/3))),x, algorithm="giac")

[Out] integrate((b*tan(d*x^(1/3) + c) + a)*x^2, x)

Mupad [F(-1)]

Timed out.

$$\int x^2 (a + b \tan(c + d\sqrt[3]{x})) dx = \int x^2 (a + b \tan(c + dx^{1/3})) dx$$

```
[In] int(x^2*(a + b*tan(c + d*x^(1/3))),x)
```

```
[Out] int(x^2*(a + b*tan(c + d*x^(1/3))), x)
```

3.48 $\int x(a + b \tan(c + d\sqrt[3]{x})) dx$

Optimal result	300
Rubi [A] (verified)	301
Mathematica [A] (verified)	304
Maple [F]	305
Fricas [F]	305
Sympy [F]	305
Maxima [B] (verification not implemented)	305
Giac [F]	306
Mupad [F(-1)]	306

Optimal result

Integrand size = 16, antiderivative size = 203

$$\begin{aligned}
 \int x(a + b \tan(c + d\sqrt[3]{x})) dx &= \frac{ax^2}{2} + \frac{1}{2}ibx^2 - \frac{3bx^{5/3} \log(1 + e^{2i(c+d\sqrt[3]{x}})}){d} \\
 &+ \frac{15ibx^{4/3} \text{PolyLog}(2, -e^{2i(c+d\sqrt[3]{x}})}){2d^2} \\
 &- \frac{15bx \text{PolyLog}(3, -e^{2i(c+d\sqrt[3]{x}})}){d^3} \\
 &- \frac{45ibx^{2/3} \text{PolyLog}(4, -e^{2i(c+d\sqrt[3]{x}})}){2d^4} \\
 &+ \frac{45b\sqrt[3]{x} \text{PolyLog}(5, -e^{2i(c+d\sqrt[3]{x}})}){2d^5} \\
 &+ \frac{45ib \text{PolyLog}(6, -e^{2i(c+d\sqrt[3]{x}})}){4d^6}
 \end{aligned}$$

```
[Out] 1/2*a*x^2+1/2*I*b*x^2-3*b*x^(5/3)*ln(1+exp(2*I*(c+d*x^(1/3))))/d+15/2*I*b*x
^(4/3)*polylog(2,-exp(2*I*(c+d*x^(1/3))))/d^2-15*b*x*polylog(3,-exp(2*I*(c+
d*x^(1/3))))/d^3-45/2*I*b*x^(2/3)*polylog(4,-exp(2*I*(c+d*x^(1/3))))/d^4+45
/2*b*x^(1/3)*polylog(5,-exp(2*I*(c+d*x^(1/3))))/d^5+45/4*I*b*polylog(6,-exp
(2*I*(c+d*x^(1/3))))/d^6
```

Rubi [A] (verified)

Time = 0.36 (sec) , antiderivative size = 203, normalized size of antiderivative = 1.00, number of steps used = 11, number of rules used = 8, $\frac{\text{number of rules}}{\text{integrand size}} = 0.500$, Rules used = {14, 3832, 3800, 2221, 2611, 6744, 2320, 6724}

$$\int x(a + b \tan(c + d\sqrt[3]{x})) dx = \frac{ax^2}{2} + \frac{45ib \operatorname{PolyLog}\left(6, -e^{2i(c+d\sqrt[3]{x})}\right)}{4d^6} + \frac{45b\sqrt[3]{x} \operatorname{PolyLog}\left(5, -e^{2i(c+d\sqrt[3]{x})}\right)}{2d^5} - \frac{45ibx^{2/3} \operatorname{PolyLog}\left(4, -e^{2i(c+d\sqrt[3]{x})}\right)}{2d^4} - \frac{15bx \operatorname{PolyLog}\left(3, -e^{2i(c+d\sqrt[3]{x})}\right)}{d^3} + \frac{15ibx^{4/3} \operatorname{PolyLog}\left(2, -e^{2i(c+d\sqrt[3]{x})}\right)}{2d^2} - \frac{3bx^{5/3} \log\left(1 + e^{2i(c+d\sqrt[3]{x})}\right)}{d} + \frac{1}{2}ibx^2$$

[In] Int[x*(a + b*Tan[c + d*x^(1/3)]),x]

[Out] (a*x^2)/2 + (I/2)*b*x^2 - (3*b*x^(5/3)*Log[1 + E^((2*I)*(c + d*x^(1/3)))])/d + (((15*I)/2)*b*x^(4/3)*PolyLog[2, -E^((2*I)*(c + d*x^(1/3)))]/d^2 - (15*b*x*x*PolyLog[3, -E^((2*I)*(c + d*x^(1/3)))]/d^3 - (((45*I)/2)*b*x^(2/3)*PolyLog[4, -E^((2*I)*(c + d*x^(1/3)))]/d^4 + (45*b*x^(1/3)*PolyLog[5, -E^((2*I)*(c + d*x^(1/3)))]/(2*d^5) + (((45*I)/4)*b*PolyLog[6, -E^((2*I)*(c + d*x^(1/3)))]/d^6

Rule 14

Int[(u_)*((c_)*(x_))^(m_), x_Symbol] :> Int[ExpandIntegrand[(c*x)^m*u, x], x] /; FreeQ[{c, m}, x] && SumQ[u] && !LinearQ[u, x] && !MatchQ[u, (a_ + (b_)*(v_)) /; FreeQ[{a, b}, x] && InverseFunctionQ[v]]

Rule 2221

Int[(((F_)^((g_)*((e_) + (f_)*(x_))))^(n_)*((c_) + (d_)*(x_))^(m_))/((a_) + (b_)*((F_)^((g_)*((e_) + (f_)*(x_))))^(n_)), x_Symbol] :> Simp[((c + d*x)^m/(b*f*g*n*Log[F]))*Log[1 + b*((F^(g*(e + f*x)))^n/a)], x] - Dist[d*(m/(b*f*g*n*Log[F])), Int[(c + d*x)^(m - 1)*Log[1 + b*((F^(g*(e + f*x)))^n/a)], x], x] /; FreeQ[{F, a, b, c, d, e, f, g, n}, x] && IGtQ[m, 0]

Rule 2320

```
Int[u_, x_Symbol] := With[{v = FunctionOfExponential[u, x]}, Dist[v/D[v, x]
, Subst[Int[FunctionOfExponentialFunction[u, x]/x, x], x, v], x]] /; Functi
onOfExponentialQ[u, x] && !MatchQ[u, (w_)*((a_.)*(v_)^(n_))^(m_)] /; FreeQ[
{a, m, n}, x] && IntegerQ[m*n] && !MatchQ[u, E^((c_.)*((a_.) + (b_.)*x))*
(F_) [v_] /; FreeQ[{a, b, c}, x] && InverseFunctionQ[F[x]]]
```

Rule 2611

```
Int[Log[1 + (e_.)*((F_)^((c_.)*((a_.) + (b_.)*(x_))))^(n_.)]*((f_.) + (g_.)
*(x_))^(m_.), x_Symbol] := Simp[(-f + g*x)^m*(PolyLog[2, (-e)*(F^(c*(a +
b*x)))^n]/(b*c*n*Log[F])), x] + Dist[g*(m/(b*c*n*Log[F])), Int[(f + g*x)^(m
- 1)*PolyLog[2, (-e)*(F^(c*(a + b*x)))^n], x], x] /; FreeQ[{F, a, b, c, e,
f, g, n}, x] && GtQ[m, 0]
```

Rule 3800

```
Int[((c_.) + (d_.)*(x_))^(m_.)*tan[(e_.) + (f_.)*(x_)], x_Symbol] := Simp[I
*((c + d*x)^(m + 1)/(d*(m + 1))), x] - Dist[2*I, Int[(c + d*x)^m*(E^(2*I*(e
+ f*x)))/(1 + E^(2*I*(e + f*x))), x], x] /; FreeQ[{c, d, e, f}, x] && IGtQ
[m, 0]
```

Rule 3832

```
Int[(x_)^(m_.)*((a_.) + (b_.)*Tan[(c_.) + (d_.)*(x_)^(n_)])^(p_.), x_Symbol
] := Dist[1/n, Subst[Int[x^(Simplify[(m + 1)/n] - 1)*(a + b*Tan[c + d*x])^p
, x], x, x^n], x] /; FreeQ[{a, b, c, d, m, n, p}, x] && IGtQ[Simplify[(m +
1)/n], 0] && IntegerQ[p]
```

Rule 6724

```
Int[PolyLog[n_, (c_.)*((a_.) + (b_.)*(x_))^(p_.)]/((d_.) + (e_.)*(x_)), x_S
ymbol] := Simp[PolyLog[n + 1, c*(a + b*x)^p]/(e*p), x] /; FreeQ[{a, b, c, d
, e, n, p}, x] && EqQ[b*d, a*e]
```

Rule 6744

```
Int[((e_.) + (f_.)*(x_))^(m_.)*PolyLog[n_, (d_.)*((F_)^((c_.)*((a_.) + (b_.)
*(x_))))^(p_.)], x_Symbol] := Simp[(e + f*x)^m*(PolyLog[n + 1, d*(F^(c*(a
+ b*x)))^p]/(b*c*p*Log[F])), x] - Dist[f*(m/(b*c*p*Log[F])), Int[(e + f*x)^(
m - 1)*PolyLog[n + 1, d*(F^(c*(a + b*x)))^p], x], x] /; FreeQ[{F, a, b, c,
d, e, f, n, p}, x] && GtQ[m, 0]
```

Rubi steps

$$\text{integral} = \int (ax + bx \tan(c + d\sqrt[3]{x})) dx$$

$$\begin{aligned}
&= \frac{ax^2}{2} + b \int x \tan(c + d\sqrt[3]{x}) dx \\
&= \frac{ax^2}{2} + (3b)\text{Subst}\left(\int x^5 \tan(c + dx) dx, x, \sqrt[3]{x}\right) \\
&= \frac{ax^2}{2} + \frac{1}{2}ibx^2 - (6ib)\text{Subst}\left(\int \frac{e^{2i(c+dx)}x^5}{1 + e^{2i(c+dx)}} dx, x, \sqrt[3]{x}\right) \\
&= \frac{ax^2}{2} + \frac{1}{2}ibx^2 - \frac{3bx^{5/3} \log\left(1 + e^{2i(c+d\sqrt[3]{x}})\right)}{d} + \frac{(15b)\text{Subst}\left(\int x^4 \log\left(1 + e^{2i(c+dx)}\right) dx, x, \sqrt[3]{x}\right)}{d} \\
&= \frac{ax^2}{2} + \frac{1}{2}ibx^2 - \frac{3bx^{5/3} \log\left(1 + e^{2i(c+d\sqrt[3]{x}})\right)}{d} + \frac{15ibx^{4/3} \text{PolyLog}\left(2, -e^{2i(c+d\sqrt[3]{x}})\right)}{2d^2} \\
&\quad - \frac{(30ib)\text{Subst}\left(\int x^3 \text{PolyLog}\left(2, -e^{2i(c+dx)}\right) dx, x, \sqrt[3]{x}\right)}{d^2} \\
&= \frac{ax^2}{2} + \frac{1}{2}ibx^2 - \frac{3bx^{5/3} \log\left(1 + e^{2i(c+d\sqrt[3]{x}})\right)}{d} + \frac{15ibx^{4/3} \text{PolyLog}\left(2, -e^{2i(c+d\sqrt[3]{x}})\right)}{2d^2} \\
&\quad - \frac{15bx \text{PolyLog}\left(3, -e^{2i(c+d\sqrt[3]{x}})\right)}{d^3} + \frac{(45b)\text{Subst}\left(\int x^2 \text{PolyLog}\left(3, -e^{2i(c+dx)}\right) dx, x, \sqrt[3]{x}\right)}{d^3} \\
&= \frac{ax^2}{2} + \frac{1}{2}ibx^2 - \frac{3bx^{5/3} \log\left(1 + e^{2i(c+d\sqrt[3]{x}})\right)}{d} + \frac{15ibx^{4/3} \text{PolyLog}\left(2, -e^{2i(c+d\sqrt[3]{x}})\right)}{2d^2} \\
&\quad - \frac{15bx \text{PolyLog}\left(3, -e^{2i(c+d\sqrt[3]{x}})\right)}{d^3} - \frac{45ibx^{2/3} \text{PolyLog}\left(4, -e^{2i(c+d\sqrt[3]{x}})\right)}{2d^4} \\
&\quad + \frac{(45ib)\text{Subst}\left(\int x \text{PolyLog}\left(4, -e^{2i(c+dx)}\right) dx, x, \sqrt[3]{x}\right)}{d^4} \\
&= \frac{ax^2}{2} + \frac{1}{2}ibx^2 - \frac{3bx^{5/3} \log\left(1 + e^{2i(c+d\sqrt[3]{x}})\right)}{d} \\
&\quad + \frac{15ibx^{4/3} \text{PolyLog}\left(2, -e^{2i(c+d\sqrt[3]{x}})\right)}{2d^2} - \frac{15bx \text{PolyLog}\left(3, -e^{2i(c+d\sqrt[3]{x}})\right)}{d^3} \\
&\quad - \frac{45ibx^{2/3} \text{PolyLog}\left(4, -e^{2i(c+d\sqrt[3]{x}})\right)}{2d^4} + \frac{45b\sqrt[3]{x} \text{PolyLog}\left(5, -e^{2i(c+d\sqrt[3]{x}})\right)}{2d^5} \\
&\quad - \frac{(45b)\text{Subst}\left(\int \text{PolyLog}\left(5, -e^{2i(c+dx)}\right) dx, x, \sqrt[3]{x}\right)}{2d^5}
\end{aligned}$$

$$\begin{aligned}
&= \frac{ax^2}{2} + \frac{1}{2}ibx^2 - \frac{3bx^{5/3} \log\left(1 + e^{2i(c+d\sqrt[3]{x})}\right)}{d} + \frac{15ibx^{4/3} \text{PolyLog}\left(2, -e^{2i(c+d\sqrt[3]{x})}\right)}{2d^2} \\
&\quad - \frac{15bx \text{PolyLog}\left(3, -e^{2i(c+d\sqrt[3]{x})}\right)}{d^3} - \frac{45ibx^{2/3} \text{PolyLog}\left(4, -e^{2i(c+d\sqrt[3]{x})}\right)}{2d^4} \\
&\quad + \frac{45b\sqrt[3]{x} \text{PolyLog}\left(5, -e^{2i(c+d\sqrt[3]{x})}\right)}{2d^5} + \frac{(45ib)\text{Subst}\left(\int \frac{\text{PolyLog}(5,-x)}{x} dx, x, e^{2i(c+d\sqrt[3]{x})}\right)}{4d^6} \\
&= \frac{ax^2}{2} + \frac{1}{2}ibx^2 - \frac{3bx^{5/3} \log\left(1 + e^{2i(c+d\sqrt[3]{x})}\right)}{d} + \frac{15ibx^{4/3} \text{PolyLog}\left(2, -e^{2i(c+d\sqrt[3]{x})}\right)}{2d^2} \\
&\quad - \frac{15bx \text{PolyLog}\left(3, -e^{2i(c+d\sqrt[3]{x})}\right)}{d^3} - \frac{45ibx^{2/3} \text{PolyLog}\left(4, -e^{2i(c+d\sqrt[3]{x})}\right)}{2d^4} \\
&\quad + \frac{45b\sqrt[3]{x} \text{PolyLog}\left(5, -e^{2i(c+d\sqrt[3]{x})}\right)}{2d^5} + \frac{45ib \text{PolyLog}\left(6, -e^{2i(c+d\sqrt[3]{x})}\right)}{4d^6}
\end{aligned}$$

Mathematica [A] (verified)

Time = 0.03 (sec) , antiderivative size = 203, normalized size of antiderivative = 1.00

$$\begin{aligned}
\int x(a + b \tan(c + d\sqrt[3]{x})) dx &= \frac{ax^2}{2} + \frac{1}{2}ibx^2 - \frac{3bx^{5/3} \log\left(1 + e^{2i(c+d\sqrt[3]{x})}\right)}{d} \\
&\quad + \frac{15ibx^{4/3} \text{PolyLog}\left(2, -e^{2i(c+d\sqrt[3]{x})}\right)}{2d^2} \\
&\quad - \frac{15bx \text{PolyLog}\left(3, -e^{2i(c+d\sqrt[3]{x})}\right)}{d^3} \\
&\quad - \frac{45ibx^{2/3} \text{PolyLog}\left(4, -e^{2i(c+d\sqrt[3]{x})}\right)}{2d^4} \\
&\quad + \frac{45b\sqrt[3]{x} \text{PolyLog}\left(5, -e^{2i(c+d\sqrt[3]{x})}\right)}{2d^5} \\
&\quad + \frac{45ib \text{PolyLog}\left(6, -e^{2i(c+d\sqrt[3]{x})}\right)}{4d^6}
\end{aligned}$$

[In] Integrate[x*(a + b*Tan[c + d*x^(1/3)]),x]

[Out] (a*x^2)/2 + (I/2)*b*x^2 - (3*b*x^(5/3)*Log[1 + E^((2*I)*(c + d*x^(1/3)))])/d + (((15*I)/2)*b*x^(4/3)*PolyLog[2, -E^((2*I)*(c + d*x^(1/3)))])/d^2 - (15*b*x*PolyLog[3, -E^((2*I)*(c + d*x^(1/3)))])/d^3 - (((45*I)/2)*b*x^(2/3)*PolyLog[4, -E^((2*I)*(c + d*x^(1/3)))])/d^4 + (45*b*x^(1/3)*PolyLog[5, -E^((2*I)*(c + d*x^(1/3)))])/(2*d^5) + (((45*I)/4)*b*PolyLog[6, -E^((2*I)*(c + d*x^(1/3)))])/d^6

Maple [F]

$$\int x \left(a + b \tan \left(c + d x^{\frac{1}{3}} \right) \right) dx$$

```
[In] int(x*(a+b*tan(c+d*x^(1/3))),x)
```

```
[Out] int(x*(a+b*tan(c+d*x^(1/3))),x)
```

Fricas [F]

$$\int x(a + b \tan(c + d\sqrt[3]{x})) dx = \int (b \tan(dx^{\frac{1}{3}} + c) + a)x dx$$

```
[In] integrate(x*(a+b*tan(c+d*x^(1/3))),x, algorithm="fricas")
```

```
[Out] integral(b*x*tan(d*x^(1/3) + c) + a*x, x)
```

Sympy [F]

$$\int x(a + b \tan(c + d\sqrt[3]{x})) dx = \int x(a + b \tan(c + d\sqrt[3]{x})) dx$$

```
[In] integrate(x*(a+b*tan(c+d*x**(1/3))),x)
```

```
[Out] Integral(x*(a + b*tan(c + d*x**(1/3))), x)
```

Maxima [B] (verification not implemented)

Both result and optimal contain complex but leaf count of result is larger than twice the leaf count of optimal. 618 vs. 2(150) = 300.

Time = 0.40 (sec) , antiderivative size = 618, normalized size of antiderivative = 3.04

$$\int x(a + b \tan(c + d\sqrt[3]{x})) dx$$

$$= \frac{5 \left(dx^{\frac{1}{3}} + c \right)^6 a + 5i \left(dx^{\frac{1}{3}} + c \right)^6 b - 30 \left(dx^{\frac{1}{3}} + c \right)^5 ac - 30i \left(dx^{\frac{1}{3}} + c \right)^5 bc + 75 \left(dx^{\frac{1}{3}} + c \right)^4 ac^2 + 75i \left(dx^{\frac{1}{3}} + c \right)^4 bc^2 - 100 \left(dx^{\frac{1}{3}} + c \right)^3 a^2 c - 100i \left(dx^{\frac{1}{3}} + c \right)^3 b^2 c + 75 \left(dx^{\frac{1}{3}} + c \right)^2 a^2 c^2 + 75i \left(dx^{\frac{1}{3}} + c \right)^2 b^2 c^2 - 100 \left(dx^{\frac{1}{3}} + c \right) a^3 - 100i \left(dx^{\frac{1}{3}} + c \right) b^3 + 75 a^4 + 75i a^4 c + 75 b^4 + 75i b^4 c}{10}$$

```
[In] integrate(x*(a+b*tan(c+d*x^(1/3))),x, algorithm="maxima")
```

```
[Out] 1/10*(5*(d*x^(1/3) + c)^6*a + 5*I*(d*x^(1/3) + c)^6*b - 30*(d*x^(1/3) + c)^5*a*c - 30*I*(d*x^(1/3) + c)^5*b*c + 75*(d*x^(1/3) + c)^4*a*c^2 + 75*I*(d*x^(1/3) + c)^4*b*c^2 - 100*(d*x^(1/3) + c)^3*a*c^3 - 100*I*(d*x^(1/3) + c)^3*b*c^3 + 75*(d*x^(1/3) + c)^2*a^2*c + 75*I*(d*x^(1/3) + c)^2*b^2*c^2 - 100*(d*x^(1/3) + c)*a^3 - 100*I*(d*x^(1/3) + c)*b^3 + 75*a^4 + 75*I*a^4*c + 75*b^4 + 75*I*b^4*c)
```

```

*b*c^3 + 75*(d*x^(1/3) + c)^2*a*c^4 + 75*I*(d*x^(1/3) + c)^2*b*c^4 - 30*(d*
x^(1/3) + c)*a*c^5 - 30*b*c^5*log(sec(d*x^(1/3) + c)) + 2*(-48*I*(d*x^(1/3)
+ c)^5*b + 150*I*(d*x^(1/3) + c)^4*b*c - 200*I*(d*x^(1/3) + c)^3*b*c^2 + 1
50*I*(d*x^(1/3) + c)^2*b*c^3 - 75*I*(d*x^(1/3) + c)*b*c^4)*arctan2(sin(2*d*
x^(1/3) + 2*c), cos(2*d*x^(1/3) + 2*c) + 1) + 15*(16*I*(d*x^(1/3) + c)^4*b
- 40*I*(d*x^(1/3) + c)^3*b*c + 40*I*(d*x^(1/3) + c)^2*b*c^2 - 20*I*(d*x^(1/
3) + c)*b*c^3 + 5*I*b*c^4)*dilog(-e^(2*I*d*x^(1/3) + 2*I*c)) - (48*(d*x^(1/
3) + c)^5*b - 150*(d*x^(1/3) + c)^4*b*c + 200*(d*x^(1/3) + c)^3*b*c^2 - 150
*(d*x^(1/3) + c)^2*b*c^3 + 75*(d*x^(1/3) + c)*b*c^4)*log(cos(2*d*x^(1/3) +
2*c)^2 + sin(2*d*x^(1/3) + 2*c)^2 + 2*cos(2*d*x^(1/3) + 2*c) + 1) + 360*I*b
*polylog(6, -e^(2*I*d*x^(1/3) + 2*I*c)) + 90*(8*(d*x^(1/3) + c)*b - 5*b*c)*
polylog(5, -e^(2*I*d*x^(1/3) + 2*I*c)) + 60*(-12*I*(d*x^(1/3) + c)^2*b + 15
*I*(d*x^(1/3) + c)*b*c - 5*I*b*c^2)*polylog(4, -e^(2*I*d*x^(1/3) + 2*I*c))
- 30*(16*(d*x^(1/3) + c)^3*b - 30*(d*x^(1/3) + c)^2*b*c + 20*(d*x^(1/3) + c
)*b*c^2 - 5*b*c^3)*polylog(3, -e^(2*I*d*x^(1/3) + 2*I*c)))/d^6

```

Giac [F]

$$\int x(a + b \tan(c + d\sqrt[3]{x})) dx = \int (b \tan(dx^{\frac{1}{3}} + c) + a)x dx$$

```
[In] integrate(x*(a+b*tan(c+d*x^(1/3))),x, algorithm="giac")
```

```
[Out] integrate((b*tan(d*x^(1/3) + c) + a)*x, x)
```

Mupad [F(-1)]

Timed out.

$$\int x(a + b \tan(c + d\sqrt[3]{x})) dx = \int x(a + b \tan(c + dx^{1/3})) dx$$

```
[In] int(x*(a + b*tan(c + d*x^(1/3))),x)
```

```
[Out] int(x*(a + b*tan(c + d*x^(1/3))), x)
```

3.49 $\int (a + b \tan (c + d\sqrt[3]{x})) dx$

Optimal result	307
Rubi [A] (verified)	307
Mathematica [A] (verified)	309
Maple [F]	310
Fricas [B] (verification not implemented)	310
Sympy [F]	310
Maxima [F]	311
Giac [F]	311
Mupad [F(-1)]	311

Optimal result

Integrand size = 14, antiderivative size = 98

$$\int (a + b \tan (c + d\sqrt[3]{x})) dx = ax + ibx - \frac{3bx^{2/3} \log (1 + e^{2i(c+d\sqrt[3]{x})})}{d} + \frac{3ib\sqrt[3]{x} \operatorname{PolyLog} (2, -e^{2i(c+d\sqrt[3]{x})})}{d^2} - \frac{3b \operatorname{PolyLog} (3, -e^{2i(c+d\sqrt[3]{x})})}{2d^3}$$

[Out] a*x+I*b*x-3*b*x^(2/3)*ln(1+exp(2*I*(c+d*x^(1/3))))/d+3*I*b*x^(1/3)*polylog(2,-exp(2*I*(c+d*x^(1/3))))/d^2-3/2*b*polylog(3,-exp(2*I*(c+d*x^(1/3))))/d^3

Rubi [A] (verified)

Time = 0.22 (sec) , antiderivative size = 98, normalized size of antiderivative = 1.00, number of steps used = 7, number of rules used = 6, $\frac{\text{number of rules}}{\text{integrand size}} = 0.429$, Rules used = {3824, 3800, 2221, 2611, 2320, 6724}

$$\int (a + b \tan (c + d\sqrt[3]{x})) dx = ax - \frac{3b \operatorname{PolyLog} (3, -e^{2i(c+d\sqrt[3]{x})})}{2d^3} + \frac{3ib\sqrt[3]{x} \operatorname{PolyLog} (2, -e^{2i(c+d\sqrt[3]{x})})}{d^2} - \frac{3bx^{2/3} \log (1 + e^{2i(c+d\sqrt[3]{x})})}{d} + ibx$$

[In] Int[a + b*Tan[c + d*x^(1/3)],x]

[Out] $a*x + I*b*x - (3*b*x^{(2/3)}*Log[1 + E^{((2*I)*(c + d*x^{(1/3)})}))/d + ((3*I)*b*x^{(1/3)}*PolyLog[2, -E^{((2*I)*(c + d*x^{(1/3)})}))/d^2 - (3*b*PolyLog[3, -E^{((2*I)*(c + d*x^{(1/3)})})]/(2*d^3)$

Rule 2221

Int[(((F_)^((g_)*(e_) + (f_)*(x_)))^(n_))*((c_) + (d_)*(x_))^(m_)]/((a_) + (b_)*((F_)^((g_)*(e_) + (f_)*(x_)))^(n_)), x_Symbol] := Simp[((c + d*x)^m/(b*f*g*n*Log[F]))*Log[1 + b*((F^(g*(e + f*x)))^n/a)], x] - Dist[d*(m/(b*f*g*n*Log[F])), Int[(c + d*x)^(m - 1)*Log[1 + b*((F^(g*(e + f*x)))^n/a)], x], x] /; FreeQ[{F, a, b, c, d, e, f, g, n}, x] && IGtQ[m, 0]

Rule 2320

Int[u_, x_Symbol] := With[{v = FunctionOfExponential[u, x]}, Dist[v/D[v, x], Subst[Int[FunctionOfExponentialFunction[u, x]/x, x], x, v], x] /; FunctionOfExponentialQ[u, x] && !MatchQ[u, (w_)*((a_)*(v_)^(n_))^(m_)] /; FreeQ[{a, m, n}, x] && IntegerQ[m*n] && !MatchQ[u, E^{(c_)*((a_) + (b_)*x)}*(F_)[v_] /; FreeQ[{a, b, c}, x] && InverseFunctionQ[F[x]]]

Rule 2611

Int[Log[1 + (e_)*((F_)^((c_)*((a_) + (b_)*(x_)))^(n_))]*((f_) + (g_)*(x_))^(m_), x_Symbol] := Simp[(-f + g*x)^m*(PolyLog[2, (-e)*(F^(c*(a + b*x)))^n]/(b*c*n*Log[F])), x] + Dist[g*(m/(b*c*n*Log[F])), Int[(f + g*x)^(m - 1)*PolyLog[2, (-e)*(F^(c*(a + b*x)))^n], x], x] /; FreeQ[{F, a, b, c, e, f, g, n}, x] && GtQ[m, 0]

Rule 3800

Int[((c_) + (d_)*(x_))^(m_)*tan[(e_) + (f_)*(x_)], x_Symbol] := Simp[I*((c + d*x)^(m + 1)/(d*(m + 1))), x] - Dist[2*I, Int[(c + d*x)^m*(E^(2*I*(e + f*x)))/(1 + E^(2*I*(e + f*x))), x], x] /; FreeQ[{c, d, e, f}, x] && IGtQ[m, 0]

Rule 3824

Int[((a_) + (b_)*Tan[(c_) + (d_)*(x_)^(n_)])^(p_), x_Symbol] := Dist[1/n, Subst[Int[x^(1/n - 1)*(a + b*Tan[c + d*x])^p, x], x, x^n], x] /; FreeQ[{a, b, c, d, p}, x] && IGtQ[1/n, 0] && IntegerQ[p]

Rule 6724

Int[PolyLog[n_, (c_)*((a_) + (b_)*(x_))^(p_)]/((d_) + (e_)*(x_)), x_Symbol] := Simp[PolyLog[n + 1, c*(a + b*x)^p]/(e*p), x] /; FreeQ[{a, b, c, d, e, n, p}, x] && EqQ[b*d, a*e]

Rubi steps

$$\begin{aligned}
 \text{integral} &= ax + b \int \tan(c + d\sqrt[3]{x}) dx \\
 &= ax + (3b)\text{Subst}\left(\int x^2 \tan(c + dx) dx, x, \sqrt[3]{x}\right) \\
 &= ax + ibx - (6ib)\text{Subst}\left(\int \frac{e^{2i(c+dx)}x^2}{1 + e^{2i(c+dx)}} dx, x, \sqrt[3]{x}\right) \\
 &= ax + ibx - \frac{3bx^{2/3} \log\left(1 + e^{2i(c+d\sqrt[3]{x})}\right)}{d} + \frac{(6b)\text{Subst}\left(\int x \log\left(1 + e^{2i(c+dx)}\right) dx, x, \sqrt[3]{x}\right)}{d} \\
 &= ax + ibx - \frac{3bx^{2/3} \log\left(1 + e^{2i(c+d\sqrt[3]{x})}\right)}{d} + \frac{3ib\sqrt[3]{x} \text{PolyLog}\left(2, -e^{2i(c+d\sqrt[3]{x})}\right)}{d^2} \\
 &\quad - \frac{(3ib)\text{Subst}\left(\int \text{PolyLog}\left(2, -e^{2i(c+dx)}\right) dx, x, \sqrt[3]{x}\right)}{d^2} \\
 &= ax + ibx - \frac{3bx^{2/3} \log\left(1 + e^{2i(c+d\sqrt[3]{x})}\right)}{d} + \frac{3ib\sqrt[3]{x} \text{PolyLog}\left(2, -e^{2i(c+d\sqrt[3]{x})}\right)}{d^2} \\
 &\quad - \frac{(3b)\text{Subst}\left(\int \frac{\text{PolyLog}(2, -x)}{x} dx, x, e^{2i(c+d\sqrt[3]{x})}\right)}{2d^3} \\
 &= ax + ibx - \frac{3bx^{2/3} \log\left(1 + e^{2i(c+d\sqrt[3]{x})}\right)}{d} \\
 &\quad + \frac{3ib\sqrt[3]{x} \text{PolyLog}\left(2, -e^{2i(c+d\sqrt[3]{x})}\right)}{d^2} - \frac{3b \text{PolyLog}\left(3, -e^{2i(c+d\sqrt[3]{x})}\right)}{2d^3}
 \end{aligned}$$

Mathematica [A] (verified)

Time = 0.02 (sec) , antiderivative size = 98, normalized size of antiderivative = 1.00

$$\begin{aligned}
 \int (a + b \tan(c + d\sqrt[3]{x})) dx &= ax + ibx - \frac{3bx^{2/3} \log\left(1 + e^{2i(c+d\sqrt[3]{x})}\right)}{d} \\
 &\quad + \frac{3ib\sqrt[3]{x} \text{PolyLog}\left(2, -e^{2i(c+d\sqrt[3]{x})}\right)}{d^2} \\
 &\quad - \frac{3b \text{PolyLog}\left(3, -e^{2i(c+d\sqrt[3]{x})}\right)}{2d^3}
 \end{aligned}$$

[In] Integrate[a + b*Tan[c + d*x^(1/3)], x]

[Out] a*x + I*b*x - (3*b*x^(2/3)*Log[1 + E^((2*I)*(c + d*x^(1/3)))])/d + ((3*I)*b*x^(1/3)*PolyLog[2, -E^((2*I)*(c + d*x^(1/3)))])/d^2 - (3*b*PolyLog[3, -E^((2*I)*(c + d*x^(1/3)))])/(2*d^3)

Maple [F]

$$\int (a + b \tan(c + d x^{\frac{1}{3}})) dx$$

[In] int(a+b*tan(c+d*x^(1/3)),x)

[Out] int(a+b*tan(c+d*x^(1/3)),x)

Fricas [B] (verification not implemented)

Both result and optimal contain complex but leaf count of result is larger than twice the leaf count of optimal. 249 vs. $2(75) = 150$.

Time = 0.27 (sec) , antiderivative size = 249, normalized size of antiderivative = 2.54

$$\int (a + b \tan(c + d\sqrt[3]{x})) dx$$

$$= \frac{4ad^3x - 6bd^2x^{\frac{2}{3}} \log\left(-\frac{2(i \tan(dx^{\frac{1}{3}}+c)-1)}{\tan(dx^{\frac{1}{3}}+c)^2+1}\right) - 6bd^2x^{\frac{2}{3}} \log\left(-\frac{2(-i \tan(dx^{\frac{1}{3}}+c)-1)}{\tan(dx^{\frac{1}{3}}+c)^2+1}\right) - 6i bdx^{\frac{1}{3}} \text{Li}_2\left(\frac{2(i \tan(dx^{\frac{1}{3}}+c)-1)}{\tan(dx^{\frac{1}{3}}+c)^2+1}\right) + 6i bdx^{\frac{1}{3}} \text{Li}_2\left(\frac{2(-i \tan(dx^{\frac{1}{3}}+c)-1)}{\tan(dx^{\frac{1}{3}}+c)^2+1}\right)}{d^3}$$

[In] integrate(a+b*tan(c+d*x^(1/3)),x, algorithm="fricas")

[Out] $\frac{1}{4}*(4*a*d^3*x - 6*b*d^2*x^{(2/3)}*\log(-2*(I*\tan(d*x^{(1/3)} + c) - 1)/(\tan(d*x^{(1/3)} + c)^2 + 1)) - 6*b*d^2*x^{(2/3)}*\log(-2*(-I*\tan(d*x^{(1/3)} + c) - 1)/(\tan(d*x^{(1/3)} + c)^2 + 1)) - 6*I*b*d*x^{(1/3)}*dilog(2*(I*\tan(d*x^{(1/3)} + c) - 1)/(\tan(d*x^{(1/3)} + c)^2 + 1) + 1) + 6*I*b*d*x^{(1/3)}*dilog(2*(-I*\tan(d*x^{(1/3)} + c) - 1)/(\tan(d*x^{(1/3)} + c)^2 + 1) + 1) - 3*b*polylog(3, (\tan(d*x^{(1/3)} + c)^2 + 2*I*\tan(d*x^{(1/3)} + c) - 1)/(\tan(d*x^{(1/3)} + c)^2 + 1)) - 3*b*polylog(3, (\tan(d*x^{(1/3)} + c)^2 - 2*I*\tan(d*x^{(1/3)} + c) - 1)/(\tan(d*x^{(1/3)} + c)^2 + 1))))/d^3$

Sympy [F]

$$\int (a + b \tan(c + d\sqrt[3]{x})) dx = \int (a + b \tan(c + d\sqrt[3]{x})) dx$$

[In] integrate(a+b*tan(c+d*x**(1/3)),x)

[Out] Integral(a + b*tan(c + d*x**(1/3)), x)

Maxima [F]

$$\int (a + b \tan(c + d\sqrt[3]{x})) dx = \int b \tan\left(dx^{\frac{1}{3}} + c\right) + a dx$$

[In] integrate(a+b*tan(c+d*x^(1/3)),x, algorithm="maxima")

[Out] a*x + 2*b*integrate(sin(2*d*x^(1/3) + 2*c)/(cos(2*d*x^(1/3) + 2*c)^2 + sin(2*d*x^(1/3) + 2*c)^2 + 2*cos(2*d*x^(1/3) + 2*c) + 1), x)

Giac [F]

$$\int (a + b \tan(c + d\sqrt[3]{x})) dx = \int b \tan\left(dx^{\frac{1}{3}} + c\right) + a dx$$

[In] integrate(a+b*tan(c+d*x^(1/3)),x, algorithm="giac")

[Out] integrate(b*tan(d*x^(1/3) + c) + a, x)

Mupad [F(-1)]

Timed out.

$$\int (a + b \tan(c + d\sqrt[3]{x})) dx = \int a + b \tan(c + dx^{1/3}) dx$$

[In] int(a + b*tan(c + d*x^(1/3)),x)

[Out] int(a + b*tan(c + d*x^(1/3)), x)

$$3.50 \quad \int \frac{a+b \tan \left(c+d \sqrt[3]{x}\right)}{x} dx$$

Optimal result	312
Rubi [N/A]	312
Mathematica [N/A]	313
Maple [N/A] (verified)	313
Fricas [N/A]	313
Sympy [N/A]	314
Maxima [N/A]	314
Giac [N/A]	314
Mupad [N/A]	315

Optimal result

Integrand size = 18, antiderivative size = 18

$$\int \frac{a+b \tan \left(c+d \sqrt[3]{x}\right)}{x} dx = a \log(x) + b \operatorname{Int}\left(\frac{\tan \left(c+d \sqrt[3]{x}\right)}{x}, x\right)$$

[Out] a*ln(x)+b*Unintegrable(tan(c+d*x^(1/3))/x,x)

Rubi [N/A]

Not integrable

Time = 0.03 (sec) , antiderivative size = 18, normalized size of antiderivative = 1.00, number of steps used = 0, number of rules used = 0, $\frac{\text{number of rules}}{\text{integrand size}} = 0.000$, Rules used = {}

$$\int \frac{a+b \tan \left(c+d \sqrt[3]{x}\right)}{x} dx = \int \frac{a+b \tan \left(c+d \sqrt[3]{x}\right)}{x} dx$$

[In] Int[(a + b*Tan[c + d*x^(1/3)])/x,x]

[Out] a*Log[x] + b*Defer[Int][Tan[c + d*x^(1/3)]/x, x]

Rubi steps

$$\begin{aligned} \text{integral} &= \int \left(\frac{a}{x} + \frac{b \tan \left(c+d \sqrt[3]{x}\right)}{x} \right) dx \\ &= a \log(x) + b \int \frac{\tan \left(c+d \sqrt[3]{x}\right)}{x} dx \end{aligned}$$

Mathematica [N/A]

Not integrable

Time = 4.95 (sec) , antiderivative size = 20, normalized size of antiderivative = 1.11

$$\int \frac{a + b \tan(c + d\sqrt[3]{x})}{x} dx = \int \frac{a + b \tan(c + d\sqrt[3]{x})}{x} dx$$

[In] Integrate[(a + b*Tan[c + d*x^(1/3)])/x,x]

[Out] Integrate[(a + b*Tan[c + d*x^(1/3)])/x, x]

Maple [N/A] (verified)

Not integrable

Time = 0.39 (sec) , antiderivative size = 16, normalized size of antiderivative = 0.89

$$\int \frac{a + b \tan(c + dx^{\frac{1}{3}})}{x} dx$$

[In] int((a+b*tan(c+d*x^(1/3)))/x,x)

[Out] int((a+b*tan(c+d*x^(1/3)))/x,x)

Fricas [N/A]

Not integrable

Time = 0.23 (sec) , antiderivative size = 18, normalized size of antiderivative = 1.00

$$\int \frac{a + b \tan(c + d\sqrt[3]{x})}{x} dx = \int \frac{b \tan(dx^{\frac{1}{3}} + c) + a}{x} dx$$

[In] integrate((a+b*tan(c+d*x^(1/3)))/x,x, algorithm="fricas")

[Out] integral((b*tan(d*x^(1/3) + c) + a)/x, x)

Sympy [N/A]

Not integrable

Time = 1.63 (sec) , antiderivative size = 15, normalized size of antiderivative = 0.83

$$\int \frac{a + b \tan(c + d\sqrt[3]{x})}{x} dx = \int \frac{a + b \tan(c + d\sqrt[3]{x})}{x} dx$$

```
[In] integrate((a+b*tan(c+d*x**(1/3)))/x,x)
```

```
[Out] Integral((a + b*tan(c + d*x**(1/3)))/x, x)
```

Maxima [N/A]

Not integrable

Time = 0.53 (sec) , antiderivative size = 68, normalized size of antiderivative = 3.78

$$\int \frac{a + b \tan(c + d\sqrt[3]{x})}{x} dx = \int \frac{b \tan\left(\frac{dx^{\frac{1}{3}}}{x} + c\right) + a}{x} dx$$

```
[In] integrate((a+b*tan(c+d*x^(1/3)))/x,x, algorithm="maxima")
```

```
[Out] 2*b*integrate(sin(2*d*x^(1/3) + 2*c)/((cos(2*d*x^(1/3) + 2*c)^2 + sin(2*d*x^(1/3) + 2*c)^2 + 2*cos(2*d*x^(1/3) + 2*c) + 1)*x), x) + a*log(x)
```

Giac [N/A]

Not integrable

Time = 0.46 (sec) , antiderivative size = 18, normalized size of antiderivative = 1.00

$$\int \frac{a + b \tan(c + d\sqrt[3]{x})}{x} dx = \int \frac{b \tan\left(\frac{dx^{\frac{1}{3}}}{x} + c\right) + a}{x} dx$$

```
[In] integrate((a+b*tan(c+d*x^(1/3)))/x,x, algorithm="giac")
```

```
[Out] integrate((b*tan(d*x^(1/3) + c) + a)/x, x)
```

Mupad [N/A]

Not integrable

Time = 4.10 (sec) , antiderivative size = 18, normalized size of antiderivative = 1.00

$$\int \frac{a + b \tan(c + d\sqrt[3]{x})}{x} dx = \int \frac{a + b \tan(c + dx^{1/3})}{x} dx$$

```
[In] int((a + b*tan(c + d*x^(1/3)))/x,x)
```

```
[Out] int((a + b*tan(c + d*x^(1/3)))/x, x)
```

$$3.51 \quad \int \frac{a+b \tan \left(c+d \sqrt[3]{x}\right)}{x^2} dx$$

Optimal result	316
Rubi [N/A]	316
Mathematica [N/A]	317
Maple [N/A] (verified)	317
Fricas [N/A]	317
Sympy [N/A]	318
Maxima [N/A]	318
Giac [N/A]	318
Mupad [N/A]	319

Optimal result

Integrand size = 18, antiderivative size = 18

$$\int \frac{a+b \tan \left(c+d \sqrt[3]{x}\right)}{x^2} dx = -\frac{a}{x} + b \operatorname{Int} \left(\frac{\tan \left(c+d \sqrt[3]{x}\right)}{x^2}, x \right)$$

[Out] `-a/x+b*Unintegrable(tan(c+d*x^(1/3))/x^2,x)`

Rubi [N/A]

Not integrable

Time = 0.03 (sec) , antiderivative size = 18, normalized size of antiderivative = 1.00, number of steps used = 0, number of rules used = 0, $\frac{\text{number of rules}}{\text{integrand size}} = 0.000$, Rules used = {}

$$\int \frac{a+b \tan \left(c+d \sqrt[3]{x}\right)}{x^2} dx = \int \frac{a+b \tan \left(c+d \sqrt[3]{x}\right)}{x^2} dx$$

[In] `Int[(a + b*Tan[c + d*x^(1/3)])/x^2,x]`

[Out] `-(a/x) + b*Defer[Int][Tan[c + d*x^(1/3)]/x^2, x]`

Rubi steps

$$\begin{aligned} \text{integral} &= \int \left(\frac{a}{x^2} + \frac{b \tan \left(c+d \sqrt[3]{x}\right)}{x^2} \right) dx \\ &= -\frac{a}{x} + b \int \frac{\tan \left(c+d \sqrt[3]{x}\right)}{x^2} dx \end{aligned}$$

Mathematica [N/A]

Not integrable

Time = 2.10 (sec) , antiderivative size = 20, normalized size of antiderivative = 1.11

$$\int \frac{a + b \tan(c + d\sqrt[3]{x})}{x^2} dx = \int \frac{a + b \tan(c + d\sqrt[3]{x})}{x^2} dx$$

[In] Integrate[(a + b*Tan[c + d*x^(1/3)])/x^2,x]

[Out] Integrate[(a + b*Tan[c + d*x^(1/3)])/x^2, x]

Maple [N/A] (verified)

Not integrable

Time = 0.35 (sec) , antiderivative size = 16, normalized size of antiderivative = 0.89

$$\int \frac{a + b \tan\left(c + dx^{\frac{1}{3}}\right)}{x^2} dx$$

[In] int((a+b*tan(c+d*x^(1/3)))/x^2,x)

[Out] int((a+b*tan(c+d*x^(1/3)))/x^2,x)

Fricas [N/A]

Not integrable

Time = 0.25 (sec) , antiderivative size = 18, normalized size of antiderivative = 1.00

$$\int \frac{a + b \tan(c + d\sqrt[3]{x})}{x^2} dx = \int \frac{b \tan\left(dx^{\frac{1}{3}} + c\right) + a}{x^2} dx$$

[In] integrate((a+b*tan(c+d*x^(1/3)))/x^2,x, algorithm="fricas")

[Out] integral((b*tan(d*x^(1/3) + c) + a)/x^2, x)

Sympy [N/A]

Not integrable

Time = 1.82 (sec) , antiderivative size = 17, normalized size of antiderivative = 0.94

$$\int \frac{a + b \tan(c + d\sqrt[3]{x})}{x^2} dx = \int \frac{a + b \tan(c + d\sqrt[3]{x})}{x^2} dx$$

[In] integrate((a+b*tan(c+d*x**(1/3)))/x**2,x)

[Out] Integral((a + b*tan(c + d*x**(1/3)))/x**2, x)

Maxima [N/A]

Not integrable

Time = 0.53 (sec) , antiderivative size = 72, normalized size of antiderivative = 4.00

$$\int \frac{a + b \tan(c + d\sqrt[3]{x})}{x^2} dx = \int \frac{b \tan\left(\frac{dx^{\frac{1}{3}}}{x} + c\right) + a}{x^2} dx$$

[In] integrate((a+b*tan(c+d*x^(1/3)))/x^2,x, algorithm="maxima")

[Out] (2*b*x*integrate(sin(2*d*x^(1/3) + 2*c)/((cos(2*d*x^(1/3) + 2*c)^2 + sin(2*d*x^(1/3) + 2*c)^2 + 2*cos(2*d*x^(1/3) + 2*c) + 1)*x^2), x) - a)/x

Giac [N/A]

Not integrable

Time = 0.46 (sec) , antiderivative size = 18, normalized size of antiderivative = 1.00

$$\int \frac{a + b \tan(c + d\sqrt[3]{x})}{x^2} dx = \int \frac{b \tan\left(\frac{dx^{\frac{1}{3}}}{x} + c\right) + a}{x^2} dx$$

[In] integrate((a+b*tan(c+d*x^(1/3)))/x^2,x, algorithm="giac")

[Out] integrate((b*tan(d*x^(1/3) + c) + a)/x^2, x)

Mupad [N/A]

Not integrable

Time = 4.10 (sec) , antiderivative size = 18, normalized size of antiderivative = 1.00

$$\int \frac{a + b \tan(c + d\sqrt[3]{x})}{x^2} dx = \int \frac{a + b \tan(c + dx^{1/3})}{x^2} dx$$

```
[In] int((a + b*tan(c + d*x^(1/3)))/x^2,x)
```

```
[Out] int((a + b*tan(c + d*x^(1/3)))/x^2, x)
```

3.52 $\int x^2 (a + b \tan (c + d\sqrt[3]{x}))^2 dx$

Optimal result	321
Rubi [A] (verified)	322
Mathematica [A] (verified)	331
Maple [F]	332
Fricas [F]	332
Sympy [F]	333
Maxima [B] (verification not implemented)	333
Giac [F]	336
Mupad [F(-1)]	336

Optimal result

Integrand size = 20, antiderivative size = 597

$$\begin{aligned}
 \int x^2 (a + b \tan(c + d\sqrt[3]{x}))^2 dx = & -\frac{3ib^2x^{8/3}}{d} + \frac{a^2x^3}{3} + \frac{2}{3}iabx^3 - \frac{b^2x^3}{3} \\
 & + \frac{24b^2x^{7/3} \log\left(1 + e^{2i(c+d\sqrt[3]{x})}\right)}{d^2} \\
 & - \frac{6abx^{8/3} \log\left(1 + e^{2i(c+d\sqrt[3]{x})}\right)}{d} \\
 & - \frac{84ib^2x^2 \operatorname{PolyLog}\left(2, -e^{2i(c+d\sqrt[3]{x})}\right)}{d^3} \\
 & + \frac{24iabx^{7/3} \operatorname{PolyLog}\left(2, -e^{2i(c+d\sqrt[3]{x})}\right)}{d^2} \\
 & + \frac{252b^2x^{5/3} \operatorname{PolyLog}\left(3, -e^{2i(c+d\sqrt[3]{x})}\right)}{d^4} \\
 & - \frac{84abx^2 \operatorname{PolyLog}\left(3, -e^{2i(c+d\sqrt[3]{x})}\right)}{d^3} \\
 & + \frac{630ib^2x^{4/3} \operatorname{PolyLog}\left(4, -e^{2i(c+d\sqrt[3]{x})}\right)}{d^5} \\
 & - \frac{252iabx^{5/3} \operatorname{PolyLog}\left(4, -e^{2i(c+d\sqrt[3]{x})}\right)}{d^4} \\
 & - \frac{1260b^2x \operatorname{PolyLog}\left(5, -e^{2i(c+d\sqrt[3]{x})}\right)}{d^6} \\
 & + \frac{630abx^{4/3} \operatorname{PolyLog}\left(5, -e^{2i(c+d\sqrt[3]{x})}\right)}{d^5} \\
 & - \frac{1890ib^2x^{2/3} \operatorname{PolyLog}\left(6, -e^{2i(c+d\sqrt[3]{x})}\right)}{d^7} \\
 & + \frac{1260iabx \operatorname{PolyLog}\left(6, -e^{2i(c+d\sqrt[3]{x})}\right)}{d^6} \\
 & + \frac{1890b^2\sqrt[3]{x} \operatorname{PolyLog}\left(7, -e^{2i(c+d\sqrt[3]{x})}\right)}{d^8} \\
 & - \frac{1890abx^{2/3} \operatorname{PolyLog}\left(7, -e^{2i(c+d\sqrt[3]{x})}\right)}{d^7} \\
 & + \frac{945ib^2 \operatorname{PolyLog}\left(8, -e^{2i(c+d\sqrt[3]{x})}\right)}{d^9} \\
 & - \frac{1890iab\sqrt[3]{x} \operatorname{PolyLog}\left(8, -e^{2i(c+d\sqrt[3]{x})}\right)}{d^8} \\
 & + \frac{945ab \operatorname{PolyLog}\left(9, -e^{2i(c+d\sqrt[3]{x})}\right)}{d^9} \\
 & - \frac{212ab^{8/3} \operatorname{PolyLog}\left(9, -e^{2i(c+d\sqrt[3]{x})}\right)}{d^8}
 \end{aligned}$$

```
[Out] 24*I*a*b*x^(7/3)*polylog(2,-exp(2*I*(c+d*x^(1/3))))/d^2+1/3*a^2*x^3-3*I*b^2
*x^(8/3)/d-1/3*b^2*x^3+24*b^2*x^(7/3)*ln(1+exp(2*I*(c+d*x^(1/3))))/d^2-6*a*
b*x^(8/3)*ln(1+exp(2*I*(c+d*x^(1/3))))/d-1890*I*a*b*x^(1/3)*polylog(8,-exp(
2*I*(c+d*x^(1/3))))/d^8+945*I*b^2*polylog(8,-exp(2*I*(c+d*x^(1/3))))/d^9+25
2*b^2*x^(5/3)*polylog(3,-exp(2*I*(c+d*x^(1/3))))/d^4-84*a*b*x^2*polylog(3,-
exp(2*I*(c+d*x^(1/3))))/d^3-84*I*b^2*x^2*polylog(2,-exp(2*I*(c+d*x^(1/3))))
/d^3+1260*I*a*b*x*polylog(6,-exp(2*I*(c+d*x^(1/3))))/d^6-1260*b^2*x*polylog
(5,-exp(2*I*(c+d*x^(1/3))))/d^6+630*a*b*x^(4/3)*polylog(5,-exp(2*I*(c+d*x^(
1/3))))/d^5+630*I*b^2*x^(4/3)*polylog(4,-exp(2*I*(c+d*x^(1/3))))/d^5-1890*I
*b^2*x^(2/3)*polylog(6,-exp(2*I*(c+d*x^(1/3))))/d^7+1890*b^2*x^(1/3)*polylo
g(7,-exp(2*I*(c+d*x^(1/3))))/d^8-1890*a*b*x^(2/3)*polylog(7,-exp(2*I*(c+d*x
^(1/3))))/d^7+2/3*I*a*b*x^3-252*I*a*b*x^(5/3)*polylog(4,-exp(2*I*(c+d*x^(1/
3))))/d^4+945*a*b*polylog(9,-exp(2*I*(c+d*x^(1/3))))/d^9+3*b^2*x^(8/3)*tan(
c+d*x^(1/3))/d
```

Rubi [A] (verified)

Time = 1.27 (sec) , antiderivative size = 597, normalized size of antiderivative = 1.00, number of steps used = 26, number of rules used = 10, $\frac{\text{number of rules}}{\text{integrand size}} = 0.500$, Rules

used = {3832, 3803, 3800, 2221, 2611, 6744, 2320, 6724, 3801, 30}

$$\begin{aligned}
\int x^2 (a + b \tan(c + d\sqrt[3]{x}))^2 dx = & \frac{a^2 x^3}{3} + \frac{945ab \operatorname{PolyLog}\left(9, -e^{2i(c+d\sqrt[3]{x})}\right)}{d^9} \\
& - \frac{1890iab\sqrt[3]{x} \operatorname{PolyLog}\left(8, -e^{2i(c+d\sqrt[3]{x})}\right)}{d^8} \\
& - \frac{1890abx^{2/3} \operatorname{PolyLog}\left(7, -e^{2i(c+d\sqrt[3]{x})}\right)}{d^7} \\
& + \frac{1260iabx \operatorname{PolyLog}\left(6, -e^{2i(c+d\sqrt[3]{x})}\right)}{d^6} \\
& + \frac{630abx^{4/3} \operatorname{PolyLog}\left(5, -e^{2i(c+d\sqrt[3]{x})}\right)}{d^5} \\
& - \frac{252iabx^{5/3} \operatorname{PolyLog}\left(4, -e^{2i(c+d\sqrt[3]{x})}\right)}{d^4} \\
& - \frac{84abx^2 \operatorname{PolyLog}\left(3, -e^{2i(c+d\sqrt[3]{x})}\right)}{d^3} \\
& + \frac{24iabx^{7/3} \operatorname{PolyLog}\left(2, -e^{2i(c+d\sqrt[3]{x})}\right)}{d^2} \\
& - \frac{6abx^{8/3} \log\left(1 + e^{2i(c+d\sqrt[3]{x})}\right)}{d} + \frac{2}{3}iabx^3 \\
& + \frac{945ib^2 \operatorname{PolyLog}\left(8, -e^{2i(c+d\sqrt[3]{x})}\right)}{d^9} \\
& + \frac{1890b^2\sqrt[3]{x} \operatorname{PolyLog}\left(7, -e^{2i(c+d\sqrt[3]{x})}\right)}{d^8} \\
& - \frac{1890ib^2x^{2/3} \operatorname{PolyLog}\left(6, -e^{2i(c+d\sqrt[3]{x})}\right)}{d^7} \\
& - \frac{1260b^2x \operatorname{PolyLog}\left(5, -e^{2i(c+d\sqrt[3]{x})}\right)}{d^6} \\
& + \frac{630ib^2x^{4/3} \operatorname{PolyLog}\left(4, -e^{2i(c+d\sqrt[3]{x})}\right)}{d^5} \\
& + \frac{252b^2x^{5/3} \operatorname{PolyLog}\left(3, -e^{2i(c+d\sqrt[3]{x})}\right)}{d^4} \\
& - \frac{84ib^2x^2 \operatorname{PolyLog}\left(2, -e^{2i(c+d\sqrt[3]{x})}\right)}{d^3} \\
& + \frac{24b^2x^{7/3} \log\left(1 + e^{2i(c+d\sqrt[3]{x})}\right)}{d^2} \\
& + \frac{3b^2x^{8/3} \tan(c + d\sqrt[3]{x})}{d} - \frac{3ib^2x^{8/3}}{d} - \frac{b^2x^3}{3}
\end{aligned}$$

[In] Int[x^2*(a + b*Tan[c + d*x^(1/3)])^2,x]

[Out]
$$\begin{aligned} &((-3I)*b^2*x^{(8/3)})/d + (a^2*x^3)/3 + ((2I)/3)*a*b*x^3 - (b^2*x^3)/3 + (2 \\ &4*b^2*x^{(7/3)}*Log[1 + E^{((2I)*(c + d*x^{(1/3)})}))/d^2 - (6*a*b*x^{(8/3)}*Log[\\ &1 + E^{((2I)*(c + d*x^{(1/3)})}))/d - ((84I)*b^2*x^2*PolyLog[2, -E^{((2I)*(c + d*x^{(1/3)})}))/d^3 + ((24I)*a*b*x^{(7/3)}*PolyLog[2, -E^{((2I)*(c + d*x^{(1/3)})}))/d^2 + (252*b^2*x^{(5/3)}*PolyLog[3, -E^{((2I)*(c + d*x^{(1/3)})}))/d^4 - (84*a*b*x^2*PolyLog[3, -E^{((2I)*(c + d*x^{(1/3)})}))/d^3 + ((630I)*b^2*x^{(4/3)}*PolyLog[4, -E^{((2I)*(c + d*x^{(1/3)})}))/d^5 - ((252I)*a*b*x^{(5/3)}*PolyLog[4, -E^{((2I)*(c + d*x^{(1/3)})}))/d^4 - (1260*b^2*x*PolyLog[5, -E^{((2I)*(c + d*x^{(1/3)})}))/d^6 + (630*a*b*x^{(4/3)}*PolyLog[5, -E^{((2I)*(c + d*x^{(1/3)})}))/d^5 - ((1890I)*b^2*x^{(2/3)}*PolyLog[6, -E^{((2I)*(c + d*x^{(1/3)})}))/d^7 + ((1260I)*a*b*x*PolyLog[6, -E^{((2I)*(c + d*x^{(1/3)})}))/d^6 + (1890*b^2*x^{(1/3)}*PolyLog[7, -E^{((2I)*(c + d*x^{(1/3)})}))/d^8 - (1890*a*b*x^{(2/3)}*PolyLog[7, -E^{((2I)*(c + d*x^{(1/3)})}))/d^7 + ((945I)*b^2*PolyLog[8, -E^{((2I)*(c + d*x^{(1/3)})}))/d^9 - ((1890I)*a*b*x^{(1/3)}*PolyLog[8, -E^{((2I)*(c + d*x^{(1/3)})}))/d^8 + (945*a*b*PolyLog[9, -E^{((2I)*(c + d*x^{(1/3)})}))/d^9 + (3*b^2*x^{(8/3)}*Tan[c + d*x^{(1/3)}])/d \end{aligned}$$

Rule 30

Int[(x_)^(m_), x_Symbol] := Simp[x^(m + 1)/(m + 1), x] /; FreeQ[m, x] && NeQ[m, -1]

Rule 2221

Int[(((F_)^((g_)*((e_) + (f_)*(x_)))^(n_))*((c_) + (d_)*(x_))^(m_))/((a_) + (b_)*((F_)^((g_)*((e_) + (f_)*(x_)))^(n_))), x_Symbol] := Simp[(((c + d*x)^m/(b*f*g*n*Log[F]))*Log[1 + b*((F^(g*(e + f*x)))^n/a)], x] - Dist[d*(m/(b*f*g*n*Log[F])), Int[(c + d*x)^(m - 1)*Log[1 + b*((F^(g*(e + f*x)))^n/a)], x], x] /; FreeQ[{F, a, b, c, d, e, f, g, n}, x] && IGtQ[m, 0]

Rule 2320

Int[u_, x_Symbol] := With[{v = FunctionOfExponential[u, x]}, Dist[v/D[v, x], Subst[Int[FunctionOfExponentialFunction[u, x]/x, x], x, v], x] /; FunctionOfExponentialQ[u, x] && !MatchQ[u, (w_)*((a_)*(v_)^(n_))^(m_)] /; FreeQ[{a, m, n}, x] && IntegerQ[m*n] && !MatchQ[u, E^{((c_)*((a_) + (b_)*x))* (F_)[v_]} /; FreeQ[{a, b, c}, x] && InverseFunctionQ[F[x]]]

Rule 2611

Int[Log[1 + (e_)*((F_)^((c_)*((a_) + (b_)*(x_)))^(n_))*((f_) + (g_)*(x_))^(m_)], x_Symbol] := Simp[(-f + g*x)^m*(PolyLog[2, (-e)*(F^(c*(a + b*x)))^n]/(b*c*n*Log[F])), x] + Dist[g*(m/(b*c*n*Log[F])), Int[(f + g*x)^(m - 1)*PolyLog[2, (-e)*(F^(c*(a + b*x)))^n], x], x] /; FreeQ[{F, a, b, c, e, f, g, n}, x] && GtQ[m, 0]

Rule 3800

```
Int[((c_.) + (d_.)*(x_))^(m_.)*tan[(e_.) + (f_.)*(x_)], x_Symbol] := Simp[
I*((c + d*x)^(m + 1)/(d*(m + 1))), x] - Dist[2*I, Int[(c + d*x)^m*(E^(2*I*(e
+ f*x)))/(1 + E^(2*I*(e + f*x)))], x], x] /; FreeQ[{c, d, e, f}, x] && IGtQ
[m, 0]
```

Rule 3801

```
Int[((c_.) + (d_.)*(x_))^(m_.)*((b_.)*tan[(e_.) + (f_.)*(x_)])^(n_), x_Symb
ol] := Simp[b*(c + d*x)^m*((b*Tan[e + f*x])^(n - 1)/(f*(n - 1))), x] + (-Di
st[b*d*(m/(f*(n - 1))), Int[(c + d*x)^(m - 1)*(b*Tan[e + f*x])^(n - 1), x],
x] - Dist[b^2, Int[(c + d*x)^m*(b*Tan[e + f*x])^(n - 2), x], x]) /; FreeQ[
{b, c, d, e, f}, x] && GtQ[n, 1] && GtQ[m, 0]
```

Rule 3803

```
Int[((c_.) + (d_.)*(x_))^(m_.)*((a_.) + (b_.)*tan[(e_.) + (f_.)*(x_)])^(n_.)
, x_Symbol] := Int[ExpandIntegrand[(c + d*x)^m, (a + b*Tan[e + f*x])^n, x],
x] /; FreeQ[{a, b, c, d, e, f, m}, x] && IGtQ[m, 0] && IGtQ[n, 0]
```

Rule 3832

```
Int[(x_)^(m_.)*((a_.) + (b_.)*Tan[(c_.) + (d_.)*(x_)^(n_)])^(p_.), x_Symbol
] := Dist[1/n, Subst[Int[x^(Simplify[(m + 1)/n] - 1)*(a + b*Tan[c + d*x])^p
, x], x, x^n], x] /; FreeQ[{a, b, c, d, m, n, p}, x] && IGtQ[Simplify[(m +
1)/n], 0] && IntegerQ[p]
```

Rule 6724

```
Int[PolyLog[n_, (c_.)*((a_.) + (b_.)*(x_))^(p_.)]/((d_.) + (e_.)*(x_)), x_S
ymbol] := Simp[PolyLog[n + 1, c*(a + b*x)^p]/(e*p), x] /; FreeQ[{a, b, c, d
, e, n, p}, x] && EqQ[b*d, a*e]
```

Rule 6744

```
Int[((e_.) + (f_.)*(x_))^(m_.)*PolyLog[n_, (d_.)*((F_)^((c_.)*((a_.) + (b_.
)*(x_))))^(p_.)], x_Symbol] := Simp[(e + f*x)^m*(PolyLog[n + 1, d*(F^(c*(a
+ b*x)))^p]/(b*c*p*Log[F])), x] - Dist[f*(m/(b*c*p*Log[F])), Int[(e + f*x)^(
m - 1)*PolyLog[n + 1, d*(F^(c*(a + b*x)))^p], x], x] /; FreeQ[{F, a, b, c,
d, e, f, n, p}, x] && GtQ[m, 0]
```

Rubi steps

$$\text{integral} = 3\text{Subst}\left(\int x^8(a + b \tan(c + dx))^2 dx, x, \sqrt[3]{x}\right)$$

$$\begin{aligned}
&= 3\text{Subst}\left(\int (a^2x^8 + 2abx^8 \tan(c + dx) + b^2x^8 \tan^2(c + dx)) dx, x, \sqrt[3]{x}\right) \\
&= \frac{a^2x^3}{3} + (6ab)\text{Subst}\left(\int x^8 \tan(c + dx) dx, x, \sqrt[3]{x}\right) \\
&\quad + (3b^2)\text{Subst}\left(\int x^8 \tan^2(c + dx) dx, x, \sqrt[3]{x}\right) \\
&= \frac{a^2x^3}{3} + \frac{2}{3}iabx^3 + \frac{3b^2x^{8/3} \tan(c + d\sqrt[3]{x})}{d} - (12iab)\text{Subst}\left(\int \frac{e^{2i(c+dx)}x^8}{1 + e^{2i(c+dx)}} dx, x, \sqrt[3]{x}\right) \\
&\quad - (3b^2)\text{Subst}\left(\int x^8 dx, x, \sqrt[3]{x}\right) - \frac{(24b^2)\text{Subst}\left(\int x^7 \tan(c + dx) dx, x, \sqrt[3]{x}\right)}{d} \\
&= -\frac{3ib^2x^{8/3}}{d} + \frac{a^2x^3}{3} + \frac{2}{3}iabx^3 - \frac{b^2x^3}{3} - \frac{6abx^{8/3} \log\left(1 + e^{2i(c+d\sqrt[3]{x})}\right)}{d} + \frac{3b^2x^{8/3} \tan(c + d\sqrt[3]{x})}{d} \\
&\quad + \frac{(48ab)\text{Subst}\left(\int x^7 \log(1 + e^{2i(c+dx)}) dx, x, \sqrt[3]{x}\right)}{d} + \frac{(48ib^2)\text{Subst}\left(\int \frac{e^{2i(c+dx)}x^7}{1 + e^{2i(c+dx)}} dx, x, \sqrt[3]{x}\right)}{d} \\
&= -\frac{3ib^2x^{8/3}}{d} + \frac{a^2x^3}{3} + \frac{2}{3}iabx^3 - \frac{b^2x^3}{3} + \frac{24b^2x^{7/3} \log\left(1 + e^{2i(c+d\sqrt[3]{x})}\right)}{d^2} \\
&\quad - \frac{6abx^{8/3} \log\left(1 + e^{2i(c+d\sqrt[3]{x})}\right)}{d} + \frac{24iabx^{7/3} \text{PolyLog}\left(2, -e^{2i(c+d\sqrt[3]{x})}\right)}{d^2} \\
&\quad + \frac{3b^2x^{8/3} \tan(c + d\sqrt[3]{x})}{d} - \frac{(168iab)\text{Subst}\left(\int x^6 \text{PolyLog}\left(2, -e^{2i(c+dx)}\right) dx, x, \sqrt[3]{x}\right)}{d^2} \\
&\quad - \frac{(168b^2)\text{Subst}\left(\int x^6 \log(1 + e^{2i(c+dx)}) dx, x, \sqrt[3]{x}\right)}{d^2} \\
&= -\frac{3ib^2x^{8/3}}{d} + \frac{a^2x^3}{3} + \frac{2}{3}iabx^3 - \frac{b^2x^3}{3} + \frac{24b^2x^{7/3} \log\left(1 + e^{2i(c+d\sqrt[3]{x})}\right)}{d^2} \\
&\quad - \frac{6abx^{8/3} \log\left(1 + e^{2i(c+d\sqrt[3]{x})}\right)}{d} - \frac{84ib^2x^2 \text{PolyLog}\left(2, -e^{2i(c+d\sqrt[3]{x})}\right)}{d^3} \\
&\quad + \frac{24iabx^{7/3} \text{PolyLog}\left(2, -e^{2i(c+d\sqrt[3]{x})}\right)}{d^2} - \frac{84abx^2 \text{PolyLog}\left(3, -e^{2i(c+d\sqrt[3]{x})}\right)}{d^3} \\
&\quad + \frac{3b^2x^{8/3} \tan(c + d\sqrt[3]{x})}{d} + \frac{(504ab)\text{Subst}\left(\int x^5 \text{PolyLog}\left(3, -e^{2i(c+dx)}\right) dx, x, \sqrt[3]{x}\right)}{d^3} \\
&\quad + \frac{(504ib^2)\text{Subst}\left(\int x^5 \text{PolyLog}\left(2, -e^{2i(c+dx)}\right) dx, x, \sqrt[3]{x}\right)}{d^3}
\end{aligned}$$

$$\begin{aligned}
&= -\frac{3ib^2x^{8/3}}{d} + \frac{a^2x^3}{3} + \frac{2}{3}iabx^3 - \frac{b^2x^3}{3} + \frac{24b^2x^{7/3} \log\left(1 + e^{2i(c+d\sqrt[3]{x}})\right)}{d^2} \\
&\quad - \frac{6abx^{8/3} \log\left(1 + e^{2i(c+d\sqrt[3]{x}})\right)}{d} - \frac{84ib^2x^2 \operatorname{PolyLog}\left(2, -e^{2i(c+d\sqrt[3]{x}})\right)}{d^3} \\
&\quad + \frac{24iabx^{7/3} \operatorname{PolyLog}\left(2, -e^{2i(c+d\sqrt[3]{x}})\right)}{d^2} + \frac{252b^2x^{5/3} \operatorname{PolyLog}\left(3, -e^{2i(c+d\sqrt[3]{x}})\right)}{d^4} \\
&\quad - \frac{84abx^2 \operatorname{PolyLog}\left(3, -e^{2i(c+d\sqrt[3]{x}})\right)}{d^3} - \frac{252iabx^{5/3} \operatorname{PolyLog}\left(4, -e^{2i(c+d\sqrt[3]{x}})\right)}{d^4} \\
&\quad + \frac{3b^2x^{8/3} \tan\left(c + d\sqrt[3]{x}\right)}{d} + \frac{(1260iab) \operatorname{Subst}\left(\int x^4 \operatorname{PolyLog}\left(4, -e^{2i(c+dx)}\right) dx, x, \sqrt[3]{x}\right)}{d^4} \\
&\quad - \frac{(1260b^2) \operatorname{Subst}\left(\int x^4 \operatorname{PolyLog}\left(3, -e^{2i(c+dx)}\right) dx, x, \sqrt[3]{x}\right)}{d^4} \\
&= -\frac{3ib^2x^{8/3}}{d} + \frac{a^2x^3}{3} + \frac{2}{3}iabx^3 - \frac{b^2x^3}{3} + \frac{24b^2x^{7/3} \log\left(1 + e^{2i(c+d\sqrt[3]{x}})\right)}{d^2} \\
&\quad - \frac{6abx^{8/3} \log\left(1 + e^{2i(c+d\sqrt[3]{x}})\right)}{d} - \frac{84ib^2x^2 \operatorname{PolyLog}\left(2, -e^{2i(c+d\sqrt[3]{x}})\right)}{d^3} \\
&\quad + \frac{24iabx^{7/3} \operatorname{PolyLog}\left(2, -e^{2i(c+d\sqrt[3]{x}})\right)}{d^2} + \frac{252b^2x^{5/3} \operatorname{PolyLog}\left(3, -e^{2i(c+d\sqrt[3]{x}})\right)}{d^4} \\
&\quad - \frac{84abx^2 \operatorname{PolyLog}\left(3, -e^{2i(c+d\sqrt[3]{x}})\right)}{d^3} + \frac{630ib^2x^{4/3} \operatorname{PolyLog}\left(4, -e^{2i(c+d\sqrt[3]{x}})\right)}{d^5} \\
&\quad - \frac{252iabx^{5/3} \operatorname{PolyLog}\left(4, -e^{2i(c+d\sqrt[3]{x}})\right)}{d^4} + \frac{630abx^{4/3} \operatorname{PolyLog}\left(5, -e^{2i(c+d\sqrt[3]{x}})\right)}{d^5} \\
&\quad + \frac{3b^2x^{8/3} \tan\left(c + d\sqrt[3]{x}\right)}{d} - \frac{(2520ab) \operatorname{Subst}\left(\int x^3 \operatorname{PolyLog}\left(5, -e^{2i(c+dx)}\right) dx, x, \sqrt[3]{x}\right)}{d^5} \\
&\quad - \frac{(2520ib^2) \operatorname{Subst}\left(\int x^3 \operatorname{PolyLog}\left(4, -e^{2i(c+dx)}\right) dx, x, \sqrt[3]{x}\right)}{d^5}
\end{aligned}$$

$$\begin{aligned}
&= -\frac{3ib^2x^{8/3}}{d} + \frac{a^2x^3}{3} + \frac{2}{3}iabx^3 - \frac{b^2x^3}{3} + \frac{24b^2x^{7/3} \log\left(1 + e^{2i(c+d\sqrt[3]{x}})\right)}{d^2} \\
&\quad - \frac{6abx^{8/3} \log\left(1 + e^{2i(c+d\sqrt[3]{x}})\right)}{d} - \frac{84ib^2x^2 \operatorname{PolyLog}\left(2, -e^{2i(c+d\sqrt[3]{x}})\right)}{d^3} \\
&\quad + \frac{24iabx^{7/3} \operatorname{PolyLog}\left(2, -e^{2i(c+d\sqrt[3]{x}})\right)}{d^2} + \frac{252b^2x^{5/3} \operatorname{PolyLog}\left(3, -e^{2i(c+d\sqrt[3]{x}})\right)}{d^4} \\
&\quad - \frac{84abx^2 \operatorname{PolyLog}\left(3, -e^{2i(c+d\sqrt[3]{x}})\right)}{d^3} + \frac{630ib^2x^{4/3} \operatorname{PolyLog}\left(4, -e^{2i(c+d\sqrt[3]{x}})\right)}{d^5} \\
&\quad - \frac{252iabx^{5/3} \operatorname{PolyLog}\left(4, -e^{2i(c+d\sqrt[3]{x}})\right)}{d^4} - \frac{1260b^2x \operatorname{PolyLog}\left(5, -e^{2i(c+d\sqrt[3]{x}})\right)}{d^6} \\
&\quad + \frac{630abx^{4/3} \operatorname{PolyLog}\left(5, -e^{2i(c+d\sqrt[3]{x}})\right)}{d^5} + \frac{1260iabx \operatorname{PolyLog}\left(6, -e^{2i(c+d\sqrt[3]{x}})\right)}{d^6} \\
&\quad + \frac{3b^2x^{8/3} \tan\left(c + d\sqrt[3]{x}\right)}{d} - \frac{(3780iab) \operatorname{Subst}\left(\int x^2 \operatorname{PolyLog}\left(6, -e^{2i(c+dx)}\right) dx, x, \sqrt[3]{x}\right)}{d^6} \\
&\quad + \frac{(3780b^2) \operatorname{Subst}\left(\int x^2 \operatorname{PolyLog}\left(5, -e^{2i(c+dx)}\right) dx, x, \sqrt[3]{x}\right)}{d^6} \\
&= -\frac{3ib^2x^{8/3}}{d} + \frac{a^2x^3}{3} + \frac{2}{3}iabx^3 - \frac{b^2x^3}{3} + \frac{24b^2x^{7/3} \log\left(1 + e^{2i(c+d\sqrt[3]{x}})\right)}{d^2} \\
&\quad - \frac{6abx^{8/3} \log\left(1 + e^{2i(c+d\sqrt[3]{x}})\right)}{d} - \frac{84ib^2x^2 \operatorname{PolyLog}\left(2, -e^{2i(c+d\sqrt[3]{x}})\right)}{d^3} \\
&\quad + \frac{24iabx^{7/3} \operatorname{PolyLog}\left(2, -e^{2i(c+d\sqrt[3]{x}})\right)}{d^2} + \frac{252b^2x^{5/3} \operatorname{PolyLog}\left(3, -e^{2i(c+d\sqrt[3]{x}})\right)}{d^4} \\
&\quad - \frac{84abx^2 \operatorname{PolyLog}\left(3, -e^{2i(c+d\sqrt[3]{x}})\right)}{d^3} + \frac{630ib^2x^{4/3} \operatorname{PolyLog}\left(4, -e^{2i(c+d\sqrt[3]{x}})\right)}{d^5} \\
&\quad - \frac{252iabx^{5/3} \operatorname{PolyLog}\left(4, -e^{2i(c+d\sqrt[3]{x}})\right)}{d^4} - \frac{1260b^2x \operatorname{PolyLog}\left(5, -e^{2i(c+d\sqrt[3]{x}})\right)}{d^6} \\
&\quad + \frac{630abx^{4/3} \operatorname{PolyLog}\left(5, -e^{2i(c+d\sqrt[3]{x}})\right)}{d^5} - \frac{1890ib^2x^{2/3} \operatorname{PolyLog}\left(6, -e^{2i(c+d\sqrt[3]{x}})\right)}{d^7} \\
&\quad + \frac{1260iabx \operatorname{PolyLog}\left(6, -e^{2i(c+d\sqrt[3]{x}})\right)}{d^6} - \frac{1890abx^{2/3} \operatorname{PolyLog}\left(7, -e^{2i(c+d\sqrt[3]{x}})\right)}{d^7} \\
&\quad + \frac{3b^2x^{8/3} \tan\left(c + d\sqrt[3]{x}\right)}{d} + \frac{(3780ab) \operatorname{Subst}\left(\int x \operatorname{PolyLog}\left(7, -e^{2i(c+dx)}\right) dx, x, \sqrt[3]{x}\right)}{d^7} \\
&\quad + \frac{(3780ib^2) \operatorname{Subst}\left(\int x \operatorname{PolyLog}\left(6, -e^{2i(c+dx)}\right) dx, x, \sqrt[3]{x}\right)}{d^7}
\end{aligned}$$

$$\begin{aligned}
&= -\frac{3ib^2x^{8/3}}{d} + \frac{a^2x^3}{3} + \frac{2}{3}iabx^3 - \frac{b^2x^3}{3} + \frac{24b^2x^{7/3} \log\left(1 + e^{2i(c+d\sqrt[3]{x}})\right)}{d^2} \\
&\quad - \frac{6abx^{8/3} \log\left(1 + e^{2i(c+d\sqrt[3]{x}})\right)}{d} - \frac{84ib^2x^2 \operatorname{PolyLog}\left(2, -e^{2i(c+d\sqrt[3]{x}})\right)}{d^3} \\
&\quad + \frac{24iabx^{7/3} \operatorname{PolyLog}\left(2, -e^{2i(c+d\sqrt[3]{x}})\right)}{d^2} + \frac{252b^2x^{5/3} \operatorname{PolyLog}\left(3, -e^{2i(c+d\sqrt[3]{x}})\right)}{d^4} \\
&\quad - \frac{84abx^2 \operatorname{PolyLog}\left(3, -e^{2i(c+d\sqrt[3]{x}})\right)}{d^3} + \frac{630ib^2x^{4/3} \operatorname{PolyLog}\left(4, -e^{2i(c+d\sqrt[3]{x}})\right)}{d^5} \\
&\quad - \frac{252iabx^{5/3} \operatorname{PolyLog}\left(4, -e^{2i(c+d\sqrt[3]{x}})\right)}{d^4} - \frac{1260b^2x \operatorname{PolyLog}\left(5, -e^{2i(c+d\sqrt[3]{x}})\right)}{d^6} \\
&\quad + \frac{630abx^{4/3} \operatorname{PolyLog}\left(5, -e^{2i(c+d\sqrt[3]{x}})\right)}{d^5} - \frac{1890ib^2x^{2/3} \operatorname{PolyLog}\left(6, -e^{2i(c+d\sqrt[3]{x}})\right)}{d^7} \\
&\quad + \frac{1260iabx \operatorname{PolyLog}\left(6, -e^{2i(c+d\sqrt[3]{x}})\right)}{d^6} + \frac{1890b^2\sqrt[3]{x} \operatorname{PolyLog}\left(7, -e^{2i(c+d\sqrt[3]{x}})\right)}{d^8} \\
&\quad - \frac{1890abx^{2/3} \operatorname{PolyLog}\left(7, -e^{2i(c+d\sqrt[3]{x}})\right)}{d^7} - \frac{1890iab\sqrt[3]{x} \operatorname{PolyLog}\left(8, -e^{2i(c+d\sqrt[3]{x}})\right)}{d^8} \\
&\quad + \frac{3b^2x^{8/3} \tan\left(c + d\sqrt[3]{x}\right)}{d} + \frac{(1890iab) \operatorname{Subst}\left(\int \operatorname{PolyLog}\left(8, -e^{2i(c+dx)}\right) dx, x, \sqrt[3]{x}\right)}{d^8} \\
&\quad - \frac{(1890b^2) \operatorname{Subst}\left(\int \operatorname{PolyLog}\left(7, -e^{2i(c+dx)}\right) dx, x, \sqrt[3]{x}\right)}{d^8}
\end{aligned}$$

$$\begin{aligned}
&= -\frac{3ib^2x^{8/3}}{d} + \frac{a^2x^3}{3} + \frac{2}{3}iabx^3 - \frac{b^2x^3}{3} + \frac{24b^2x^{7/3} \log\left(1 + e^{2i(c+d\sqrt[3]{x}})\right)}{d^2} \\
&\quad - \frac{6abx^{8/3} \log\left(1 + e^{2i(c+d\sqrt[3]{x}})\right)}{d} - \frac{84ib^2x^2 \operatorname{PolyLog}\left(2, -e^{2i(c+d\sqrt[3]{x}})\right)}{d^3} \\
&\quad + \frac{24iabx^{7/3} \operatorname{PolyLog}\left(2, -e^{2i(c+d\sqrt[3]{x}})\right)}{d^2} + \frac{252b^2x^{5/3} \operatorname{PolyLog}\left(3, -e^{2i(c+d\sqrt[3]{x}})\right)}{d^4} \\
&\quad - \frac{84abx^2 \operatorname{PolyLog}\left(3, -e^{2i(c+d\sqrt[3]{x}})\right)}{d^3} + \frac{630ib^2x^{4/3} \operatorname{PolyLog}\left(4, -e^{2i(c+d\sqrt[3]{x}})\right)}{d^5} \\
&\quad - \frac{252iabx^{5/3} \operatorname{PolyLog}\left(4, -e^{2i(c+d\sqrt[3]{x}})\right)}{d^4} - \frac{1260b^2x \operatorname{PolyLog}\left(5, -e^{2i(c+d\sqrt[3]{x}})\right)}{d^6} \\
&\quad + \frac{630abx^{4/3} \operatorname{PolyLog}\left(5, -e^{2i(c+d\sqrt[3]{x}})\right)}{d^5} - \frac{1890ib^2x^{2/3} \operatorname{PolyLog}\left(6, -e^{2i(c+d\sqrt[3]{x}})\right)}{d^7} \\
&\quad + \frac{1260iabx \operatorname{PolyLog}\left(6, -e^{2i(c+d\sqrt[3]{x}})\right)}{d^6} + \frac{1890b^2\sqrt[3]{x} \operatorname{PolyLog}\left(7, -e^{2i(c+d\sqrt[3]{x}})\right)}{d^8} \\
&\quad - \frac{1890abx^{2/3} \operatorname{PolyLog}\left(7, -e^{2i(c+d\sqrt[3]{x}})\right)}{d^7} - \frac{1890iab\sqrt[3]{x} \operatorname{PolyLog}\left(8, -e^{2i(c+d\sqrt[3]{x}})\right)}{d^8} \\
&\quad + \frac{3b^2x^{8/3} \tan\left(c + d\sqrt[3]{x}\right)}{d} + \frac{(945ab) \operatorname{Subst}\left(\int \frac{\operatorname{PolyLog}(8, -x)}{x} dx, x, e^{2i(c+d\sqrt[3]{x}})\right)}{d^9} \\
&\quad + \frac{(945ib^2) \operatorname{Subst}\left(\int \frac{\operatorname{PolyLog}(7, -x)}{x} dx, x, e^{2i(c+d\sqrt[3]{x}})\right)}{d^9}
\end{aligned}$$

$$\begin{aligned}
&= -\frac{3ib^2x^{8/3}}{d} + \frac{a^2x^3}{3} + \frac{2}{3}iabx^3 - \frac{b^2x^3}{3} + \frac{24b^2x^{7/3} \log\left(1 + e^{2i(c+d\sqrt[3]{x}})\right)}{d^2} \\
&\quad - \frac{6abx^{8/3} \log\left(1 + e^{2i(c+d\sqrt[3]{x}})\right)}{d} - \frac{84ib^2x^2 \operatorname{PolyLog}\left(2, -e^{2i(c+d\sqrt[3]{x}})\right)}{d^3} \\
&\quad + \frac{24iabx^{7/3} \operatorname{PolyLog}\left(2, -e^{2i(c+d\sqrt[3]{x}})\right)}{d^2} + \frac{252b^2x^{5/3} \operatorname{PolyLog}\left(3, -e^{2i(c+d\sqrt[3]{x}})\right)}{d^4} \\
&\quad - \frac{84abx^2 \operatorname{PolyLog}\left(3, -e^{2i(c+d\sqrt[3]{x}})\right)}{d^3} + \frac{630ib^2x^{4/3} \operatorname{PolyLog}\left(4, -e^{2i(c+d\sqrt[3]{x}})\right)}{d^5} \\
&\quad - \frac{252iabx^{5/3} \operatorname{PolyLog}\left(4, -e^{2i(c+d\sqrt[3]{x}})\right)}{d^4} - \frac{1260b^2x \operatorname{PolyLog}\left(5, -e^{2i(c+d\sqrt[3]{x}})\right)}{d^6} \\
&\quad + \frac{630abx^{4/3} \operatorname{PolyLog}\left(5, -e^{2i(c+d\sqrt[3]{x}})\right)}{d^5} - \frac{1890ib^2x^{2/3} \operatorname{PolyLog}\left(6, -e^{2i(c+d\sqrt[3]{x}})\right)}{d^7} \\
&\quad + \frac{1260iabx \operatorname{PolyLog}\left(6, -e^{2i(c+d\sqrt[3]{x}})\right)}{d^6} + \frac{1890b^2\sqrt[3]{x} \operatorname{PolyLog}\left(7, -e^{2i(c+d\sqrt[3]{x}})\right)}{d^8} \\
&\quad - \frac{1890abx^{2/3} \operatorname{PolyLog}\left(7, -e^{2i(c+d\sqrt[3]{x}})\right)}{d^7} + \frac{945ib^2 \operatorname{PolyLog}\left(8, -e^{2i(c+d\sqrt[3]{x}})\right)}{d^9} \\
&\quad - \frac{1890iab\sqrt[3]{x} \operatorname{PolyLog}\left(8, -e^{2i(c+d\sqrt[3]{x}})\right)}{d^8} \\
&\quad + \frac{945ab \operatorname{PolyLog}\left(9, -e^{2i(c+d\sqrt[3]{x}})\right)}{d^9} + \frac{3b^2x^{8/3} \tan\left(c + d\sqrt[3]{x}\right)}{d}
\end{aligned}$$

Mathematica [A] (verified)

Time = 4.70 (sec) , antiderivative size = 828, normalized size of antiderivative = 1.39

$$\begin{aligned}
&\int x^2(a + b \tan(c + d\sqrt[3]{x}))^2 dx \\
&= \frac{1}{3} \left(-\frac{ibe^{2ic} \left(-18bd^8 e^{-2ic} x^{8/3} + 4ad^9 e^{-2ic} x^3 + 72ibd^7 e^{-2ic} (1 + e^{2ic}) x^{7/3} \log\left(1 + e^{-2i(c+d\sqrt[3]{x}})\right) - 18iad^8 e^{-2ic} \right)}{d^9} \right. \\
&\quad \left. + \frac{9b^2x^{8/3} \sec(c) \sec(c + d\sqrt[3]{x}) \sin(d\sqrt[3]{x})}{d} + x^3(a^2 - b^2 + 2ab \tan(c)) \right)
\end{aligned}$$

[In] Integrate[x^2*(a + b*Tan[c + d*x^(1/3)])^2,x]

[Out] (((-I)*b*E^((2*I)*c))*((-18*b*d^8*x^(8/3))/E^((2*I)*c) + (4*a*d^9*x^3)/E^((2*I)*c) + ((72*I)*b*d^7*(1 + E^((2*I)*c))*x^(7/3)*Log[1 + E^((-2*I)*(c + d*x^(1/3)))]))/E^((2*I)*c) - ((18*I)*a*d^8*(1 + E^((2*I)*c))*x^(8/3)*Log[1 + E^

$$\begin{aligned} &((-2*I)*(c + d*x^{(1/3)}))/E^{((2*I)*c)} - 252*b*d^6*(1 + E^{((-2*I)*c)})*x^2*P \\ &olyLog[2, -E^{((-2*I)*(c + d*x^{(1/3)}))}] + 72*a*d^7*(1 + E^{((-2*I)*c)})*x^{(7/3)} \\ &)*PolyLog[2, -E^{((-2*I)*(c + d*x^{(1/3)}))}] + ((756*I)*b*d^5*(1 + E^{((2*I)*c)} \\ &)*x^{(5/3)}*PolyLog[3, -E^{((-2*I)*(c + d*x^{(1/3)}))}]/E^{((2*I)*c)} - ((252*I)*a \\ &*d^6*(1 + E^{((2*I)*c)})*x^2*PolyLog[3, -E^{((-2*I)*(c + d*x^{(1/3)}))}]/E^{((2*I) \\ &)*c)} + 1890*b*d^4*(1 + E^{((-2*I)*c)})*x^{(4/3)}*PolyLog[4, -E^{((-2*I)*(c + d*x \\ &^{(1/3)}))}] - 756*a*d^5*(1 + E^{((-2*I)*c)})*x^{(5/3)}*PolyLog[4, -E^{((-2*I)*(c + \\ &d*x^{(1/3)}))}] - ((3780*I)*b*d^3*(1 + E^{((2*I)*c)})*x*PolyLog[5, -E^{((-2*I)* \\ &c + d*x^{(1/3)}))}]/E^{((2*I)*c)} + ((1890*I)*a*d^4*(1 + E^{((2*I)*c)})*x^{(4/3)}*P \\ &olyLog[5, -E^{((-2*I)*(c + d*x^{(1/3)}))}]/E^{((2*I)*c)} - 5670*b*d^2*(1 + E^{((- \\ &2*I)*c)})*x^{(2/3)}*PolyLog[6, -E^{((-2*I)*(c + d*x^{(1/3)}))}] + 3780*a*d^3*(1 + \\ &E^{((-2*I)*c)})*x*PolyLog[6, -E^{((-2*I)*(c + d*x^{(1/3)}))}] + ((5670*I)*b*d*(1 \\ &+ E^{((2*I)*c)})*x^{(1/3)}*PolyLog[7, -E^{((-2*I)*(c + d*x^{(1/3)}))}]/E^{((2*I)*c)} \\ &- ((5670*I)*a*d^2*(1 + E^{((2*I)*c)})*x^{(2/3)}*PolyLog[7, -E^{((-2*I)*(c + d*x \\ &^{(1/3)}))}]/E^{((2*I)*c)} + 2835*b*(1 + E^{((-2*I)*c)})*PolyLog[8, -E^{((-2*I)*(c \\ &+ d*x^{(1/3)}))}] - 5670*a*d*(1 + E^{((-2*I)*c)})*x^{(1/3)}*PolyLog[8, -E^{((-2*I) \\ &*(c + d*x^{(1/3)}))}] + ((2835*I)*a*(1 + E^{((2*I)*c)})*PolyLog[9, -E^{((-2*I)*(c \\ &+ d*x^{(1/3)}))}]/E^{((2*I)*c)}))/(d^9*(1 + E^{((2*I)*c)})) + (9*b^2*x^{(8/3)}*Sec \\ &[c]*Sec[c + d*x^{(1/3)}]*Sin[d*x^{(1/3)}])/d + x^3*(a^2 - b^2 + 2*a*b*Tan[c]))/ \\ &3 \end{aligned}$$

Maple [F]

$$\int x^2 \left(a + b \tan \left(c + d x^{\frac{1}{3}} \right) \right)^2 dx$$

[In] int(x^2*(a+b*tan(c+d*x^(1/3)))^2,x)

[Out] int(x^2*(a+b*tan(c+d*x^(1/3)))^2,x)

Fricas [F]

$$\int x^2 (a + b \tan(c + d\sqrt[3]{x}))^2 dx = \int \left(b \tan \left(dx^{\frac{1}{3}} + c \right) + a \right)^2 x^2 dx$$

[In] integrate(x^2*(a+b*tan(c+d*x^(1/3)))^2,x, algorithm="fricas")

[Out] integral(b^2*x^2*tan(d*x^(1/3) + c)^2 + 2*a*b*x^2*tan(d*x^(1/3) + c) + a^2*x^2, x)

$$\begin{aligned}
& + c)^2 + 105*(2*I*a*b*c^7 + 7*I*b^2*c^6)*(d*x^(1/3) + c))*\sin(2*d*x^(1/3) \\
& + 2*c))*\arctan2(\sin(2*d*x^(1/3) + 2*c), \cos(2*d*x^(1/3) + 2*c) + 1) - 35*((\\
& 2*a*b + I*b^2)*(d*x^(1/3) + c)^9 - 9*(2*b^2 + (2*a*b + I*b^2)*c)*(d*x^(1/3) \\
& + c)^8 + 36*(4*b^2*c + (2*a*b + I*b^2)*c^2)*(d*x^(1/3) + c)^7 - 84*(6*b^2* \\
& c^2 + (2*a*b + I*b^2)*c^3)*(d*x^(1/3) + c)^6 + 126*(8*b^2*c^3 + (2*a*b + I* \\
& b^2)*c^4)*(d*x^(1/3) + c)^5 - 126*(10*b^2*c^4 + (2*a*b + I*b^2)*c^5)*(d*x^(\\
& 1/3) + c)^4 + 84*(12*b^2*c^5 + (2*a*b + I*b^2)*c^6)*(d*x^(1/3) + c)^3 - 36* \\
& (14*b^2*c^6 + (2*a*b + I*b^2)*c^7)*(d*x^(1/3) + c)^2 + 9*(I*b^2*c^8 + 16*b^ \\
& 2*c^7)*(d*x^(1/3) + c))*\cos(2*d*x^(1/3) + 2*c) - 1260*(32*(d*x^(1/3) + c)^7 \\
& *a*b - 2*a*b*c^7 - 7*b^2*c^6 - 64*(2*a*b*c + b^2)*(d*x^(1/3) + c)^6 + 224*(\\
& a*b*c^2 + b^2*c)*(d*x^(1/3) + c)^5 - 112*(2*a*b*c^3 + 3*b^2*c^2)*(d*x^(1/3) \\
& + c)^4 + 140*(a*b*c^4 + 2*b^2*c^3)*(d*x^(1/3) + c)^3 - 28*(2*a*b*c^5 + 5*b \\
& ^2*c^4)*(d*x^(1/3) + c)^2 + 14*(a*b*c^6 + 3*b^2*c^5)*(d*x^(1/3) + c) + (32* \\
& (d*x^(1/3) + c)^7*a*b - 2*a*b*c^7 - 7*b^2*c^6 - 64*(2*a*b*c + b^2)*(d*x^(1/ \\
& 3) + c)^6 + 224*(a*b*c^2 + b^2*c)*(d*x^(1/3) + c)^5 - 112*(2*a*b*c^3 + 3*b^ \\
& 2*c^2)*(d*x^(1/3) + c)^4 + 140*(a*b*c^4 + 2*b^2*c^3)*(d*x^(1/3) + c)^3 - 28 \\
& *(2*a*b*c^5 + 5*b^2*c^4)*(d*x^(1/3) + c)^2 + 14*(a*b*c^6 + 3*b^2*c^5)*(d*x^ \\
& (1/3) + c))*\cos(2*d*x^(1/3) + 2*c) + (32*I*(d*x^(1/3) + c)^7*a*b - 2*I*a*b* \\
& c^7 - 7*I*b^2*c^6 + 64*(-2*I*a*b*c - I*b^2)*(d*x^(1/3) + c)^6 + 224*(I*a*b* \\
& c^2 + I*b^2*c)*(d*x^(1/3) + c)^5 + 112*(-2*I*a*b*c^3 - 3*I*b^2*c^2)*(d*x^(1 \\
& /3) + c)^4 + 140*(I*a*b*c^4 + 2*I*b^2*c^3)*(d*x^(1/3) + c)^3 + 28*(-2*I*a*b \\
& *c^5 - 5*I*b^2*c^4)*(d*x^(1/3) + c)^2 + 14*(I*a*b*c^6 + 3*I*b^2*c^5)*(d*x^(\\
& 1/3) + c))*\sin(2*d*x^(1/3) + 2*c))*\operatorname{dilog}(-e^(2*I*d*x^(1/3) + 2*I*c)) - 12*(\\
& 420*I*(d*x^(1/3) + c)^8*a*b + 105*I*b^2*c^7 + 960*(-2*I*a*b*c - I*b^2)*(d*x \\
& ^{(1/3) + c)^7 + 3920*(I*a*b*c^2 + I*b^2*c)*(d*x^(1/3) + c)^6 + 2352*(-2*I*a \\
& *b*c^3 - 3*I*b^2*c^2)*(d*x^(1/3) + c)^5 + 3675*(I*a*b*c^4 + 2*I*b^2*c^3)*(d \\
& *x^(1/3) + c)^4 + 980*(-2*I*a*b*c^5 - 5*I*b^2*c^4)*(d*x^(1/3) + c)^3 + 735* \\
& (I*a*b*c^6 + 3*I*b^2*c^5)*(d*x^(1/3) + c)^2 + 105*(-2*I*a*b*c^7 - 7*I*b^2*c \\
& ^6)*(d*x^(1/3) + c) + (420*I*(d*x^(1/3) + c)^8*a*b + 105*I*b^2*c^7 + 960*(- \\
& 2*I*a*b*c - I*b^2)*(d*x^(1/3) + c)^7 + 3920*(I*a*b*c^2 + I*b^2*c)*(d*x^(1/3 \\
&) + c)^6 + 2352*(-2*I*a*b*c^3 - 3*I*b^2*c^2)*(d*x^(1/3) + c)^5 + 3675*(I*a* \\
& b*c^4 + 2*I*b^2*c^3)*(d*x^(1/3) + c)^4 + 980*(-2*I*a*b*c^5 - 5*I*b^2*c^4)*(\\
& d*x^(1/3) + c)^3 + 735*(I*a*b*c^6 + 3*I*b^2*c^5)*(d*x^(1/3) + c)^2 + 105*(- \\
& 2*I*a*b*c^7 - 7*I*b^2*c^6)*(d*x^(1/3) + c))*\cos(2*d*x^(1/3) + 2*c) - (420*(\\
& d*x^(1/3) + c)^8*a*b + 105*b^2*c^7 - 960*(2*a*b*c + b^2)*(d*x^(1/3) + c)^7 \\
& + 3920*(a*b*c^2 + b^2*c)*(d*x^(1/3) + c)^6 - 2352*(2*a*b*c^3 + 3*b^2*c^2)*(\\
& d*x^(1/3) + c)^5 + 3675*(a*b*c^4 + 2*b^2*c^3)*(d*x^(1/3) + c)^4 - 980*(2*a* \\
& b*c^5 + 5*b^2*c^4)*(d*x^(1/3) + c)^3 + 735*(a*b*c^6 + 3*b^2*c^5)*(d*x^(1/3) \\
& + c)^2 - 105*(2*a*b*c^7 + 7*b^2*c^6)*(d*x^(1/3) + c))*\sin(2*d*x^(1/3) + 2* \\
& c))*\log(\cos(2*d*x^(1/3) + 2*c)^2 + \sin(2*d*x^(1/3) + 2*c)^2 + 2*\cos(2*d*x^(\\
& 1/3) + 2*c) + 1) - 1587600*(-I*a*b*\cos(2*d*x^(1/3) + 2*c) + a*b*\sin(2*d*x^(\\
& 1/3) + 2*c) - I*a*b)*\operatorname{polylog}(9, -e^(2*I*d*x^(1/3) + 2*I*c)) + 453600*(7*(d* \\
& x^(1/3) + c)*a*b - 4*a*b*c - 2*b^2 + (7*(d*x^(1/3) + c)*a*b - 4*a*b*c - 2*b \\
& ^2)*\cos(2*d*x^(1/3) + 2*c) - (-7*I*(d*x^(1/3) + c)*a*b + 4*I*a*b*c + 2*I*b^ \\
& 2)*\sin(2*d*x^(1/3) + 2*c))*\operatorname{polylog}(8, -e^(2*I*d*x^(1/3) + 2*I*c)) - 151200*
\end{aligned}$$

$$\begin{aligned}
& (21*I*(d*x^{(1/3)} + c)^2*a*b + 7*I*a*b*c^2 + 7*I*b^2*c + 12*(-2*I*a*b*c - I*b^2)*(d*x^{(1/3)} + c) + (21*I*(d*x^{(1/3)} + c)^2*a*b + 7*I*a*b*c^2 + 7*I*b^2*c + 12*(-2*I*a*b*c - I*b^2)*(d*x^{(1/3)} + c))*\cos(2*d*x^{(1/3)} + 2*c) - (21*(d*x^{(1/3)} + c)^2*a*b + 7*a*b*c^2 + 7*b^2*c - 12*(2*a*b*c + b^2)*(d*x^{(1/3)} + c))*\sin(2*d*x^{(1/3)} + 2*c))*\text{polylog}(7, -e^{(2*I*d*x^{(1/3)} + 2*I*c)}) - 30240*(70*(d*x^{(1/3)} + c)^3*a*b - 14*a*b*c^3 - 21*b^2*c^2 - 60*(2*a*b*c + b^2)*(d*x^{(1/3)} + c)^2 + 70*(a*b*c^2 + b^2*c)*(d*x^{(1/3)} + c) + (70*(d*x^{(1/3)} + c)^3*a*b - 14*a*b*c^3 - 21*b^2*c^2 - 60*(2*a*b*c + b^2)*(d*x^{(1/3)} + c)^2 + 70*(a*b*c^2 + b^2*c)*(d*x^{(1/3)} + c))*\cos(2*d*x^{(1/3)} + 2*c) + (70*I*(d*x^{(1/3)} + c)^3*a*b - 14*I*a*b*c^3 - 21*I*b^2*c^2 + 60*(-2*I*a*b*c - I*b^2)*(d*x^{(1/3)} + c)^2 + 70*(I*a*b*c^2 + I*b^2*c)*(d*x^{(1/3)} + c))*\sin(2*d*x^{(1/3)} + 2*c))*\text{polylog}(6, -e^{(2*I*d*x^{(1/3)} + 2*I*c)}) - 3780*(-280*I*(d*x^{(1/3)} + c)^4*a*b - 35*I*a*b*c^4 - 70*I*b^2*c^3 + 320*(2*I*a*b*c + I*b^2)*(d*x^{(1/3)} + c)^3 + 560*(-I*a*b*c^2 - I*b^2*c)*(d*x^{(1/3)} + c)^2 + 112*(2*I*a*b*c^3 + 3*I*b^2*c^2)*(d*x^{(1/3)} + c) + (-280*I*(d*x^{(1/3)} + c)^4*a*b - 35*I*a*b*c^4 - 70*I*b^2*c^3 + 320*(2*I*a*b*c + I*b^2)*(d*x^{(1/3)} + c)^3 + 560*(-I*a*b*c^2 - I*b^2*c)*(d*x^{(1/3)} + c)^2 + 112*(2*I*a*b*c^3 + 3*I*b^2*c^2)*(d*x^{(1/3)} + c))*\cos(2*d*x^{(1/3)} + 2*c) + (280*(d*x^{(1/3)} + c)^4*a*b + 35*a*b*c^4 + 70*b^2*c^3 - 320*(2*a*b*c + b^2)*(d*x^{(1/3)} + c)^3 + 560*(a*b*c^2 + b^2*c)*(d*x^{(1/3)} + c)^2 - 112*(2*a*b*c^3 + 3*b^2*c^2)*(d*x^{(1/3)} + c))*\sin(2*d*x^{(1/3)} + 2*c))*\text{polylog}(5, -e^{(2*I*d*x^{(1/3)} + 2*I*c)}) + 2520*(168*(d*x^{(1/3)} + c)^5*a*b - 14*a*b*c^5 - 35*b^2*c^4 - 240*(2*a*b*c + b^2)*(d*x^{(1/3)} + c)^4 + 560*(a*b*c^2 + b^2*c)*(d*x^{(1/3)} + c)^3 - 168*(2*a*b*c^3 + 3*b^2*c^2)*(d*x^{(1/3)} + c)^2 + 105*(a*b*c^4 + 2*b^2*c^3)*(d*x^{(1/3)} + c) + (168*(d*x^{(1/3)} + c)^5*a*b - 14*a*b*c^5 - 35*b^2*c^4 - 240*(2*a*b*c + b^2)*(d*x^{(1/3)} + c)^4 + 560*(a*b*c^2 + b^2*c)*(d*x^{(1/3)} + c)^3 - 168*(2*a*b*c^3 + 3*b^2*c^2)*(d*x^{(1/3)} + c)^2 + 105*(a*b*c^4 + 2*b^2*c^3)*(d*x^{(1/3)} + c))*\cos(2*d*x^{(1/3)} + 2*c) - (-168*I*(d*x^{(1/3)} + c)^5*a*b + 14*I*a*b*c^5 + 35*I*b^2*c^4 + 240*(2*I*a*b*c + I*b^2)*(d*x^{(1/3)} + c)^4 + 560*(-I*a*b*c^2 - I*b^2*c)*(d*x^{(1/3)} + c)^3 + 168*(2*I*a*b*c^3 + 3*I*b^2*c^2)*(d*x^{(1/3)} + c)^2 + 105*(-I*a*b*c^4 - 2*I*b^2*c^3)*(d*x^{(1/3)} + c))*\sin(2*d*x^{(1/3)} + 2*c))*\text{polylog}(4, -e^{(2*I*d*x^{(1/3)} + 2*I*c)}) - 1260*(112*I*(d*x^{(1/3)} + c)^6*a*b + 7*I*a*b*c^6 + 21*I*b^2*c^5 + 192*(-2*I*a*b*c - I*b^2)*(d*x^{(1/3)} + c)^5 + 560*(I*a*b*c^2 + I*b^2*c)*(d*x^{(1/3)} + c)^4 + 224*(-2*I*a*b*c^3 - 3*I*b^2*c^2)*(d*x^{(1/3)} + c)^3 + 210*(I*a*b*c^4 + 2*I*b^2*c^3)*(d*x^{(1/3)} + c)^2 + 28*(-2*I*a*b*c^5 - 5*I*b^2*c^4)*(d*x^{(1/3)} + c) + (112*I*(d*x^{(1/3)} + c)^6*a*b + 7*I*a*b*c^6 + 21*I*b^2*c^5 + 192*(-2*I*a*b*c - I*b^2)*(d*x^{(1/3)} + c)^5 + 560*(I*a*b*c^2 + I*b^2*c)*(d*x^{(1/3)} + c)^4 + 224*(-2*I*a*b*c^3 - 3*I*b^2*c^2)*(d*x^{(1/3)} + c)^3 + 210*(I*a*b*c^4 + 2*I*b^2*c^3)*(d*x^{(1/3)} + c)^2 + 28*(-2*I*a*b*c^5 - 5*I*b^2*c^4)*(d*x^{(1/3)} + c))*\cos(2*d*x^{(1/3)} + 2*c) - (112*(d*x^{(1/3)} + c)^6*a*b + 7*a*b*c^6 + 21*b^2*c^5 - 192*(2*a*b*c + b^2)*(d*x^{(1/3)} + c)^5 + 560*(a*b*c^2 + b^2*c)*(d*x^{(1/3)} + c)^4 - 224*(2*a*b*c^3 + 3*b^2*c^2)*(d*x^{(1/3)} + c)^3 + 210*(a*b*c^4 + 2*b^2*c^3)*(d*x^{(1/3)} + c)^2 - 28*(2*a*b*c^5 + 5*b^2*c^4)*(d*x^{(1/3)} + c))*\sin(2*d*x^{(1/3)} + 2*c))*\text{polylog}(3, -e^{(2*I*d*x^{(1/3)} + 2*I*c)}) - 35*((2*I*a*b - b^2)*(d*x^{(1/3)} + c)^
\end{aligned}$$

$$9 + 9*(-2*I*b^2 + (-2*I*a*b + b^2)*c)*(d*x^(1/3) + c)^8 + 36*(4*I*b^2*c + (2*I*a*b - b^2)*c^2)*(d*x^(1/3) + c)^7 + 84*(-6*I*b^2*c^2 + (-2*I*a*b + b^2)*c^3)*(d*x^(1/3) + c)^6 + 126*(8*I*b^2*c^3 + (2*I*a*b - b^2)*c^4)*(d*x^(1/3) + c)^5 + 126*(-10*I*b^2*c^4 + (-2*I*a*b + b^2)*c^5)*(d*x^(1/3) + c)^4 + 84*(12*I*b^2*c^5 + (2*I*a*b - b^2)*c^6)*(d*x^(1/3) + c)^3 + 36*(-14*I*b^2*c^6 + (-2*I*a*b + b^2)*c^7)*(d*x^(1/3) + c)^2 - 9*(b^2*c^8 - 16*I*b^2*c^7)*(d*x^(1/3) + c)*\sin(2*d*x^(1/3) + 2*c)/(-315*I*\cos(2*d*x^(1/3) + 2*c) + 315*\sin(2*d*x^(1/3) + 2*c) - 315*I)/d^9$$

Giac [F]

$$\int x^2(a + b \tan(c + d\sqrt[3]{x}))^2 dx = \int (b \tan(dx^{1/3} + c) + a)^2 x^2 dx$$

[In] integrate(x^2*(a+b*tan(c+d*x^(1/3)))^2,x, algorithm="giac")

[Out] integrate((b*tan(d*x^(1/3) + c) + a)^2*x^2, x)

Mupad [F(-1)]

Timed out.

$$\int x^2(a + b \tan(c + d\sqrt[3]{x}))^2 dx = \int x^2(a + b \tan(c + dx^{1/3}))^2 dx$$

[In] int(x^2*(a + b*tan(c + d*x^(1/3)))^2,x)

[Out] int(x^2*(a + b*tan(c + d*x^(1/3)))^2, x)

3.53 $\int x(a + b \tan(c + d\sqrt[3]{x}))^2 dx$

Optimal result	338
Rubi [A] (verified)	339
Mathematica [A] (verified)	344
Maple [F]	345
Fricas [F]	345
Sympy [F]	345
Maxima [B] (verification not implemented)	345
Giac [F]	347
Mupad [F(-1)]	347

Optimal result

Integrand size = 18, antiderivative size = 408

$$\begin{aligned}
 \int x(a + b \tan(c + d\sqrt[3]{x}))^2 dx = & -\frac{3ib^2x^{5/3}}{d} + \frac{a^2x^2}{2} + iabx^2 - \frac{b^2x^2}{2} \\
 & + \frac{15b^2x^{4/3} \log\left(1 + e^{2i(c+d\sqrt[3]{x})}\right)}{d^2} \\
 & - \frac{6abx^{5/3} \log\left(1 + e^{2i(c+d\sqrt[3]{x})}\right)}{d} \\
 & - \frac{30ib^2x \operatorname{PolyLog}\left(2, -e^{2i(c+d\sqrt[3]{x})}\right)}{d^3} \\
 & + \frac{15iabx^{4/3} \operatorname{PolyLog}\left(2, -e^{2i(c+d\sqrt[3]{x})}\right)}{d^2} \\
 & + \frac{45b^2x^{2/3} \operatorname{PolyLog}\left(3, -e^{2i(c+d\sqrt[3]{x})}\right)}{d^4} \\
 & - \frac{30abx \operatorname{PolyLog}\left(3, -e^{2i(c+d\sqrt[3]{x})}\right)}{d^3} \\
 & + \frac{45ib^2\sqrt[3]{x} \operatorname{PolyLog}\left(4, -e^{2i(c+d\sqrt[3]{x})}\right)}{d^5} \\
 & - \frac{45iabx^{2/3} \operatorname{PolyLog}\left(4, -e^{2i(c+d\sqrt[3]{x})}\right)}{d^4} \\
 & - \frac{45b^2 \operatorname{PolyLog}\left(5, -e^{2i(c+d\sqrt[3]{x})}\right)}{2d^6} \\
 & + \frac{45ab\sqrt[3]{x} \operatorname{PolyLog}\left(5, -e^{2i(c+d\sqrt[3]{x})}\right)}{d^5} \\
 & + \frac{45iab \operatorname{PolyLog}\left(6, -e^{2i(c+d\sqrt[3]{x})}\right)}{2d^6} + \frac{3b^2x^{5/3} \tan(c + d\sqrt[3]{x})}{d}
 \end{aligned}$$

[Out] 15*I*a*b*x^(4/3)*polylog(2,-exp(2*I*(c+d*x^(1/3))))/d^2+1/2*a^2*x^2-30*I*b^2*x*polylog(2,-exp(2*I*(c+d*x^(1/3))))/d^3-1/2*b^2*x^2+15*b^2*x^(4/3)*ln(1+exp(2*I*(c+d*x^(1/3))))/d^2-6*a*b*x^(5/3)*ln(1+exp(2*I*(c+d*x^(1/3))))/d-45*I*a*b*x^(2/3)*polylog(4,-exp(2*I*(c+d*x^(1/3))))/d^4-3*I*b^2*x^(5/3)/d+45*b^2*x^(2/3)*polylog(3,-exp(2*I*(c+d*x^(1/3))))/d^4-30*a*b*x*polylog(3,-exp(2*I*(c+d*x^(1/3))))/d^3+45*I*b^2*x^(1/3)*polylog(4,-exp(2*I*(c+d*x^(1/3))))/d^5+45/2*I*a*b*polylog(6,-exp(2*I*(c+d*x^(1/3))))/d^6-45/2*b^2*polylog(5,-exp(2*I*(c+d*x^(1/3))))/d^6+45*a*b*x^(1/3)*polylog(5,-exp(2*I*(c+d*x^(1/3))))/d^5+I*a*b*x^2+3*b^2*x^(5/3)*tan(c+d*x^(1/3))/d

Rubi [A] (verified)

Time = 0.87 (sec) , antiderivative size = 408, normalized size of antiderivative = 1.00, number of steps used = 20, number of rules used = 10, $\frac{\text{number of rules}}{\text{integrand size}} = 0.556$, Rules used = {3832, 3803, 3800, 2221, 2611, 6744, 2320, 6724, 3801, 30}

$$\int x(a + b \tan(c + d\sqrt[3]{x}))^2 dx = \frac{a^2 x^2}{2} + \frac{45iab \operatorname{PolyLog}\left(6, -e^{2i(c+d\sqrt[3]{x})}\right)}{2d^6} + \frac{45ab\sqrt[3]{x} \operatorname{PolyLog}\left(5, -e^{2i(c+d\sqrt[3]{x})}\right)}{d^5} - \frac{45iabx^{2/3} \operatorname{PolyLog}\left(4, -e^{2i(c+d\sqrt[3]{x})}\right)}{d^4} - \frac{30abx \operatorname{PolyLog}\left(3, -e^{2i(c+d\sqrt[3]{x})}\right)}{d^3} + \frac{15iabx^{4/3} \operatorname{PolyLog}\left(2, -e^{2i(c+d\sqrt[3]{x})}\right)}{d^2} - \frac{6abx^{5/3} \log\left(1 + e^{2i(c+d\sqrt[3]{x})}\right)}{d} + iabx^2 - \frac{45b^2 \operatorname{PolyLog}\left(5, -e^{2i(c+d\sqrt[3]{x})}\right)}{2d^6} + \frac{45ib^2\sqrt[3]{x} \operatorname{PolyLog}\left(4, -e^{2i(c+d\sqrt[3]{x})}\right)}{d^5} + \frac{45b^2x^{2/3} \operatorname{PolyLog}\left(3, -e^{2i(c+d\sqrt[3]{x})}\right)}{d^4} - \frac{30ib^2x \operatorname{PolyLog}\left(2, -e^{2i(c+d\sqrt[3]{x})}\right)}{d^3} + \frac{15b^2x^{4/3} \log\left(1 + e^{2i(c+d\sqrt[3]{x})}\right)}{d^2} + \frac{3b^2x^{5/3} \tan(c + d\sqrt[3]{x})}{d} - \frac{3ib^2x^{5/3}}{d} - \frac{1}{2}b^2x^2$$

[In] Int[x*(a + b*Tan[c + d*x^(1/3)])^2,x]

[Out] ((-3*I)*b^2*x^(5/3))/d + (a^2*x^2)/2 + I*a*b*x^2 - (b^2*x^2)/2 + (15*b^2*x^(4/3)*Log[1 + E^((2*I)*(c + d*x^(1/3)))])/d^2 - (6*a*b*x^(5/3)*Log[1 + E^((2*I)*(c + d*x^(1/3)))])/d - ((30*I)*b^2*x*PolyLog[2, -E^((2*I)*(c + d*x^(1/3)))])/d^3 + ((15*I)*a*b*x^(4/3)*PolyLog[2, -E^((2*I)*(c + d*x^(1/3)))])/d^2 + (45*b^2*x^(2/3)*PolyLog[3, -E^((2*I)*(c + d*x^(1/3)))])/d^4 - (30*a*b*x*PolyLog[3, -E^((2*I)*(c + d*x^(1/3)))])/d^3 + ((45*I)*b^2*x^(1/3)*PolyLog[

4, $-E^{((2*I)*(c + d*x^{(1/3))))}/d^5 - ((45*I)*a*b*x^{(2/3)}*PolyLog[4, -E^{((2*I)*(c + d*x^{(1/3))))}/d^4 - (45*b^2*PolyLog[5, -E^{((2*I)*(c + d*x^{(1/3))))})/(2*d^6) + (45*a*b*x^{(1/3)}*PolyLog[5, -E^{((2*I)*(c + d*x^{(1/3))))})/d^5 + ((45*I)/2)*a*b*PolyLog[6, -E^{((2*I)*(c + d*x^{(1/3))))})/d^6 + (3*b^2*x^{(5/3)}*Tan[c + d*x^{(1/3)})]/d$

Rule 30

Int[(x_)^(m_), x_Symbol] := Simp[x^(m + 1)/(m + 1), x] /; FreeQ[m, x] && NeQ[m, -1]

Rule 2221

Int[(((F_)^(g_)*((e_) + (f_)*(x_)))^(n_)*((c_) + (d_)*(x_))^(m_))/((a_) + (b_)*((F_)^(g_)*((e_) + (f_)*(x_)))^(n_)), x_Symbol] := Simp[((c + d*x)^m/(b*f*g*n*Log[F]))*Log[1 + b*((F^(g*(e + f*x)))^n/a)], x] - Dist[d*(m/(b*f*g*n*Log[F])), Int[(c + d*x)^(m - 1)*Log[1 + b*((F^(g*(e + f*x)))^n/a)], x], x] /; FreeQ[{F, a, b, c, d, e, f, g, n}, x] && IGtQ[m, 0]

Rule 2320

Int[u_, x_Symbol] := With[{v = FunctionOfExponential[u, x]}, Dist[v/D[v, x], Subst[Int[FunctionOfExponentialFunction[u, x]/x, x], x, v], x] /; FunctionOfExponentialQ[u, x] && !MatchQ[u, (w_)*((a_)*(v_)^(n_))^(m_) /; FreeQ[{a, m, n}, x] && IntegerQ[m*n] && !MatchQ[u, E^{(c_)*((a_) + (b_)*x)}*(F_)[v_] /; FreeQ[{a, b, c}, x] && InverseFunctionQ[F[x]]]

Rule 2611

Int[Log[1 + (e_)*((F_)^(c_)*((a_) + (b_)*(x_)))^(n_)]*((f_) + (g_)*(x_))^(m_), x_Symbol] := Simp[(-f + g*x)^m*(PolyLog[2, (-e)*(F^(c*(a + b*x)))^n]/(b*c*n*Log[F])), x] + Dist[g*(m/(b*c*n*Log[F])), Int[(f + g*x)^(m - 1)*PolyLog[2, (-e)*(F^(c*(a + b*x)))^n], x], x] /; FreeQ[{F, a, b, c, e, f, g, n}, x] && GtQ[m, 0]

Rule 3800

Int[(((c_) + (d_)*(x_))^(m_)*tan[(e_) + (f_)*(x_)], x_Symbol] := Simp[I*((c + d*x)^(m + 1)/(d*(m + 1))), x] - Dist[2*I, Int[(c + d*x)^m*(E^(2*I*(e + f*x)))/(1 + E^(2*I*(e + f*x))), x], x] /; FreeQ[{c, d, e, f}, x] && IGtQ[m, 0]

Rule 3801

Int[(((c_) + (d_)*(x_))^(m_)*((b_)*tan[(e_) + (f_)*(x_)]^(n_)), x_Symbol] := Simp[b*(c + d*x)^m*((b*Tan[e + f*x])^(n - 1)/(f*(n - 1))), x] + (-Dist[b*d*(m/(f*(n - 1))), Int[(c + d*x)^(m - 1)*(b*Tan[e + f*x])^(n - 1), x],

$x] - \text{Dist}[b^2, \text{Int}[(c + d*x)^m*(b*\text{Tan}[e + f*x])^{(n - 2)}, x], x] /; \text{FreeQ}[\{b, c, d, e, f\}, x] \ \&\& \ \text{GtQ}[n, 1] \ \&\& \ \text{GtQ}[m, 0]$

Rule 3803

$\text{Int}[(c + d*x)^m*(a + b*\text{Tan}[e + f*x])^{(n)}, x_Symbol] \rightarrow \text{Int}[\text{ExpandIntegrand}[(c + d*x)^m, (a + b*\text{Tan}[e + f*x])^n, x], x] /; \text{FreeQ}[\{a, b, c, d, e, f, m\}, x] \ \&\& \ \text{IGtQ}[m, 0] \ \&\& \ \text{IGtQ}[n, 0]$

Rule 3832

$\text{Int}[(x)^m*(a + b*\text{Tan}[c + d*x])^{(p)}, x_Symbol] \rightarrow \text{Dist}[1/n, \text{Subst}[\text{Int}[x^{(\text{Simplify}[(m + 1)/n] - 1)*(a + b*\text{Tan}[c + d*x])^p}, x], x, x^n], x] /; \text{FreeQ}[\{a, b, c, d, m, n, p\}, x] \ \&\& \ \text{IGtQ}[\text{Simplify}[(m + 1)/n], 0] \ \&\& \ \text{IntegerQ}[p]$

Rule 6724

$\text{Int}[\text{PolyLog}[n, (c + d*x)^m]/((d + e*x)), x_Symbol] \rightarrow \text{Simp}[\text{PolyLog}[n + 1, c*(a + b*x)^p/(e*p), x] /; \text{FreeQ}[\{a, b, c, d, e, n, p\}, x] \ \&\& \ \text{EqQ}[b*d, a*e]$

Rule 6744

$\text{Int}[(e + f*x)^m*\text{PolyLog}[n, (d + e*x)^m*(a + b*x)^p], x_Symbol] \rightarrow \text{Simp}[(e + f*x)^m*(\text{PolyLog}[n + 1, d*(F^{(c + b*x)})^p]/(b*c*p*\text{Log}[F])), x] - \text{Dist}[f*(m/(b*c*p*\text{Log}[F])), \text{Int}[(e + f*x)^{m - 1}*\text{PolyLog}[n + 1, d*(F^{(c + b*x)})^p], x], x] /; \text{FreeQ}[\{F, a, b, c, d, e, f, n, p\}, x] \ \&\& \ \text{GtQ}[m, 0]$

Rubi steps

$$\begin{aligned}
 \text{integral} &= 3\text{Subst}\left(\int x^5(a + b \tan(c + dx))^2 dx, x, \sqrt[3]{x}\right) \\
 &= 3\text{Subst}\left(\int (a^2x^5 + 2abx^5 \tan(c + dx) + b^2x^5 \tan^2(c + dx)) dx, x, \sqrt[3]{x}\right) \\
 &= \frac{a^2x^2}{2} + (6ab)\text{Subst}\left(\int x^5 \tan(c + dx) dx, x, \sqrt[3]{x}\right) \\
 &\quad + (3b^2)\text{Subst}\left(\int x^5 \tan^2(c + dx) dx, x, \sqrt[3]{x}\right) \\
 &= \frac{a^2x^2}{2} + iabx^2 + \frac{3b^2x^{5/3} \tan(c + d\sqrt[3]{x})}{d} - (12iab)\text{Subst}\left(\int \frac{e^{2i(c+dx)}x^5}{1 + e^{2i(c+dx)}} dx, x, \sqrt[3]{x}\right) \\
 &\quad - (3b^2)\text{Subst}\left(\int x^5 dx, x, \sqrt[3]{x}\right) - \frac{(15b^2)\text{Subst}\left(\int x^4 \tan(c + dx) dx, x, \sqrt[3]{x}\right)}{d}
 \end{aligned}$$

$$\begin{aligned}
&= -\frac{3ib^2x^{5/3}}{d} + \frac{a^2x^2}{2} + iabx^2 - \frac{b^2x^2}{2} - \frac{6abx^{5/3} \log\left(1 + e^{2i(c+d\sqrt[3]{x})}\right)}{d} + \frac{3b^2x^{5/3} \tan(c + d\sqrt[3]{x})}{d} \\
&\quad + \frac{(30ab)\text{Subst}\left(\int x^4 \log\left(1 + e^{2i(c+dx)}\right) dx, x, \sqrt[3]{x}\right)}{d} + \frac{(30ib^2)\text{Subst}\left(\int \frac{e^{2i(c+dx)}x^4}{1+e^{2i(c+dx)}} dx, x, \sqrt[3]{x}\right)}{d} \\
&= -\frac{3ib^2x^{5/3}}{d} + \frac{a^2x^2}{2} + iabx^2 - \frac{b^2x^2}{2} + \frac{15b^2x^{4/3} \log\left(1 + e^{2i(c+d\sqrt[3]{x})}\right)}{d^2} \\
&\quad - \frac{6abx^{5/3} \log\left(1 + e^{2i(c+d\sqrt[3]{x})}\right)}{d} + \frac{15iabx^{4/3} \text{PolyLog}\left(2, -e^{2i(c+d\sqrt[3]{x})}\right)}{d^2} \\
&\quad + \frac{3b^2x^{5/3} \tan(c + d\sqrt[3]{x})}{d} - \frac{(60iab)\text{Subst}\left(\int x^3 \text{PolyLog}\left(2, -e^{2i(c+dx)}\right) dx, x, \sqrt[3]{x}\right)}{d^2} \\
&\quad - \frac{(60b^2)\text{Subst}\left(\int x^3 \log\left(1 + e^{2i(c+dx)}\right) dx, x, \sqrt[3]{x}\right)}{d^2} \\
&= -\frac{3ib^2x^{5/3}}{d} + \frac{a^2x^2}{2} + iabx^2 - \frac{b^2x^2}{2} + \frac{15b^2x^{4/3} \log\left(1 + e^{2i(c+d\sqrt[3]{x})}\right)}{d^2} \\
&\quad - \frac{6abx^{5/3} \log\left(1 + e^{2i(c+d\sqrt[3]{x})}\right)}{d} - \frac{30ib^2x \text{PolyLog}\left(2, -e^{2i(c+d\sqrt[3]{x})}\right)}{d^3} \\
&\quad + \frac{15iabx^{4/3} \text{PolyLog}\left(2, -e^{2i(c+d\sqrt[3]{x})}\right)}{d^2} - \frac{30abx \text{PolyLog}\left(3, -e^{2i(c+d\sqrt[3]{x})}\right)}{d^3} \\
&\quad + \frac{3b^2x^{5/3} \tan(c + d\sqrt[3]{x})}{d} + \frac{(90ab)\text{Subst}\left(\int x^2 \text{PolyLog}\left(3, -e^{2i(c+dx)}\right) dx, x, \sqrt[3]{x}\right)}{d^3} \\
&\quad + \frac{(90ib^2)\text{Subst}\left(\int x^2 \text{PolyLog}\left(2, -e^{2i(c+dx)}\right) dx, x, \sqrt[3]{x}\right)}{d^3} \\
&= -\frac{3ib^2x^{5/3}}{d} + \frac{a^2x^2}{2} + iabx^2 - \frac{b^2x^2}{2} + \frac{15b^2x^{4/3} \log\left(1 + e^{2i(c+d\sqrt[3]{x})}\right)}{d^2} \\
&\quad - \frac{6abx^{5/3} \log\left(1 + e^{2i(c+d\sqrt[3]{x})}\right)}{d} - \frac{30ib^2x \text{PolyLog}\left(2, -e^{2i(c+d\sqrt[3]{x})}\right)}{d^3} \\
&\quad + \frac{15iabx^{4/3} \text{PolyLog}\left(2, -e^{2i(c+d\sqrt[3]{x})}\right)}{d^2} + \frac{45b^2x^{2/3} \text{PolyLog}\left(3, -e^{2i(c+d\sqrt[3]{x})}\right)}{d^4} \\
&\quad - \frac{30abx \text{PolyLog}\left(3, -e^{2i(c+d\sqrt[3]{x})}\right)}{d^3} - \frac{45iabx^{2/3} \text{PolyLog}\left(4, -e^{2i(c+d\sqrt[3]{x})}\right)}{d^4} \\
&\quad + \frac{3b^2x^{5/3} \tan(c + d\sqrt[3]{x})}{d} + \frac{(90iab)\text{Subst}\left(\int x \text{PolyLog}\left(4, -e^{2i(c+dx)}\right) dx, x, \sqrt[3]{x}\right)}{d^4} \\
&\quad - \frac{(90b^2)\text{Subst}\left(\int x \text{PolyLog}\left(3, -e^{2i(c+dx)}\right) dx, x, \sqrt[3]{x}\right)}{d^4}
\end{aligned}$$

$$\begin{aligned}
&= -\frac{3ib^2x^{5/3}}{d} + \frac{a^2x^2}{2} + iabx^2 - \frac{b^2x^2}{2} + \frac{15b^2x^{4/3} \log\left(1 + e^{2i(c+d\sqrt[3]{x}})\right)}{d^2} \\
&\quad - \frac{6abx^{5/3} \log\left(1 + e^{2i(c+d\sqrt[3]{x}})\right)}{d} - \frac{30ib^2x \operatorname{PolyLog}\left(2, -e^{2i(c+d\sqrt[3]{x}})\right)}{d^3} \\
&\quad + \frac{15iabx^{4/3} \operatorname{PolyLog}\left(2, -e^{2i(c+d\sqrt[3]{x}})\right)}{d^2} + \frac{45b^2x^{2/3} \operatorname{PolyLog}\left(3, -e^{2i(c+d\sqrt[3]{x}})\right)}{d^4} \\
&\quad - \frac{30abx \operatorname{PolyLog}\left(3, -e^{2i(c+d\sqrt[3]{x}})\right)}{d^3} + \frac{45ib^2\sqrt[3]{x} \operatorname{PolyLog}\left(4, -e^{2i(c+d\sqrt[3]{x}})\right)}{d^5} \\
&\quad - \frac{45iabx^{2/3} \operatorname{PolyLog}\left(4, -e^{2i(c+d\sqrt[3]{x}})\right)}{d^4} + \frac{45ab\sqrt[3]{x} \operatorname{PolyLog}\left(5, -e^{2i(c+d\sqrt[3]{x}})\right)}{d^5} \\
&\quad + \frac{3b^2x^{5/3} \tan(c + d\sqrt[3]{x})}{d} - \frac{(45ab) \operatorname{Subst}\left(\int \operatorname{PolyLog}\left(5, -e^{2i(c+dx)}\right) dx, x, \sqrt[3]{x}\right)}{d^5} \\
&\quad - \frac{(45ib^2) \operatorname{Subst}\left(\int \operatorname{PolyLog}\left(4, -e^{2i(c+dx)}\right) dx, x, \sqrt[3]{x}\right)}{d^5} \\
&= -\frac{3ib^2x^{5/3}}{d} + \frac{a^2x^2}{2} + iabx^2 - \frac{b^2x^2}{2} + \frac{15b^2x^{4/3} \log\left(1 + e^{2i(c+d\sqrt[3]{x}})\right)}{d^2} \\
&\quad - \frac{6abx^{5/3} \log\left(1 + e^{2i(c+d\sqrt[3]{x}})\right)}{d} - \frac{30ib^2x \operatorname{PolyLog}\left(2, -e^{2i(c+d\sqrt[3]{x}})\right)}{d^3} \\
&\quad + \frac{15iabx^{4/3} \operatorname{PolyLog}\left(2, -e^{2i(c+d\sqrt[3]{x}})\right)}{d^2} + \frac{45b^2x^{2/3} \operatorname{PolyLog}\left(3, -e^{2i(c+d\sqrt[3]{x}})\right)}{d^4} \\
&\quad - \frac{30abx \operatorname{PolyLog}\left(3, -e^{2i(c+d\sqrt[3]{x}})\right)}{d^3} + \frac{45ib^2\sqrt[3]{x} \operatorname{PolyLog}\left(4, -e^{2i(c+d\sqrt[3]{x}})\right)}{d^5} \\
&\quad - \frac{45iabx^{2/3} \operatorname{PolyLog}\left(4, -e^{2i(c+d\sqrt[3]{x}})\right)}{d^4} + \frac{45ab\sqrt[3]{x} \operatorname{PolyLog}\left(5, -e^{2i(c+d\sqrt[3]{x}})\right)}{d^5} \\
&\quad + \frac{3b^2x^{5/3} \tan(c + d\sqrt[3]{x})}{d} + \frac{(45iab) \operatorname{Subst}\left(\int \frac{\operatorname{PolyLog}(5, -x)}{x} dx, x, e^{2i(c+d\sqrt[3]{x}})\right)}{2d^6} \\
&\quad - \frac{(45b^2) \operatorname{Subst}\left(\int \frac{\operatorname{PolyLog}(4, -x)}{x} dx, x, e^{2i(c+d\sqrt[3]{x}})\right)}{2d^6}
\end{aligned}$$

$$\begin{aligned}
&= -\frac{3ib^2x^{5/3}}{d} + \frac{a^2x^2}{2} + iabx^2 - \frac{b^2x^2}{2} + \frac{15b^2x^{4/3} \log\left(1 + e^{2i(c+d\sqrt[3]{x})}\right)}{d^2} \\
&\quad - \frac{6abx^{5/3} \log\left(1 + e^{2i(c+d\sqrt[3]{x})}\right)}{d} - \frac{30ib^2x \operatorname{PolyLog}\left(2, -e^{2i(c+d\sqrt[3]{x})}\right)}{d^3} \\
&\quad + \frac{15iabx^{4/3} \operatorname{PolyLog}\left(2, -e^{2i(c+d\sqrt[3]{x})}\right)}{d^2} \\
&\quad + \frac{45b^2x^{2/3} \operatorname{PolyLog}\left(3, -e^{2i(c+d\sqrt[3]{x})}\right)}{d^4} - \frac{30abx \operatorname{PolyLog}\left(3, -e^{2i(c+d\sqrt[3]{x})}\right)}{d^3} \\
&\quad + \frac{45ib^2\sqrt[3]{x} \operatorname{PolyLog}\left(4, -e^{2i(c+d\sqrt[3]{x})}\right)}{d^5} - \frac{45iabx^{2/3} \operatorname{PolyLog}\left(4, -e^{2i(c+d\sqrt[3]{x})}\right)}{d^4} \\
&\quad - \frac{45b^2 \operatorname{PolyLog}\left(5, -e^{2i(c+d\sqrt[3]{x})}\right)}{2d^6} + \frac{45ab\sqrt[3]{x} \operatorname{PolyLog}\left(5, -e^{2i(c+d\sqrt[3]{x})}\right)}{d^5} \\
&\quad + \frac{45iab \operatorname{PolyLog}\left(6, -e^{2i(c+d\sqrt[3]{x})}\right)}{2d^6} + \frac{3b^2x^{5/3} \tan(c + d\sqrt[3]{x})}{d}
\end{aligned}$$

Mathematica [A] (verified)

Time = 3.85 (sec) , antiderivative size = 571, normalized size of antiderivative = 1.40

$$\begin{aligned}
&\int x(a + b \tan(c + d\sqrt[3]{x}))^2 dx \\
&= \frac{1}{2} \left(-\frac{ibe^{2ic} \left(-12bd^5 e^{-2ic} x^{5/3} + 4ad^6 e^{-2ic} x^2 + 30ibd^4 e^{-2ic} (1 + e^{2ic}) x^{4/3} \log\left(1 + e^{-2i(c+d\sqrt[3]{x})}\right) - 12iad^5 e^{-2ic} \right)}{2d^6} \right. \\
&\quad \left. + \frac{6b^2x^{5/3} \sec(c) \sec(c + d\sqrt[3]{x}) \sin(d\sqrt[3]{x})}{d} + x^2(a^2 - b^2 + 2ab \tan(c)) \right)
\end{aligned}$$

[In] Integrate[x*(a + b*Tan[c + d*x^(1/3)])^2,x]

[Out] (((-I)*b*E^((2*I)*c))*((-12*b*d^5*x^(5/3))/E^((2*I)*c) + (4*a*d^6*x^2)/E^((2*I)*c) + ((30*I)*b*d^4*(1 + E^((2*I)*c))*x^(4/3)*Log[1 + E^((-2*I)*(c + d*x^(1/3)))]))/E^((2*I)*c) - ((12*I)*a*d^5*(1 + E^((2*I)*c))*x^(5/3)*Log[1 + E^((-2*I)*(c + d*x^(1/3)))])/E^((2*I)*c) - 60*b*d^3*(1 + E^((-2*I)*c))*x*PolyLog[2, -E^((-2*I)*(c + d*x^(1/3)))] + 30*a*d^4*(1 + E^((-2*I)*c))*x^(4/3)*PolyLog[2, -E^((-2*I)*(c + d*x^(1/3)))] + ((90*I)*b*d^2*(1 + E^((2*I)*c))*x^(2/3)*PolyLog[3, -E^((-2*I)*(c + d*x^(1/3)))])/E^((2*I)*c) - ((60*I)*a*d^3*(1 + E^((2*I)*c))*x*PolyLog[3, -E^((-2*I)*(c + d*x^(1/3)))])/E^((2*I)*c) + 90*b*d*(1 + E^((-2*I)*c))*x^(1/3)*PolyLog[4, -E^((-2*I)*(c + d*x^(1/3)))] - 90*a*d^2*(1 + E^((-2*I)*c))*x^(2/3)*PolyLog[4, -E^((-2*I)*(c + d*x^(1/3)))] - ((45*I)*b*(1 + E^((2*I)*c))*PolyLog[5, -E^((-2*I)*(c + d*x^(1/3)))])/E^

$$\frac{((2*I)*c) + ((90*I)*a*d*(1 + E^{((2*I)*c)})*x^{(1/3)}*PolyLog[5, -E^{((-2*I)*(c + d*x^{(1/3)})}))/E^{((2*I)*c) + 45*a*(1 + E^{((-2*I)*c)})*PolyLog[6, -E^{((-2*I)*(c + d*x^{(1/3)})}]))/(d^6*(1 + E^{((2*I)*c)})) + (6*b^2*x^{(5/3)}*Sec[c]*Sec[c + d*x^{(1/3)}]*Sin[d*x^{(1/3)}])/d + x^2*(a^2 - b^2 + 2*a*b*Tan[c]))/2$$

Maple [F]

$$\int x \left(a + b \tan \left(c + d x^{\frac{1}{3}} \right) \right)^2 dx$$

[In] int(x*(a+b*tan(c+d*x^(1/3)))^2,x)

[Out] int(x*(a+b*tan(c+d*x^(1/3)))^2,x)

Fricas [F]

$$\int x(a + b \tan(c + d\sqrt[3]{x}))^2 dx = \int (b \tan(dx^{\frac{1}{3}} + c) + a)^2 x dx$$

[In] integrate(x*(a+b*tan(c+d*x^(1/3)))^2,x, algorithm="fricas")

[Out] integral(b^2*x*tan(d*x^(1/3) + c)^2 + 2*a*b*x*tan(d*x^(1/3) + c) + a^2*x, x)

Sympy [F]

$$\int x(a + b \tan(c + d\sqrt[3]{x}))^2 dx = \int x(a + b \tan(c + d\sqrt[3]{x}))^2 dx$$

[In] integrate(x*(a+b*tan(c+d*x**(1/3)))**2,x)

[Out] Integral(x*(a + b*tan(c + d*x**(1/3)))**2, x)

Maxima [B] (verification not implemented)

Both result and optimal contain complex but leaf count of result is larger than twice the leaf count of optimal. 2421 vs. 2(320) = 640.

Time = 0.55 (sec) , antiderivative size = 2421, normalized size of antiderivative = 5.93

$$\int x(a + b \tan(c + d\sqrt[3]{x}))^2 dx = \text{Too large to display}$$

[In] integrate(x*(a+b*tan(c+d*x^(1/3)))^2,x, algorithm="maxima")

```
[Out] 1/2*((d*x^(1/3) + c)^6*a^2 - 6*(d*x^(1/3) + c)^5*a^2*c + 15*(d*x^(1/3) + c)
^4*a^2*c^2 - 20*(d*x^(1/3) + c)^3*a^2*c^3 + 15*(d*x^(1/3) + c)^2*a^2*c^4 -
6*(d*x^(1/3) + c)*a^2*c^5 - 12*a*b*c^5*log(sec(d*x^(1/3) + c)) - 6*(30*I*(d
*x^(1/3) + c)*b^2*c^5 - 5*(2*a*b + I*b^2)*(d*x^(1/3) + c)^6 + 30*(2*a*b + I
*b^2)*(d*x^(1/3) + c)^5*c - 75*(2*a*b + I*b^2)*(d*x^(1/3) + c)^4*c^2 + 100*
(2*a*b + I*b^2)*(d*x^(1/3) + c)^3*c^3 - 75*(2*a*b + I*b^2)*(d*x^(1/3) + c)^
2*c^4 + 60*b^2*c^5 + 2*(96*(d*x^(1/3) + c)^5*a*b - 75*b^2*c^4 - 150*(2*a*b*c
+ b^2)*(d*x^(1/3) + c)^4 + 400*(a*b*c^2 + b^2*c)*(d*x^(1/3) + c)^3 - 150*
(2*a*b*c^3 + 3*b^2*c^2)*(d*x^(1/3) + c)^2 + 150*(a*b*c^4 + 2*b^2*c^3)*(d*x^
(1/3) + c) + (96*(d*x^(1/3) + c)^5*a*b - 75*b^2*c^4 - 150*(2*a*b*c + b^2)*
(d*x^(1/3) + c)^4 + 400*(a*b*c^2 + b^2*c)*(d*x^(1/3) + c)^3 - 150*(2*a*b*c^3
+ 3*b^2*c^2)*(d*x^(1/3) + c)^2 + 150*(a*b*c^4 + 2*b^2*c^3)*(d*x^(1/3) + c)
)*cos(2*d*x^(1/3) + 2*c) - (-96*I*(d*x^(1/3) + c)^5*a*b + 75*I*b^2*c^4 + 15
0*(2*I*a*b*c + I*b^2)*(d*x^(1/3) + c)^4 + 400*(-I*a*b*c^2 - I*b^2*c)*(d*x^(
1/3) + c)^3 + 150*(2*I*a*b*c^3 + 3*I*b^2*c^2)*(d*x^(1/3) + c)^2 + 150*(-I*a
*b*c^4 - 2*I*b^2*c^3)*(d*x^(1/3) + c))*sin(2*d*x^(1/3) + 2*c))*arctan2(sin(
2*d*x^(1/3) + 2*c), cos(2*d*x^(1/3) + 2*c) + 1) - 5*((2*a*b + I*b^2)*(d*x^(
1/3) + c)^6 - 6*(2*b^2 + (2*a*b + I*b^2)*c)*(d*x^(1/3) + c)^5 + 15*(4*b^2*c
+ (2*a*b + I*b^2)*c^2)*(d*x^(1/3) + c)^4 - 20*(6*b^2*c^2 + (2*a*b + I*b^2)
*c^3)*(d*x^(1/3) + c)^3 + 15*(8*b^2*c^3 + (2*a*b + I*b^2)*c^4)*(d*x^(1/3) +
c)^2 + 6*(-I*b^2*c^5 - 10*b^2*c^4)*(d*x^(1/3) + c))*cos(2*d*x^(1/3) + 2*c)
- 30*(16*(d*x^(1/3) + c)^4*a*b + 5*a*b*c^4 + 10*b^2*c^3 - 20*(2*a*b*c + b^
2)*(d*x^(1/3) + c)^3 + 40*(a*b*c^2 + b^2*c)*(d*x^(1/3) + c)^2 - 10*(2*a*b*c
^3 + 3*b^2*c^2)*(d*x^(1/3) + c) + (16*(d*x^(1/3) + c)^4*a*b + 5*a*b*c^4 + 1
0*b^2*c^3 - 20*(2*a*b*c + b^2)*(d*x^(1/3) + c)^3 + 40*(a*b*c^2 + b^2*c)*(d*
x^(1/3) + c)^2 - 10*(2*a*b*c^3 + 3*b^2*c^2)*(d*x^(1/3) + c))*cos(2*d*x^(1/3
) + 2*c) + (16*I*(d*x^(1/3) + c)^4*a*b + 5*I*a*b*c^4 + 10*I*b^2*c^3 + 20*(-
2*I*a*b*c - I*b^2)*(d*x^(1/3) + c)^3 + 40*(I*a*b*c^2 + I*b^2*c)*(d*x^(1/3)
+ c)^2 + 10*(-2*I*a*b*c^3 - 3*I*b^2*c^2)*(d*x^(1/3) + c))*sin(2*d*x^(1/3) +
2*c))*dilog(-e^(2*I*d*x^(1/3) + 2*I*c)) + (-96*I*(d*x^(1/3) + c)^5*a*b + 7
5*I*b^2*c^4 - 150*(-2*I*a*b*c - I*b^2)*(d*x^(1/3) + c)^4 - 400*(I*a*b*c^2 +
I*b^2*c)*(d*x^(1/3) + c)^3 - 150*(-2*I*a*b*c^3 - 3*I*b^2*c^2)*(d*x^(1/3) +
c)^2 - 150*(I*a*b*c^4 + 2*I*b^2*c^3)*(d*x^(1/3) + c) + (-96*I*(d*x^(1/3) +
c)^5*a*b + 75*I*b^2*c^4 - 150*(-2*I*a*b*c - I*b^2)*(d*x^(1/3) + c)^4 - 400
*(I*a*b*c^2 + I*b^2*c)*(d*x^(1/3) + c)^3 - 150*(-2*I*a*b*c^3 - 3*I*b^2*c^2)
*(d*x^(1/3) + c)^2 - 150*(I*a*b*c^4 + 2*I*b^2*c^3)*(d*x^(1/3) + c))*cos(2*d
*x^(1/3) + 2*c) + (96*(d*x^(1/3) + c)^5*a*b - 75*b^2*c^4 - 150*(2*a*b*c + b
^2)*(d*x^(1/3) + c)^4 + 400*(a*b*c^2 + b^2*c)*(d*x^(1/3) + c)^3 - 150*(2*a*
b*c^3 + 3*b^2*c^2)*(d*x^(1/3) + c)^2 + 150*(a*b*c^4 + 2*b^2*c^3)*(d*x^(1/3)
+ c))*sin(2*d*x^(1/3) + 2*c))*log(cos(2*d*x^(1/3) + 2*c)^2 + sin(2*d*x^(1/
3) + 2*c)^2 + 2*cos(2*d*x^(1/3) + 2*c) + 1) - 720*(a*b*cos(2*d*x^(1/3) + 2*
c) + I*a*b*sin(2*d*x^(1/3) + 2*c) + a*b)*polylog(6, -e^(2*I*d*x^(1/3) + 2*I
*c)) - 90*(-16*I*(d*x^(1/3) + c)*a*b + 10*I*a*b*c + 5*I*b^2 + (-16*I*(d*x^(
1/3) + c)*a*b + 10*I*a*b*c + 5*I*b^2)*cos(2*d*x^(1/3) + 2*c) + (16*(d*x^(1/
3) + c)*a*b - 10*a*b*c - 5*b^2)*sin(2*d*x^(1/3) + 2*c))*polylog(5, -e^(2*I
```

$$\begin{aligned}
& d*x^{(1/3)} + 2*I*c)) + 60*(24*(d*x^{(1/3)} + c)^2*a*b + 10*a*b*c^2 + 10*b^2*c \\
& - 15*(2*a*b*c + b^2)*(d*x^{(1/3)} + c) + (24*(d*x^{(1/3)} + c)^2*a*b + 10*a*b*c \\
& ^2 + 10*b^2*c - 15*(2*a*b*c + b^2)*(d*x^{(1/3)} + c))*\cos(2*d*x^{(1/3)} + 2*c) \\
& - (-24*I*(d*x^{(1/3)} + c)^2*a*b - 10*I*a*b*c^2 - 10*I*b^2*c + 15*(2*I*a*b*c \\
& + I*b^2)*(d*x^{(1/3)} + c))*\sin(2*d*x^{(1/3)} + 2*c))*\text{polylog}(4, -e^{(2*I*d*x^{(1/3)} + 2*I*c)}) \\
& - 30*(32*I*(d*x^{(1/3)} + c)^3*a*b - 10*I*a*b*c^3 - 15*I*b^2*c^2 + 30*(-2*I*a*b*c - I*b^2)*(d*x^{(1/3)} + c)^2 + 40*(I*a*b*c^2 + I*b^2*c)*(d \\
& *x^{(1/3)} + c) + (32*I*(d*x^{(1/3)} + c)^3*a*b - 10*I*a*b*c^3 - 15*I*b^2*c^2 + \\
& 30*(-2*I*a*b*c - I*b^2)*(d*x^{(1/3)} + c)^2 + 40*(I*a*b*c^2 + I*b^2*c)*(d*x^{(1/3)} + c)) \\
& *\cos(2*d*x^{(1/3)} + 2*c) - (32*(d*x^{(1/3)} + c)^3*a*b - 10*a*b*c^3 - 15*b^2*c^2 - 30*(2*a*b*c + b^2)*(d*x^{(1/3)} + c)^2 + 40*(a*b*c^2 + b^2*c) \\
& *(d*x^{(1/3)} + c))*\sin(2*d*x^{(1/3)} + 2*c))*\text{polylog}(3, -e^{(2*I*d*x^{(1/3)} + 2*I*c)}) \\
& - 5*((2*I*a*b - b^2)*(d*x^{(1/3)} + c)^6 + 6*(-2*I*b^2 + (-2*I*a*b + b^2)*c)*(d*x^{(1/3)} + c)^5 + 15*(4*I*b^2*c + (2*I*a*b - b^2)*c^2)*(d*x^{(1/3)} + c)^4 + 20*(-6*I*b^2*c^2 + (-2*I*a*b + b^2)*c^3)*(d*x^{(1/3)} + c)^3 + 15*(8*I*b^2*c^3 + (2*I*a*b - b^2)*c^4)*(d*x^{(1/3)} + c)^2 + 6*(b^2*c^5 - 10*I*b^2*c^4)*(d*x^{(1/3)} + c))*\sin(2*d*x^{(1/3)} + 2*c))/(-30*I*\cos(2*d*x^{(1/3)} + 2*c) + 30*\sin(2*d*x^{(1/3)} + 2*c) - 30*I))/d^6
\end{aligned}$$

Giac [F]

$$\int x(a + b \tan(c + d\sqrt[3]{x}))^2 dx = \int (b \tan(dx^{1/3} + c) + a)^2 x dx$$

[In] integrate(x*(a+b*tan(c+d*x^(1/3)))^2,x, algorithm="giac")

[Out] integrate((b*tan(d*x^(1/3) + c) + a)^2*x, x)

Mupad [F(-1)]

Timed out.

$$\int x(a + b \tan(c + d\sqrt[3]{x}))^2 dx = \int x(a + b \tan(c + dx^{1/3}))^2 dx$$

[In] int(x*(a + b*tan(c + d*x^(1/3)))^2,x)

[Out] int(x*(a + b*tan(c + d*x^(1/3)))^2, x)

3.54 $\int (a + b \tan(c + d\sqrt[3]{x}))^2 dx$

Optimal result	348
Rubi [A] (verified)	349
Mathematica [A] (verified)	352
Maple [F]	353
Fricas [A] (verification not implemented)	353
Sympy [F]	353
Maxima [F]	354
Giac [F]	354
Mupad [F(-1)]	354

Optimal result

Integrand size = 16, antiderivative size = 206

$$\int (a + b \tan(c + d\sqrt[3]{x}))^2 dx = -\frac{3ib^2x^{2/3}}{d} + a^2x + 2iabx - b^2x + \frac{6b^2\sqrt[3]{x} \log(1 + e^{2i(c+d\sqrt[3]{x}})})}{d^2}$$

$$- \frac{6abx^{2/3} \log(1 + e^{2i(c+d\sqrt[3]{x}})})}{d}$$

$$- \frac{3ib^2 \text{PolyLog}\left(2, -e^{2i(c+d\sqrt[3]{x}})\right)}{d^3}$$

$$+ \frac{6iab\sqrt[3]{x} \text{PolyLog}\left(2, -e^{2i(c+d\sqrt[3]{x}})\right)}{d^2}$$

$$- \frac{3ab \text{PolyLog}\left(3, -e^{2i(c+d\sqrt[3]{x}})\right)}{d^3} + \frac{3b^2x^{2/3} \tan(c + d\sqrt[3]{x})}{d}$$

```
[Out] -3*I*b^2*x^(2/3)/d+a^2*x+2*I*a*b*x-b^2*x+6*b^2*x^(1/3)*ln(1+exp(2*I*(c+d*x^(1/3))))/d^2-6*a*b*x^(2/3)*ln(1+exp(2*I*(c+d*x^(1/3))))/d-3*I*b^2*polylog(2,-exp(2*I*(c+d*x^(1/3))))/d^3+6*I*a*b*x^(1/3)*polylog(2,-exp(2*I*(c+d*x^(1/3))))/d^2-3*a*b*polylog(3,-exp(2*I*(c+d*x^(1/3))))/d^3+3*b^2*x^(2/3)*tan(c+d*x^(1/3))/d
```

Rubi [A] (verified)

Time = 0.42 (sec) , antiderivative size = 206, normalized size of antiderivative = 1.00, number of steps used = 14, number of rules used = 11, $\frac{\text{number of rules}}{\text{integrand size}} = 0.688$, Rules used = {3824, 3803, 3800, 2221, 2611, 2320, 6724, 3801, 2317, 2438, 30}

$$\int (a + b \tan(c + d\sqrt[3]{x}))^2 dx = a^2x - \frac{3ab \operatorname{PolyLog}\left(3, -e^{2i(c+d\sqrt[3]{x})}\right)}{d^3} + \frac{6iab\sqrt[3]{x} \operatorname{PolyLog}\left(2, -e^{2i(c+d\sqrt[3]{x})}\right)}{d^2} - \frac{6abx^{2/3} \log\left(1 + e^{2i(c+d\sqrt[3]{x})}\right)}{d} + 2iabx - \frac{3ib^2 \operatorname{PolyLog}\left(2, -e^{2i(c+d\sqrt[3]{x})}\right)}{d^3} + \frac{6b^2\sqrt[3]{x} \log\left(1 + e^{2i(c+d\sqrt[3]{x})}\right)}{d^2} + \frac{3b^2x^{2/3} \tan(c + d\sqrt[3]{x})}{d} - \frac{3ib^2x^{2/3}}{d} - b^2x$$

[In] Int[(a + b*Tan[c + d*x^(1/3)])^2,x]

[Out] ((-3*I)*b^2*x^(2/3))/d + a^2*x + (2*I)*a*b*x - b^2*x + (6*b^2*x^(1/3)*Log[1 + E^((2*I)*(c + d*x^(1/3)))])/d^2 - (6*a*b*x^(2/3)*Log[1 + E^((2*I)*(c + d*x^(1/3)))])/d - ((3*I)*b^2*PolyLog[2, -E^((2*I)*(c + d*x^(1/3)))])/d^3 + ((6*I)*a*b*x^(1/3)*PolyLog[2, -E^((2*I)*(c + d*x^(1/3)))])/d^2 - (3*a*b*PolyLog[3, -E^((2*I)*(c + d*x^(1/3)))])/d^3 + (3*b^2*x^(2/3)*Tan[c + d*x^(1/3)])/d

Rule 30

Int[(x_)^(m_), x_Symbol] := Simp[x^(m + 1)/(m + 1), x] /; FreeQ[m, x] && NeQ[m, -1]

Rule 2221

Int[(((F_)^(g_)*((e_) + (f_)*(x_)))^(n_)*((c_) + (d_)*(x_))^(m_))/((a_) + (b_)*((F_)^(g_)*((e_) + (f_)*(x_)))^(n_)), x_Symbol] := Simp[(((c + d*x)^m/(b*f*g*n*Log[F]))*Log[1 + b*((F^(g*(e + f*x)))^n/a)], x] - Dist[d*(m/(b*f*g*n*Log[F])), Int[(c + d*x)^(m - 1)*Log[1 + b*((F^(g*(e + f*x)))^n/a)], x], x] /; FreeQ[{F, a, b, c, d, e, f, g, n}, x] && IGtQ[m, 0]

Rule 2317

Int[Log[(a_) + (b_)*((F_)^(e_)*((c_) + (d_)*(x_)))^(n_)], x_Symbol] := Dist[1/(d*e*n*Log[F]), Subst[Int[Log[a + b*x]/x, x], x, (F^(e*(c + d*x)))]

)ⁿ, x] /; FreeQ[{F, a, b, c, d, e, n}, x] && GtQ[a, 0]

Rule 2320

Int[u_, x_Symbol] := With[{v = FunctionOfExponential[u, x]}, Dist[v/D[v, x], Subst[Int[FunctionOfExponentialFunction[u, x]/x, x], x, v], x] /; FunctionOfExponentialQ[u, x] && !MatchQ[u, (w_)*((a_)*(v_)^(n_))^(m_)] /; FreeQ[{a, m, n}, x] && IntegerQ[m*n] && !MatchQ[u, E^((c_)*((a_) + (b_)*x))*(F_)[v_] /; FreeQ[{a, b, c}, x] && InverseFunctionQ[F[x]]]

Rule 2438

Int[Log[(c_)*((d_) + (e_)*(x_)^(n_))]/(x_), x_Symbol] := Simp[-PolyLog[2, (-c)*e*x^n/n, x] /; FreeQ[{c, d, e, n}, x] && EqQ[c*d, 1]

Rule 2611

Int[Log[1 + (e_)*((F_)^(c_)*((a_) + (b_)*(x_)))^(n_)]*((f_) + (g_)*(x_)^(m_)), x_Symbol] := Simp[(-f + g*x)^m*(PolyLog[2, (-e)*(F^(c*(a + b*x)))^n/(b*c*n*Log[F])], x] + Dist[g*(m/(b*c*n*Log[F])), Int[(f + g*x)^(m - 1)*PolyLog[2, (-e)*(F^(c*(a + b*x)))^n], x], x] /; FreeQ[{F, a, b, c, e, f, g, n}, x] && GtQ[m, 0]

Rule 3800

Int[((c_) + (d_)*(x_)^(m_))*tan[(e_) + (f_)*(x_)], x_Symbol] := Simp[I*((c + d*x)^(m + 1)/(d*(m + 1))), x] - Dist[2*I, Int[(c + d*x)^m*(E^(2*I*(e + f*x)))/(1 + E^(2*I*(e + f*x))), x], x] /; FreeQ[{c, d, e, f}, x] && IGtQ[m, 0]

Rule 3801

Int[((c_) + (d_)*(x_)^(m_))*((b_)*tan[(e_) + (f_)*(x_)])^(n_), x_Symbol] := Simp[b*(c + d*x)^m*((b*Tan[e + f*x])^(n - 1)/(f*(n - 1))), x] + (-Dist[b*d*(m/(f*(n - 1))), Int[(c + d*x)^(m - 1)*(b*Tan[e + f*x])^(n - 1), x], x] - Dist[b^2, Int[(c + d*x)^m*(b*Tan[e + f*x])^(n - 2), x], x]) /; FreeQ[{b, c, d, e, f}, x] && GtQ[n, 1] && GtQ[m, 0]

Rule 3803

Int[((c_) + (d_)*(x_)^(m_))*((a_) + (b_)*tan[(e_) + (f_)*(x_)])^(n_), x_Symbol] := Int[ExpandIntegrand[(c + d*x)^m, (a + b*Tan[e + f*x])^n, x], x] /; FreeQ[{a, b, c, d, e, f, m}, x] && IGtQ[m, 0] && IGtQ[n, 0]

Rule 3824

```
Int[((a_.) + (b_.)*Tan[(c_.) + (d_.)*(x_)^(n_)])^(p_.), x_Symbol] := Dist[1/n, Subst[Int[x^(1/n - 1)*(a + b*Tan[c + d*x])^p, x], x, x^n], x] /; FreeQ[{a, b, c, d, p}, x] && IGtQ[1/n, 0] && IntegerQ[p]
```

Rule 6724

```
Int[PolyLog[n_, (c_.)*((a_.) + (b_.)*(x_))^(p_.)]/((d_.) + (e_.)*(x_)), x_Symbol] := Simp[PolyLog[n + 1, c*(a + b*x)^p]/(e*p), x] /; FreeQ[{a, b, c, d, e, n, p}, x] && EqQ[b*d, a*e]
```

Rubi steps

$$\begin{aligned}
\text{integral} &= 3\text{Subst}\left(\int x^2(a + b \tan(c + dx))^2 dx, x, \sqrt[3]{x}\right) \\
&= 3\text{Subst}\left(\int (a^2x^2 + 2abx^2 \tan(c + dx) + b^2x^2 \tan^2(c + dx)) dx, x, \sqrt[3]{x}\right) \\
&= a^2x + (6ab)\text{Subst}\left(\int x^2 \tan(c + dx) dx, x, \sqrt[3]{x}\right) + (3b^2)\text{Subst}\left(\int x^2 \tan^2(c + dx) dx, x, \sqrt[3]{x}\right) \\
&= a^2x + 2iabx + \frac{3b^2x^{2/3} \tan(c + d\sqrt[3]{x})}{d} - (12iab)\text{Subst}\left(\int \frac{e^{2i(c+dx)}x^2}{1 + e^{2i(c+dx)}} dx, x, \sqrt[3]{x}\right) \\
&\quad - (3b^2)\text{Subst}\left(\int x^2 dx, x, \sqrt[3]{x}\right) - \frac{(6b^2)\text{Subst}\left(\int x \tan(c + dx) dx, x, \sqrt[3]{x}\right)}{d} \\
&= -\frac{3ib^2x^{2/3}}{d} + a^2x + 2iabx - b^2x - \frac{6abx^{2/3} \log(1 + e^{2i(c+d\sqrt[3]{x}})})}{d} + \frac{3b^2x^{2/3} \tan(c + d\sqrt[3]{x})}{d} \\
&\quad + \frac{(12iab)\text{Subst}\left(\int x \log(1 + e^{2i(c+dx)}) dx, x, \sqrt[3]{x}\right)}{d} + \frac{(12ib^2)\text{Subst}\left(\int \frac{e^{2i(c+dx)}x}{1 + e^{2i(c+dx)}} dx, x, \sqrt[3]{x}\right)}{d} \\
&= -\frac{3ib^2x^{2/3}}{d} + a^2x + 2iabx - b^2x + \frac{6b^2\sqrt[3]{x} \log(1 + e^{2i(c+d\sqrt[3]{x}})})}{d^2} \\
&\quad - \frac{6abx^{2/3} \log(1 + e^{2i(c+d\sqrt[3]{x}})})}{d} + \frac{6iab\sqrt[3]{x} \text{PolyLog}(2, -e^{2i(c+d\sqrt[3]{x}})})}{d^2} \\
&\quad + \frac{3b^2x^{2/3} \tan(c + d\sqrt[3]{x})}{d} - \frac{(6iab)\text{Subst}\left(\int \text{PolyLog}(2, -e^{2i(c+dx)}) dx, x, \sqrt[3]{x}\right)}{d^2} \\
&\quad - \frac{(6b^2)\text{Subst}\left(\int \log(1 + e^{2i(c+dx)}) dx, x, \sqrt[3]{x}\right)}{d^2}
\end{aligned}$$

$$\begin{aligned}
&= -\frac{3ib^2x^{2/3}}{d} + a^2x + 2iabx - b^2x + \frac{6b^2\sqrt[3]{x}\log\left(1 + e^{2i(c+d\sqrt[3]{x})}\right)}{d^2} \\
&\quad - \frac{6abx^{2/3}\log\left(1 + e^{2i(c+d\sqrt[3]{x})}\right)}{d} + \frac{6iab\sqrt[3]{x}\operatorname{PolyLog}\left(2, -e^{2i(c+d\sqrt[3]{x})}\right)}{d^2} \\
&\quad + \frac{3b^2x^{2/3}\tan\left(c + d\sqrt[3]{x}\right)}{d} - \frac{(3ab)\operatorname{Subst}\left(\int \frac{\operatorname{PolyLog}(2,-x)}{x} dx, x, e^{2i(c+d\sqrt[3]{x})}\right)}{d^3} \\
&\quad + \frac{(3ib^2)\operatorname{Subst}\left(\int \frac{\log(1+x)}{x} dx, x, e^{2i(c+d\sqrt[3]{x})}\right)}{d^3} \\
&= -\frac{3ib^2x^{2/3}}{d} + a^2x + 2iabx - b^2x + \frac{6b^2\sqrt[3]{x}\log\left(1 + e^{2i(c+d\sqrt[3]{x})}\right)}{d^2} \\
&\quad - \frac{6abx^{2/3}\log\left(1 + e^{2i(c+d\sqrt[3]{x})}\right)}{d} - \frac{3ib^2\operatorname{PolyLog}\left(2, -e^{2i(c+d\sqrt[3]{x})}\right)}{d^3} \\
&\quad + \frac{6iab\sqrt[3]{x}\operatorname{PolyLog}\left(2, -e^{2i(c+d\sqrt[3]{x})}\right)}{d^2} \\
&\quad - \frac{3ab\operatorname{PolyLog}\left(3, -e^{2i(c+d\sqrt[3]{x})}\right)}{d^3} + \frac{3b^2x^{2/3}\tan\left(c + d\sqrt[3]{x}\right)}{d}
\end{aligned}$$

Mathematica [A] (verified)

Time = 1.60 (sec) , antiderivative size = 185, normalized size of antiderivative = 0.90

$$\begin{aligned}
&\int (a + b \tan(c + d\sqrt[3]{x}))^2 dx \\
&= \frac{b\left(\frac{6ibd^2x^{2/3} - 4iad^3x}{1 + e^{2ic}} + 6d(b - ad\sqrt[3]{x})\sqrt[3]{x}\log\left(1 + e^{-2i(c+d\sqrt[3]{x})}\right) + 3i(b - 2ad\sqrt[3]{x})\operatorname{PolyLog}\left(2, -e^{-2i(c+d\sqrt[3]{x})}\right)\right)}{d^3} \\
&\quad + \frac{3b^2x^{2/3}\sec(c)\sec(c + d\sqrt[3]{x})\sin(d\sqrt[3]{x})}{d} + x(a^2 - b^2 + 2ab\tan(c))
\end{aligned}$$

[In] Integrate[(a + b*Tan[c + d*x^(1/3)])^2,x]

[Out] (b*(((6*I)*b*d^2*x^(2/3) - (4*I)*a*d^3*x)/(1 + E^((2*I)*c)) + 6*d*(b - a*d*x^(1/3))*x^(1/3)*Log[1 + E^((-2*I)*(c + d*x^(1/3)))] + (3*I)*(b - 2*a*d*x^(1/3))*PolyLog[2, -E^((-2*I)*(c + d*x^(1/3)))] - 3*a*PolyLog[3, -E^((-2*I)*(c + d*x^(1/3)))]))/d^3 + (3*b^2*x^(2/3)*Sec[c]*Sec[c + d*x^(1/3)]*Sin[d*x^(1/3)])/d + x*(a^2 - b^2 + 2*a*b*Tan[c])

Maple [F]

$$\int \left(a + b \tan \left(c + d x^{\frac{1}{3}} \right) \right)^2 dx$$

[In] int((a+b*tan(c+d*x^(1/3)))^2,x)

[Out] int((a+b*tan(c+d*x^(1/3)))^2,x)

Fricas [A] (verification not implemented)

none

Time = 0.27 (sec) , antiderivative size = 320, normalized size of antiderivative = 1.55

$$\int (a + b \tan(c + d\sqrt[3]{x}))^2 dx$$

$$= \frac{6b^2d^2x^{\frac{2}{3}} \tan\left(dx^{\frac{1}{3}} + c\right) + 2(a^2 - b^2)d^3x - 3ab \operatorname{polylog}\left(3, \frac{\tan\left(dx^{\frac{1}{3}} + c\right)^2 + 2i \tan\left(dx^{\frac{1}{3}} + c\right) - 1}{\tan\left(dx^{\frac{1}{3}} + c\right)^2 + 1}\right) - 3ab \operatorname{polylog}\left(3, \frac{\tan\left(dx^{\frac{1}{3}} + c\right)^2 + 2i \tan\left(dx^{\frac{1}{3}} + c\right) - 1}{\tan\left(dx^{\frac{1}{3}} + c\right)^2 + 1}\right)}{d^3}$$

[In] integrate((a+b*tan(c+d*x^(1/3)))^2,x, algorithm="fricas")

[Out] 1/2*(6*b^2*d^2*x^(2/3)*tan(d*x^(1/3) + c) + 2*(a^2 - b^2)*d^3*x - 3*a*b*pol
ylog(3, (tan(d*x^(1/3) + c)^2 + 2*I*tan(d*x^(1/3) + c) - 1)/(tan(d*x^(1/3)
+ c)^2 + 1)) - 3*a*b*polylog(3, (tan(d*x^(1/3) + c)^2 - 2*I*tan(d*x^(1/3) +
c) - 1)/(tan(d*x^(1/3) + c)^2 + 1)) - 3*(2*I*a*b*d*x^(1/3) - I*b^2)*dilog(
2*(I*tan(d*x^(1/3) + c) - 1)/(tan(d*x^(1/3) + c)^2 + 1) + 1) - 3*(-2*I*a*b*
d*x^(1/3) + I*b^2)*dilog(2*(-I*tan(d*x^(1/3) + c) - 1)/(tan(d*x^(1/3) + c)^
2 + 1) + 1) - 6*(a*b*d^2*x^(2/3) - b^2*d*x^(1/3))*log(-2*(I*tan(d*x^(1/3) +
c) - 1)/(tan(d*x^(1/3) + c)^2 + 1)) - 6*(a*b*d^2*x^(2/3) - b^2*d*x^(1/3))*
log(-2*(-I*tan(d*x^(1/3) + c) - 1)/(tan(d*x^(1/3) + c)^2 + 1)))/d^3

Sympy [F]

$$\int (a + b \tan(c + d\sqrt[3]{x}))^2 dx = \int (a + b \tan(c + d\sqrt[3]{x}))^2 dx$$

[In] integrate((a+b*tan(c+d*x**(1/3)))**2,x)

[Out] Integral((a + b*tan(c + d*x**(1/3)))**2, x)

Maxima [F]

$$\int (a + b \tan(c + d\sqrt[3]{x}))^2 dx = \int (b \tan(dx^{\frac{1}{3}} + c) + a)^2 dx$$

[In] integrate((a+b*tan(c+d*x^(1/3)))^2,x, algorithm="maxima")

[Out] a^2*x + (6*b^2*x^(2/3)*sin(2*d*x^(1/3) + 2*c) - (b^2*d*cos(2*d*x^(1/3) + 2*c)^2 + b^2*d*sin(2*d*x^(1/3) + 2*c)^2 + 2*b^2*d*cos(2*d*x^(1/3) + 2*c) + b^2*d)*x - (d*cos(2*d*x^(1/3) + 2*c)^2 + d*sin(2*d*x^(1/3) + 2*c)^2 + 2*d*cos(2*d*x^(1/3) + 2*c) + d)*integrate(-4*(a*b*d*x*sin(2*d*x^(1/3) + 2*c) - b^2*x^(2/3)*sin(2*d*x^(1/3) + 2*c))/((d*cos(2*d*x^(1/3) + 2*c)^2 + d*sin(2*d*x^(1/3) + 2*c)^2 + 2*d*cos(2*d*x^(1/3) + 2*c) + d)*x), x)/(d*cos(2*d*x^(1/3) + 2*c)^2 + d*sin(2*d*x^(1/3) + 2*c)^2 + 2*d*cos(2*d*x^(1/3) + 2*c) + d)

Giac [F]

$$\int (a + b \tan(c + d\sqrt[3]{x}))^2 dx = \int (b \tan(dx^{\frac{1}{3}} + c) + a)^2 dx$$

[In] integrate((a+b*tan(c+d*x^(1/3)))^2,x, algorithm="giac")

[Out] integrate((b*tan(d*x^(1/3) + c) + a)^2, x)

Mupad [F(-1)]

Timed out.

$$\int (a + b \tan(c + d\sqrt[3]{x}))^2 dx = \int (a + b \tan(c + dx^{1/3}))^2 dx$$

[In] int((a + b*tan(c + d*x^(1/3)))^2,x)

[Out] int((a + b*tan(c + d*x^(1/3)))^2, x)

$$3.55 \quad \int \frac{\left(a + b \tan\left(c + d \sqrt[3]{x}\right)\right)^2}{x} dx$$

Optimal result	355
Rubi [N/A]	355
Mathematica [N/A]	356
Maple [N/A] (verified)	356
Fricas [N/A]	356
Sympy [N/A]	357
Maxima [N/A]	357
Giac [N/A]	357
Mupad [N/A]	358

Optimal result

Integrand size = 20, antiderivative size = 20

$$\int \frac{\left(a + b \tan\left(c + d \sqrt[3]{x}\right)\right)^2}{x} dx = \text{Int}\left(\frac{\left(a + b \tan\left(c + d \sqrt[3]{x}\right)\right)^2}{x}, x\right)$$

[Out] Unintegrable((a+b*tan(c+d*x^(1/3)))^2/x,x)

Rubi [N/A]

Not integrable

Time = 0.02 (sec) , antiderivative size = 20, normalized size of antiderivative = 1.00, number of steps used = 0, number of rules used = 0, $\frac{\text{number of rules}}{\text{integrand size}} = 0.000$, Rules used = {}

$$\int \frac{\left(a + b \tan\left(c + d \sqrt[3]{x}\right)\right)^2}{x} dx = \int \frac{\left(a + b \tan\left(c + d \sqrt[3]{x}\right)\right)^2}{x} dx$$

[In] Int[(a + b*Tan[c + d*x^(1/3)])^2/x,x]

[Out] Defer[Int][(a + b*Tan[c + d*x^(1/3)])^2/x, x]

Rubi steps

$$\text{integral} = \int \frac{\left(a + b \tan\left(c + d \sqrt[3]{x}\right)\right)^2}{x} dx$$

Mathematica [N/A]

Not integrable

Time = 123.77 (sec) , antiderivative size = 22, normalized size of antiderivative = 1.10

$$\int \frac{(a + b \tan(c + d\sqrt[3]{x}))^2}{x} dx = \int \frac{(a + b \tan(c + d\sqrt[3]{x}))^2}{x} dx$$

[In] Integrate[(a + b*Tan[c + d*x^(1/3)])^2/x,x]

[Out] Integrate[(a + b*Tan[c + d*x^(1/3)])^2/x, x]

Maple [N/A] (verified)

Not integrable

Time = 0.94 (sec) , antiderivative size = 18, normalized size of antiderivative = 0.90

$$\int \frac{(a + b \tan(c + dx^{\frac{1}{3}}))^2}{x} dx$$

[In] int((a+b*tan(c+d*x^(1/3)))^2/x,x)

[Out] int((a+b*tan(c+d*x^(1/3)))^2/x,x)

Fricas [N/A]

Not integrable

Time = 0.25 (sec) , antiderivative size = 36, normalized size of antiderivative = 1.80

$$\int \frac{(a + b \tan(c + d\sqrt[3]{x}))^2}{x} dx = \int \frac{(b \tan(dx^{\frac{1}{3}} + c) + a)^2}{x} dx$$

[In] integrate((a+b*tan(c+d*x^(1/3)))^2/x,x, algorithm="fricas")

[Out] integral((b^2*tan(d*x^(1/3) + c)^2 + 2*a*b*tan(d*x^(1/3) + c) + a^2)/x, x)

Sympy [N/A]

Not integrable

Time = 8.78 (sec) , antiderivative size = 17, normalized size of antiderivative = 0.85

$$\int \frac{(a + b \tan(c + d\sqrt[3]{x}))^2}{x} dx = \int \frac{(a + b \tan(c + d\sqrt[3]{x}))^2}{x} dx$$

[In] integrate((a+b*tan(c+d*x**(1/3)))**2/x,x)

[Out] Integral((a + b*tan(c + d*x**(1/3)))**2/x, x)

Maxima [N/A]

Not integrable

Time = 0.72 (sec) , antiderivative size = 298, normalized size of antiderivative = 14.90

$$\int \frac{(a + b \tan(c + d\sqrt[3]{x}))^2}{x} dx = \int \frac{(b \tan(dx^{\frac{1}{3}} + c) + a)^2}{x} dx$$

[In] integrate((a+b*tan(c+d*x^(1/3)))^2/x,x, algorithm="maxima")

[Out] (6*b^2*x^(2/3)*sin(2*d*x^(1/3) + 2*c) + (d*cos(2*d*x^(1/3) + 2*c)^2 + d*sin(2*d*x^(1/3) + 2*c)^2 + 2*d*cos(2*d*x^(1/3) + 2*c) + d)*x*integrate(2*(2*a*b*d*x*sin(2*d*x^(1/3) + 2*c) + b^2*x^(2/3)*sin(2*d*x^(1/3) + 2*c))/((d*cos(2*d*x^(1/3) + 2*c)^2 + d*sin(2*d*x^(1/3) + 2*c)^2 + 2*d*cos(2*d*x^(1/3) + 2*c) + d)*x^2), x) + ((a^2 - b^2)*d*cos(2*d*x^(1/3) + 2*c)^2 + (a^2 - b^2)*d*sin(2*d*x^(1/3) + 2*c)^2 + 2*(a^2 - b^2)*d*cos(2*d*x^(1/3) + 2*c) + (a^2 - b^2)*d)*x*log(x))/((d*cos(2*d*x^(1/3) + 2*c)^2 + d*sin(2*d*x^(1/3) + 2*c)^2 + 2*d*cos(2*d*x^(1/3) + 2*c) + d)*x)

Giac [N/A]

Not integrable

Time = 0.88 (sec) , antiderivative size = 20, normalized size of antiderivative = 1.00

$$\int \frac{(a + b \tan(c + d\sqrt[3]{x}))^2}{x} dx = \int \frac{(b \tan(dx^{\frac{1}{3}} + c) + a)^2}{x} dx$$

[In] integrate((a+b*tan(c+d*x^(1/3)))^2/x,x, algorithm="giac")

[Out] integrate((b*tan(d*x^(1/3) + c) + a)^2/x, x)

Mupad [N/A]

Not integrable

Time = 4.54 (sec) , antiderivative size = 20, normalized size of antiderivative = 1.00

$$\int \frac{(a + b \tan(c + d\sqrt[3]{x}))^2}{x} dx = \int \frac{(a + b \tan(c + dx^{1/3}))^2}{x} dx$$

```
[In] int((a + b*tan(c + d*x^(1/3)))^2/x,x)
```

```
[Out] int((a + b*tan(c + d*x^(1/3)))^2/x, x)
```

$$3.56 \quad \int \frac{\left(a+b \tan \left(c+d \sqrt[3]{x}\right)\right)^2}{x^2} dx$$

Optimal result	359
Rubi [N/A]	359
Mathematica [N/A]	360
Maple [N/A] (verified)	360
Fricas [N/A]	360
Sympy [N/A]	361
Maxima [N/A]	361
Giac [N/A]	361
Mupad [N/A]	362

Optimal result

Integrand size = 20, antiderivative size = 20

$$\int \frac{\left(a+b \tan \left(c+d \sqrt[3]{x}\right)\right)^2}{x^2} dx = \text{Int}\left(\frac{\left(a+b \tan \left(c+d \sqrt[3]{x}\right)\right)^2}{x^2}, x\right)$$

[Out] Unintegrable((a+b*tan(c+d*x^(1/3)))^2/x^2,x)

Rubi [N/A]

Not integrable

Time = 0.02 (sec) , antiderivative size = 20, normalized size of antiderivative = 1.00, number of steps used = 0, number of rules used = 0, $\frac{\text{number of rules}}{\text{integrand size}} = 0.000$, Rules used = {}

$$\int \frac{\left(a+b \tan \left(c+d \sqrt[3]{x}\right)\right)^2}{x^2} dx = \int \frac{\left(a+b \tan \left(c+d \sqrt[3]{x}\right)\right)^2}{x^2} dx$$

[In] Int[(a + b*Tan[c + d*x^(1/3)])^2/x^2,x]

[Out] Defer[Int] [(a + b*Tan[c + d*x^(1/3)])^2/x^2, x]

Rubi steps

$$\text{integral} = \int \frac{\left(a+b \tan \left(c+d \sqrt[3]{x}\right)\right)^2}{x^2} dx$$

Mathematica [N/A]

Not integrable

Time = 19.05 (sec) , antiderivative size = 22, normalized size of antiderivative = 1.10

$$\int \frac{(a + b \tan(c + d\sqrt[3]{x}))^2}{x^2} dx = \int \frac{(a + b \tan(c + d\sqrt[3]{x}))^2}{x^2} dx$$

[In] Integrate[(a + b*Tan[c + d*x^(1/3)])^2/x^2,x]

[Out] Integrate[(a + b*Tan[c + d*x^(1/3)])^2/x^2, x]

Maple [N/A] (verified)

Not integrable

Time = 1.21 (sec) , antiderivative size = 18, normalized size of antiderivative = 0.90

$$\int \frac{(a + b \tan(c + dx^{\frac{1}{3}}))^2}{x^2} dx$$

[In] int((a+b*tan(c+d*x^(1/3)))^2/x^2,x)

[Out] int((a+b*tan(c+d*x^(1/3)))^2/x^2,x)

Fricas [N/A]

Not integrable

Time = 0.23 (sec) , antiderivative size = 36, normalized size of antiderivative = 1.80

$$\int \frac{(a + b \tan(c + d\sqrt[3]{x}))^2}{x^2} dx = \int \frac{(b \tan(dx^{\frac{1}{3}} + c) + a)^2}{x^2} dx$$

[In] integrate((a+b*tan(c+d*x^(1/3)))^2/x^2,x, algorithm="fricas")

[Out] integral((b^2*tan(d*x^(1/3) + c)^2 + 2*a*b*tan(d*x^(1/3) + c) + a^2)/x^2, x)

Sympy [N/A]

Not integrable

Time = 2.60 (sec) , antiderivative size = 19, normalized size of antiderivative = 0.95

$$\int \frac{(a + b \tan(c + d\sqrt[3]{x}))^2}{x^2} dx = \int \frac{(a + b \tan(c + d\sqrt[3]{x}))^2}{x^2} dx$$

[In] integrate((a+b*tan(c+d*x**(1/3)))**2/x**2,x)

[Out] Integral((a + b*tan(c + d*x**(1/3)))**2/x**2, x)

Maxima [N/A]

Not integrable

Time = 1.02 (sec) , antiderivative size = 299, normalized size of antiderivative = 14.95

$$\int \frac{(a + b \tan(c + d\sqrt[3]{x}))^2}{x^2} dx = \int \frac{(b \tan(dx^{\frac{1}{3}} + c) + a)^2}{x^2} dx$$

[In] integrate((a+b*tan(c+d*x^(1/3)))^2/x^2,x, algorithm="maxima")

[Out] ((d*cos(2*d*x^(1/3) + 2*c)^2 + d*sin(2*d*x^(1/3) + 2*c)^2 + 2*d*cos(2*d*x^(1/3) + 2*c) + d)*x^2*integrate(4*(a*b*d*x*sin(2*d*x^(1/3) + 2*c) + 2*b^2*x^(2/3)*sin(2*d*x^(1/3) + 2*c))/((d*cos(2*d*x^(1/3) + 2*c)^2 + d*sin(2*d*x^(1/3) + 2*c)^2 + 2*d*cos(2*d*x^(1/3) + 2*c) + d)*x^3, x) + 6*b^2*x^(2/3)*sin(2*d*x^(1/3) + 2*c) - ((a^2 - b^2)*d*cos(2*d*x^(1/3) + 2*c)^2 + (a^2 - b^2)*d*sin(2*d*x^(1/3) + 2*c)^2 + 2*(a^2 - b^2)*d*cos(2*d*x^(1/3) + 2*c) + (a^2 - b^2)*d)*x)/((d*cos(2*d*x^(1/3) + 2*c)^2 + d*sin(2*d*x^(1/3) + 2*c)^2 + 2*d*cos(2*d*x^(1/3) + 2*c) + d)*x^2)

Giac [N/A]

Not integrable

Time = 0.87 (sec) , antiderivative size = 20, normalized size of antiderivative = 1.00

$$\int \frac{(a + b \tan(c + d\sqrt[3]{x}))^2}{x^2} dx = \int \frac{(b \tan(dx^{\frac{1}{3}} + c) + a)^2}{x^2} dx$$

[In] integrate((a+b*tan(c+d*x^(1/3)))^2/x^2,x, algorithm="giac")

[Out] integrate((b*tan(d*x^(1/3) + c) + a)^2/x^2, x)

Mupad [N/A]

Not integrable

Time = 4.28 (sec) , antiderivative size = 20, normalized size of antiderivative = 1.00

$$\int \frac{(a + b \tan(c + d\sqrt[3]{x}))^2}{x^2} dx = \int \frac{(a + b \tan(c + dx^{1/3}))^2}{x^2} dx$$

```
[In] int((a + b*tan(c + d*x^(1/3)))^2/x^2,x)
```

```
[Out] int((a + b*tan(c + d*x^(1/3)))^2/x^2, x)
```

$$3.57 \quad \int \frac{x^2}{a+b \tan(c+d \sqrt[3]{x})} dx$$

Optimal result	364
Rubi [A] (verified)	365
Mathematica [A] (verified)	373
Maple [F]	374
Fricas [F]	374
Sympy [F(-1)]	374
Maxima [B] (verification not implemented)	375
Giac [F]	376
Mupad [F(-1)]	376

Optimal result

Integrand size = 20, antiderivative size = 511

$$\begin{aligned}
 \int \frac{x^2}{a + b \tan(c + d\sqrt[3]{x})} dx &= \frac{x^3}{3(a + ib)} + \frac{3bx^{8/3} \log\left(1 + \frac{(a^2 + b^2)e^{2i(c + d\sqrt[3]{x})}}{(a + ib)^2}\right)}{(a^2 + b^2)d} \\
 &- \frac{12ibx^{7/3} \operatorname{PolyLog}\left(2, -\frac{(a^2 + b^2)e^{2i(c + d\sqrt[3]{x})}}{(a + ib)^2}\right)}{(a^2 + b^2)d^2} \\
 &+ \frac{42bx^2 \operatorname{PolyLog}\left(3, -\frac{(a^2 + b^2)e^{2i(c + d\sqrt[3]{x})}}{(a + ib)^2}\right)}{(a^2 + b^2)d^3} \\
 &+ \frac{126ibx^{5/3} \operatorname{PolyLog}\left(4, -\frac{(a^2 + b^2)e^{2i(c + d\sqrt[3]{x})}}{(a + ib)^2}\right)}{(a^2 + b^2)d^4} \\
 &- \frac{315bx^{4/3} \operatorname{PolyLog}\left(5, -\frac{(a^2 + b^2)e^{2i(c + d\sqrt[3]{x})}}{(a + ib)^2}\right)}{(a^2 + b^2)d^5} \\
 &- \frac{630ibx \operatorname{PolyLog}\left(6, -\frac{(a^2 + b^2)e^{2i(c + d\sqrt[3]{x})}}{(a + ib)^2}\right)}{(a^2 + b^2)d^6} \\
 &+ \frac{945bx^{2/3} \operatorname{PolyLog}\left(7, -\frac{(a^2 + b^2)e^{2i(c + d\sqrt[3]{x})}}{(a + ib)^2}\right)}{(a^2 + b^2)d^7} \\
 &+ \frac{945ib\sqrt[3]{x} \operatorname{PolyLog}\left(8, -\frac{(a^2 + b^2)e^{2i(c + d\sqrt[3]{x})}}{(a + ib)^2}\right)}{(a^2 + b^2)d^8} \\
 &- \frac{945b \operatorname{PolyLog}\left(9, -\frac{(a^2 + b^2)e^{2i(c + d\sqrt[3]{x})}}{(a + ib)^2}\right)}{2(a^2 + b^2)d^9}
 \end{aligned}$$

```

[Out] 1/3*x^3/(a+I*b)+3*b*x^(8/3)*ln(1+(a^2+b^2)*exp(2*I*(c+d*x^(1/3)))/(a+I*b)^2
)/(a^2+b^2)/d-12*I*b*x^(7/3)*polylog(2,-(a^2+b^2)*exp(2*I*(c+d*x^(1/3)))/(a
+I*b)^2)/(a^2+b^2)/d^2+42*b*x^2*polylog(3,-(a^2+b^2)*exp(2*I*(c+d*x^(1/3))
)/(a+I*b)^2)/(a^2+b^2)/d^3+126*I*b*x^(5/3)*polylog(4,-(a^2+b^2)*exp(2*I*(c+d
*x^(1/3)))/(a+I*b)^2)/(a^2+b^2)/d^4-315*b*x^(4/3)*polylog(5,-(a^2+b^2)*exp(
2*I*(c+d*x^(1/3)))/(a+I*b)^2)/(a^2+b^2)/d^5-630*I*b*x*polylog(6,-(a^2+b^2)*
exp(2*I*(c+d*x^(1/3)))/(a+I*b)^2)/(a^2+b^2)/d^6+945*b*x^(2/3)*polylog(7,-(a
^2+b^2)*exp(2*I*(c+d*x^(1/3)))/(a+I*b)^2)/(a^2+b^2)/d^7+945*I*b*x^(1/3)*pol
ylog(8,-(a^2+b^2)*exp(2*I*(c+d*x^(1/3)))/(a+I*b)^2)/(a^2+b^2)/d^8-945/2*b*p
olylog(9,-(a^2+b^2)*exp(2*I*(c+d*x^(1/3)))/(a+I*b)^2)/(a^2+b^2)/d^9

```

Rubi [A] (verified)

Time = 0.75 (sec) , antiderivative size = 511, normalized size of antiderivative = 1.00, number of steps used = 12, number of rules used = 7, $\frac{\text{number of rules}}{\text{integrand size}} = 0.350$, Rules used = {3832, 3813, 2221, 2611, 6744, 2320, 6724}

$$\int \frac{x^2}{a + b \tan(c + d\sqrt[3]{x})} dx = -\frac{945b \operatorname{PolyLog}\left(9, -\frac{(a^2+b^2)e^{2i(c+d\sqrt[3]{x})}}{(a+ib)^2}\right)}{2d^9(a^2+b^2)} + \frac{945ib\sqrt[3]{x} \operatorname{PolyLog}\left(8, -\frac{(a^2+b^2)e^{2i(c+d\sqrt[3]{x})}}{(a+ib)^2}\right)}{d^8(a^2+b^2)} + \frac{945bx^{2/3} \operatorname{PolyLog}\left(7, -\frac{(a^2+b^2)e^{2i(c+d\sqrt[3]{x})}}{(a+ib)^2}\right)}{d^7(a^2+b^2)} - \frac{630ibx \operatorname{PolyLog}\left(6, -\frac{(a^2+b^2)e^{2i(c+d\sqrt[3]{x})}}{(a+ib)^2}\right)}{d^6(a^2+b^2)} - \frac{315bx^{4/3} \operatorname{PolyLog}\left(5, -\frac{(a^2+b^2)e^{2i(c+d\sqrt[3]{x})}}{(a+ib)^2}\right)}{d^5(a^2+b^2)} + \frac{126ibx^{5/3} \operatorname{PolyLog}\left(4, -\frac{(a^2+b^2)e^{2i(c+d\sqrt[3]{x})}}{(a+ib)^2}\right)}{d^4(a^2+b^2)} + \frac{42bx^2 \operatorname{PolyLog}\left(3, -\frac{(a^2+b^2)e^{2i(c+d\sqrt[3]{x})}}{(a+ib)^2}\right)}{d^3(a^2+b^2)} - \frac{12ibx^{7/3} \operatorname{PolyLog}\left(2, -\frac{(a^2+b^2)e^{2i(c+d\sqrt[3]{x})}}{(a+ib)^2}\right)}{d^2(a^2+b^2)} + \frac{3bx^{8/3} \log\left(1 + \frac{(a^2+b^2)e^{2i(c+d\sqrt[3]{x})}}{(a+ib)^2}\right)}{d(a^2+b^2)} + \frac{x^3}{3(a+ib)}$$

[In] Int[x^2/(a + b*Tan[c + d*x^(1/3)]),x]

[Out] x^3/(3*(a + I*b)) + (3*b*x^(8/3)*Log[1 + ((a^2 + b^2)*E^((2*I)*(c + d*x^(1/3))))/(a + I*b)^2])/((a^2 + b^2)*d) - ((12*I)*b*x^(7/3)*PolyLog[2, -((a^2 + b^2)*E^((2*I)*(c + d*x^(1/3))))/(a + I*b)^2])/((a^2 + b^2)*d^2) + (42*b*x^2*PolyLog[3, -((a^2 + b^2)*E^((2*I)*(c + d*x^(1/3))))/(a + I*b)^2])/((a^2 + b^2)*d^3) + ((126*I)*b*x^(5/3)*PolyLog[4, -((a^2 + b^2)*E^((2*I)*(c + d*x^(1/3))))/(a + I*b)^2])/((a^2 + b^2)*d^4) - (315*b*x^(4/3)*PolyLog[5,

$$\begin{aligned}
& -(((a^2 + b^2)*E^{((2*I)*(c + d*x^{(1/3))})}/(a + I*b)^2)]/((a^2 + b^2)*d^5) \\
& - ((630*I)*b*x*PolyLog[6, -(((a^2 + b^2)*E^{((2*I)*(c + d*x^{(1/3))})}/(a + I*b)^2)]/((a^2 + b^2)*d^6) + (945*b*x^{(2/3)}*PolyLog[7, -(((a^2 + b^2)*E^{((2*I)*(c + d*x^{(1/3))})}/(a + I*b)^2)]/((a^2 + b^2)*d^7) + ((945*I)*b*x^{(1/3)}*PolyLog[8, -(((a^2 + b^2)*E^{((2*I)*(c + d*x^{(1/3))})}/(a + I*b)^2)]/((a^2 + b^2)*d^8) - (945*b*PolyLog[9, -(((a^2 + b^2)*E^{((2*I)*(c + d*x^{(1/3))})}/(a + I*b)^2)]/((2*(a^2 + b^2)*d^9)
\end{aligned}$$
Rule 2221

```

Int[(((F_)^((g_)*(e_) + (f_)*(x_)))^(n_))*((c_) + (d_)*(x_))^(m_)]/
((a_) + (b_)*((F_)^((g_)*(e_) + (f_)*(x_)))^(n_)), x_Symbol] := Simp
[((c + d*x)^m/(b*f*g*n*Log[F]))*Log[1 + b*((F^(g*(e + f*x)))^n/a)], x] - Di
st[d*(m/(b*f*g*n*Log[F])), Int[(c + d*x)^(m - 1)*Log[1 + b*((F^(g*(e + f*x)
))^n/a)], x], x] /; FreeQ[{F, a, b, c, d, e, f, g, n}, x] && IGtQ[m, 0]

```

Rule 2320

```

Int[u_, x_Symbol] := With[{v = FunctionOfExponential[u, x]}, Dist[v/D[v, x]
, Subst[Int[FunctionOfExponentialFunction[u, x]/x, x], x, v], x]] /; Functi
onOfExponentialQ[u, x] && !MatchQ[u, (w_)*((a_)*(v_)^(n_))^(m_)] /; FreeQ[
{a, m, n}, x] && IntegerQ[m*n] && !MatchQ[u, E^((c_)*((a_) + (b_)*x))*
(F_)[v_] /; FreeQ[{a, b, c}, x] && InverseFunctionQ[F[x]]]

```

Rule 2611

```

Int[Log[1 + (e_)*((F_)^((c_)*((a_) + (b_)*(x_)))^(n_))]*((f_) + (g_)
*(x_))^(m_), x_Symbol] := Simp[(-f + g*x)^m*(PolyLog[2, (-e)*(F^(c*(a +
b*x)))^n]/(b*c*n*Log[F])), x] + Dist[g*(m/(b*c*n*Log[F])), Int[(f + g*x)^(m
- 1)*PolyLog[2, (-e)*(F^(c*(a + b*x)))^n], x], x] /; FreeQ[{F, a, b, c, e,
f, g, n}, x] && GtQ[m, 0]

```

Rule 3813

```

Int[(((c_) + (d_)*(x_))^(m_))/((a_) + (b_)*tan[(e_) + (f_)*(x_)]), x_Sy
mbol] := Simp[(c + d*x)^(m + 1)/(d*(m + 1)*(a + I*b)), x] + Dist[2*I*b, Int
[(c + d*x)^m*(E^Simp[2*I*(e + f*x), x]/((a + I*b)^2 + (a^2 + b^2)*E^Simp[2*
I*(e + f*x), x])), x], x] /; FreeQ[{a, b, c, d, e, f}, x] && NeQ[a^2 + b^2,
0] && IGtQ[m, 0]

```

Rule 3832

```

Int[(x_)^(m_)*((a_) + (b_)*Tan[(c_) + (d_)*(x_)]^(n_))^(p_), x_Symbol
] := Dist[1/n, Subst[Int[x^(Simplify[(m + 1)/n] - 1)*(a + b*Tan[c + d*x])^p
, x], x, x^n], x] /; FreeQ[{a, b, c, d, m, n, p}, x] && IGtQ[Simplify[(m +
1)/n], 0] && IntegerQ[p]

```

Rule 6724

Int[PolyLog[n_, (c_.)*(a_.) + (b_.)*(x_.)]^p]/((d_.) + (e_.)*(x_.)), x_Symbol] := Simp[PolyLog[n + 1, c*(a + b*x)^p]/(e*p), x] /; FreeQ[{a, b, c, d, e, n, p}, x] && EqQ[b*d, a*e]

Rule 6744

Int[((e_.) + (f_.)*(x_.))^m_*PolyLog[n_, (d_.)*(F_)^((c_.)*(a_.) + (b_.)*(x_.))]^p], x_Symbol] := Simp[(e + f*x)^m*(PolyLog[n + 1, d*(F^(c*(a + b*x)))^p]/(b*c*p*Log[F])), x] - Dist[f*(m/(b*c*p*Log[F])), Int[(e + f*x)^(m - 1)*PolyLog[n + 1, d*(F^(c*(a + b*x)))^p], x], x] /; FreeQ[{F, a, b, c, d, e, f, n, p}, x] && GtQ[m, 0]

Rubi steps

$$\begin{aligned}
 \text{integral} &= 3\text{Subst}\left(\int \frac{x^8}{a + b \tan(c + dx)} dx, x, \sqrt[3]{x}\right) \\
 &= \frac{x^3}{3(a + ib)} + (6ib)\text{Subst}\left(\int \frac{e^{2i(c+dx)}x^8}{(a + ib)^2 + (a^2 + b^2)e^{2i(c+dx)}} dx, x, \sqrt[3]{x}\right) \\
 &= \frac{x^3}{3(a + ib)} + \frac{3bx^{8/3} \log\left(1 + \frac{(a^2+b^2)e^{2i(c+d\sqrt[3]{x}})}{(a+ib)^2}\right)}{(a^2 + b^2)d} \\
 &\quad - \frac{(24b)\text{Subst}\left(\int x^7 \log\left(1 + \frac{(a^2+b^2)e^{2i(c+dx)}}{(a+ib)^2}\right) dx, x, \sqrt[3]{x}\right)}{(a^2 + b^2)d} \\
 &= \frac{x^3}{3(a + ib)} + \frac{3bx^{8/3} \log\left(1 + \frac{(a^2+b^2)e^{2i(c+d\sqrt[3]{x}})}{(a+ib)^2}\right)}{(a^2 + b^2)d} \\
 &\quad - \frac{12ibx^{7/3} \text{PolyLog}\left(2, -\frac{(a^2+b^2)e^{2i(c+d\sqrt[3]{x}})}{(a+ib)^2}\right)}{(a^2 + b^2)d^2} \\
 &\quad + \frac{(84ib)\text{Subst}\left(\int x^6 \text{PolyLog}\left(2, -\frac{(a^2+b^2)e^{2i(c+dx)}}{(a+ib)^2}\right) dx, x, \sqrt[3]{x}\right)}{(a^2 + b^2)d^2}
 \end{aligned}$$

$$\begin{aligned}
&= \frac{x^3}{3(a+ib)} + \frac{3bx^{8/3} \log\left(1 + \frac{(a^2+b^2)e^{2i(c+d\sqrt[3]{x}})}{(a+ib)^2}\right)}{(a^2+b^2)d} \\
&\quad - \frac{12ibx^{7/3} \text{PolyLog}\left(2, -\frac{(a^2+b^2)e^{2i(c+d\sqrt[3]{x}})}{(a+ib)^2}\right)}{(a^2+b^2)d^2} \\
&\quad + \frac{42bx^2 \text{PolyLog}\left(3, -\frac{(a^2+b^2)e^{2i(c+d\sqrt[3]{x}})}{(a+ib)^2}\right)}{(a^2+b^2)d^3} \\
&\quad - \frac{(252b) \text{Subst}\left(\int x^5 \text{PolyLog}\left(3, -\frac{(a^2+b^2)e^{2i(c+dx)}}{(a+ib)^2}\right) dx, x, \sqrt[3]{x}\right)}{(a^2+b^2)d^3} \\
&= \frac{x^3}{3(a+ib)} + \frac{3bx^{8/3} \log\left(1 + \frac{(a^2+b^2)e^{2i(c+d\sqrt[3]{x}})}{(a+ib)^2}\right)}{(a^2+b^2)d} \\
&\quad - \frac{12ibx^{7/3} \text{PolyLog}\left(2, -\frac{(a^2+b^2)e^{2i(c+d\sqrt[3]{x}})}{(a+ib)^2}\right)}{(a^2+b^2)d^2} \\
&\quad + \frac{42bx^2 \text{PolyLog}\left(3, -\frac{(a^2+b^2)e^{2i(c+d\sqrt[3]{x}})}{(a+ib)^2}\right)}{(a^2+b^2)d^3} \\
&\quad + \frac{126ibx^{5/3} \text{PolyLog}\left(4, -\frac{(a^2+b^2)e^{2i(c+d\sqrt[3]{x}})}{(a+ib)^2}\right)}{(a^2+b^2)d^4} \\
&\quad - \frac{(630ib) \text{Subst}\left(\int x^4 \text{PolyLog}\left(4, -\frac{(a^2+b^2)e^{2i(c+dx)}}{(a+ib)^2}\right) dx, x, \sqrt[3]{x}\right)}{(a^2+b^2)d^4}
\end{aligned}$$

$$\begin{aligned}
&= \frac{x^3}{3(a+ib)} + \frac{3bx^{8/3} \log\left(1 + \frac{(a^2+b^2)e^{2i(c+d\sqrt[3]{x}})}{(a+ib)^2}\right)}{(a^2+b^2)d} \\
&\quad - \frac{12ibx^{7/3} \text{PolyLog}\left(2, -\frac{(a^2+b^2)e^{2i(c+d\sqrt[3]{x}})}{(a+ib)^2}\right)}{(a^2+b^2)d^2} \\
&\quad + \frac{42bx^2 \text{PolyLog}\left(3, -\frac{(a^2+b^2)e^{2i(c+d\sqrt[3]{x}})}{(a+ib)^2}\right)}{(a^2+b^2)d^3} \\
&\quad + \frac{126ibx^{5/3} \text{PolyLog}\left(4, -\frac{(a^2+b^2)e^{2i(c+d\sqrt[3]{x}})}{(a+ib)^2}\right)}{(a^2+b^2)d^4} \\
&\quad - \frac{315bx^{4/3} \text{PolyLog}\left(5, -\frac{(a^2+b^2)e^{2i(c+d\sqrt[3]{x}})}{(a+ib)^2}\right)}{(a^2+b^2)d^5} \\
&\quad + \frac{(1260b) \text{Subst}\left(\int x^3 \text{PolyLog}\left(5, -\frac{(a^2+b^2)e^{2i(c+dx)}}{(a+ib)^2}\right) dx, x, \sqrt[3]{x}\right)}{(a^2+b^2)d^5} \\
&= \frac{x^3}{3(a+ib)} + \frac{3bx^{8/3} \log\left(1 + \frac{(a^2+b^2)e^{2i(c+d\sqrt[3]{x}})}{(a+ib)^2}\right)}{(a^2+b^2)d} \\
&\quad - \frac{12ibx^{7/3} \text{PolyLog}\left(2, -\frac{(a^2+b^2)e^{2i(c+d\sqrt[3]{x}})}{(a+ib)^2}\right)}{(a^2+b^2)d^2} \\
&\quad + \frac{42bx^2 \text{PolyLog}\left(3, -\frac{(a^2+b^2)e^{2i(c+d\sqrt[3]{x}})}{(a+ib)^2}\right)}{(a^2+b^2)d^3} \\
&\quad + \frac{126ibx^{5/3} \text{PolyLog}\left(4, -\frac{(a^2+b^2)e^{2i(c+d\sqrt[3]{x}})}{(a+ib)^2}\right)}{(a^2+b^2)d^4} \\
&\quad - \frac{315bx^{4/3} \text{PolyLog}\left(5, -\frac{(a^2+b^2)e^{2i(c+d\sqrt[3]{x}})}{(a+ib)^2}\right)}{(a^2+b^2)d^5} \\
&\quad - \frac{630ibx \text{PolyLog}\left(6, -\frac{(a^2+b^2)e^{2i(c+d\sqrt[3]{x}})}{(a+ib)^2}\right)}{(a^2+b^2)d^6} \\
&\quad + \frac{(1890ib) \text{Subst}\left(\int x^2 \text{PolyLog}\left(6, -\frac{(a^2+b^2)e^{2i(c+dx)}}{(a+ib)^2}\right) dx, x, \sqrt[3]{x}\right)}{(a^2+b^2)d^6}
\end{aligned}$$

$$\begin{aligned}
&= \frac{x^3}{3(a+ib)} + \frac{3bx^{8/3} \log\left(1 + \frac{(a^2+b^2)e^{2i(c+d\sqrt[3]{x}})}{(a+ib)^2}\right)}{(a^2+b^2)d} \\
&\quad - \frac{12ibx^{7/3} \text{PolyLog}\left(2, -\frac{(a^2+b^2)e^{2i(c+d\sqrt[3]{x}})}{(a+ib)^2}\right)}{(a^2+b^2)d^2} \\
&\quad + \frac{42bx^2 \text{PolyLog}\left(3, -\frac{(a^2+b^2)e^{2i(c+d\sqrt[3]{x}})}{(a+ib)^2}\right)}{(a^2+b^2)d^3} \\
&\quad + \frac{126ibx^{5/3} \text{PolyLog}\left(4, -\frac{(a^2+b^2)e^{2i(c+d\sqrt[3]{x}})}{(a+ib)^2}\right)}{(a^2+b^2)d^4} \\
&\quad - \frac{315bx^{4/3} \text{PolyLog}\left(5, -\frac{(a^2+b^2)e^{2i(c+d\sqrt[3]{x}})}{(a+ib)^2}\right)}{(a^2+b^2)d^5} \\
&\quad - \frac{630ibx \text{PolyLog}\left(6, -\frac{(a^2+b^2)e^{2i(c+d\sqrt[3]{x}})}{(a+ib)^2}\right)}{(a^2+b^2)d^6} \\
&\quad + \frac{945bx^{2/3} \text{PolyLog}\left(7, -\frac{(a^2+b^2)e^{2i(c+d\sqrt[3]{x}})}{(a+ib)^2}\right)}{(a^2+b^2)d^7} \\
&\quad - \frac{(1890b) \text{Subst}\left(\int x \text{PolyLog}\left(7, -\frac{(a^2+b^2)e^{2i(c+dx)}}{(a+ib)^2}\right) dx, x, \sqrt[3]{x}\right)}{(a^2+b^2)d^7}
\end{aligned}$$

$$\begin{aligned}
&= \frac{x^3}{3(a+ib)} + \frac{3bx^{8/3} \log\left(1 + \frac{(a^2+b^2)e^{2i(c+d\sqrt[3]{x}})}{(a+ib)^2}\right)}{(a^2+b^2)d} \\
&\quad - \frac{12ibx^{7/3} \text{PolyLog}\left(2, -\frac{(a^2+b^2)e^{2i(c+d\sqrt[3]{x}})}{(a+ib)^2}\right)}{(a^2+b^2)d^2} \\
&\quad + \frac{42bx^2 \text{PolyLog}\left(3, -\frac{(a^2+b^2)e^{2i(c+d\sqrt[3]{x}})}{(a+ib)^2}\right)}{(a^2+b^2)d^3} \\
&\quad + \frac{126ibx^{5/3} \text{PolyLog}\left(4, -\frac{(a^2+b^2)e^{2i(c+d\sqrt[3]{x}})}{(a+ib)^2}\right)}{(a^2+b^2)d^4} \\
&\quad - \frac{315bx^{4/3} \text{PolyLog}\left(5, -\frac{(a^2+b^2)e^{2i(c+d\sqrt[3]{x}})}{(a+ib)^2}\right)}{(a^2+b^2)d^5} \\
&\quad - \frac{630ibx \text{PolyLog}\left(6, -\frac{(a^2+b^2)e^{2i(c+d\sqrt[3]{x}})}{(a+ib)^2}\right)}{(a^2+b^2)d^6} \\
&\quad + \frac{945bx^{2/3} \text{PolyLog}\left(7, -\frac{(a^2+b^2)e^{2i(c+d\sqrt[3]{x}})}{(a+ib)^2}\right)}{(a^2+b^2)d^7} \\
&\quad + \frac{945ib\sqrt[3]{x} \text{PolyLog}\left(8, -\frac{(a^2+b^2)e^{2i(c+d\sqrt[3]{x}})}{(a+ib)^2}\right)}{(a^2+b^2)d^8} \\
&\quad - \frac{(945ib) \text{Subst}\left(\int \text{PolyLog}\left(8, -\frac{(a^2+b^2)e^{2i(c+dx)}}{(a+ib)^2}\right) dx, x, \sqrt[3]{x}\right)}{(a^2+b^2)d^8}
\end{aligned}$$

$$\begin{aligned}
&= \frac{x^3}{3(a+ib)} + \frac{3bx^{8/3} \log\left(1 + \frac{(a^2+b^2)e^{2i(c+d\sqrt[3]{x})}}{(a+ib)^2}\right)}{(a^2+b^2)d} \\
&\quad - \frac{12ibx^{7/3} \text{PolyLog}\left(2, -\frac{(a^2+b^2)e^{2i(c+d\sqrt[3]{x})}}{(a+ib)^2}\right)}{(a^2+b^2)d^2} \\
&\quad + \frac{42bx^2 \text{PolyLog}\left(3, -\frac{(a^2+b^2)e^{2i(c+d\sqrt[3]{x})}}{(a+ib)^2}\right)}{(a^2+b^2)d^3} \\
&\quad + \frac{126ibx^{5/3} \text{PolyLog}\left(4, -\frac{(a^2+b^2)e^{2i(c+d\sqrt[3]{x})}}{(a+ib)^2}\right)}{(a^2+b^2)d^4} \\
&\quad - \frac{315bx^{4/3} \text{PolyLog}\left(5, -\frac{(a^2+b^2)e^{2i(c+d\sqrt[3]{x})}}{(a+ib)^2}\right)}{(a^2+b^2)d^5} \\
&\quad - \frac{630ibx \text{PolyLog}\left(6, -\frac{(a^2+b^2)e^{2i(c+d\sqrt[3]{x})}}{(a+ib)^2}\right)}{(a^2+b^2)d^6} \\
&\quad + \frac{945bx^{2/3} \text{PolyLog}\left(7, -\frac{(a^2+b^2)e^{2i(c+d\sqrt[3]{x})}}{(a+ib)^2}\right)}{(a^2+b^2)d^7} \\
&\quad + \frac{945ib\sqrt[3]{x} \text{PolyLog}\left(8, -\frac{(a^2+b^2)e^{2i(c+d\sqrt[3]{x})}}{(a+ib)^2}\right)}{(a^2+b^2)d^8} \\
&\quad - \frac{(945b)\text{Subst}\left(\int \frac{\text{PolyLog}\left(8, -\frac{(a^2+b^2)x}{(a+ib)^2}\right)}{x} dx, x, e^{2i(c+d\sqrt[3]{x})}\right)}{2(a^2+b^2)d^9}
\end{aligned}$$

$$\begin{aligned}
&= \frac{x^3}{3(a+ib)} + \frac{3bx^{8/3} \log\left(1 + \frac{(a^2+b^2)e^{2i(c+d\sqrt[3]{x}})}{(a+ib)^2}\right)}{(a^2+b^2)d} \\
&\quad - \frac{12ibx^{7/3} \text{PolyLog}\left(2, -\frac{(a^2+b^2)e^{2i(c+d\sqrt[3]{x}})}{(a+ib)^2}\right)}{(a^2+b^2)d^2} \\
&\quad + \frac{42bx^2 \text{PolyLog}\left(3, -\frac{(a^2+b^2)e^{2i(c+d\sqrt[3]{x}})}{(a+ib)^2}\right)}{(a^2+b^2)d^3} \\
&\quad + \frac{126ibx^{5/3} \text{PolyLog}\left(4, -\frac{(a^2+b^2)e^{2i(c+d\sqrt[3]{x}})}{(a+ib)^2}\right)}{(a^2+b^2)d^4} \\
&\quad - \frac{315bx^{4/3} \text{PolyLog}\left(5, -\frac{(a^2+b^2)e^{2i(c+d\sqrt[3]{x}})}{(a+ib)^2}\right)}{(a^2+b^2)d^5} \\
&\quad - \frac{630ibx \text{PolyLog}\left(6, -\frac{(a^2+b^2)e^{2i(c+d\sqrt[3]{x}})}{(a+ib)^2}\right)}{(a^2+b^2)d^6} \\
&\quad + \frac{945bx^{2/3} \text{PolyLog}\left(7, -\frac{(a^2+b^2)e^{2i(c+d\sqrt[3]{x}})}{(a+ib)^2}\right)}{(a^2+b^2)d^7} \\
&\quad + \frac{945ib\sqrt[3]{x} \text{PolyLog}\left(8, -\frac{(a^2+b^2)e^{2i(c+d\sqrt[3]{x}})}{(a+ib)^2}\right)}{(a^2+b^2)d^8} \\
&\quad - \frac{945b \text{PolyLog}\left(9, -\frac{(a^2+b^2)e^{2i(c+d\sqrt[3]{x}})}{(a+ib)^2}\right)}{2(a^2+b^2)d^9}
\end{aligned}$$

Mathematica [A] (verified)

Time = 1.66 (sec) , antiderivative size = 451, normalized size of antiderivative = 0.88

$$\int \frac{x^2}{a + b \tan(c + d\sqrt[3]{x})} dx$$

$$= \frac{2ad^9x^3 + 2ibd^9x^3 + 18bd^8x^{8/3} \log\left(1 + \frac{(a+ib)e^{-2i(c+d\sqrt[3]{x}})}{a-ib}\right) + 72ibd^7x^{7/3} \text{PolyLog}\left(2, \frac{(-a-ib)e^{-2i(c+d\sqrt[3]{x}})}{a-ib}\right)}{2(a^2+b^2)d^9} + \dots$$

[In] Integrate[x^2/(a + b*Tan[c + d*x^(1/3)]), x]

[Out] (2*a*d^9*x^3 + (2*I)*b*d^9*x^3 + 18*b*d^8*x^(8/3)*Log[1 + (a + I*b)/((a - I*b)*E^((2*I)*(c + d*x^(1/3)))] + (72*I)*b*d^7*x^(7/3)*PolyLog[2, (-a - I*b

)/((a - I*b)*E^((2*I)*(c + d*x^(1/3))))] + 252*b*d^6*x^2*PolyLog[3, (-a - I*b)/((a - I*b)*E^((2*I)*(c + d*x^(1/3))))] - (756*I)*b*d^5*x^(5/3)*PolyLog[4, (-a - I*b)/((a - I*b)*E^((2*I)*(c + d*x^(1/3))))] - 1890*b*d^4*x^(4/3)*PolyLog[5, (-a - I*b)/((a - I*b)*E^((2*I)*(c + d*x^(1/3))))] + (3780*I)*b*d^3*x*PolyLog[6, (-a - I*b)/((a - I*b)*E^((2*I)*(c + d*x^(1/3))))] + 5670*b*d^2*x^(2/3)*PolyLog[7, (-a - I*b)/((a - I*b)*E^((2*I)*(c + d*x^(1/3))))] - (5670*I)*b*d*x^(1/3)*PolyLog[8, (-a - I*b)/((a - I*b)*E^((2*I)*(c + d*x^(1/3))))] - 2835*b*PolyLog[9, (-a - I*b)/((a - I*b)*E^((2*I)*(c + d*x^(1/3))))] / (6*(a^2 + b^2)*d^9)

Maple [F]

$$\int \frac{x^2}{a + b \tan\left(c + d x^{\frac{1}{3}}\right)} dx$$

[In] int(x^2/(a+b*tan(c+d*x^(1/3))),x)

[Out] int(x^2/(a+b*tan(c+d*x^(1/3))),x)

Fricas [F]

$$\int \frac{x^2}{a + b \tan\left(c + d \sqrt[3]{x}\right)} dx = \int \frac{x^2}{b \tan\left(dx^{\frac{1}{3}} + c\right) + a} dx$$

[In] integrate(x^2/(a+b*tan(c+d*x^(1/3))),x, algorithm="fricas")

[Out] integral(x^2/(b*tan(d*x^(1/3) + c) + a), x)

Sympy [F(-1)]

Timed out.

$$\int \frac{x^2}{a + b \tan\left(c + d \sqrt[3]{x}\right)} dx = \text{Timed out}$$

[In] integrate(x**2/(a+b*tan(c+d*x**(1/3))),x)

[Out] Timed out

Maxima [B] (verification not implemented)

Both result and optimal contain complex but leaf count of result is larger than twice the leaf count of optimal. 1315 vs. $2(430) = 860$.

Time = 0.68 (sec) , antiderivative size = 1315, normalized size of antiderivative = 2.57

$$\int \frac{x^2}{a + b \tan(c + d\sqrt[3]{x})} dx = \text{Too large to display}$$

[In] integrate(x^2/(a+b*tan(c+d*x^(1/3))),x, algorithm="maxima")

[Out] $\frac{1}{210} \cdot (315 \cdot (2 \cdot (d \cdot x^{1/3}) + c) \cdot a / (a^2 + b^2) + 2 \cdot b \cdot \log(b \cdot \tan(d \cdot x^{1/3}) + c) + a) / (a^2 + b^2) - b \cdot \log(\tan(d \cdot x^{1/3}) + c)^2 + 1) / (a^2 + b^2) \cdot c^8 + 2 \cdot (35 \cdot (d \cdot x^{1/3}) + c)^9 \cdot (a - I \cdot b) - 315 \cdot (d \cdot x^{1/3}) + c)^8 \cdot (a - I \cdot b) \cdot c + 1260 \cdot (d \cdot x^{1/3}) + c)^7 \cdot (a - I \cdot b) \cdot c^2 - 2940 \cdot (d \cdot x^{1/3}) + c)^6 \cdot (a - I \cdot b) \cdot c^3 + 4410 \cdot (d \cdot x^{1/3}) + c)^5 \cdot (a - I \cdot b) \cdot c^4 - 4410 \cdot (d \cdot x^{1/3}) + c)^4 \cdot (a - I \cdot b) \cdot c^5 + 2940 \cdot (d \cdot x^{1/3}) + c)^3 \cdot (a - I \cdot b) \cdot c^6 - 1260 \cdot (d \cdot x^{1/3}) + c)^2 \cdot (a - I \cdot b) \cdot c^7 - 12 \cdot (420 \cdot I \cdot (d \cdot x^{1/3}) + c)^8 \cdot b - 1920 \cdot I \cdot (d \cdot x^{1/3}) + c)^7 \cdot b \cdot c + 3920 \cdot I \cdot (d \cdot x^{1/3}) + c)^6 \cdot b \cdot c^2 - 4704 \cdot I \cdot (d \cdot x^{1/3}) + c)^5 \cdot b \cdot c^3 + 3675 \cdot I \cdot (d \cdot x^{1/3}) + c)^4 \cdot b \cdot c^4 - 1960 \cdot I \cdot (d \cdot x^{1/3}) + c)^3 \cdot b \cdot c^5 + 735 \cdot I \cdot (d \cdot x^{1/3}) + c)^2 \cdot b \cdot c^6 - 210 \cdot I \cdot (d \cdot x^{1/3}) + c) \cdot b \cdot c^7) \cdot \arctan2((2 \cdot a \cdot b \cdot \cos(2 \cdot d \cdot x^{1/3}) + 2 \cdot c) - (a^2 - b^2) \cdot \sin(2 \cdot d \cdot x^{1/3}) + 2 \cdot c)) / (a^2 + b^2), (2 \cdot a \cdot b \cdot \sin(2 \cdot d \cdot x^{1/3}) + 2 \cdot c) + a^2 + b^2 + (a^2 - b^2) \cdot \cos(2 \cdot d \cdot x^{1/3}) + 2 \cdot c)) / (a^2 + b^2)) - 1260 \cdot (16 \cdot I \cdot (d \cdot x^{1/3}) + c)^7 \cdot b - 64 \cdot I \cdot (d \cdot x^{1/3}) + c)^6 \cdot b \cdot c + 112 \cdot I \cdot (d \cdot x^{1/3}) + c)^5 \cdot b \cdot c^2 - 112 \cdot I \cdot (d \cdot x^{1/3}) + c)^4 \cdot b \cdot c^3 + 70 \cdot I \cdot (d \cdot x^{1/3}) + c)^3 \cdot b \cdot c^4 - 28 \cdot I \cdot (d \cdot x^{1/3}) + c)^2 \cdot b \cdot c^5 + 7 \cdot I \cdot (d \cdot x^{1/3}) + c) \cdot b \cdot c^6 - I \cdot b \cdot c^7) \cdot \text{dilog}((I \cdot a + b) \cdot e^{(2 \cdot I \cdot d \cdot x^{1/3}) + 2 \cdot I \cdot c)} / (-I \cdot a + b)) + 6 \cdot (420 \cdot (d \cdot x^{1/3}) + c)^8 \cdot b - 1920 \cdot (d \cdot x^{1/3}) + c)^7 \cdot b \cdot c + 3920 \cdot (d \cdot x^{1/3}) + c)^6 \cdot b \cdot c^2 - 4704 \cdot (d \cdot x^{1/3}) + c)^5 \cdot b \cdot c^3 + 3675 \cdot (d \cdot x^{1/3}) + c)^4 \cdot b \cdot c^4 - 1960 \cdot (d \cdot x^{1/3}) + c)^3 \cdot b \cdot c^5 + 735 \cdot (d \cdot x^{1/3}) + c)^2 \cdot b \cdot c^6 - 210 \cdot (d \cdot x^{1/3}) + c) \cdot b \cdot c^7) \cdot \log(((a^2 + b^2) \cdot \cos(2 \cdot d \cdot x^{1/3}) + 2 \cdot c)^2 + 4 \cdot a \cdot b \cdot \sin(2 \cdot d \cdot x^{1/3}) + 2 \cdot c) + (a^2 + b^2) \cdot \sin(2 \cdot d \cdot x^{1/3}) + 2 \cdot c)^2 + a^2 + b^2 + 2 \cdot (a^2 - b^2) \cdot \cos(2 \cdot d \cdot x^{1/3}) + 2 \cdot c)) / (a^2 + b^2)) - 793800 \cdot b \cdot \text{polylog}(9, (I \cdot a + b) \cdot e^{(2 \cdot I \cdot d \cdot x^{1/3}) + 2 \cdot I \cdot c)} / (-I \cdot a + b)) - 226800 \cdot (-7 \cdot I \cdot (d \cdot x^{1/3}) + c) \cdot b + 4 \cdot I \cdot b \cdot c) \cdot \text{polylog}(8, (I \cdot a + b) \cdot e^{(2 \cdot I \cdot d \cdot x^{1/3}) + 2 \cdot I \cdot c)} / (-I \cdot a + b)) + 75600 \cdot (21 \cdot (d \cdot x^{1/3}) + c)^2 \cdot b - 24 \cdot (d \cdot x^{1/3}) + c) \cdot b \cdot c + 7 \cdot b \cdot c^2) \cdot \text{polylog}(7, (I \cdot a + b) \cdot e^{(2 \cdot I \cdot d \cdot x^{1/3}) + 2 \cdot I \cdot c)} / (-I \cdot a + b)) - 30240 \cdot (35 \cdot I \cdot (d \cdot x^{1/3}) + c)^3 \cdot b - 60 \cdot I \cdot (d \cdot x^{1/3}) + c)^2 \cdot b \cdot c + 35 \cdot I \cdot (d \cdot x^{1/3}) + c) \cdot b \cdot c^2 - 7 \cdot I \cdot b \cdot c^3) \cdot \text{polylog}(6, (I \cdot a + b) \cdot e^{(2 \cdot I \cdot d \cdot x^{1/3}) + 2 \cdot I \cdot c)} / (-I \cdot a + b)) - 1890 \cdot (280 \cdot (d \cdot x^{1/3}) + c)^4 \cdot b - 640 \cdot (d \cdot x^{1/3}) + c)^3 \cdot b \cdot c + 560 \cdot (d \cdot x^{1/3}) + c)^2 \cdot b \cdot c^2 - 224 \cdot (d \cdot x^{1/3}) + c) \cdot b \cdot c^3 + 35 \cdot b \cdot c^4) \cdot \text{polylog}(5, (I \cdot a + b) \cdot e^{(2 \cdot I \cdot d \cdot x^{1/3}) + 2 \cdot I \cdot c)} / (-I \cdot a + b)) - 1260 \cdot (-168 \cdot I \cdot (d \cdot x^{1/3}) + c)^5 \cdot b + 480 \cdot I \cdot (d \cdot x^{1/3}) + c)^4 \cdot b \cdot c - 560 \cdot I \cdot (d \cdot x^{1/3}) + c)^3 \cdot b \cdot c^2 + 336 \cdot I \cdot (d \cdot x^{1/3}) + c)^2 \cdot b \cdot c^3 - 105 \cdot I \cdot (d \cdot x^{1/3}) + c) \cdot b \cdot c^4 + 14 \cdot I \cdot b \cdot c^5) \cdot \text{polylog}(4, (I \cdot a + b) \cdot e^{(2 \cdot I \cdot d \cdot x^{1/3}) + 2 \cdot I \cdot c)} / (-I \cdot a + b)) + 630 \cdot (112 \cdot (d \cdot x^{1/3}) + c)^6 \cdot b - 384 \cdot (d \cdot x^{1/3}) + c)^5 \cdot b \cdot c + 560 \cdot (d \cdot x^{1/3}) +$

$c)^4 b c^2 - 448(d x^{1/3} + c)^3 b c^3 + 210(d x^{1/3} + c)^2 b c^4 - 56(d x^{1/3} + c) b c^5 + 7 b c^6) \text{polylog}(3, (I a + b) e^{(2 I d x^{1/3} + 2 I c)/(-I a + b)}) / (a^2 + b^2) / d^9$

Giac [F]

$$\int \frac{x^2}{a + b \tan(c + d \sqrt[3]{x})} dx = \int \frac{x^2}{b \tan(dx^{1/3} + c) + a} dx$$

[In] integrate(x^2/(a+b*tan(c+d*x^(1/3))),x, algorithm="giac")

[Out] integrate(x^2/(b*tan(d*x^(1/3) + c) + a), x)

Mupad [F(-1)]

Timed out.

$$\int \frac{x^2}{a + b \tan(c + d \sqrt[3]{x})} dx = \int \frac{x^2}{a + b \tan(c + d x^{1/3})} dx$$

[In] int(x^2/(a + b*tan(c + d*x^(1/3))),x)

[Out] int(x^2/(a + b*tan(c + d*x^(1/3))), x)

$$3.58 \quad \int \frac{x}{a+b \tan\left(c+d \sqrt[3]{x}\right)} dx$$

Optimal result	377
Rubi [A] (verified)	378
Mathematica [A] (verified)	382
Maple [F]	383
Fricas [F]	383
Sympy [F]	383
Maxima [B] (verification not implemented)	384
Giac [F]	384
Mupad [F(-1)]	385

Optimal result

Integrand size = 18, antiderivative size = 352

$$\int \frac{x}{a+b \tan\left(c+d \sqrt[3]{x}\right)} dx = \frac{x^2}{2(a+ib)} + \frac{3bx^{5/3} \log\left(1 + \frac{(a^2+b^2)e^{2i(c+d \sqrt[3]{x})}}{(a+ib)^2}\right)}{(a^2+b^2)d}$$

$$- \frac{15ibx^{4/3} \text{PolyLog}\left(2, -\frac{(a^2+b^2)e^{2i(c+d \sqrt[3]{x})}}{(a+ib)^2}\right)}{2(a^2+b^2)d^2}$$

$$+ \frac{15bx \text{PolyLog}\left(3, -\frac{(a^2+b^2)e^{2i(c+d \sqrt[3]{x})}}{(a+ib)^2}\right)}{(a^2+b^2)d^3}$$

$$+ \frac{45ibx^{2/3} \text{PolyLog}\left(4, -\frac{(a^2+b^2)e^{2i(c+d \sqrt[3]{x})}}{(a+ib)^2}\right)}{2(a^2+b^2)d^4}$$

$$- \frac{45b \sqrt[3]{x} \text{PolyLog}\left(5, -\frac{(a^2+b^2)e^{2i(c+d \sqrt[3]{x})}}{(a+ib)^2}\right)}{2(a^2+b^2)d^5}$$

$$- \frac{45ib \text{PolyLog}\left(6, -\frac{(a^2+b^2)e^{2i(c+d \sqrt[3]{x})}}{(a+ib)^2}\right)}{4(a^2+b^2)d^6}$$

```
[Out] 1/2*x^2/(a+I*b)+3*b*x^(5/3)*ln(1+(a^2+b^2)*exp(2*I*(c+d*x^(1/3)))/(a+I*b)^2)
)/(a^2+b^2)/d-15/2*I*b*x^(4/3)*polylog(2,-(a^2+b^2)*exp(2*I*(c+d*x^(1/3)))/(a+I*b)^2)/(a^2+b^2)/d^2+15*b*x*polylog(3,-(a^2+b^2)*exp(2*I*(c+d*x^(1/3)))/(a+I*b)^2)/(a^2+b^2)/d^3+45/2*I*b*x^(2/3)*polylog(4,-(a^2+b^2)*exp(2*I*(c+d*x^(1/3)))/(a+I*b)^2)/(a^2+b^2)/d^4-45/2*b*x^(1/3)*polylog(5,-(a^2+b^2)*exp(2*I*(c+d*x^(1/3)))/(a+I*b)^2)/(a^2+b^2)/d^5-45/4*I*b*polylog(6,-(a^2+b^2)*exp(2*I*(c+d*x^(1/3)))/(a+I*b)^2)/(a^2+b^2)/d^6
```

$p(2*I*(c+d*x^(1/3)))/(a+I*b)^2/(a^2+b^2)/d^5-45/4*I*b*polylog(6,-(a^2+b^2)*exp(2*I*(c+d*x^(1/3)))/(a+I*b)^2)/(a^2+b^2)/d^6$

Rubi [A] (verified)

Time = 0.53 (sec) , antiderivative size = 352, normalized size of antiderivative = 1.00, number of steps used = 9, number of rules used = 7, $\frac{\text{number of rules}}{\text{integrand size}} = 0.389$, Rules used = {3832, 3813, 2221, 2611, 6744, 2320, 6724}

$$\int \frac{x}{a + b \tan(c + d\sqrt[3]{x})} dx = -\frac{45ib \operatorname{PolyLog}\left(6, -\frac{(a^2+b^2)e^{2i(c+d\sqrt[3]{x})}}{(a+ib)^2}\right)}{4d^6(a^2+b^2)} - \frac{45b\sqrt[3]{x} \operatorname{PolyLog}\left(5, -\frac{(a^2+b^2)e^{2i(c+d\sqrt[3]{x})}}{(a+ib)^2}\right)}{2d^5(a^2+b^2)} + \frac{45ibx^{2/3} \operatorname{PolyLog}\left(4, -\frac{(a^2+b^2)e^{2i(c+d\sqrt[3]{x})}}{(a+ib)^2}\right)}{2d^4(a^2+b^2)} + \frac{15bx \operatorname{PolyLog}\left(3, -\frac{(a^2+b^2)e^{2i(c+d\sqrt[3]{x})}}{(a+ib)^2}\right)}{d^3(a^2+b^2)} - \frac{15ibx^{4/3} \operatorname{PolyLog}\left(2, -\frac{(a^2+b^2)e^{2i(c+d\sqrt[3]{x})}}{(a+ib)^2}\right)}{2d^2(a^2+b^2)} + \frac{3bx^{5/3} \log\left(1 + \frac{(a^2+b^2)e^{2i(c+d\sqrt[3]{x})}}{(a+ib)^2}\right)}{d(a^2+b^2)} + \frac{x^2}{2(a+ib)}$$

[In] Int[x/(a + b*Tan[c + d*x^(1/3)]),x]

[Out] $x^2/(2*(a + I*b)) + (3*b*x^{5/3}*Log[1 + ((a^2 + b^2)*E^((2*I)*(c + d*x^{1/3})))]/(a + I*b)^2)/((a^2 + b^2)*d) - (((15*I)/2)*b*x^{4/3}*PolyLog[2, -(((a^2 + b^2)*E^((2*I)*(c + d*x^{1/3})))]/(a + I*b)^2)]/(a^2 + b^2)*d^2) + (15*b*x*x^{2/3}*PolyLog[3, -(((a^2 + b^2)*E^((2*I)*(c + d*x^{1/3})))]/(a + I*b)^2)]/(a^2 + b^2)*d^3) + (((45*I)/2)*b*x^{2/3}*PolyLog[4, -(((a^2 + b^2)*E^((2*I)*(c + d*x^{1/3})))]/(a + I*b)^2)]/(a^2 + b^2)*d^4) - (45*b*x^{1/3}*PolyLog[5, -(((a^2 + b^2)*E^((2*I)*(c + d*x^{1/3})))]/(a + I*b)^2)]/(2*(a^2 + b^2)*d^5) - (((45*I)/4)*b*x^{1/3}*PolyLog[6, -(((a^2 + b^2)*E^((2*I)*(c + d*x^{1/3})))]/(a + I*b)^2)]/(a^2 + b^2)*d^6)$

Rule 2221

Int[(((F_)^((g_)*(e_) + (f_)*(x_)))^(n_)*((c_) + (d_)*(x_))^(m_))/((a_) + (b_)*((F_)^((g_)*(e_) + (f_)*(x_)))^(n_)), x_Symbol] :> Simp

```

[((c + d*x)^m/(b*f*g*n*Log[F]))*Log[1 + b*((F^(g*(e + f*x)))^n/a)], x] - Di
st[d*(m/(b*f*g*n*Log[F])), Int[(c + d*x)^(m - 1)*Log[1 + b*((F^(g*(e + f*x)
))^n/a)], x], x] /; FreeQ[{F, a, b, c, d, e, f, g, n}, x] && IGtQ[m, 0]

```

Rule 2320

```

Int[u_, x_Symbol] := With[{v = FunctionOfExponential[u, x]}, Dist[v/D[v, x]
, Subst[Int[FunctionOfExponentialFunction[u, x]/x, x], x, v], x] /; Functi
onOfExponentialQ[u, x] && !MatchQ[u, (w_)*((a_.)*(v_)^(n_))^(m_)] /; FreeQ[
{a, m, n}, x] && IntegerQ[m*n] && !MatchQ[u, E^((c_.)*((a_.) + (b_.)*x))*
(F_) [v_] /; FreeQ[{a, b, c}, x] && InverseFunctionQ[F[x]]]

```

Rule 2611

```

Int[Log[1 + (e_.)*((F_)^((c_.)*((a_.) + (b_.)*(x_))))^(n_.)]*(f_.) + (g_.)
*(x_)^(m_.), x_Symbol] := Simp[(-f + g*x)^m*(PolyLog[2, (-e)*(F^(c*(a +
b*x)))^n]/(b*c*n*Log[F])), x] + Dist[g*(m/(b*c*n*Log[F])), Int[(f + g*x)^(m
- 1)*PolyLog[2, (-e)*(F^(c*(a + b*x)))^n], x], x] /; FreeQ[{F, a, b, c, e,
f, g, n}, x] && GtQ[m, 0]

```

Rule 3813

```

Int[((c_.) + (d_.)*(x_))^(m_.)/((a_.) + (b_.)*tan[(e_.) + (f_.)*(x_)]), x_Sy
mbol] := Simp[(c + d*x)^(m + 1)/(d*(m + 1)*(a + I*b)), x] + Dist[2*I*b, Int
[(c + d*x)^m*(E^Simp[2*I*(e + f*x), x]/((a + I*b)^2 + (a^2 + b^2)*E^Simp[2*
I*(e + f*x), x])), x], x] /; FreeQ[{a, b, c, d, e, f}, x] && NeQ[a^2 + b^2,
0] && IGtQ[m, 0]

```

Rule 3832

```

Int[(x_)^(m_.)*((a_.) + (b_.)*Tan[(c_.) + (d_.)*(x_)^(n_)])^(p_.), x_Symbol
] := Dist[1/n, Subst[Int[x^(Simplify[(m + 1)/n] - 1)*(a + b*Tan[c + d*x])^p
, x], x, x^n], x] /; FreeQ[{a, b, c, d, m, n, p}, x] && IGtQ[Simplify[(m +
1)/n], 0] && IntegerQ[p]

```

Rule 6724

```

Int[PolyLog[n_, (c_.)*((a_.) + (b_.)*(x_))^(p_.)]/((d_.) + (e_.)*(x_)), x_S
ymbol] := Simp[PolyLog[n + 1, c*(a + b*x)^p]/(e*p), x] /; FreeQ[{a, b, c, d
, e, n, p}, x] && EqQ[b*d, a*e]

```

Rule 6744

```

Int[((e_.) + (f_.)*(x_))^(m_.)*PolyLog[n_, (d_.)*((F_)^((c_.)*((a_.) + (b_.
)*(x_))))^(p_.)], x_Symbol] := Simp[(e + f*x)^m*(PolyLog[n + 1, d*(F^(c*(a
+ b*x)))^p]/(b*c*p*Log[F])), x] - Dist[f*(m/(b*c*p*Log[F])), Int[(e + f*x)^

```

`(m - 1)*PolyLog[n + 1, d*(F^(c*(a + b*x)))^p], x], x] /; FreeQ[{F, a, b, c, d, e, f, n, p}, x] && GtQ[m, 0]`

Rubi steps

$$\begin{aligned}
 \text{integral} &= 3\text{Subst}\left(\int \frac{x^5}{a + b \tan(c + dx)} dx, x, \sqrt[3]{x}\right) \\
 &= \frac{x^2}{2(a + ib)} + (6ib)\text{Subst}\left(\int \frac{e^{2i(c+dx)} x^5}{(a + ib)^2 + (a^2 + b^2) e^{2i(c+dx)}} dx, x, \sqrt[3]{x}\right) \\
 &= \frac{x^2}{2(a + ib)} + \frac{3bx^{5/3} \log\left(1 + \frac{(a^2+b^2)e^{2i(c+d\sqrt[3]{x}})}{(a+ib)^2}\right)}{(a^2 + b^2) d} \\
 &\quad - \frac{(15b)\text{Subst}\left(\int x^4 \log\left(1 + \frac{(a^2+b^2)e^{2i(c+dx)}}{(a+ib)^2}\right) dx, x, \sqrt[3]{x}\right)}{(a^2 + b^2) d} \\
 &= \frac{x^2}{2(a + ib)} + \frac{3bx^{5/3} \log\left(1 + \frac{(a^2+b^2)e^{2i(c+d\sqrt[3]{x}})}{(a+ib)^2}\right)}{(a^2 + b^2) d} \\
 &\quad - \frac{15ibx^{4/3} \text{PolyLog}\left(2, -\frac{(a^2+b^2)e^{2i(c+d\sqrt[3]{x}})}{(a+ib)^2}\right)}{2(a^2 + b^2) d^2} \\
 &\quad + \frac{(30ib)\text{Subst}\left(\int x^3 \text{PolyLog}\left(2, -\frac{(a^2+b^2)e^{2i(c+dx)}}{(a+ib)^2}\right) dx, x, \sqrt[3]{x}\right)}{(a^2 + b^2) d^2} \\
 &= \frac{x^2}{2(a + ib)} + \frac{3bx^{5/3} \log\left(1 + \frac{(a^2+b^2)e^{2i(c+d\sqrt[3]{x}})}{(a+ib)^2}\right)}{(a^2 + b^2) d} \\
 &\quad - \frac{15ibx^{4/3} \text{PolyLog}\left(2, -\frac{(a^2+b^2)e^{2i(c+d\sqrt[3]{x}})}{(a+ib)^2}\right)}{2(a^2 + b^2) d^2} \\
 &\quad + \frac{15bx \text{PolyLog}\left(3, -\frac{(a^2+b^2)e^{2i(c+d\sqrt[3]{x}})}{(a+ib)^2}\right)}{(a^2 + b^2) d^3} \\
 &\quad - \frac{(45b)\text{Subst}\left(\int x^2 \text{PolyLog}\left(3, -\frac{(a^2+b^2)e^{2i(c+dx)}}{(a+ib)^2}\right) dx, x, \sqrt[3]{x}\right)}{(a^2 + b^2) d^3}
 \end{aligned}$$

$$\begin{aligned}
&= \frac{x^2}{2(a+ib)} + \frac{3bx^{5/3} \log\left(1 + \frac{(a^2+b^2)e^{2i(c+d\sqrt[3]{x}})}{(a+ib)^2}\right)}{(a^2+b^2)d} \\
&\quad - \frac{15ibx^{4/3} \text{PolyLog}\left(2, -\frac{(a^2+b^2)e^{2i(c+d\sqrt[3]{x}})}{(a+ib)^2}\right)}{2(a^2+b^2)d^2} \\
&\quad + \frac{15bx \text{PolyLog}\left(3, -\frac{(a^2+b^2)e^{2i(c+d\sqrt[3]{x}})}{(a+ib)^2}\right)}{(a^2+b^2)d^3} \\
&\quad + \frac{45ibx^{2/3} \text{PolyLog}\left(4, -\frac{(a^2+b^2)e^{2i(c+d\sqrt[3]{x}})}{(a+ib)^2}\right)}{2(a^2+b^2)d^4} \\
&\quad - \frac{(45ib)\text{Subst}\left(\int x \text{PolyLog}\left(4, -\frac{(a^2+b^2)e^{2i(c+dx)}}{(a+ib)^2}\right) dx, x, \sqrt[3]{x}\right)}{(a^2+b^2)d^4} \\
&= \frac{x^2}{2(a+ib)} + \frac{3bx^{5/3} \log\left(1 + \frac{(a^2+b^2)e^{2i(c+d\sqrt[3]{x}})}{(a+ib)^2}\right)}{(a^2+b^2)d} \\
&\quad - \frac{15ibx^{4/3} \text{PolyLog}\left(2, -\frac{(a^2+b^2)e^{2i(c+d\sqrt[3]{x}})}{(a+ib)^2}\right)}{2(a^2+b^2)d^2} \\
&\quad + \frac{15bx \text{PolyLog}\left(3, -\frac{(a^2+b^2)e^{2i(c+d\sqrt[3]{x}})}{(a+ib)^2}\right)}{(a^2+b^2)d^3} \\
&\quad + \frac{45ibx^{2/3} \text{PolyLog}\left(4, -\frac{(a^2+b^2)e^{2i(c+d\sqrt[3]{x}})}{(a+ib)^2}\right)}{2(a^2+b^2)d^4} \\
&\quad - \frac{45b\sqrt[3]{x} \text{PolyLog}\left(5, -\frac{(a^2+b^2)e^{2i(c+d\sqrt[3]{x}})}{(a+ib)^2}\right)}{2(a^2+b^2)d^5} \\
&\quad + \frac{(45b)\text{Subst}\left(\int \text{PolyLog}\left(5, -\frac{(a^2+b^2)e^{2i(c+dx)}}{(a+ib)^2}\right) dx, x, \sqrt[3]{x}\right)}{2(a^2+b^2)d^5}
\end{aligned}$$

$$\begin{aligned}
&= \frac{x^2}{2(a+ib)} + \frac{3bx^{5/3} \log\left(1 + \frac{(a^2+b^2)e^{2i(c+d\sqrt[3]{x}})}{(a+ib)^2}\right)}{(a^2+b^2)d} \\
&\quad - \frac{15ibx^{4/3} \text{PolyLog}\left(2, -\frac{(a^2+b^2)e^{2i(c+d\sqrt[3]{x}})}{(a+ib)^2}\right)}{2(a^2+b^2)d^2} \\
&\quad + \frac{15bx \text{PolyLog}\left(3, -\frac{(a^2+b^2)e^{2i(c+d\sqrt[3]{x}})}{(a+ib)^2}\right)}{(a^2+b^2)d^3} \\
&\quad + \frac{45ibx^{2/3} \text{PolyLog}\left(4, -\frac{(a^2+b^2)e^{2i(c+d\sqrt[3]{x}})}{(a+ib)^2}\right)}{2(a^2+b^2)d^4} \\
&\quad - \frac{45b\sqrt[3]{x} \text{PolyLog}\left(5, -\frac{(a^2+b^2)e^{2i(c+d\sqrt[3]{x}})}{(a+ib)^2}\right)}{2(a^2+b^2)d^5} \\
&\quad - \frac{(45ib) \text{Subst}\left(\int \frac{\text{PolyLog}\left(5, -\frac{(a^2+b^2)x}{(a+ib)^2}\right)}{x} dx, x, e^{2i(c+d\sqrt[3]{x})}\right)}{4(a^2+b^2)d^6} \\
&= \frac{x^2}{2(a+ib)} + \frac{3bx^{5/3} \log\left(1 + \frac{(a^2+b^2)e^{2i(c+d\sqrt[3]{x}})}{(a+ib)^2}\right)}{(a^2+b^2)d} - \frac{15ibx^{4/3} \text{PolyLog}\left(2, -\frac{(a^2+b^2)e^{2i(c+d\sqrt[3]{x}})}{(a+ib)^2}\right)}{2(a^2+b^2)d^2} \\
&\quad + \frac{15bx \text{PolyLog}\left(3, -\frac{(a^2+b^2)e^{2i(c+d\sqrt[3]{x}})}{(a+ib)^2}\right)}{(a^2+b^2)d^3} + \frac{45ibx^{2/3} \text{PolyLog}\left(4, -\frac{(a^2+b^2)e^{2i(c+d\sqrt[3]{x}})}{(a+ib)^2}\right)}{2(a^2+b^2)d^4} \\
&\quad - \frac{45b\sqrt[3]{x} \text{PolyLog}\left(5, -\frac{(a^2+b^2)e^{2i(c+d\sqrt[3]{x}})}{(a+ib)^2}\right)}{2(a^2+b^2)d^5} - \frac{45ib \text{PolyLog}\left(6, -\frac{(a^2+b^2)e^{2i(c+d\sqrt[3]{x}})}{(a+ib)^2}\right)}{4(a^2+b^2)d^6}
\end{aligned}$$

Mathematica [A] (verified)

Time = 1.12 (sec) , antiderivative size = 310, normalized size of antiderivative = 0.88

$$\begin{aligned}
&\int \frac{x}{a + b \tan(c + d\sqrt[3]{x})} dx \\
&= \frac{2ad^6x^2 + 2ibd^6x^2 + 12bd^5x^{5/3} \log\left(1 + \frac{(a+ib)e^{-2i(c+d\sqrt[3]{x}})}{a-ib}\right) + 30ibd^4x^{4/3} \text{PolyLog}\left(2, \frac{(-a-ib)e^{-2i(c+d\sqrt[3]{x}})}{a-ib}\right) + 6}{\dots}
\end{aligned}$$

[In] Integrate[x/(a + b*Tan[c + d*x^(1/3)]),x]

```
[Out] (2*a*d^6*x^2 + (2*I)*b*d^6*x^2 + 12*b*d^5*x^(5/3)*Log[1 + (a + I*b)/((a - I*b)*E^((2*I)*(c + d*x^(1/3)))] + (30*I)*b*d^4*x^(4/3)*PolyLog[2, (-a - I*b)/((a - I*b)*E^((2*I)*(c + d*x^(1/3)))] + 60*b*d^3*x*PolyLog[3, (-a - I*b)/((a - I*b)*E^((2*I)*(c + d*x^(1/3)))] - (90*I)*b*d^2*x^(2/3)*PolyLog[4, (-a - I*b)/((a - I*b)*E^((2*I)*(c + d*x^(1/3)))] - 90*b*d*x^(1/3)*PolyLog[5, (-a - I*b)/((a - I*b)*E^((2*I)*(c + d*x^(1/3)))] + (45*I)*b*PolyLog[6, (-a - I*b)/((a - I*b)*E^((2*I)*(c + d*x^(1/3)))])/(4*(a^2 + b^2)*d^6)
```

Maple [F]

$$\int \frac{x}{a + b \tan\left(c + dx^{\frac{1}{3}}\right)} dx$$

```
[In] int(x/(a+b*tan(c+d*x^(1/3))),x)
```

```
[Out] int(x/(a+b*tan(c+d*x^(1/3))),x)
```

Fricas [F]

$$\int \frac{x}{a + b \tan\left(c + d\sqrt[3]{x}\right)} dx = \int \frac{x}{b \tan\left(dx^{\frac{1}{3}} + c\right) + a} dx$$

```
[In] integrate(x/(a+b*tan(c+d*x^(1/3))),x, algorithm="fricas")
```

```
[Out] integral(x/(b*tan(d*x^(1/3) + c) + a), x)
```

Sympy [F]

$$\int \frac{x}{a + b \tan\left(c + d\sqrt[3]{x}\right)} dx = \int \frac{x}{a + b \tan\left(c + d\sqrt[3]{x}\right)} dx$$

```
[In] integrate(x/(a+b*tan(c+d*x**(1/3))),x)
```

```
[Out] Integral(x/(a + b*tan(c + d*x**(1/3))), x)
```

Maxima [B] (verification not implemented)

Both result and optimal contain complex but leaf count of result is larger than twice the leaf count of optimal. 813 vs. $2(289) = 578$.

Time = 0.51 (sec) , antiderivative size = 813, normalized size of antiderivative = 2.31

$$\int \frac{x}{a + b \tan(c + d\sqrt[3]{x})} dx = \text{Too large to display}$$

[In] integrate(x/(a+b*tan(c+d*x^(1/3))),x, algorithm="maxima")

[Out]
$$\begin{aligned} & -1/10*(15*(2*(d*x^{1/3} + c)*a/(a^2 + b^2) + 2*b*\log(b*\tan(d*x^{1/3} + c) + \\ & a)/(a^2 + b^2) - b*\log(\tan(d*x^{1/3} + c)^2 + 1)/(a^2 + b^2))*c^5 - (5*(d* \\ & x^{1/3} + c)^6*(a - I*b) - 30*(d*x^{1/3} + c)^5*(a - I*b)*c + 75*(d*x^{1/3} \\ & + c)^4*(a - I*b)*c^2 - 100*(d*x^{1/3} + c)^3*(a - I*b)*c^3 + 75*(d*x^{1/3} \\ & + c)^2*(a - I*b)*c^4 - 2*(48*I*(d*x^{1/3} + c)^5*b - 150*I*(d*x^{1/3} + c) \\ & ^4*b*c + 200*I*(d*x^{1/3} + c)^3*b*c^2 - 150*I*(d*x^{1/3} + c)^2*b*c^3 + 75 \\ & *I*(d*x^{1/3} + c)*b*c^4)*\arctan2((2*a*b*\cos(2*d*x^{1/3} + 2*c) - (a^2 - b^2) \\ & *\sin(2*d*x^{1/3} + 2*c))/(a^2 + b^2), (2*a*b*\sin(2*d*x^{1/3} + 2*c) + a^2 \\ & + b^2 + (a^2 - b^2)*\cos(2*d*x^{1/3} + 2*c))/(a^2 + b^2)) - 15*(16*I*(d*x^{1/3} \\ & + c)^4*b - 40*I*(d*x^{1/3} + c)^3*b*c + 40*I*(d*x^{1/3} + c)^2*b*c^2 - \\ & 20*I*(d*x^{1/3} + c)*b*c^3 + 5*I*b*c^4)*\operatorname{dilog}((I*a + b)*e^{(2*I*d*x^{1/3} + \\ & 2*I*c)/(-I*a + b)} + (48*(d*x^{1/3} + c)^5*b - 150*(d*x^{1/3} + c)^4*b*c + \\ & 200*(d*x^{1/3} + c)^3*b*c^2 - 150*(d*x^{1/3} + c)^2*b*c^3 + 75*(d*x^{1/3} \\ & + c)*b*c^4)*\log(((a^2 + b^2)*\cos(2*d*x^{1/3} + 2*c)^2 + 4*a*b*\sin(2*d*x^{1/3} \\ & + 2*c) + (a^2 + b^2)*\sin(2*d*x^{1/3} + 2*c)^2 + a^2 + b^2 + 2*(a^2 - b^2) \\ & *\cos(2*d*x^{1/3} + 2*c))/(a^2 + b^2)) - 360*I*b*\operatorname{polylog}(6, (I*a + b)*e^{(2* \\ & I*d*x^{1/3} + 2*I*c)/(-I*a + b)} - 90*(8*(d*x^{1/3} + c)*b - 5*b*c)*\operatorname{polylog} \\ & (5, (I*a + b)*e^{(2*I*d*x^{1/3} + 2*I*c)/(-I*a + b)} - 60*(-12*I*(d*x^{1/3} \\ & + c)^2*b + 15*I*(d*x^{1/3} + c)*b*c - 5*I*b*c^2)*\operatorname{polylog}(4, (I*a + b)*e^{(2* \\ & I*d*x^{1/3} + 2*I*c)/(-I*a + b)} + 30*(16*(d*x^{1/3} + c)^3*b - 30*(d*x^{1/3} \\ & + c)^2*b*c + 20*(d*x^{1/3} + c)*b*c^2 - 5*b*c^3)*\operatorname{polylog}(3, (I*a + b)*e^{ \\ & (2*I*d*x^{1/3} + 2*I*c)/(-I*a + b)}))/(a^2 + b^2))/d^6 \end{aligned}$$

Giac [F]

$$\int \frac{x}{a + b \tan(c + d\sqrt[3]{x})} dx = \int \frac{x}{b \tan(dx^{\frac{1}{3}} + c) + a} dx$$

[In] integrate(x/(a+b*tan(c+d*x^(1/3))),x, algorithm="giac")

[Out] integrate(x/(b*tan(d*x^(1/3) + c) + a), x)

Mupad [F(-1)]

Timed out.

$$\int \frac{x}{a + b \tan(c + d\sqrt[3]{x})} dx = \int \frac{x}{a + b \tan(c + dx^{1/3})} dx$$

```
[In] int(x/(a + b*tan(c + d*x^(1/3))),x)
```

```
[Out] int(x/(a + b*tan(c + d*x^(1/3))), x)
```

$$3.59 \quad \int \frac{1}{a+b \tan\left(c+d \sqrt[3]{x}\right)} dx$$

Optimal result	386
Rubi [A] (verified)	386
Mathematica [A] (verified)	389
Maple [F]	390
Fricas [B] (verification not implemented)	390
Sympy [F]	391
Maxima [B] (verification not implemented)	391
Giac [F]	392
Mupad [F(-1)]	392

Optimal result

Integrand size = 16, antiderivative size = 176

$$\int \frac{1}{a+b \tan\left(c+d \sqrt[3]{x}\right)} dx = \frac{x}{a+ib} + \frac{3bx^{2/3} \log\left(1 + \frac{(a^2+b^2)e^{2i(c+d \sqrt[3]{x})}}{(a+ib)^2}\right)}{(a^2+b^2)d} - \frac{3ib \sqrt[3]{x} \operatorname{PolyLog}\left(2, -\frac{(a^2+b^2)e^{2i(c+d \sqrt[3]{x})}}{(a+ib)^2}\right)}{(a^2+b^2)d^2} + \frac{3b \operatorname{PolyLog}\left(3, -\frac{(a^2+b^2)e^{2i(c+d \sqrt[3]{x})}}{(a+ib)^2}\right)}{2(a^2+b^2)d^3}$$

```
[Out] x/(a+I*b)+3*b*x^(2/3)*ln(1+(a^2+b^2)*exp(2*I*(c+d*x^(1/3)))/(a+I*b)^2)/(a^2+b^2)/d-3*I*b*x^(1/3)*polylog(2,-(a^2+b^2)*exp(2*I*(c+d*x^(1/3)))/(a+I*b)^2)/(a^2+b^2)/d^2+3/2*b*polylog(3,-(a^2+b^2)*exp(2*I*(c+d*x^(1/3)))/(a+I*b)^2)/(a^2+b^2)/d^3
```

Rubi [A] (verified)

Time = 0.33 (sec) , antiderivative size = 176, normalized size of antiderivative = 1.00, number of steps used = 6, number of rules used = 6, $\frac{\text{number of rules}}{\text{integrand size}} = 0.375$, Rules used

= {3824, 3813, 2221, 2611, 2320, 6724}

$$\int \frac{1}{a + b \tan(c + d\sqrt[3]{x})} dx = \frac{3b \operatorname{PolyLog}\left(3, -\frac{(a^2+b^2)e^{2i(c+d\sqrt[3]{x})}}{(a+ib)^2}\right)}{2d^3(a^2+b^2)} - \frac{3ib\sqrt[3]{x} \operatorname{PolyLog}\left(2, -\frac{(a^2+b^2)e^{2i(c+d\sqrt[3]{x})}}{(a+ib)^2}\right)}{d^2(a^2+b^2)} + \frac{3bx^{2/3} \log\left(1 + \frac{(a^2+b^2)e^{2i(c+d\sqrt[3]{x})}}{(a+ib)^2}\right)}{d(a^2+b^2)} + \frac{x}{a+ib}$$

[In] Int[(a + b*Tan[c + d*x^(1/3)])^(-1), x]

[Out] x/(a + I*b) + (3*b*x^(2/3)*Log[1 + ((a^2 + b^2)*E^((2*I)*(c + d*x^(1/3))))]/(a + I*b)^2)]/((a^2 + b^2)*d) - ((3*I)*b*x^(1/3)*PolyLog[2, -(((a^2 + b^2)*E^((2*I)*(c + d*x^(1/3))))/(a + I*b)^2)]/(a^2 + b^2)*d^2) + (3*b*PolyLog[3, -(((a^2 + b^2)*E^((2*I)*(c + d*x^(1/3))))/(a + I*b)^2)]/(2*(a^2 + b^2)*d^3)

Rule 2221

Int[(((F_)^((g_)*(e_) + (f_)*(x_)))^(n_))*((c_) + (d_)*(x_))^(m_)]/((a_) + (b_)*((F_)^((g_)*(e_) + (f_)*(x_)))^(n_)), x_Symbol] :> Simp[(((c + d*x)^m/(b*f*g*n*Log[F]))*Log[1 + b*((F^(g*(e + f*x)))^n/a)], x] - Dist[d*(m/(b*f*g*n*Log[F])), Int[(c + d*x)^(m - 1)*Log[1 + b*((F^(g*(e + f*x)))^n/a)], x], x] /; FreeQ[{F, a, b, c, d, e, f, g, n}, x] && IGtQ[m, 0]

Rule 2320

Int[u_, x_Symbol] :> With[{v = FunctionOfExponential[u, x]}, Dist[v/D[v, x], Subst[Int[FunctionOfExponentialFunction[u, x]/x, x], x, v], x] /; FunctionOfExponentialQ[u, x] && !MatchQ[u, (w_)*((a_)*(v_)^(n_))^(m_)] /; FreeQ[{a, m, n}, x] && IntegerQ[m*n] && !MatchQ[u, E^((c_)*((a_) + (b_)*x))*(F_)[v_] /; FreeQ[{a, b, c}, x] && InverseFunctionQ[F[x]]]

Rule 2611

Int[Log[1 + (e_)*((F_)^((c_)*((a_) + (b_)*(x_)))^(n_))]*((f_) + (g_)*(x_))^(m_), x_Symbol] :> Simp[(-f + g*x)^m*(PolyLog[2, (-e)*(F^(c*(a + b*x)))^n]/(b*c*n*Log[F])), x] + Dist[g*(m/(b*c*n*Log[F])), Int[(f + g*x)^(m - 1)*PolyLog[2, (-e)*(F^(c*(a + b*x)))^n], x], x] /; FreeQ[{F, a, b, c, e, f, g, n}, x] && GtQ[m, 0]

Rule 3813

```
Int[((c_.) + (d_.)*(x_))^(m_.)/((a_.) + (b_.)*tan[(e_.) + (f_.)*(x_)]), x_Sy
mbol] := Simp[(c + d*x)^(m + 1)/(d*(m + 1)*(a + I*b)), x] + Dist[2*I*b, Int
[(c + d*x)^m*(E^Simp[2*I*(e + f*x), x]/((a + I*b)^2 + (a^2 + b^2)*E^Simp[2*
I*(e + f*x), x])), x], x] /; FreeQ[{a, b, c, d, e, f}, x] && NeQ[a^2 + b^2,
0] && IGtQ[m, 0]
```

Rule 3824

```
Int[((a_.) + (b_.)*Tan[(c_.) + (d_.)*(x_)^(n_)])^(p_.), x_Symbol] := Dist[1
/n, Subst[Int[x^(1/n - 1)*(a + b*Tan[c + d*x])^p, x], x, x^n], x] /; FreeQ[
{a, b, c, d, p}, x] && IGtQ[1/n, 0] && IntegerQ[p]
```

Rule 6724

```
Int[PolyLog[n_, (c_.)*((a_.) + (b_.)*(x_))^(p_.)]/((d_.) + (e_.)*(x_)), x_S
ymbol] := Simp[PolyLog[n + 1, c*(a + b*x)^p]/(e*p), x] /; FreeQ[{a, b, c, d
, e, n, p}, x] && EqQ[b*d, a*e]
```

Rubi steps

$$\begin{aligned}
\text{integral} &= 3\text{Subst}\left(\int \frac{x^2}{a + b \tan(c + dx)} dx, x, \sqrt[3]{x}\right) \\
&= \frac{x}{a + ib} + (6ib)\text{Subst}\left(\int \frac{e^{2i(c+dx)}x^2}{(a + ib)^2 + (a^2 + b^2)e^{2i(c+dx)}} dx, x, \sqrt[3]{x}\right) \\
&= \frac{x}{a + ib} + \frac{3bx^{2/3} \log\left(1 + \frac{(a^2+b^2)e^{2i(c+d\sqrt[3]{x}})}{(a+ib)^2}\right)}{(a^2 + b^2)d} \\
&\quad - \frac{(6b)\text{Subst}\left(\int x \log\left(1 + \frac{(a^2+b^2)e^{2i(c+dx)}}{(a+ib)^2}\right) dx, x, \sqrt[3]{x}\right)}{(a^2 + b^2)d} \\
&= \frac{x}{a + ib} + \frac{3bx^{2/3} \log\left(1 + \frac{(a^2+b^2)e^{2i(c+d\sqrt[3]{x}})}{(a+ib)^2}\right)}{(a^2 + b^2)d} \\
&\quad - \frac{3ib\sqrt[3]{x} \text{PolyLog}\left(2, -\frac{(a^2+b^2)e^{2i(c+d\sqrt[3]{x}})}{(a+ib)^2}\right)}{(a^2 + b^2)d^2} \\
&\quad + \frac{(3ib)\text{Subst}\left(\int \text{PolyLog}\left(2, -\frac{(a^2+b^2)e^{2i(c+dx)}}{(a+ib)^2}\right) dx, x, \sqrt[3]{x}\right)}{(a^2 + b^2)d^2}
\end{aligned}$$

$$\begin{aligned}
&= \frac{x}{a+ib} + \frac{3bx^{2/3} \log\left(1 + \frac{(a^2+b^2)e^{2i(c+d\sqrt[3]{x}})}{(a+ib)^2}\right)}{(a^2+b^2)d} \\
&\quad - \frac{3ib\sqrt[3]{x} \operatorname{PolyLog}\left(2, -\frac{(a^2+b^2)e^{2i(c+d\sqrt[3]{x}})}{(a+ib)^2}\right)}{(a^2+b^2)d^2} \\
&\quad + \frac{(3b)\operatorname{Subst}\left(\int \frac{\operatorname{PolyLog}\left(2, -\frac{(a^2+b^2)x}{(a+ib)^2}\right)}{x} dx, x, e^{2i(c+d\sqrt[3]{x})}\right)}{2(a^2+b^2)d^3} \\
&= \frac{x}{a+ib} + \frac{3bx^{2/3} \log\left(1 + \frac{(a^2+b^2)e^{2i(c+d\sqrt[3]{x}})}{(a+ib)^2}\right)}{(a^2+b^2)d} \\
&\quad - \frac{3ib\sqrt[3]{x} \operatorname{PolyLog}\left(2, -\frac{(a^2+b^2)e^{2i(c+d\sqrt[3]{x}})}{(a+ib)^2}\right)}{(a^2+b^2)d^2} + \frac{3b \operatorname{PolyLog}\left(3, -\frac{(a^2+b^2)e^{2i(c+d\sqrt[3]{x}})}{(a+ib)^2}\right)}{2(a^2+b^2)d^3}
\end{aligned}$$

Mathematica [A] (verified)

Time = 0.88 (sec) , antiderivative size = 165, normalized size of antiderivative = 0.94

$$\int \frac{1}{a+b \tan(c+d\sqrt[3]{x})} dx = \frac{2ad^3x + 2ibd^3x + 6bd^2x^{2/3} \log\left(1 + \frac{(a+ib)e^{-2i(c+d\sqrt[3]{x}})}{a-ib}\right) + 6ibd\sqrt[3]{x} \operatorname{PolyLog}\left(2, \frac{(-a-ib)e^{-2i(c+d\sqrt[3]{x}})}{a-ib}\right) + 3b \operatorname{PolyLog}\left(3, \frac{(-a-ib)e^{-2i(c+d\sqrt[3]{x}})}{a-ib}\right)}{2(a^2+b^2)d^3}$$

[In] Integrate[(a + b*Tan[c + d*x^(1/3)])^(-1), x]

[Out] (2*a*d^3*x + (2*I)*b*d^3*x + 6*b*d^2*x^(2/3)*Log[1 + (a + I*b)/((a - I*b)*E^((2*I)*(c + d*x^(1/3)))] + (6*I)*b*d*x^(1/3)*PolyLog[2, (-a - I*b)/((a - I*b)*E^((2*I)*(c + d*x^(1/3)))] + 3*b*PolyLog[3, (-a - I*b)/((a - I*b)*E^((2*I)*(c + d*x^(1/3)))])/(2*(a^2 + b^2)*d^3)

Maple [F]

$$\int \frac{1}{a + b \tan\left(c + d x^{\frac{1}{3}}\right)} dx$$

[In] int(1/(a+b*tan(c+d*x^(1/3))),x)

[Out] int(1/(a+b*tan(c+d*x^(1/3))),x)

Fricas [B] (verification not implemented)

Both result and optimal contain complex but leaf count of result is larger than twice the leaf count of optimal. 746 vs. $2(147) = 294$.

Time = 0.26 (sec) , antiderivative size = 746, normalized size of antiderivative = 4.24

$$\int \frac{1}{a + b \tan\left(c + d \sqrt[3]{x}\right)} dx$$

$$= \frac{4ad^3x + 6bc^2 \log\left(\frac{(iab+b^2)\tan(dx^{\frac{1}{3}}+c)^2 - a^2 + iab + (ia^2+ib^2)\tan(dx^{\frac{1}{3}}+c)}{\tan(dx^{\frac{1}{3}}+c)^2 + 1}\right) + 6bc^2 \log\left(\frac{(iab-b^2)\tan(dx^{\frac{1}{3}}+c)^2 + a^2 + iab + (ia^2-ib^2)\tan(dx^{\frac{1}{3}}+c)}{\tan(dx^{\frac{1}{3}}+c)^2 + 1}\right)}{1}$$

[In] integrate(1/(a+b*tan(c+d*x^(1/3))),x, algorithm="fricas")

[Out] $\frac{1}{4}*(4*a*d^3*x + 6*b*c^2*\log(((I*a*b + b^2)*\tan(d*x^(1/3) + c))^2 - a^2 + I*a*b + (I*a^2 + I*b^2)*\tan(d*x^(1/3) + c))/(\tan(d*x^(1/3) + c)^2 + 1)) + 6*b*c^2*\log(((I*a*b - b^2)*\tan(d*x^(1/3) + c))^2 + a^2 + I*a*b + (I*a^2 + I*b^2)*\tan(d*x^(1/3) + c))/(\tan(d*x^(1/3) + c)^2 + 1)) + 6*I*b*d*x^(1/3)*\operatorname{dilog}(2*((I*a*b - b^2)*\tan(d*x^(1/3) + c))^2 - a^2 - I*a*b + (I*a^2 - 2*a*b - I*b^2)*\tan(d*x^(1/3) + c))/((a^2 + b^2)*\tan(d*x^(1/3) + c)^2 + a^2 + b^2) + 1) - 6*I*b*d*x^(1/3)*\operatorname{dilog}(2*((-I*a*b - b^2)*\tan(d*x^(1/3) + c))^2 - a^2 + I*a*b + (-I*a^2 - 2*a*b + I*b^2)*\tan(d*x^(1/3) + c))/((a^2 + b^2)*\tan(d*x^(1/3) + c)^2 + a^2 + b^2) + 1) + 6*(b*d^2*x^(2/3) - b*c^2)*\log(-2*((I*a*b - b^2)*\tan(d*x^(1/3) + c))^2 - a^2 - I*a*b + (I*a^2 - 2*a*b - I*b^2)*\tan(d*x^(1/3) + c))/((a^2 + b^2)*\tan(d*x^(1/3) + c)^2 + a^2 + b^2)) + 6*(b*d^2*x^(2/3) - b*c^2)*\log(-2*((-I*a*b - b^2)*\tan(d*x^(1/3) + c))^2 - a^2 + I*a*b + (-I*a^2 - 2*a*b + I*b^2)*\tan(d*x^(1/3) + c))/((a^2 + b^2)*\tan(d*x^(1/3) + c)^2 + a^2 + b^2)) + 3*b*polylog(3, ((a^2 + 2*I*a*b - b^2)*\tan(d*x^(1/3) + c))^2 - a^2 - 2*I*a*b + b^2 - 2*(-I*a^2 + 2*a*b + I*b^2)*\tan(d*x^(1/3) + c))/((a^2 + b^2)*\tan(d*x^(1/3) + c)^2 + a^2 + b^2)) + 3*b*polylog(3, ((a^2 - 2*I*a*b - b^2)*\tan(d*x^(1/3) + c))^2 - a^2 + 2*I*a*b + b^2 - 2*(I*a^2 + 2*a*b - I*b^2)*\tan(d*x^(1/3) + c))/((a^2 + b^2)*\tan(d*x^(1/3) + c)^2 + a^2 + b^2)))/((a^2 + b^2)*d^3)$

SymPy [F]

$$\int \frac{1}{a + b \tan(c + d\sqrt[3]{x})} dx = \int \frac{1}{a + b \tan(c + d\sqrt[3]{x})} dx$$

[In] integrate(1/(a+b*tan(c+d*x**(1/3))),x)

[Out] Integral(1/(a + b*tan(c + d*x**(1/3))), x)

Maxima [B] (verification not implemented)

Both result and optimal contain complex but leaf count of result is larger than twice the leaf count of optimal. 446 vs. $2(147) = 294$.

Time = 0.46 (sec) , antiderivative size = 446, normalized size of antiderivative = 2.53

$$\int \frac{1}{a + b \tan(c + d\sqrt[3]{x})} dx$$

$$= \frac{3 \left(\frac{2(dx^{\frac{1}{3}}+c)a}{a^2+b^2} + \frac{2b \log(b \tan(dx^{\frac{1}{3}}+c)+a)}{a^2+b^2} - \frac{b \log(\tan(dx^{\frac{1}{3}}+c)+1)}{a^2+b^2} \right) c^2 + \frac{2(dx^{\frac{1}{3}}+c)^3(a-ib)-6(dx^{\frac{1}{3}}+c)^2(a-ib)c-6(i(dx^{\frac{1}{3}}+c))}{a^2+b^2}}{d^3}$$

[In] integrate(1/(a+b*tan(c+d*x^(1/3))),x, algorithm="maxima")

[Out] $\frac{1}{2} * (3 * (2 * (d * x^{1/3} + c) * a / (a^2 + b^2) + 2 * b * \log(b * \tan(d * x^{1/3} + c) + a) / (a^2 + b^2) - b * \log(\tan(d * x^{1/3} + c)^2 + 1) / (a^2 + b^2)) * c^2 + (2 * (d * x^{1/3} + c)^3 * (a - I * b) - 6 * (d * x^{1/3} + c)^2 * (a - I * b) * c - 6 * (I * (d * x^{1/3} + c)^2 * b - 2 * I * (d * x^{1/3} + c) * b * c) * \arctan2((2 * a * b * \cos(2 * d * x^{1/3} + 2 * c) - (a^2 - b^2) * \sin(2 * d * x^{1/3} + 2 * c)) / (a^2 + b^2), (2 * a * b * \sin(2 * d * x^{1/3} + 2 * c) + a^2 + b^2 + (a^2 - b^2) * \cos(2 * d * x^{1/3} + 2 * c)) / (a^2 + b^2)) - 6 * (I * (d * x^{1/3} + c) * b - I * b * c) * \operatorname{dilog}((I * a + b) * e^{(2 * I * d * x^{1/3} + 2 * I * c)} / (-I * a + b)) + 3 * ((d * x^{1/3} + c)^2 * b - 2 * (d * x^{1/3} + c) * b * c) * \log(((a^2 + b^2) * \cos(2 * d * x^{1/3} + 2 * c))^2 + 4 * a * b * \sin(2 * d * x^{1/3} + 2 * c) + (a^2 + b^2) * \sin(2 * d * x^{1/3} + 2 * c))^2 + a^2 + b^2 + 2 * (a^2 - b^2) * \cos(2 * d * x^{1/3} + 2 * c)) / (a^2 + b^2)) + 3 * b * \operatorname{polylog}(3, (I * a + b) * e^{(2 * I * d * x^{1/3} + 2 * I * c)} / (-I * a + b))) / (a^2 + b^2) / d^3$

Giac [F]

$$\int \frac{1}{a + b \tan(c + d\sqrt[3]{x})} dx = \int \frac{1}{b \tan(dx^{\frac{1}{3}} + c) + a} dx$$

[In] integrate(1/(a+b*tan(c+d*x^(1/3))),x, algorithm="giac")

[Out] integrate(1/(b*tan(d*x^(1/3) + c) + a), x)

Mupad [F(-1)]

Timed out.

$$\int \frac{1}{a + b \tan(c + d\sqrt[3]{x})} dx = \int \frac{1}{a + b \tan(c + dx^{1/3})} dx$$

[In] int(1/(a + b*tan(c + d*x^(1/3))),x)

[Out] int(1/(a + b*tan(c + d*x^(1/3))), x)

$$3.60 \quad \int \frac{1}{x \left(a + b \tan \left(c + d \sqrt[3]{x} \right) \right)} dx$$

Optimal result	393
Rubi [N/A]	393
Mathematica [N/A]	394
Maple [N/A] (verified)	394
Fricas [N/A]	394
Sympy [N/A]	395
Maxima [N/A]	395
Giac [N/A]	395
Mupad [N/A]	396

Optimal result

Integrand size = 20, antiderivative size = 20

$$\int \frac{1}{x \left(a + b \tan \left(c + d \sqrt[3]{x} \right) \right)} dx = \text{Int} \left(\frac{1}{x \left(a + b \tan \left(c + d \sqrt[3]{x} \right) \right)}, x \right)$$

[Out] Unintegrable(1/x/(a+b*tan(c+d*x^(1/3))),x)

Rubi [N/A]

Not integrable

Time = 0.03 (sec) , antiderivative size = 20, normalized size of antiderivative = 1.00, number of steps used = 0, number of rules used = 0, $\frac{\text{number of rules}}{\text{integrand size}} = 0.000$, Rules used = {}

$$\int \frac{1}{x \left(a + b \tan \left(c + d \sqrt[3]{x} \right) \right)} dx = \int \frac{1}{x \left(a + b \tan \left(c + d \sqrt[3]{x} \right) \right)} dx$$

[In] Int[1/(x*(a + b*Tan[c + d*x^(1/3)])),x]

[Out] Defer[Int][1/(x*(a + b*Tan[c + d*x^(1/3)])), x]

Rubi steps

$$\text{integral} = \int \frac{1}{x \left(a + b \tan \left(c + d \sqrt[3]{x} \right) \right)} dx$$

Mathematica [N/A]

Not integrable

Time = 4.39 (sec) , antiderivative size = 22, normalized size of antiderivative = 1.10

$$\int \frac{1}{x (a + b \tan (c + d \sqrt[3]{x}))} dx = \int \frac{1}{x (a + b \tan (c + d \sqrt[3]{x}))} dx$$

`[In] Integrate[1/(x*(a + b*Tan[c + d*x^(1/3)])),x]``[Out] Integrate[1/(x*(a + b*Tan[c + d*x^(1/3)])), x]`**Maple [N/A] (verified)**

Not integrable

Time = 0.43 (sec) , antiderivative size = 18, normalized size of antiderivative = 0.90

$$\int \frac{1}{x (a + b \tan (c + d x^{\frac{1}{3}}))} dx$$

`[In] int(1/x/(a+b*tan(c+d*x^(1/3))),x)``[Out] int(1/x/(a+b*tan(c+d*x^(1/3))),x)`**Fricas [N/A]**

Not integrable

Time = 0.23 (sec) , antiderivative size = 19, normalized size of antiderivative = 0.95

$$\int \frac{1}{x (a + b \tan (c + d \sqrt[3]{x}))} dx = \int \frac{1}{(b \tan (dx^{\frac{1}{3}} + c) + a)x} dx$$

`[In] integrate(1/x/(a+b*tan(c+d*x^(1/3))),x, algorithm="fricas")``[Out] integral(1/(b*x*tan(d*x^(1/3) + c) + a*x), x)`

Sympy [N/A]

Not integrable

Time = 2.15 (sec) , antiderivative size = 17, normalized size of antiderivative = 0.85

$$\int \frac{1}{x(a + b \tan(c + d\sqrt[3]{x}))} dx = \int \frac{1}{x(a + b \tan(c + d\sqrt[3]{x}))} dx$$

[In] integrate(1/x/(a+b*tan(c+d*x**(1/3))),x)

[Out] Integral(1/(x*(a + b*tan(c + d*x**(1/3)))), x)

Maxima [N/A]

Not integrable

Time = 1.00 (sec) , antiderivative size = 496, normalized size of antiderivative = 24.80

$$\int \frac{1}{x(a + b \tan(c + d\sqrt[3]{x}))} dx = \int \frac{1}{(b \tan(dx^{\frac{1}{3}} + c) + a)x} dx$$

[In] integrate(1/x/(a+b*tan(c+d*x^(1/3))),x, algorithm="maxima")

[Out] $-(2*(a^2*b + b^3)*\text{integrate}((a^2*\sin(2*d*x^{(1/3)} + 2*c) - (2*a*b*\cos(2*c) + b^2*\sin(2*c))*\cos(2*d*x^{(1/3)}) - (b^2*\cos(2*c) - 2*a*b*\sin(2*c))*\sin(2*d*x^{(1/3)})))/((a^4*\cos(2*d*x^{(1/3)} + 2*c)^2 + a^4*\sin(2*d*x^{(1/3)} + 2*c)^2 + a^4 + 2*a^2*b^2 + b^4 + ((4*a^2*b^2 + b^4)*\cos(2*c)^2 + (4*a^2*b^2 + b^4)*\sin(2*c)^2)*\cos(2*d*x^{(1/3)})^2 + ((4*a^2*b^2 + b^4)*\cos(2*c)^2 + (4*a^2*b^2 + b^4)*\sin(2*c)^2)*\sin(2*d*x^{(1/3)})^2 - 2*((a^2*b^2 + b^4)*\cos(2*c) - 2*(a^3*b + a*b^3)*\sin(2*c))*\cos(2*d*x^{(1/3)}) + 2*(a^4 + a^2*b^2 - (a^2*b^2*\cos(2*c) - 2*a^3*b*\sin(2*c))*\cos(2*d*x^{(1/3)}) + (2*a^3*b*\cos(2*c) + a^2*b^2*\sin(2*c))*\sin(2*d*x^{(1/3)}))*\cos(2*d*x^{(1/3)} + 2*c) + 2*(2*(a^3*b + a*b^3)*\cos(2*c) + (a^2*b^2 + b^4)*\sin(2*c))*\sin(2*d*x^{(1/3)}) - 2*((2*a^3*b*\cos(2*c) + a^2*b^2*\sin(2*c))*\cos(2*d*x^{(1/3)}) + (a^2*b^2*\cos(2*c) - 2*a^3*b*\sin(2*c))*\sin(2*d*x^{(1/3)}))*\sin(2*d*x^{(1/3)} + 2*c))*x), x) - a*\log(x))/(a^2 + b^2)$

Giac [N/A]

Not integrable

Time = 0.76 (sec) , antiderivative size = 20, normalized size of antiderivative = 1.00

$$\int \frac{1}{x(a + b \tan(c + d\sqrt[3]{x}))} dx = \int \frac{1}{(b \tan(dx^{\frac{1}{3}} + c) + a)x} dx$$

[In] integrate(1/x/(a+b*tan(c+d*x^(1/3))),x, algorithm="giac")

[Out] integrate(1/((b*tan(d*x^(1/3) + c) + a)*x), x)

Mupad [N/A]

Not integrable

Time = 3.97 (sec) , antiderivative size = 20, normalized size of antiderivative = 1.00

$$\int \frac{1}{x (a + b \tan (c + d \sqrt[3]{x}))} dx = \int \frac{1}{x (a + b \tan (c + d x^{1/3}))} dx$$

```
[In] int(1/(x*(a + b*tan(c + d*x^(1/3)))),x)
```

```
[Out] int(1/(x*(a + b*tan(c + d*x^(1/3)))), x)
```

$$3.61 \quad \int \frac{1}{x^2 \left(a + b \tan \left(c + d \sqrt[3]{x} \right) \right)} dx$$

Optimal result	397
Rubi [N/A]	397
Mathematica [N/A]	398
Maple [N/A] (verified)	398
Fricas [N/A]	398
Sympy [N/A]	399
Maxima [N/A]	399
Giac [N/A]	399
Mupad [N/A]	400

Optimal result

Integrand size = 20, antiderivative size = 20

$$\int \frac{1}{x^2 (a + b \tan (c + d \sqrt[3]{x}))} dx = \text{Int} \left(\frac{1}{x^2 (a + b \tan (c + d \sqrt[3]{x}))}, x \right)$$

[Out] Unintegrable(1/x^2/(a+b*tan(c+d*x^(1/3))),x)

Rubi [N/A]

Not integrable

Time = 0.03 (sec) , antiderivative size = 20, normalized size of antiderivative = 1.00, number of steps used = 0, number of rules used = 0, $\frac{\text{number of rules}}{\text{integrand size}} = 0.000$, Rules used = {}

$$\int \frac{1}{x^2 (a + b \tan (c + d \sqrt[3]{x}))} dx = \int \frac{1}{x^2 (a + b \tan (c + d \sqrt[3]{x}))} dx$$

[In] Int[1/(x^2*(a + b*Tan[c + d*x^(1/3)])),x]

[Out] Defer[Int][1/(x^2*(a + b*Tan[c + d*x^(1/3)])), x]

Rubi steps

$$\text{integral} = \int \frac{1}{x^2 (a + b \tan (c + d \sqrt[3]{x}))} dx$$

Mathematica [N/A]

Not integrable

Time = 5.26 (sec) , antiderivative size = 22, normalized size of antiderivative = 1.10

$$\int \frac{1}{x^2 (a + b \tan (c + d \sqrt[3]{x}))} dx = \int \frac{1}{x^2 (a + b \tan (c + d \sqrt[3]{x}))} dx$$

[In] Integrate[1/(x^2*(a + b*Tan[c + d*x^(1/3)])),x]

[Out] Integrate[1/(x^2*(a + b*Tan[c + d*x^(1/3)])), x]

Maple [N/A] (verified)

Not integrable

Time = 0.47 (sec) , antiderivative size = 18, normalized size of antiderivative = 0.90

$$\int \frac{1}{x^2 (a + b \tan (c + d x^{\frac{1}{3}}))} dx$$

[In] int(1/x^2/(a+b*tan(c+d*x^(1/3))),x)

[Out] int(1/x^2/(a+b*tan(c+d*x^(1/3))),x)

Fricas [N/A]

Not integrable

Time = 0.23 (sec) , antiderivative size = 23, normalized size of antiderivative = 1.15

$$\int \frac{1}{x^2 (a + b \tan (c + d \sqrt[3]{x}))} dx = \int \frac{1}{(b \tan (dx^{\frac{1}{3}} + c) + a) x^2} dx$$

[In] integrate(1/x^2/(a+b*tan(c+d*x^(1/3))),x, algorithm="fricas")

[Out] integral(1/(b*x^2*tan(d*x^(1/3) + c) + a*x^2), x)

Sympy [N/A]

Not integrable

Time = 12.64 (sec) , antiderivative size = 19, normalized size of antiderivative = 0.95

$$\int \frac{1}{x^2 (a + b \tan (c + d \sqrt[3]{x}))} dx = \int \frac{1}{x^2 (a + b \tan (c + d \sqrt[3]{x}))} dx$$

[In] integrate(1/x**2/(a+b*tan(c+d*x**(1/3))),x)

[Out] Integral(1/(x**2*(a + b*tan(c + d*x**(1/3)))), x)

Maxima [N/A]

Not integrable

Time = 1.46 (sec) , antiderivative size = 496, normalized size of antiderivative = 24.80

$$\int \frac{1}{x^2 (a + b \tan (c + d \sqrt[3]{x}))} dx = \int \frac{1}{(b \tan (dx^{\frac{1}{3}} + c) + a) x^2} dx$$

[In] integrate(1/x^2/(a+b*tan(c+d*x^(1/3))),x, algorithm="maxima")

[Out] $-(2*(a^2*b + b^3)*x*\text{integrate}((a^2*\sin(2*d*x^{(1/3)} + 2*c) - (2*a*b*\cos(2*c) + b^2*\sin(2*c))*\cos(2*d*x^{(1/3)}) - (b^2*\cos(2*c) - 2*a*b*\sin(2*c))*\sin(2*d*x^{(1/3)})))/((a^4*\cos(2*d*x^{(1/3)} + 2*c)^2 + a^4*\sin(2*d*x^{(1/3)} + 2*c)^2 + a^4 + 2*a^2*b^2 + b^4 + ((4*a^2*b^2 + b^4)*\cos(2*c)^2 + (4*a^2*b^2 + b^4)*\sin(2*c)^2)*\cos(2*d*x^{(1/3)})^2 + ((4*a^2*b^2 + b^4)*\cos(2*c)^2 + (4*a^2*b^2 + b^4)*\sin(2*c)^2)*\sin(2*d*x^{(1/3)})^2 - 2*((a^2*b^2 + b^4)*\cos(2*c) - 2*(a^3*b + a*b^3)*\sin(2*c))*\cos(2*d*x^{(1/3)}) + 2*(a^4 + a^2*b^2 - (a^2*b^2*\cos(2*c) - 2*a^3*b*\sin(2*c))*\cos(2*d*x^{(1/3)}) + (2*a^3*b*\cos(2*c) + a^2*b^2*\sin(2*c))*\sin(2*d*x^{(1/3)}))*\cos(2*d*x^{(1/3)} + 2*c) + 2*(2*(a^3*b + a*b^3)*\cos(2*c) + (a^2*b^2 + b^4)*\sin(2*c))*\sin(2*d*x^{(1/3)}) - 2*((2*a^3*b*\cos(2*c) + a^2*b^2*\sin(2*c))*\cos(2*d*x^{(1/3)}) + (a^2*b^2*\cos(2*c) - 2*a^3*b*\sin(2*c))*\sin(2*d*x^{(1/3)}))*\sin(2*d*x^{(1/3)} + 2*c))*x^2, x) + a)/((a^2 + b^2)*x)$

Giac [N/A]

Not integrable

Time = 0.68 (sec) , antiderivative size = 20, normalized size of antiderivative = 1.00

$$\int \frac{1}{x^2 (a + b \tan (c + d \sqrt[3]{x}))} dx = \int \frac{1}{(b \tan (dx^{\frac{1}{3}} + c) + a) x^2} dx$$

[In] integrate(1/x^2/(a+b*tan(c+d*x^(1/3))),x, algorithm="giac")

[Out] integrate(1/((b*tan(d*x^(1/3) + c) + a)*x^2), x)

Mupad [N/A]

Not integrable

Time = 3.96 (sec) , antiderivative size = 20, normalized size of antiderivative = 1.00

$$\int \frac{1}{x^2 (a + b \tan (c + d \sqrt[3]{x}))} dx = \int \frac{1}{x^2 (a + b \tan (c + d x^{1/3}))} dx$$

```
[In] int(1/(x^2*(a + b*tan(c + d*x^(1/3))))),x)
```

```
[Out] int(1/(x^2*(a + b*tan(c + d*x^(1/3))))), x)
```


$$3.62 \quad \int \frac{x^2}{(a+b \tan(c+d \sqrt[3]{x}))^2} dx$$

Optimal result	402
Rubi [A] (verified)	403
Mathematica [A] (verified)	412
Maple [F]	413
Fricas [F]	413
Sympy [F]	413
Maxima [B] (verification not implemented)	413
Giac [F]	418
Mupad [F(-1)]	418

Optimal result

Integrand size = 20, antiderivative size = 1691

$$\begin{aligned}
 \int \frac{x^2}{(a + b \tan(c + d\sqrt[3]{x}))^2} dx = & -\frac{6ib^2x^{8/3}}{(a^2 + b^2)^2 d} \\
 & + \frac{6b^2x^{8/3}}{(a + ib)(ia + b)^2 d (ia - b + (ia + b)e^{2i(c+d\sqrt[3]{x})})} \\
 & + \frac{x^3}{3(a - ib)^2} + \frac{4bx^3}{3(ia - b)(a - ib)^2} - \frac{4b^2x^3}{3(a^2 + b^2)^2} \\
 & + \frac{24b^2x^{7/3} \log\left(1 + \frac{(a-ib)e^{2i(c+d\sqrt[3]{x})}}{a+ib}\right)}{(a^2 + b^2)^2 d^2} \\
 & + \frac{6bx^{8/3} \log\left(1 + \frac{(a-ib)e^{2i(c+d\sqrt[3]{x})}}{a+ib}\right)}{(a - ib)^2(a + ib)d} \\
 & + \frac{6ib^2x^{8/3} \log\left(1 + \frac{(a-ib)e^{2i(c+d\sqrt[3]{x})}}{a+ib}\right)}{(a^2 + b^2)^2 d} \\
 & - \frac{84ib^2x^2 \operatorname{PolyLog}\left(2, -\frac{(a-ib)e^{2i(c+d\sqrt[3]{x})}}{a+ib}\right)}{(a^2 + b^2)^2 d^3} \\
 & + \frac{24bx^{7/3} \operatorname{PolyLog}\left(2, -\frac{(a-ib)e^{2i(c+d\sqrt[3]{x})}}{a+ib}\right)}{(ia - b)(a - ib)^2 d^2} \\
 & - \frac{24b^2x^{7/3} \operatorname{PolyLog}\left(2, -\frac{(a-ib)e^{2i(c+d\sqrt[3]{x})}}{a+ib}\right)}{(a^2 + b^2)^2 d^2} \\
 & + \frac{252b^2x^{5/3} \operatorname{PolyLog}\left(3, -\frac{(a-ib)e^{2i(c+d\sqrt[3]{x})}}{a+ib}\right)}{(a^2 + b^2)^2 d^4} \\
 & + \frac{84bx^2 \operatorname{PolyLog}\left(3, -\frac{(a-ib)e^{2i(c+d\sqrt[3]{x})}}{a+ib}\right)}{(a - ib)^2(a + ib)d^3} \\
 & - \frac{84ib^2x^2 \operatorname{PolyLog}\left(3, -\frac{(a-ib)e^{2i(c+d\sqrt[3]{x})}}{a+ib}\right)}{(a^2 + b^2)^2 d^3} \\
 & + \frac{630ib^2x^{4/3} \operatorname{PolyLog}\left(4, -\frac{(a-ib)e^{2i(c+d\sqrt[3]{x})}}{a+ib}\right)}{(a^2 + b^2)^2 d^5} \\
 & - \frac{252bx^{5/3} \operatorname{PolyLog}\left(4, -\frac{(a-ib)e^{2i(c+d\sqrt[3]{x})}}{a+ib}\right)}{(ia - b)(a - ib)^2 d^4} \\
 & + \frac{252b^2x^{5/3} \operatorname{PolyLog}\left(4, -\frac{(a-ib)e^{2i(c+d\sqrt[3]{x})}}{a+ib}\right)}{(a^2 + b^2)^2 d^5}
 \end{aligned}$$

[Out] $630*I*b^2*x^{(4/3)}*polylog(5, -(a-I*b)*exp(2*I*(c+d*x^{(1/3)}))/(a+I*b))/(a^2+b^2)^2/d^5+630*I*b^2*x^{(4/3)}*polylog(4, -(a-I*b)*exp(2*I*(c+d*x^{(1/3)}))/(a+I*b))/(a^2+b^2)^2/d^5+4/3*b*x^3/(I*a-b)/(a-I*b)^2+252*b^2*x^{(5/3)}*polylog(4, -(a-I*b)*exp(2*I*(c+d*x^{(1/3)}))/(a+I*b))/(a^2+b^2)^2/d^4-1260*b^2*x*polylog(5, -(a-I*b)*exp(2*I*(c+d*x^{(1/3)}))/(a+I*b))/(a^2+b^2)^2/d^6-1260*b^2*x*polylog(6, -(a-I*b)*exp(2*I*(c+d*x^{(1/3)}))/(a+I*b))/(a^2+b^2)^2/d^6+1890*b^2*x^{(1/3)}*polylog(7, -(a-I*b)*exp(2*I*(c+d*x^{(1/3)}))/(a+I*b))/(a^2+b^2)^2/d^8+1890*b^2*x^{(1/3)}*polylog(8, -(a-I*b)*exp(2*I*(c+d*x^{(1/3)}))/(a+I*b))/(a^2+b^2)^2/d^8-945*b*polylog(9, -(a-I*b)*exp(2*I*(c+d*x^{(1/3)}))/(a+I*b))/(a-I*b)^2/(a+I*b)/d^9-6*I*b^2*x^{(8/3)}/(a^2+b^2)^2/d+24*b^2*x^{(7/3)}*ln(1+(a-I*b)*exp(2*I*(c+d*x^{(1/3)}))/(a+I*b))/(a^2+b^2)^2/d^2-24*b^2*x^{(7/3)}*polylog(2, -(a-I*b)*exp(2*I*(c+d*x^{(1/3)}))/(a+I*b))/(a^2+b^2)^2/d^2+252*b^2*x^{(5/3)}*polylog(3, -(a-I*b)*exp(2*I*(c+d*x^{(1/3)}))/(a+I*b))/(a^2+b^2)^2/d^4+945*I*b^2*polylog(8, -(a-I*b)*exp(2*I*(c+d*x^{(1/3)}))/(a+I*b))/(a^2+b^2)^2/d^9+945*I*b^2*polylog(9, -(a-I*b)*exp(2*I*(c+d*x^{(1/3)}))/(a+I*b))/(a^2+b^2)^2/d^9-84*I*b^2*x^2*polylog(3, -(a-I*b)*exp(2*I*(c+d*x^{(1/3)}))/(a+I*b))/(a^2+b^2)^2/d^3-1890*I*b^2*x^{(2/3)}*polylog(6, -(a-I*b)*exp(2*I*(c+d*x^{(1/3)}))/(a+I*b))/(a^2+b^2)^2/d^7-1890*I*b^2*x^{(2/3)}*polylog(7, -(a-I*b)*exp(2*I*(c+d*x^{(1/3)}))/(a+I*b))/(a^2+b^2)^2/d^7+6*b^2*x^{(8/3)}/(a+I*b)/(I*a+b)^2/d/(I*a-b+(I*a+b)*exp(2*I*(c+d*x^{(1/3)}))/(a+I*b))+24*b*x^{(7/3)}*polylog(2, -(a-I*b)*exp(2*I*(c+d*x^{(1/3)}))/(a+I*b))/(I*a-b)/(a-I*b)^2/d^2+84*b*x^2*polylog(3, -(a-I*b)*exp(2*I*(c+d*x^{(1/3)}))/(a+I*b))/(a-I*b)^2/(a+I*b)/d^3-252*b*x^{(5/3)}*polylog(4, -(a-I*b)*exp(2*I*(c+d*x^{(1/3)}))/(a+I*b))/(I*a-b)/(a-I*b)^2/d^4-630*b*x^{(4/3)}*polylog(5, -(a-I*b)*exp(2*I*(c+d*x^{(1/3)}))/(a+I*b))/(a-I*b)^2/(a+I*b)/d^5+1260*b*x*polylog(6, -(a-I*b)*exp(2*I*(c+d*x^{(1/3)}))/(a+I*b))/(I*a-b)/(a-I*b)^2/d^6+1890*b*x^{(2/3)}*polylog(7, -(a-I*b)*exp(2*I*(c+d*x^{(1/3)}))/(a+I*b))/(a-I*b)^2/(a+I*b)/d^7+6*b*x^{(8/3)}*ln(1+(a-I*b)*exp(2*I*(c+d*x^{(1/3)}))/(a+I*b))/(a-I*b)^2/(a+I*b)/d-1890*b*x^{(1/3)}*polylog(8, -(a-I*b)*exp(2*I*(c+d*x^{(1/3)}))/(a+I*b))/(I*a-b)/(a-I*b)^2/d^8-6*I*b^2*x^{(8/3)}*ln(1+(a-I*b)*exp(2*I*(c+d*x^{(1/3)}))/(a+I*b))/(a^2+b^2)^2/d-84*I*b^2*x^2*polylog(2, -(a-I*b)*exp(2*I*(c+d*x^{(1/3)}))/(a+I*b))/(a^2+b^2)^2/d^3-4/3*b^2*x^3/(a^2+b^2)^2+1/3*x^3/(a-I*b)^2$

Rubi [A] (verified)

Time = 3.29 (sec) , antiderivative size = 1691, normalized size of antiderivative = 1.00, number of steps used = 37, number of rules used = 10, $\frac{\text{number of rules}}{\text{integrand size}} = 0.500$, Rules

used = {3832, 3815, 2216, 2215, 2221, 2611, 6744, 2320, 6724, 2222}

$$\begin{aligned}
 \int \frac{x^2}{(a + b \tan(c + d\sqrt[3]{x}))^2} dx &= \frac{4bx^3}{3(ia - b)(a - ib)^2} + \frac{x^3}{3(a - ib)^2} - \frac{4b^2x^3}{3(a^2 + b^2)^2} \\
 &+ \frac{6b \log\left(\frac{e^{2i(c+d\sqrt[3]{x})(a-ib)}}{a+ib} + 1\right) x^{8/3}}{(a - ib)^2(a + ib)d} \\
 &- \frac{6ib^2 \log\left(\frac{e^{2i(c+d\sqrt[3]{x})(a-ib)}}{a+ib} + 1\right) x^{8/3}}{(a^2 + b^2)^2 d} - \frac{6ib^2 x^{8/3}}{(a^2 + b^2)^2 d} \\
 &+ \frac{6b^2 x^{8/3}}{(a + ib)(ia + b)^2 d (ia + (ia + b)e^{2i(c+d\sqrt[3]{x}}) - b)} \\
 &+ \frac{24b^2 \log\left(\frac{e^{2i(c+d\sqrt[3]{x})(a-ib)}}{a+ib} + 1\right) x^{7/3}}{(a^2 + b^2)^2 d^2} \\
 &+ \frac{24b \operatorname{PolyLog}\left(2, -\frac{(a-ib)e^{2i(c+d\sqrt[3]{x}})}{a+ib}\right) x^{7/3}}{(ia - b)(a - ib)^2 d^2} \\
 &- \frac{24b^2 \operatorname{PolyLog}\left(2, -\frac{(a-ib)e^{2i(c+d\sqrt[3]{x}})}{a+ib}\right) x^{7/3}}{(a^2 + b^2)^2 d^2} \\
 &- \frac{84ib^2 \operatorname{PolyLog}\left(2, -\frac{(a-ib)e^{2i(c+d\sqrt[3]{x}})}{a+ib}\right) x^2}{(a^2 + b^2)^2 d^3} \\
 &+ \frac{84b \operatorname{PolyLog}\left(3, -\frac{(a-ib)e^{2i(c+d\sqrt[3]{x}})}{a+ib}\right) x^2}{(a - ib)^2(a + ib)d^3} \\
 &- \frac{84ib^2 \operatorname{PolyLog}\left(3, -\frac{(a-ib)e^{2i(c+d\sqrt[3]{x}})}{a+ib}\right) x^2}{(a^2 + b^2)^2 d^3} \\
 &+ \frac{252b^2 \operatorname{PolyLog}\left(3, -\frac{(a-ib)e^{2i(c+d\sqrt[3]{x}})}{a+ib}\right) x^{5/3}}{(a^2 + b^2)^2 d^4} \\
 &- \frac{252b \operatorname{PolyLog}\left(4, -\frac{(a-ib)e^{2i(c+d\sqrt[3]{x}})}{a+ib}\right) x^{5/3}}{(ia - b)(a - ib)^2 d^4} \\
 &+ \frac{252b^2 \operatorname{PolyLog}\left(4, -\frac{(a-ib)e^{2i(c+d\sqrt[3]{x}})}{a+ib}\right) x^{5/3}}{(a^2 + b^2)^2 d^4} \\
 &+ \frac{630ib^2 \operatorname{PolyLog}\left(4, -\frac{(a-ib)e^{2i(c+d\sqrt[3]{x}})}{a+ib}\right) x^{4/3}}{(a^2 + b^2)^2 d^5} \\
 &- \frac{630b \operatorname{PolyLog}\left(5, -\frac{(a-ib)e^{2i(c+d\sqrt[3]{x}})}{a+ib}\right) x^{4/3}}{(a - ib)^2(a + ib)d^5}
 \end{aligned}$$

[In] Int[x^2/(a + b*Tan[c + d*x^(1/3)])^2,x]

[Out]
$$\frac{(-6I)b^2x^{8/3}}{(a^2 + b^2)^2d} + \frac{6b^2x^{8/3}}{(a + Ib)(Ia + b)^2d(Ia - b + (Ia + b)E^{(2I)(c + dx^{1/3})})} + \frac{x^3}{3(a - Ib)^2} + \frac{4bx^3}{3(Ia - b)(a - Ib)^2} - \frac{4b^2x^3}{3(a^2 + b^2)^2} + \frac{24b^2x^{7/3}\text{Log}[1 + ((a - Ib)E^{(2I)(c + dx^{1/3})})/(a + Ib)]}{(a^2 + b^2)^2d^2} + \frac{6b^2x^{8/3}\text{Log}[1 + ((a - Ib)E^{(2I)(c + dx^{1/3})})/(a + Ib)]}{(a + Ib)} - \frac{((6I)b^2x^{8/3}\text{Log}[1 + ((a - Ib)E^{(2I)(c + dx^{1/3})})/(a + Ib)])/((a^2 + b^2)^2d) - ((84I)b^2x^2\text{PolyLog}[2, -((a - Ib)E^{(2I)(c + dx^{1/3})})/(a + Ib)])}{(a^2 + b^2)^2d^3} + \frac{24b^2x^{7/3}\text{PolyLog}[2, -((a - Ib)E^{(2I)(c + dx^{1/3})})/(a + Ib)]}{(Ia - b)(a - Ib)^2d^2} - \frac{24b^2x^{7/3}\text{PolyLog}[2, -((a - Ib)E^{(2I)(c + dx^{1/3})})/(a + Ib)]}{(a^2 + b^2)^2d^2} + \frac{252b^2x^{5/3}\text{PolyLog}[3, -((a - Ib)E^{(2I)(c + dx^{1/3})})/(a + Ib)]}{(a^2 + b^2)^2d^4} + \frac{84b^2x^2\text{PolyLog}[3, -((a - Ib)E^{(2I)(c + dx^{1/3})})/(a + Ib)]}{(a - Ib)^2(a + Ib)d^3} - \frac{(84I)b^2x^2\text{PolyLog}[3, -((a - Ib)E^{(2I)(c + dx^{1/3})})/(a + Ib)]}{(a^2 + b^2)^2d^3} + \frac{(630I)b^2x^{4/3}\text{PolyLog}[4, -((a - Ib)E^{(2I)(c + dx^{1/3})})/(a + Ib)]}{(a^2 + b^2)^2d^5} - \frac{252b^2x^{5/3}\text{PolyLog}[4, -((a - Ib)E^{(2I)(c + dx^{1/3})})/(a + Ib)]}{(Ia - b)(a - Ib)^2d^4} + \frac{252b^2x^{5/3}\text{PolyLog}[4, -((a - Ib)E^{(2I)(c + dx^{1/3})})/(a + Ib)]}{(a^2 + b^2)^2d^4} - \frac{1260b^2x\text{PolyLog}[5, -((a - Ib)E^{(2I)(c + dx^{1/3})})/(a + Ib)]}{(a^2 + b^2)^2d^6} - \frac{630b^2x^{4/3}\text{PolyLog}[5, -((a - Ib)E^{(2I)(c + dx^{1/3})})/(a + Ib)]}{(a - Ib)^2(a + Ib)d^5} + \frac{(630I)b^2x^{4/3}\text{PolyLog}[5, -((a - Ib)E^{(2I)(c + dx^{1/3})})/(a + Ib)]}{(a^2 + b^2)^2d^5} - \frac{(1890I)b^2x^{2/3}\text{PolyLog}[6, -((a - Ib)E^{(2I)(c + dx^{1/3})})/(a + Ib)]}{(a^2 + b^2)^2d^7} + \frac{1260b^2x\text{PolyLog}[6, -((a - Ib)E^{(2I)(c + dx^{1/3})})/(a + Ib)]}{(Ia - b)(a - Ib)^2d^6} - \frac{1260b^2x\text{PolyLog}[6, -((a - Ib)E^{(2I)(c + dx^{1/3})})/(a + Ib)]}{(a^2 + b^2)^2d^6} + \frac{1890b^2x^{1/3}\text{PolyLog}[7, -((a - Ib)E^{(2I)(c + dx^{1/3})})/(a + Ib)]}{(a^2 + b^2)^2d^8} + \frac{1890b^2x^{2/3}\text{PolyLog}[7, -((a - Ib)E^{(2I)(c + dx^{1/3})})/(a + Ib)]}{(a - Ib)^2(a + Ib)d^7} - \frac{(1890I)b^2x^{2/3}\text{PolyLog}[7, -((a - Ib)E^{(2I)(c + dx^{1/3})})/(a + Ib)]}{(a^2 + b^2)^2d^7} + \frac{(945I)b^2\text{PolyLog}[8, -((a - Ib)E^{(2I)(c + dx^{1/3})})/(a + Ib)]}{(a^2 + b^2)^2d^9} - \frac{1890b^2x^{1/3}\text{PolyLog}[8, -((a - Ib)E^{(2I)(c + dx^{1/3})})/(a + Ib)]}{(Ia - b)(a - Ib)^2d^8} + \frac{1890b^2x^{1/3}\text{PolyLog}[8, -((a - Ib)E^{(2I)(c + dx^{1/3})})/(a + Ib)]}{(a^2 + b^2)^2d^8} - \frac{945b\text{PolyLog}[9, -((a - Ib)E^{(2I)(c + dx^{1/3})})/(a + Ib)]}{(a + Ib)} - \frac{(945I)b^2\text{PolyLog}[9, -((a - Ib)E^{(2I)(c + dx^{1/3})})/(a + Ib)]}{(a - Ib)^2(a + Ib)d^9} + \frac{(945I)b^2\text{PolyLog}[9, -((a - Ib)E^{(2I)(c + dx^{1/3})})/(a + Ib)]}{(a^2 + b^2)^2d^9}$$

Rule 2215

Int[((c_.) + (d_.)*(x_))^(m_.)/((a_.) + (b_.)*((F_)^(g_.)*(e_.) + (f_.)*(x_)))^(n_.), x_Symbol] := Simp[(c + d*x)^(m + 1)/(a*d*(m + 1)), x] - Dist[b/a, Int[(c + d*x)^m*((F^(g*(e + f*x)))^n/(a + b*(F^(g*(e + f*x)))^n)), x],

x] /; FreeQ[{F, a, b, c, d, e, f, g, n}, x] && IGtQ[m, 0]

Rule 2216

Int[((a_) + (b_)*((F_)^((g_)*((e_) + (f_)*(x_))))^(n_))^(p_)*((c_) + (d_)*(x_))^(m_), x_Symbol] := Dist[1/a, Int[(c + d*x)^m*(a + b*(F^(g*(e + f*x)))^n)^(p + 1), x], x] - Dist[b/a, Int[(c + d*x)^m*(F^(g*(e + f*x)))^n*(a + b*(F^(g*(e + f*x)))^n)^p, x], x] /; FreeQ[{F, a, b, c, d, e, f, g, n}, x] && ILtQ[p, 0] && IGtQ[m, 0]

Rule 2221

Int[(((F_)^((g_)*((e_) + (f_)*(x_))))^(n_)*((c_) + (d_)*(x_))^(m_))/((a_) + (b_)*((F_)^((g_)*((e_) + (f_)*(x_))))^(n_)), x_Symbol] := Simp[(c + d*x)^m/(b*f*g*n*Log[F])*Log[1 + b*((F^(g*(e + f*x)))^n/a)], x] - Dist[d*(m/(b*f*g*n*Log[F])), Int[(c + d*x)^(m - 1)*Log[1 + b*((F^(g*(e + f*x)))^n/a)], x], x] /; FreeQ[{F, a, b, c, d, e, f, g, n}, x] && IGtQ[m, 0]

Rule 2222

Int[((F_)^((g_)*((e_) + (f_)*(x_))))^(n_)*((a_) + (b_)*((F_)^((g_)*((e_) + (f_)*(x_))))^(n_))^(p_)*((c_) + (d_)*(x_))^(m_), x_Symbol] := Simp[(c + d*x)^m*((a + b*(F^(g*(e + f*x)))^n)^(p + 1)/(b*f*g*n*(p + 1)*Log[F])), x] - Dist[d*(m/(b*f*g*n*(p + 1)*Log[F])), Int[(c + d*x)^(m - 1)*(a + b*(F^(g*(e + f*x)))^n)^(p + 1), x], x] /; FreeQ[{F, a, b, c, d, e, f, g, m, n, p}, x] && NeQ[p, -1]

Rule 2320

Int[u_, x_Symbol] := With[{v = FunctionOfExponential[u, x]}, Dist[v/D[v, x], Subst[Int[FunctionOfExponentialFunction[u, x]/x, x], x, v], x] /; FunctionOfExponentialQ[u, x] && !MatchQ[u, (w_)*((a_)*(v_)^(n_))^(m_) /; FreeQ[{a, m, n}, x] && IntegerQ[m*n] && !MatchQ[u, E^((c_)*((a_) + (b_)*x))*(F_)[v_] /; FreeQ[{a, b, c}, x] && InverseFunctionQ[F[x]]]

Rule 2611

Int[Log[1 + (e_)*((F_)^((c_)*((a_) + (b_)*(x_))))^(n_)]*((f_) + (g_)*(x_))^(m_), x_Symbol] := Simp[(-f + g*x)^m*(PolyLog[2, (-e)*(F^(c*(a + b*x)))^n]/(b*c*n*Log[F])), x] + Dist[g*(m/(b*c*n*Log[F])), Int[(f + g*x)^(m - 1)*PolyLog[2, (-e)*(F^(c*(a + b*x)))^n], x], x] /; FreeQ[{F, a, b, c, e, f, g, n}, x] && GtQ[m, 0]

Rule 3815

Int[((c_) + (d_)*(x_))^(m_)*((a_) + (b_)*tan[(e_) + (f_)*(x_)])^(n_), x_Symbol] := Int[ExpandIntegrand[(c + d*x)^m, (1/(a - I*b) - 2*I*(b/(a^2 +

$b^2 + (a - I*b)^2 * E^{(2*I*(e + f*x))} \wedge (-n), x, x] /;$ FreeQ[{a, b, c, d, e, f}, x] && NeQ[a^2 + b^2, 0] && ILtQ[n, 0] && IGtQ[m, 0]

Rule 3832

Int[(x_)^(m_)*((a_) + (b_)*Tan[(c_) + (d_)*(x_)^(n_)])^(p_), x_Symbol] := Dist[1/n, Subst[Int[x^(Simplify[(m + 1)/n] - 1)*(a + b*Tan[c + d*x])^p, x], x, x^n], x] /; FreeQ[{a, b, c, d, m, n, p}, x] && IGtQ[Simplify[(m + 1)/n], 0] && IntegerQ[p]

Rule 6724

Int[PolyLog[n_, (c_)*((a_) + (b_)*(x_))^(p_)]/((d_) + (e_)*(x_)), x_Symbol] := Simp[PolyLog[n + 1, c*(a + b*x)^p]/(e*p), x] /; FreeQ[{a, b, c, d, e, n, p}, x] && EqQ[b*d, a*e]

Rule 6744

Int[((e_) + (f_)*(x_))^(m_)*PolyLog[n_, (d_)*((F_)^(c_)*((a_) + (b_)*(x_)))^(p_)], x_Symbol] := Simp[(e + f*x)^m*(PolyLog[n + 1, d*(F^(c*(a + b*x)))^p]/(b*c*p*Log[F])), x] - Dist[f*(m/(b*c*p*Log[F])), Int[(e + f*x)^(m - 1)*PolyLog[n + 1, d*(F^(c*(a + b*x)))^p], x], x] /; FreeQ[{F, a, b, c, d, e, f, n, p}, x] && GtQ[m, 0]

Rubi steps

$$\begin{aligned}
 \text{integral} &= 3 \text{Subst} \left(\int \frac{x^8}{(a + b \tan(c + dx))^2} dx, x, \sqrt[3]{x} \right) \\
 &= 3 \text{Subst} \left(\int \left(\frac{x^8}{(a - ib)^2} - \frac{4b^2 x^8}{(ia + b)^2 (ia(1 + \frac{ib}{a}) + ia(1 - \frac{ib}{a}) e^{2ic + 2idx})^2} \right. \right. \\
 &\quad \left. \left. + \frac{4bx^8}{(a - ib)^2 (ia(1 + \frac{ib}{a}) + ia(1 - \frac{ib}{a}) e^{2ic + 2idx})} \right) dx, x, \sqrt[3]{x} \right) \\
 &= \frac{x^3}{3(a - ib)^2} + \frac{(12b) \text{Subst} \left(\int \frac{x^8}{ia(1 + \frac{ib}{a}) + ia(1 - \frac{ib}{a}) e^{2ic + 2idx}} dx, x, \sqrt[3]{x} \right)}{(a - ib)^2} \\
 &\quad - \frac{(12b^2) \text{Subst} \left(\int \frac{x^8}{(ia(1 + \frac{ib}{a}) + ia(1 - \frac{ib}{a}) e^{2ic + 2idx})^2} dx, x, \sqrt[3]{x} \right)}{(ia + b)^2}
 \end{aligned}$$

$$\begin{aligned}
&= \frac{x^3}{3(a-ib)^2} + \frac{4bx^3}{3(ia-b)(a-ib)^2} \\
&\quad + \frac{(12b^2) \text{Subst} \left(\int \frac{x^8}{ia(1+\frac{ib}{a})+ia(1-\frac{ib}{a})e^{2ic+2idx}} dx, x, \sqrt[3]{x} \right)}{(ia-b)(a-ib)^2} \\
&\quad - \frac{(12b) \text{Subst} \left(\int \frac{e^{2ic+2idx} x^8}{ia(1+\frac{ib}{a})+ia(1-\frac{ib}{a})e^{2ic+2idx}} dx, x, \sqrt[3]{x} \right)}{a^2+b^2} \\
&\quad - \frac{(12b^2) \text{Subst} \left(\int \frac{e^{2ic+2idx} x^8}{(ia(1+\frac{ib}{a})+ia(1-\frac{ib}{a})e^{2ic+2idx})^2} dx, x, \sqrt[3]{x} \right)}{a^2+b^2} \\
&= -\frac{6b^2 x^{8/3}}{(a-ib)^2(a+ib)d(ia-b+(ia+b)e^{2i(c+d\sqrt[3]{x}})} + \frac{x^3}{3(a-ib)^2} \\
&\quad + \frac{4bx^3}{3(ia-b)(a-ib)^2} - \frac{4b^2 x^3}{3(a^2+b^2)^2} + \frac{6bx^{8/3} \log \left(1 + \frac{(a-ib)e^{2i(c+d\sqrt[3]{x}})}{a+ib} \right)}{(a-ib)^2(a+ib)d} \\
&\quad - \frac{(12b^2) \text{Subst} \left(\int \frac{e^{2ic+2idx} x^8}{ia(1+\frac{ib}{a})+ia(1-\frac{ib}{a})e^{2ic+2idx}} dx, x, \sqrt[3]{x} \right)}{(a+ib)^2(ia+b)} \\
&\quad - \frac{(48b) \text{Subst} \left(\int x^7 \log \left(1 + \frac{(1-\frac{ib}{a})e^{2ic+2idx}}{1+\frac{ib}{a}} \right) dx, x, \sqrt[3]{x} \right)}{(a-ib)^2(a+ib)d} \\
&\quad + \frac{(48b^2) \text{Subst} \left(\int \frac{x^7}{ia(1+\frac{ib}{a})+ia(1-\frac{ib}{a})e^{2ic+2idx}} dx, x, \sqrt[3]{x} \right)}{(a-ib)^2(a+ib)d}
\end{aligned}$$

$$\begin{aligned}
&= -\frac{6ib^2x^{8/3}}{(a^2+b^2)^2d} - \frac{6b^2x^{8/3}}{(a-ib)^2(a+ib)d} \frac{ia-b+(ia+b)e^{2i(c+d\sqrt[3]{x})}}{3(a-ib)^2} + \frac{x^3}{3(a-ib)^2} \\
&+ \frac{4bx^3}{3(ia-b)(a-ib)^2} - \frac{4b^2x^3}{3(a^2+b^2)^2} + \frac{6bx^{8/3} \log\left(1 + \frac{(a-ib)e^{2i(c+d\sqrt[3]{x})}}{a+ib}\right)}{(a-ib)^2(a+ib)d} \\
&- \frac{6ib^2x^{8/3} \log\left(1 + \frac{(a-ib)e^{2i(c+d\sqrt[3]{x})}}{a+ib}\right)}{(a^2+b^2)^2d} + \frac{24bx^{7/3} \text{PolyLog}\left(2, -\frac{(a-ib)e^{2i(c+d\sqrt[3]{x})}}{a+ib}\right)}{(ia-b)(a-ib)^2d^2} \\
&- \frac{(168b) \text{Subst}\left(\int x^6 \text{PolyLog}\left(2, -\frac{(1-\frac{ib}{a})e^{2ic+2idx}}{1+\frac{ib}{a}}\right) dx, x, \sqrt[3]{x}\right)}{(ia-b)(a-ib)^2d^2} \\
&- \frac{(48b^2) \text{Subst}\left(\int \frac{e^{2ic+2idx}x^7}{ia(1+\frac{ib}{a})+ia(1-\frac{ib}{a})e^{2ic+2idx}} dx, x, \sqrt[3]{x}\right)}{(a-ib)(a+ib)^2d} \\
&+ \frac{(48ib^2) \text{Subst}\left(\int x^7 \log\left(1 + \frac{(1-\frac{ib}{a})e^{2ic+2idx}}{1+\frac{ib}{a}}\right) dx, x, \sqrt[3]{x}\right)}{(a^2+b^2)^2d} \\
&= -\frac{6ib^2x^{8/3}}{(a^2+b^2)^2d} - \frac{6b^2x^{8/3}}{(a-ib)^2(a+ib)d} \frac{ia-b+(ia+b)e^{2i(c+d\sqrt[3]{x})}}{3(a-ib)^2} \\
&+ \frac{x^3}{3(a-ib)^2} + \frac{4bx^3}{3(ia-b)(a-ib)^2} - \frac{4b^2x^3}{3(a^2+b^2)^2} \\
&+ \frac{24b^2x^{7/3} \log\left(1 + \frac{(a-ib)e^{2i(c+d\sqrt[3]{x})}}{a+ib}\right)}{(a^2+b^2)^2d^2} + \frac{6bx^{8/3} \log\left(1 + \frac{(a-ib)e^{2i(c+d\sqrt[3]{x})}}{a+ib}\right)}{(a-ib)^2(a+ib)d} \\
&- \frac{6ib^2x^{8/3} \log\left(1 + \frac{(a-ib)e^{2i(c+d\sqrt[3]{x})}}{a+ib}\right)}{(a^2+b^2)^2d} + \frac{24bx^{7/3} \text{PolyLog}\left(2, -\frac{(a-ib)e^{2i(c+d\sqrt[3]{x})}}{a+ib}\right)}{(ia-b)(a-ib)^2d^2} \\
&- \frac{24b^2x^{7/3} \text{PolyLog}\left(2, -\frac{(a-ib)e^{2i(c+d\sqrt[3]{x})}}{a+ib}\right)}{(a^2+b^2)^2d^2} + \frac{84bx^2 \text{PolyLog}\left(3, -\frac{(a-ib)e^{2i(c+d\sqrt[3]{x})}}{a+ib}\right)}{(a-ib)^2(a+ib)d^3} \\
&- \frac{(504b) \text{Subst}\left(\int x^5 \text{PolyLog}\left(3, -\frac{(1-\frac{ib}{a})e^{2ic+2idx}}{1+\frac{ib}{a}}\right) dx, x, \sqrt[3]{x}\right)}{(a-ib)^2(a+ib)d^3} \\
&- \frac{(168b^2) \text{Subst}\left(\int x^6 \log\left(1 + \frac{(1-\frac{ib}{a})e^{2ic+2idx}}{1+\frac{ib}{a}}\right) dx, x, \sqrt[3]{x}\right)}{(a^2+b^2)^2d^2} \\
&- \frac{(168b^2) \text{Subst}\left(\int x^6 \text{PolyLog}\left(2, -\frac{(1-\frac{ib}{a})e^{2ic+2idx}}{1+\frac{ib}{a}}\right) dx, x, \sqrt[3]{x}\right)}{(a^2+b^2)^2d^2} \\
&+ \frac{(168b^2) \text{Subst}\left(\int x^6 \text{PolyLog}\left(2, -\frac{(1-\frac{ib}{a})e^{2ic+2idx}}{1+\frac{ib}{a}}\right) dx, x, \sqrt[3]{x}\right)}{(a^2+b^2)^2d^2}
\end{aligned}$$

$$\begin{aligned}
&= -\frac{6ib^2x^{8/3}}{(a^2+b^2)^2d} - \frac{6b^2x^{8/3}}{(a-ib)^2(a+ib)d} \frac{e^{2i(c+d\sqrt[3]{x})}}{(ia-b+(a+b)e^{2i(c+d\sqrt[3]{x})})} + \frac{x^3}{3(a-ib)^2} \\
&+ \frac{4bx^3}{3(ia-b)(a-ib)^2} - \frac{4b^2x^3}{3(a^2+b^2)^2} + \frac{24b^2x^{7/3} \log\left(1 + \frac{(a-ib)e^{2i(c+d\sqrt[3]{x})}}{a+ib}\right)}{(a^2+b^2)^2d^2} \\
&+ \frac{6bx^{8/3} \log\left(1 + \frac{(a-ib)e^{2i(c+d\sqrt[3]{x})}}{a+ib}\right)}{(a-ib)^2(a+ib)d} - \frac{6ib^2x^{8/3} \log\left(1 + \frac{(a-ib)e^{2i(c+d\sqrt[3]{x})}}{a+ib}\right)}{(a^2+b^2)^2d} \\
&- \frac{84ib^2x^2 \text{PolyLog}\left(2, -\frac{(a-ib)e^{2i(c+d\sqrt[3]{x})}}{a+ib}\right)}{(a^2+b^2)^2d^3} + \frac{24bx^{7/3} \text{PolyLog}\left(2, -\frac{(a-ib)e^{2i(c+d\sqrt[3]{x})}}{a+ib}\right)}{(ia-b)(a-ib)^2d^2} \\
&- \frac{24b^2x^{7/3} \text{PolyLog}\left(2, -\frac{(a-ib)e^{2i(c+d\sqrt[3]{x})}}{a+ib}\right)}{(a^2+b^2)^2d^2} \\
&+ \frac{84bx^2 \text{PolyLog}\left(3, -\frac{(a-ib)e^{2i(c+d\sqrt[3]{x})}}{a+ib}\right)}{(a-ib)^2(a+ib)d^3} - \frac{84ib^2x^2 \text{PolyLog}\left(3, -\frac{(a-ib)e^{2i(c+d\sqrt[3]{x})}}{a+ib}\right)}{(a^2+b^2)^2d^3} \\
&- \frac{252bx^{5/3} \text{PolyLog}\left(4, -\frac{(a-ib)e^{2i(c+d\sqrt[3]{x})}}{a+ib}\right)}{(ia-b)(a-ib)^2d^4} \\
&+ \frac{(1260b) \text{Subst}\left(\int x^4 \text{PolyLog}\left(4, -\frac{\left(1-\frac{ib}{a}\right)e^{2ic+2idx}}{1+\frac{ib}{a}}\right) dx, x, \sqrt[3]{x}\right)}{(ia-b)(a-ib)^2d^4} \\
&+ \frac{(504ib^2) \text{Subst}\left(\int x^5 \text{PolyLog}\left(2, -\frac{\left(1-\frac{ib}{a}\right)e^{2ic+2idx}}{1+\frac{ib}{a}}\right) dx, x, \sqrt[3]{x}\right)}{(a^2+b^2)^2d^3} \\
&+ \frac{(504ib^2) \text{Subst}\left(\int x^5 \text{PolyLog}\left(3, -\frac{\left(1-\frac{ib}{a}\right)e^{2ic+2idx}}{1+\frac{ib}{a}}\right) dx, x, \sqrt[3]{x}\right)}{(a^2+b^2)^2d^3}
\end{aligned}$$

$$\begin{aligned}
&= -\frac{6ib^2x^{8/3}}{(a^2+b^2)^2d} - \frac{6b^2x^{8/3}}{(a-ib)^2(a+ib)d} \frac{e^{2i(c+d\sqrt[3]{x})}}{(ia-b+(ia+b)e^{2i(c+d\sqrt[3]{x})})} + \frac{x^3}{3(a-ib)^2} \\
&+ \frac{4bx^3}{3(ia-b)(a-ib)^2} - \frac{4b^2x^3}{3(a^2+b^2)^2} + \frac{24b^2x^{7/3} \log\left(1 + \frac{(a-ib)e^{2i(c+d\sqrt[3]{x})}}{a+ib}\right)}{(a^2+b^2)^2d^2} \\
&+ \frac{6bx^{8/3} \log\left(1 + \frac{(a-ib)e^{2i(c+d\sqrt[3]{x})}}{a+ib}\right)}{(a-ib)^2(a+ib)d} - \frac{6ib^2x^{8/3} \log\left(1 + \frac{(a-ib)e^{2i(c+d\sqrt[3]{x})}}{a+ib}\right)}{(a^2+b^2)^2d} \\
&- \frac{84ib^2x^2 \text{PolyLog}\left(2, -\frac{(a-ib)e^{2i(c+d\sqrt[3]{x})}}{a+ib}\right)}{(a^2+b^2)^2d^3} + \frac{24bx^{7/3} \text{PolyLog}\left(2, -\frac{(a-ib)e^{2i(c+d\sqrt[3]{x})}}{a+ib}\right)}{(ia-b)(a-ib)^2d^2} \\
&- \frac{24b^2x^{7/3} \text{PolyLog}\left(2, -\frac{(a-ib)e^{2i(c+d\sqrt[3]{x})}}{a+ib}\right)}{(a^2+b^2)^2d^2} \\
&+ \frac{252b^2x^{5/3} \text{PolyLog}\left(3, -\frac{(a-ib)e^{2i(c+d\sqrt[3]{x})}}{a+ib}\right)}{(a^2+b^2)^2d^4} \\
&+ \frac{84bx^2 \text{PolyLog}\left(3, -\frac{(a-ib)e^{2i(c+d\sqrt[3]{x})}}{a+ib}\right)}{(a-ib)^2(a+ib)d^3} - \frac{84ib^2x^2 \text{PolyLog}\left(3, -\frac{(a-ib)e^{2i(c+d\sqrt[3]{x})}}{a+ib}\right)}{(a^2+b^2)^2d^3} \\
&- \frac{252bx^{5/3} \text{PolyLog}\left(4, -\frac{(a-ib)e^{2i(c+d\sqrt[3]{x})}}{a+ib}\right)}{(ia-b)(a-ib)^2d^4} \\
&+ \frac{252b^2x^{5/3} \text{PolyLog}\left(4, -\frac{(a-ib)e^{2i(c+d\sqrt[3]{x})}}{a+ib}\right)}{(a^2+b^2)^2d^4} \\
&- \frac{630bx^{4/3} \text{PolyLog}\left(5, -\frac{(a-ib)e^{2i(c+d\sqrt[3]{x})}}{a+ib}\right)}{(a-ib)^2(a+ib)d^5} \\
&+ \frac{(2520b) \text{Subst}\left(\int x^3 \text{PolyLog}\left(5, -\frac{(1-\frac{ib}{a})e^{2ic+2idx}}{1+\frac{ib}{a}}\right) dx, x, \sqrt[3]{x}\right)}{(a-ib)^2(a+ib)d^5} \\
&- \frac{(1260b^2) \text{Subst}\left(\int x^4 \text{PolyLog}\left(3, -\frac{(1-\frac{ib}{a})e^{2ic+2idx}}{1+\frac{ib}{a}}\right) dx, x, \sqrt[3]{x}\right)}{(a^2+b^2)^2d^4} \\
&- \frac{(1260b^2) \text{Subst}\left(\int x^4 \text{PolyLog}\left(4, -\frac{(1-\frac{ib}{a})e^{2ic+2idx}}{1+\frac{ib}{a}}\right) dx, x, \sqrt[3]{x}\right)}{(a^2+b^2)^2d^4}
\end{aligned}$$

= Too large to display

Mathematica [A] (verified)

Time = 4.27 (sec) , antiderivative size = 1136, normalized size of antiderivative = 0.67

$$\int \frac{x^2}{(a + b \tan(c + d\sqrt[3]{x}))^2} dx$$

$$ib \left(18(a+ib)b(ia+b)d^8x^{8/3} + 4a(a+ib)(ia+b)d^9x^3 + 72(a-ib)bd^7(-ib(-1+e^{2ic})+a(1+e^{2ic}))x^{7/3} \log \left(1 + \frac{(a+ib)e^{-2i(c+d\sqrt[3]{x})}}{a-ib} \right) + 18a(a-ib)d^8 \right)$$

```
[In] Integrate[x^2/(a + b*Tan[c + d*x^(1/3)])^2,x]
```

```
[Out] (((-I)*b*(18*(a + I*b)*b*(I*a + b)*d^8*x^(8/3) + 4*a*(a + I*b)*(I*a + b)*d^9*x^3 + 72*(a - I*b)*b*d^7*((-I)*b*(-1 + E^((2*I)*c)) + a*(1 + E^((2*I)*c))) *x^(7/3)*Log[1 + (a + I*b)/((a - I*b)*E^((2*I)*(c + d*x^(1/3)))]) + 18*a*(a - I*b)*d^8*((-I)*b*(-1 + E^((2*I)*c)) + a*(1 + E^((2*I)*c)))*x^(8/3)*Log[1 + (a + I*b)/((a - I*b)*E^((2*I)*(c + d*x^(1/3)))]) + 63*b*(I*a + b)*(b*(-1 + E^((2*I)*c)) + I*a*(1 + E^((2*I)*c)))*((-4*I)*d^6*x^2*PolyLog[2, (-a - I*b)/((a - I*b)*E^((2*I)*(c + d*x^(1/3)))]) - 12*d^5*x^(5/3)*PolyLog[3, (-a - I*b)/((a - I*b)*E^((2*I)*(c + d*x^(1/3)))]) + (15*I)*(2*d^4*x^(4/3)*PolyLog[4, (-a - I*b)/((a - I*b)*E^((2*I)*(c + d*x^(1/3)))]) - (4*I)*d^3*x*PolyLog[5, (-a - I*b)/((a - I*b)*E^((2*I)*(c + d*x^(1/3)))]) - 6*d^2*x^(2/3)*PolyLog[6, (-a - I*b)/((a - I*b)*E^((2*I)*(c + d*x^(1/3)))]) + (6*I)*d*x^(1/3)*PolyLog[7, (-a - I*b)/((a - I*b)*E^((2*I)*(c + d*x^(1/3)))]) + 3*PolyLog[8, (-a - I*b)/((a - I*b)*E^((2*I)*(c + d*x^(1/3)))])]) + 9*a*(a - I*b)*((-I)*b*(-1 + E^((2*I)*c)) + a*(1 + E^((2*I)*c)))*((8*I)*d^7*x^(7/3)*PolyLog[2, (-a - I*b)/((a - I*b)*E^((2*I)*(c + d*x^(1/3)))]) + 28*d^6*x^2*PolyLog[3, (-a - I*b)/((a - I*b)*E^((2*I)*(c + d*x^(1/3)))]) - (84*I)*d^5*x^(5/3)*PolyLog[4, (-a - I*b)/((a - I*b)*E^((2*I)*(c + d*x^(1/3)))]) - 105*(2*d^4*x^(4/3)*PolyLog[5, (-a - I*b)/((a - I*b)*E^((2*I)*(c + d*x^(1/3)))]) - (4*I)*d^3*x*PolyLog[6, (-a - I*b)/((a - I*b)*E^((2*I)*(c + d*x^(1/3)))]) - 6*d^2*x^(2/3)*PolyLog[7, (-a - I*b)/((a - I*b)*E^((2*I)*(c + d*x^(1/3)))]) + (6*I)*d*x^(1/3)*PolyLog[8, (-a - I*b)/((a - I*b)*E^((2*I)*(c + d*x^(1/3)))]) + 3*PolyLog[9, (-a - I*b)/((a - I*b)*E^((2*I)*(c + d*x^(1/3)))])])]/(d^9*(b - b *E^((2*I)*c) - I*a*(1 + E^((2*I)*c))) + ((a - I*b)^2*(a + I*b)*x^3*(a*Cos[c] - b*Sin[c]))/(a*Cos[c] + b*Sin[c]) + (9*(a - I*b)^2*(a + I*b)*b^2*x^(8/3)*Sin[d*x^(1/3)]/(d*(a*Cos[c] + b*Sin[c])*(a*Cos[c + d*x^(1/3)] + b*Sin[c + d*x^(1/3)])))/(3*(a - I*b)^3*(a + I*b)^2)
```

Maple [F]

$$\int \frac{x^2}{\left(a + b \tan\left(c + d x^{\frac{1}{3}}\right)\right)^2} dx$$

[In] int(x^2/(a+b*tan(c+d*x^(1/3)))^2,x)

[Out] int(x^2/(a+b*tan(c+d*x^(1/3)))^2,x)

Fricas [F]

$$\int \frac{x^2}{\left(a + b \tan\left(c + d \sqrt[3]{x}\right)\right)^2} dx = \int \frac{x^2}{\left(b \tan\left(d x^{\frac{1}{3}} + c\right) + a\right)^2} dx$$

[In] integrate(x^2/(a+b*tan(c+d*x^(1/3)))^2,x, algorithm="fricas")

[Out] integral(x^2/(b^2*tan(d*x^(1/3) + c)^2 + 2*a*b*tan(d*x^(1/3) + c) + a^2), x)

Sympy [F]

$$\int \frac{x^2}{\left(a + b \tan\left(c + d \sqrt[3]{x}\right)\right)^2} dx = \int \frac{x^2}{\left(a + b \tan\left(c + d \sqrt[3]{x}\right)\right)^2} dx$$

[In] integrate(x**2/(a+b*tan(c+d*x**(1/3)))**2,x)

[Out] Integral(x**2/(a + b*tan(c + d*x**(1/3)))**2, x)

Maxima [B] (verification not implemented)

Both result and optimal contain complex but leaf count of result is larger than twice the leaf count of optimal. 8152 vs. $2(1362) = 2724$.

Time = 2.64 (sec) , antiderivative size = 8152, normalized size of antiderivative = 4.82

$$\int \frac{x^2}{\left(a + b \tan\left(c + d \sqrt[3]{x}\right)\right)^2} dx = \text{Too large to display}$$

[In] integrate(x^2/(a+b*tan(c+d*x^(1/3)))^2,x, algorithm="maxima")

[Out] $\frac{1}{105} \cdot (315 \cdot (2 \cdot a \cdot b \cdot \log(b \cdot \tan(d \cdot x^{\frac{1}{3}} + c) + a) / (a^4 + 2 \cdot a^2 \cdot b^2 + b^4) - a \cdot b \cdot \log(\tan(d \cdot x^{\frac{1}{3}} + c)^2 + 1) / (a^4 + 2 \cdot a^2 \cdot b^2 + b^4) + (a^2 - b^2) \cdot (d \cdot x$

$$\begin{aligned}
& (I*a*b^2 + b^3)*c^6)*(d*x^{(1/3)} + c)^2*\cos(2*d*x^{(1/3)} + 2*c) - 1260*(32* \\
& (I*a^2*b - a*b^2)*(d*x^{(1/3)} + c)^7 + 2*(-I*a^2*b + a*b^2)*c^7 + 64*(I*a*b^2 \\
& 2 - b^3 + 2*(-I*a^2*b + a*b^2)*c)*(d*x^{(1/3)} + c)^6 + 7*(I*a*b^2 - b^3)*c^6 \\
& + 224*((I*a^2*b - a*b^2)*c^2 + (-I*a*b^2 + b^3)*c)*(d*x^{(1/3)} + c)^5 + 112 \\
& *(2*(-I*a^2*b + a*b^2)*c^3 + 3*(I*a*b^2 - b^3)*c^2)*(d*x^{(1/3)} + c)^4 + 140 \\
& *((I*a^2*b - a*b^2)*c^4 + 2*(-I*a*b^2 + b^3)*c^3)*(d*x^{(1/3)} + c)^3 + 28*(2 \\
& *(-I*a^2*b + a*b^2)*c^5 + 5*(I*a*b^2 - b^3)*c^4)*(d*x^{(1/3)} + c)^2 + 14*((I \\
& *a^2*b - a*b^2)*c^6 + 3*(-I*a*b^2 + b^3)*c^5)*(d*x^{(1/3)} + c) + (32*(I*a^2* \\
& b + a*b^2)*(d*x^{(1/3)} + c)^7 + 2*(-I*a^2*b - a*b^2)*c^7 + 64*(I*a*b^2 + b^3 \\
& + 2*(-I*a^2*b - a*b^2)*c)*(d*x^{(1/3)} + c)^6 + 7*(I*a*b^2 + b^3)*c^6 + 224* \\
& ((I*a^2*b + a*b^2)*c^2 + (-I*a*b^2 - b^3)*c)*(d*x^{(1/3)} + c)^5 + 112*(2*(-I \\
& *a^2*b - a*b^2)*c^3 + 3*(I*a*b^2 + b^3)*c^2)*(d*x^{(1/3)} + c)^4 + 140*((I*a^ \\
& 2*b + a*b^2)*c^4 + 2*(-I*a*b^2 - b^3)*c^3)*(d*x^{(1/3)} + c)^3 + 28*(2*(-I*a^ \\
& 2*b - a*b^2)*c^5 + 5*(I*a*b^2 + b^3)*c^4)*(d*x^{(1/3)} + c)^2 + 14*((I*a^2*b \\
& + a*b^2)*c^6 + 3*(-I*a*b^2 - b^3)*c^5)*(d*x^{(1/3)} + c))*\cos(2*d*x^{(1/3)} + 2 \\
& *c) - (32*(a^2*b - I*a*b^2)*(d*x^{(1/3)} + c)^7 - 2*(a^2*b - I*a*b^2)*c^7 + 6 \\
& 4*(a*b^2 - I*b^3 - 2*(a^2*b - I*a*b^2)*c)*(d*x^{(1/3)} + c)^6 + 7*(a*b^2 - I* \\
& b^3)*c^6 + 224*((a^2*b - I*a*b^2)*c^2 - (a*b^2 - I*b^3)*c)*(d*x^{(1/3)} + c)^ \\
& 5 - 112*(2*(a^2*b - I*a*b^2)*c^3 - 3*(a*b^2 - I*b^3)*c^2)*(d*x^{(1/3)} + c)^4 \\
& + 140*((a^2*b - I*a*b^2)*c^4 - 2*(a*b^2 - I*b^3)*c^3)*(d*x^{(1/3)} + c)^3 - \\
& 28*(2*(a^2*b - I*a*b^2)*c^5 - 5*(a*b^2 - I*b^3)*c^4)*(d*x^{(1/3)} + c)^2 + 14 \\
& *((a^2*b - I*a*b^2)*c^6 - 3*(a*b^2 - I*b^3)*c^5)*(d*x^{(1/3)} + c))*\sin(2*d*x \\
& ^{(1/3)} + 2*c))*\operatorname{dilog}((I*a + b)*e^{(2*I*d*x^{(1/3)} + 2*I*c)/(-I*a + b)} - 1260 \\
& *((a*b^2 - I*b^3)*c^7*\cos(2*d*x^{(1/3)} + 2*c) + (I*a*b^2 + b^3)*c^7*\sin(2*d* \\
& x^{(1/3)} + 2*c) + (a*b^2 + I*b^3)*c^7)*\log((a^2 + b^2)*\cos(2*d*x^{(1/3)} + 2*c \\
&)^2 + 4*a*b*\sin(2*d*x^{(1/3)} + 2*c) + (a^2 + b^2)*\sin(2*d*x^{(1/3)} + 2*c)^2 + \\
& a^2 + b^2 + 2*(a^2 - b^2)*\cos(2*d*x^{(1/3)} + 2*c)) + 12*(420*(a^2*b + I*a*b \\
& ^2)*(d*x^{(1/3)} + c)^8 + 960*(a*b^2 + I*b^3 - 2*(a^2*b + I*a*b^2)*c)*(d*x^{(1 \\
& /3)} + c)^7 + 3920*((a^2*b + I*a*b^2)*c^2 - (a*b^2 + I*b^3)*c)*(d*x^{(1/3)} + \\
& c)^6 - 2352*(2*(a^2*b + I*a*b^2)*c^3 - 3*(a*b^2 + I*b^3)*c^2)*(d*x^{(1/3)} + \\
& c)^5 + 3675*((a^2*b + I*a*b^2)*c^4 - 2*(a*b^2 + I*b^3)*c^3)*(d*x^{(1/3)} + c) \\
& ^4 - 980*(2*(a^2*b + I*a*b^2)*c^5 - 5*(a*b^2 + I*b^3)*c^4)*(d*x^{(1/3)} + c)^ \\
& 3 + 735*((a^2*b + I*a*b^2)*c^6 - 3*(a*b^2 + I*b^3)*c^5)*(d*x^{(1/3)} + c)^2 - \\
& 105*(2*(a^2*b + I*a*b^2)*c^7 - 7*(a*b^2 + I*b^3)*c^6)*(d*x^{(1/3)} + c) + (4 \\
& 20*(a^2*b - I*a*b^2)*(d*x^{(1/3)} + c)^8 + 960*(a*b^2 - I*b^3 - 2*(a^2*b - I* \\
& a*b^2)*c)*(d*x^{(1/3)} + c)^7 + 3920*((a^2*b - I*a*b^2)*c^2 - (a*b^2 - I*b^3) \\
& *c)*(d*x^{(1/3)} + c)^6 - 2352*(2*(a^2*b - I*a*b^2)*c^3 - 3*(a*b^2 - I*b^3)*c \\
& ^2)*(d*x^{(1/3)} + c)^5 + 3675*((a^2*b - I*a*b^2)*c^4 - 2*(a*b^2 - I*b^3)*c^3 \\
&)*(d*x^{(1/3)} + c)^4 - 980*(2*(a^2*b - I*a*b^2)*c^5 - 5*(a*b^2 - I*b^3)*c^4) \\
& *(d*x^{(1/3)} + c)^3 + 735*((a^2*b - I*a*b^2)*c^6 - 3*(a*b^2 - I*b^3)*c^5)*(d \\
& *x^{(1/3)} + c)^2 - 105*(2*(a^2*b - I*a*b^2)*c^7 - 7*(a*b^2 - I*b^3)*c^6)*(d* \\
& x^{(1/3)} + c))*\cos(2*d*x^{(1/3)} + 2*c) - (420*(-I*a^2*b - a*b^2)*(d*x^{(1/3)} + \\
& c)^8 + 960*(-I*a*b^2 - b^3 + 2*(I*a^2*b + a*b^2)*c)*(d*x^{(1/3)} + c)^7 + 39 \\
& 20*((-I*a^2*b - a*b^2)*c^2 + (I*a*b^2 + b^3)*c)*(d*x^{(1/3)} + c)^6 + 2352*(2 \\
& *(I*a^2*b + a*b^2)*c^3 + 3*(-I*a*b^2 - b^3)*c^2)*(d*x^{(1/3)} + c)^5 + 3675*(
\end{aligned}$$

$$\begin{aligned}
& (-Ia^2b - ab^2)c^4 + 2*(Ia*b^2 + b^3)c^3*(dx^{(1/3)} + c)^4 + 980*(2*(Ia^2b + ab^2)c^5 + 5*(-Ia*b^2 - b^3)c^4)*(dx^{(1/3)} + c)^3 + 735*((-Ia^2b - ab^2)c^6 + 3*(Ia*b^2 + b^3)c^5)*(dx^{(1/3)} + c)^2 + 105*(2*(Ia^2b + ab^2)c^7 + 7*(-Ia*b^2 - b^3)c^6)*(dx^{(1/3)} + c))*\sin(2*dx^{(1/3)} + 2*c))*\log(((a^2 + b^2)*\cos(2*dx^{(1/3)} + 2*c))^2 + 4*a*b*\sin(2*dx^{(1/3)} + 2*c) + (a^2 + b^2)*\sin(2*dx^{(1/3)} + 2*c)^2 + a^2 + b^2 + 2*(a^2 - b^2)*\cos(2*dx^{(1/3)} + 2*c))/(a^2 + b^2)) - 1587600*(a^2*b + Ia*b^2 + (a^2*b - Ia*b^2)*\cos(2*dx^{(1/3)} + 2*c) + (Ia^2*b + ab^2)*\sin(2*dx^{(1/3)} + 2*c))*\text{polylog}(9, (Ia + b)*e^{(2*I*dx^{(1/3)} + 2*I*c)/(-Ia + b)}) - 453600*(-2*Ia*b^2 + 2*b^3 + 7*(-Ia^2*b + ab^2)*(dx^{(1/3)} + c) + 4*(Ia^2*b - ab^2)*c + (-2*Ia*b^2 - 2*b^3 + 7*(-Ia^2*b - ab^2)*(dx^{(1/3)} + c) + 4*(Ia^2*b + ab^2)*c)*\cos(2*dx^{(1/3)} + 2*c) + (2*a*b^2 - 2*I*b^3 + 7*(a^2*b - Ia*b^2)*(dx^{(1/3)} + c) - 4*(a^2*b - Ia*b^2)*c)*\sin(2*dx^{(1/3)} + 2*c))*\text{polylog}(8, (Ia + b)*e^{(2*I*dx^{(1/3)} + 2*I*c)/(-Ia + b)}) + 151200*(21*(a^2*b + Ia*b^2)*(dx^{(1/3)} + c)^2 + 7*(a^2*b + Ia*b^2)*c^2 + 12*(a*b^2 + I*b^3 - 2*(a^2*b + Ia*b^2)*c)*(dx^{(1/3)} + c) - 7*(a*b^2 + I*b^3)*c + (21*(a^2*b - Ia*b^2)*(dx^{(1/3)} + c)^2 + 7*(a^2*b - Ia*b^2)*c^2 + 12*(a*b^2 - I*b^3 - 2*(a^2*b - Ia*b^2)*c)*(dx^{(1/3)} + c) - 7*(a*b^2 - I*b^3)*c)*\cos(2*dx^{(1/3)} + 2*c) - (21*(-Ia^2*b - ab^2)*(dx^{(1/3)} + c)^2 + 7*(-Ia^2*b - ab^2)*c^2 + 12*(-Ia*b^2 - b^3 + 2*(Ia^2*b + ab^2)*c)*(dx^{(1/3)} + c) + 7*(Ia*b^2 + b^3)*c)*\sin(2*dx^{(1/3)} + 2*c))*\text{polylog}(7, (Ia + b)*e^{(2*I*dx^{(1/3)} + 2*I*c)/(-Ia + b)}) - 30240*(70*(Ia^2*b - ab^2)*(dx^{(1/3)} + c)^3 + 14*(-Ia^2*b + ab^2)*c^3 + 60*(Ia*b^2 - b^3 + 2*(-Ia^2*b + ab^2)*c)*(dx^{(1/3)} + c)^2 + 21*(Ia*b^2 - b^3)*c^2 + 70*((Ia^2*b - ab^2)*c^2 + (-Ia*b^2 + b^3)*c)*(dx^{(1/3)} + c) + (70*(Ia^2*b + ab^2)*(dx^{(1/3)} + c)^3 + 14*(-Ia^2*b - ab^2)*c^3 + 60*(Ia*b^2 + b^3 + 2*(-Ia^2*b - ab^2)*c)*(dx^{(1/3)} + c)^2 + 21*(Ia*b^2 + b^3)*c^2 + 70*((Ia^2*b + ab^2)*c^2 + (-Ia*b^2 - b^3)*c)*(dx^{(1/3)} + c))*\cos(2*dx^{(1/3)} + 2*c) - (70*(a^2*b - Ia*b^2)*(dx^{(1/3)} + c)^3 - 14*(a^2*b - Ia*b^2)*c^3 + 60*(a*b^2 - I*b^3 - 2*(a^2*b - Ia*b^2)*c)*(dx^{(1/3)} + c)^2 + 21*(a*b^2 - I*b^3)*c^2 + 70*((a^2*b - Ia*b^2)*c^2 - (a*b^2 - I*b^3)*c)*(dx^{(1/3)} + c))*\sin(2*dx^{(1/3)} + 2*c))*\text{polylog}(6, (Ia + b)*e^{(2*I*dx^{(1/3)} + 2*I*c)/(-Ia + b)}) - 3780*(280*(a^2*b + Ia*b^2)*(dx^{(1/3)} + c)^4 + 35*(a^2*b + Ia*b^2)*c^4 + 320*(a*b^2 + I*b^3 - 2*(a^2*b + Ia*b^2)*c)*(dx^{(1/3)} + c)^3 - 70*(a*b^2 + I*b^3)*c^3 + 560*((a^2*b + Ia*b^2)*c^2 - (a*b^2 + I*b^3)*c)*(dx^{(1/3)} + c)^2 - 112*(2*(a^2*b + Ia*b^2)*c^3 - 3*(a*b^2 + I*b^3)*c^2)*(dx^{(1/3)} + c) + (280*(a^2*b - Ia*b^2)*(dx^{(1/3)} + c)^4 + 35*(a^2*b - Ia*b^2)*c^4 + 320*(a*b^2 - I*b^3 - 2*(a^2*b - Ia*b^2)*c)*(dx^{(1/3)} + c)^3 - 70*(a*b^2 - I*b^3)*c^3 + 560*((a^2*b - Ia*b^2)*c^2 - (a*b^2 - I*b^3)*c)*(dx^{(1/3)} + c)^2 - 112*(2*(a^2*b - Ia*b^2)*c^3 - 3*(a*b^2 - I*b^3)*c^2)*(dx^{(1/3)} + c))*\cos(2*dx^{(1/3)} + 2*c) + (280*(Ia^2*b + ab^2)*(dx^{(1/3)} + c)^4 + 35*(Ia^2*b + ab^2)*c^4 + 320*(Ia*b^2 + b^3 + 2*(-Ia^2*b - ab^2)*c)*(dx^{(1/3)} + c)^3 + 70*(-Ia*b^2 - b^3)*c^3 + 560*((Ia^2*b + ab^2)*c^2 + (-Ia*b^2 - b^3)*c)*(dx^{(1/3)} + c)^2 + 112*(2*(-Ia^2*b - ab^2)*c^3 + 3*(Ia*b^2 + b^3)*c^2)*(dx^{(1/3)} + c))*\sin(2*dx^{(1/3)} + 2*c))*\text{polylog}(5, (Ia + b)*e^{(2*I*dx^{(1/3)} + 2*I*c)/(-Ia + b)})
\end{aligned}$$

$$\begin{aligned}
& 1/3) + 2*I*c)/(-I*a + b)) - 2520*(168*(-I*a^2*b + a*b^2)*(d*x^(1/3) + c)^5 \\
& + 14*(I*a^2*b - a*b^2)*c^5 + 240*(-I*a*b^2 + b^3 + 2*(I*a^2*b - a*b^2)*c)*(\\
& d*x^(1/3) + c)^4 + 35*(-I*a*b^2 + b^3)*c^4 + 560*((-I*a^2*b + a*b^2)*c^2 + \\
& (I*a*b^2 - b^3)*c)*(d*x^(1/3) + c)^3 + 168*(2*(I*a^2*b - a*b^2)*c^3 + 3*(-I \\
& *a*b^2 + b^3)*c^2)*(d*x^(1/3) + c)^2 + 105*((-I*a^2*b + a*b^2)*c^4 + 2*(I*a \\
& *b^2 - b^3)*c^3)*(d*x^(1/3) + c) + (168*(-I*a^2*b - a*b^2)*(d*x^(1/3) + c)^ \\
& 5 + 14*(I*a^2*b + a*b^2)*c^5 + 240*(-I*a*b^2 - b^3 + 2*(I*a^2*b + a*b^2)*c) \\
& *(d*x^(1/3) + c)^4 + 35*(-I*a*b^2 - b^3)*c^4 + 560*((-I*a^2*b - a*b^2)*c^2 \\
& + (I*a*b^2 + b^3)*c)*(d*x^(1/3) + c)^3 + 168*(2*(I*a^2*b + a*b^2)*c^3 + 3*(\\
& -I*a*b^2 - b^3)*c^2)*(d*x^(1/3) + c)^2 + 105*((-I*a^2*b - a*b^2)*c^4 + 2*(I \\
& *a*b^2 + b^3)*c^3)*(d*x^(1/3) + c))*cos(2*d*x^(1/3) + 2*c) + (168*(a^2*b - \\
& I*a*b^2)*(d*x^(1/3) + c)^5 - 14*(a^2*b - I*a*b^2)*c^5 + 240*(a*b^2 - I*b^3 \\
& - 2*(a^2*b - I*a*b^2)*c)*(d*x^(1/3) + c)^4 + 35*(a*b^2 - I*b^3)*c^4 + 560*(\\
& (a^2*b - I*a*b^2)*c^2 - (a*b^2 - I*b^3)*c)*(d*x^(1/3) + c)^3 - 168*(2*(a^2*b \\
& b - I*a*b^2)*c^3 - 3*(a*b^2 - I*b^3)*c^2)*(d*x^(1/3) + c)^2 + 105*((a^2*b - \\
& I*a*b^2)*c^4 - 2*(a*b^2 - I*b^3)*c^3)*(d*x^(1/3) + c))*sin(2*d*x^(1/3) + 2 \\
& *c))*polylog(4, (I*a + b)*e^(2*I*d*x^(1/3) + 2*I*c)/(-I*a + b)) + 1260*(112 \\
& *(a^2*b + I*a*b^2)*(d*x^(1/3) + c)^6 + 7*(a^2*b + I*a*b^2)*c^6 + 192*(a*b^2 \\
& + I*b^3 - 2*(a^2*b + I*a*b^2)*c)*(d*x^(1/3) + c)^5 - 21*(a*b^2 + I*b^3)*c^ \\
& 5 + 560*((a^2*b + I*a*b^2)*c^2 - (a*b^2 + I*b^3)*c)*(d*x^(1/3) + c)^4 - 224 \\
& *(2*(a^2*b + I*a*b^2)*c^3 - 3*(a*b^2 + I*b^3)*c^2)*(d*x^(1/3) + c)^3 + 210* \\
& ((a^2*b + I*a*b^2)*c^4 - 2*(a*b^2 + I*b^3)*c^3)*(d*x^(1/3) + c)^2 - 28*(2*(\\
& a^2*b + I*a*b^2)*c^5 - 5*(a*b^2 + I*b^3)*c^4)*(d*x^(1/3) + c) + (112*(a^2*b \\
& - I*a*b^2)*(d*x^(1/3) + c)^6 + 7*(a^2*b - I*a*b^2)*c^6 + 192*(a*b^2 - I*b^ \\
& 3 - 2*(a^2*b - I*a*b^2)*c)*(d*x^(1/3) + c)^5 - 21*(a*b^2 - I*b^3)*c^5 + 560 \\
& *((a^2*b - I*a*b^2)*c^2 - (a*b^2 - I*b^3)*c)*(d*x^(1/3) + c)^4 - 224*(2*(a^ \\
& 2*b - I*a*b^2)*c^3 - 3*(a*b^2 - I*b^3)*c^2)*(d*x^(1/3) + c)^3 + 210*((a^2*b \\
& - I*a*b^2)*c^4 - 2*(a*b^2 - I*b^3)*c^3)*(d*x^(1/3) + c)^2 - 28*(2*(a^2*b - \\
& I*a*b^2)*c^5 - 5*(a*b^2 - I*b^3)*c^4)*(d*x^(1/3) + c))*cos(2*d*x^(1/3) + 2 \\
& *c) - (112*(-I*a^2*b - a*b^2)*(d*x^(1/3) + c)^6 + 7*(-I*a^2*b - a*b^2)*c^6 \\
& + 192*(-I*a*b^2 - b^3 + 2*(I*a^2*b + a*b^2)*c)*(d*x^(1/3) + c)^5 + 21*(I*a* \\
& b^2 + b^3)*c^5 + 560*((-I*a^2*b - a*b^2)*c^2 + (I*a*b^2 + b^3)*c)*(d*x^(1/3 \\
&) + c)^4 + 224*(2*(I*a^2*b + a*b^2)*c^3 + 3*(-I*a*b^2 - b^3)*c^2)*(d*x^(1/3 \\
&) + c)^3 + 210*((-I*a^2*b - a*b^2)*c^4 + 2*(I*a*b^2 + b^3)*c^3)*(d*x^(1/3) \\
& + c)^2 + 28*(2*(I*a^2*b + a*b^2)*c^5 + 5*(-I*a*b^2 - b^3)*c^4)*(d*x^(1/3) + \\
& c))*sin(2*d*x^(1/3) + 2*c))*polylog(3, (I*a + b)*e^(2*I*d*x^(1/3) + 2*I*c) \\
& /(-I*a + b)) - 35*((-I*a^3 - 3*a^2*b + 3*I*a*b^2 + b^3)*(d*x^(1/3) + c)^9 - \\
& 9*(2*a*b^2 - 2*I*b^3 - (I*a^3 + 3*a^2*b - 3*I*a*b^2 - b^3)*c)*(d*x^(1/3) + \\
& c)^8 + 144*(a*b^2 - I*b^3)*(d*x^(1/3) + c)*c^7 + 36*((-I*a^3 - 3*a^2*b + 3 \\
& *I*a*b^2 + b^3)*c^2 + 4*(a*b^2 - I*b^3)*c)*(d*x^(1/3) + c)^7 + 84*((I*a^3 + \\
& 3*a^2*b - 3*I*a*b^2 - b^3)*c^3 - 6*(a*b^2 - I*b^3)*c^2)*(d*x^(1/3) + c)^6 \\
& + 126*((-I*a^3 - 3*a^2*b + 3*I*a*b^2 + b^3)*c^4 + 8*(a*b^2 - I*b^3)*c^3)*(d \\
& *x^(1/3) + c)^5 + 126*((I*a^3 + 3*a^2*b - 3*I*a*b^2 - b^3)*c^5 - 10*(a*b^2 \\
& - I*b^3)*c^4)*(d*x^(1/3) + c)^4 + 84*((-I*a^3 - 3*a^2*b + 3*I*a*b^2 + b^3)* \\
& c^6 + 12*(a*b^2 - I*b^3)*c^5)*(d*x^(1/3) + c)^3 + 36*((I*a^3 + 3*a^2*b - 3*
\end{aligned}$$

$$\frac{I*a*b^2 - b^3)*c^7 - 14*(a*b^2 - I*b^3)*c^6)*(d*x^{(1/3)} + c)^2*\sin(2*d*x^{(1/3)} + 2*c))/(a^5 + I*a^4*b + 2*a^3*b^2 + 2*I*a^2*b^3 + a*b^4 + I*b^5 + (a^5 - I*a^4*b + 2*a^3*b^2 - 2*I*a^2*b^3 + a*b^4 - I*b^5)*\cos(2*d*x^{(1/3)} + 2*c) - (-I*a^5 - a^4*b - 2*I*a^3*b^2 - 2*a^2*b^3 - I*a*b^4 - b^5)*\sin(2*d*x^{(1/3)} + 2*c)))/d^9$$

Giac [F]

$$\int \frac{x^2}{(a + b \tan(c + d\sqrt[3]{x}))^2} dx = \int \frac{x^2}{(b \tan(dx^{\frac{1}{3}} + c) + a)^2} dx$$

[In] integrate(x^2/(a+b*tan(c+d*x^(1/3)))^2,x, algorithm="giac")

[Out] integrate(x^2/(b*tan(d*x^(1/3) + c) + a)^2, x)

Mupad [F(-1)]

Timed out.

$$\int \frac{x^2}{(a + b \tan(c + d\sqrt[3]{x}))^2} dx = \int \frac{x^2}{(a + b \tan(c + dx^{1/3}))^2} dx$$

[In] int(x^2/(a + b*tan(c + d*x^(1/3)))^2,x)

[Out] int(x^2/(a + b*tan(c + d*x^(1/3)))^2, x)

3.63
$$\int \frac{x}{\left(a+b \tan \left(c+d \sqrt[3]{x}\right)\right)^2} dx$$

Optimal result	420
Rubi [A] (verified)	421
Mathematica [A] (verified)	433
Maple [F]	433
Fricas [F]	434
Sympy [F]	434
Maxima [B] (verification not implemented)	434
Giac [F]	437
Mupad [F(-1)]	437

Optimal result

Integrand size = 18, antiderivative size = 1155

$$\begin{aligned}
 \int \frac{x}{(a + b \tan(c + d\sqrt[3]{x}))^2} dx = & -\frac{6ib^2x^{5/3}}{(a^2 + b^2)^2 d} \\
 & + \frac{6b^2x^{5/3}}{(a + ib)(ia + b)^2 d (ia - b + (ia + b)e^{2i(c+d\sqrt[3]{x})})} \\
 & + \frac{x^2}{2(a - ib)^2} + \frac{2bx^2}{(ia - b)(a - ib)^2} - \frac{2b^2x^2}{(a^2 + b^2)^2} \\
 & + \frac{15b^2x^{4/3} \log\left(1 + \frac{(a-ib)e^{2i(c+d\sqrt[3]{x})}}{a+ib}\right)}{(a^2 + b^2)^2 d^2} \\
 & + \frac{6bx^{5/3} \log\left(1 + \frac{(a-ib)e^{2i(c+d\sqrt[3]{x})}}{a+ib}\right)}{(a - ib)^2(a + ib)d} \\
 & - \frac{6ib^2x^{5/3} \log\left(1 + \frac{(a-ib)e^{2i(c+d\sqrt[3]{x})}}{a+ib}\right)}{(a^2 + b^2)^2 d} \\
 & - \frac{30ib^2x \operatorname{PolyLog}\left(2, -\frac{(a-ib)e^{2i(c+d\sqrt[3]{x})}}{a+ib}\right)}{(a^2 + b^2)^2 d^3} \\
 & + \frac{15bx^{4/3} \operatorname{PolyLog}\left(2, -\frac{(a-ib)e^{2i(c+d\sqrt[3]{x})}}{a+ib}\right)}{(ia - b)(a - ib)^2 d^2} \\
 & - \frac{15b^2x^{4/3} \operatorname{PolyLog}\left(2, -\frac{(a-ib)e^{2i(c+d\sqrt[3]{x})}}{a+ib}\right)}{(a^2 + b^2)^2 d^2} \\
 & + \frac{45b^2x^{2/3} \operatorname{PolyLog}\left(3, -\frac{(a-ib)e^{2i(c+d\sqrt[3]{x})}}{a+ib}\right)}{(a^2 + b^2)^2 d^4} \\
 & + \frac{30bx \operatorname{PolyLog}\left(3, -\frac{(a-ib)e^{2i(c+d\sqrt[3]{x})}}{a+ib}\right)}{(a - ib)^2(a + ib)d^3} \\
 & - \frac{30ib^2x \operatorname{PolyLog}\left(3, -\frac{(a-ib)e^{2i(c+d\sqrt[3]{x})}}{a+ib}\right)}{(a^2 + b^2)^2 d^3} \\
 & + \frac{45ib^2\sqrt[3]{x} \operatorname{PolyLog}\left(4, -\frac{(a-ib)e^{2i(c+d\sqrt[3]{x})}}{a+ib}\right)}{(a^2 + b^2)^2 d^5} \\
 & - \frac{45bx^{2/3} \operatorname{PolyLog}\left(4, -\frac{(a-ib)e^{2i(c+d\sqrt[3]{x})}}{a+ib}\right)}{(ia - b)(a - ib)^2 d^4} \\
 & + \frac{45b^2x^{2/3} \operatorname{PolyLog}\left(4, -\frac{(a-ib)e^{2i(c+d\sqrt[3]{x})}}{a+ib}\right)}{(a^2 + b^2)^2 d^4}
 \end{aligned}$$

```
[Out] -6*I*b^2*x^(5/3)*ln(1+(a-I*b)*exp(2*I*(c+d*x^(1/3)))/(a+I*b))/(a^2+b^2)^2/d
+6*b^2*x^(5/3)/(a+I*b)/(I*a+b)^2/d/(I*a-b+(I*a+b)*exp(2*I*(c+d*x^(1/3))))+1
/2*x^2/(a-I*b)^2+2*b*x^2/(I*a-b)/(a-I*b)^2-2*b^2*x^2/(a^2+b^2)^2+15*b^2*x^(
4/3)*ln(1+(a-I*b)*exp(2*I*(c+d*x^(1/3)))/(a+I*b))/(a^2+b^2)^2/d^2+6*b*x^(5/
3)*ln(1+(a-I*b)*exp(2*I*(c+d*x^(1/3)))/(a+I*b))/(a-I*b)^2/(a+I*b)/d+45*I*b^
2*x^(1/3)*polylog(4,-(a-I*b)*exp(2*I*(c+d*x^(1/3)))/(a+I*b))/(a^2+b^2)^2/d^
5-30*I*b^2*x*polylog(2,-(a-I*b)*exp(2*I*(c+d*x^(1/3)))/(a+I*b))/(a^2+b^2)^2
/d^3+15*b*x^(4/3)*polylog(2,-(a-I*b)*exp(2*I*(c+d*x^(1/3)))/(a+I*b))/(I*a-b
)/(a-I*b)^2/d^2-15*b^2*x^(4/3)*polylog(2,-(a-I*b)*exp(2*I*(c+d*x^(1/3)))/(a
+I*b))/(a^2+b^2)^2/d^2+45*b^2*x^(2/3)*polylog(3,-(a-I*b)*exp(2*I*(c+d*x^(1/
3)))/(a+I*b))/(a^2+b^2)^2/d^4+30*b*x*polylog(3,-(a-I*b)*exp(2*I*(c+d*x^(1/3
)))/(a+I*b))/(a-I*b)^2/(a+I*b)/d^3-30*I*b^2*x*polylog(3,-(a-I*b)*exp(2*I*(c
+d*x^(1/3)))/(a+I*b))/(a^2+b^2)^2/d^3+45*I*b^2*x^(1/3)*polylog(5,-(a-I*b)*e
xp(2*I*(c+d*x^(1/3)))/(a+I*b))/(a^2+b^2)^2/d^5-45*b*x^(2/3)*polylog(4,-(a-I
*b)*exp(2*I*(c+d*x^(1/3)))/(a+I*b))/(I*a-b)/(a-I*b)^2/d^4+45*b^2*x^(2/3)*po
lylog(4,-(a-I*b)*exp(2*I*(c+d*x^(1/3)))/(a+I*b))/(a^2+b^2)^2/d^4-45/2*b^2*p
olylog(5,-(a-I*b)*exp(2*I*(c+d*x^(1/3)))/(a+I*b))/(a^2+b^2)^2/d^6-45*b*x^(1
/3)*polylog(5,-(a-I*b)*exp(2*I*(c+d*x^(1/3)))/(a+I*b))/(a-I*b)^2/(a+I*b)/d^
5-6*I*b^2*x^(5/3)/(a^2+b^2)^2/d+45/2*b*polylog(6,-(a-I*b)*exp(2*I*(c+d*x^(1
/3)))/(a+I*b))/(I*a-b)/(a-I*b)^2/d^6-45/2*b^2*polylog(6,-(a-I*b)*exp(2*I*(c
+d*x^(1/3)))/(a+I*b))/(a^2+b^2)^2/d^6
```

Rubi [A] (verified)

Time = 2.43 (sec) , antiderivative size = 1155, normalized size of antiderivative = 1.00, number of steps used = 28, number of rules used = 10, $\frac{\text{number of rules}}{\text{integrand size}} = 0.556$, Rules

used = {3832, 3815, 2216, 2215, 2221, 2611, 6744, 2320, 6724, 2222}

$$\begin{aligned}
 \int \frac{x}{(a + b \tan(c + d\sqrt[3]{x}))^2} dx = & -\frac{2x^2b^2}{(a^2 + b^2)^2} - \frac{6ix^{5/3}b^2}{(a^2 + b^2)^2 d} \\
 & + \frac{6x^{5/3}b^2}{(a + ib)(ia + b)^2 d (ia + (ia + b)e^{2i(c+d\sqrt[3]{x})} - b)} \\
 & - \frac{6ix^{5/3} \log\left(\frac{e^{2i(c+d\sqrt[3]{x})}(a-ib)}{a+ib} + 1\right) b^2}{(a^2 + b^2)^2 d} \\
 & + \frac{15x^{4/3} \log\left(\frac{e^{2i(c+d\sqrt[3]{x})}(a-ib)}{a+ib} + 1\right) b^2}{(a^2 + b^2)^2 d^2} \\
 & - \frac{15x^{4/3} \text{PolyLog}\left(2, -\frac{(a-ib)e^{2i(c+d\sqrt[3]{x})}}{a+ib}\right) b^2}{(a^2 + b^2)^2 d^2} \\
 & - \frac{30ix \text{PolyLog}\left(2, -\frac{(a-ib)e^{2i(c+d\sqrt[3]{x})}}{a+ib}\right) b^2}{(a^2 + b^2)^2 d^3} \\
 & - \frac{30ix \text{PolyLog}\left(3, -\frac{(a-ib)e^{2i(c+d\sqrt[3]{x})}}{a+ib}\right) b^2}{(a^2 + b^2)^2 d^3} \\
 & + \frac{45x^{2/3} \text{PolyLog}\left(3, -\frac{(a-ib)e^{2i(c+d\sqrt[3]{x})}}{a+ib}\right) b^2}{(a^2 + b^2)^2 d^4} \\
 & + \frac{45x^{2/3} \text{PolyLog}\left(4, -\frac{(a-ib)e^{2i(c+d\sqrt[3]{x})}}{a+ib}\right) b^2}{(a^2 + b^2)^2 d^4} \\
 & + \frac{45i\sqrt[3]{x} \text{PolyLog}\left(4, -\frac{(a-ib)e^{2i(c+d\sqrt[3]{x})}}{a+ib}\right) b^2}{(a^2 + b^2)^2 d^5} \\
 & + \frac{45i\sqrt[3]{x} \text{PolyLog}\left(5, -\frac{(a-ib)e^{2i(c+d\sqrt[3]{x})}}{a+ib}\right) b^2}{(a^2 + b^2)^2 d^5} \\
 & - \frac{45 \text{PolyLog}\left(5, -\frac{(a-ib)e^{2i(c+d\sqrt[3]{x})}}{a+ib}\right) b^2}{2(a^2 + b^2)^2 d^6} \\
 & - \frac{45 \text{PolyLog}\left(6, -\frac{(a-ib)e^{2i(c+d\sqrt[3]{x})}}{a+ib}\right) b^2}{2(a^2 + b^2)^2 d^6} \\
 & + \frac{2x^2b}{(ia - b)(a - ib)^2} + \frac{6x^{5/3} \log\left(\frac{e^{2i(c+d\sqrt[3]{x})}(a-ib)}{a+ib} + 1\right) b}{(a - ib)^2(a + ib)d} \\
 & + \frac{15x^{4/3} \text{PolyLog}\left(2, -\frac{(a-ib)e^{2i(c+d\sqrt[3]{x})}}{a+ib}\right) b}{(a - ib)(a + ib)^2 d}
 \end{aligned}$$

[In] Int[x/(a + b*Tan[c + d*x^(1/3)])^2,x]

[Out]
$$\begin{aligned} &((-6*I)*b^2*x^{(5/3)})/((a^2 + b^2)^2*d) + (6*b^2*x^{(5/3)})/((a + I*b)*(I*a + b)^2*d*(I*a - b + (I*a + b)*E^{((2*I)*(c + d*x^{(1/3)})})) + x^2/(2*(a - I*b)^2) \\ &+ (2*b*x^2)/((I*a - b)*(a - I*b)^2) - (2*b^2*x^2)/(a^2 + b^2)^2 + (15*b^2*x^{(4/3)}*Log[1 + ((a - I*b)*E^{((2*I)*(c + d*x^{(1/3)})}))]/(a + I*b)]/((a^2 + b^2)^2*d^2) \\ &+ (6*b*x^{(5/3)}*Log[1 + ((a - I*b)*E^{((2*I)*(c + d*x^{(1/3)})}))]/(a + I*b)]/((a - I*b)^2*(a + I*b)*d) - ((6*I)*b^2*x^{(5/3)}*Log[1 + ((a - I*b)*E^{((2*I)*(c + d*x^{(1/3)})}))]/(a + I*b)]/((a^2 + b^2)^2*d) \\ &- ((30*I)*b^2*x*PolyLog[2, -(((a - I*b)*E^{((2*I)*(c + d*x^{(1/3)})}))]/(a + I*b))]/((a^2 + b^2)^2*d^3) + (15*b*x^{(4/3)}*PolyLog[2, -(((a - I*b)*E^{((2*I)*(c + d*x^{(1/3)})}))]/(a + I*b))]/((I*a - b)*(a - I*b)^2*d^2) \\ &- (15*b^2*x^{(4/3)}*PolyLog[2, -(((a - I*b)*E^{((2*I)*(c + d*x^{(1/3)})}))]/(a + I*b))]/((a^2 + b^2)^2*d^2) + (45*b^2*x^{(2/3)}*PolyLog[3, -(((a - I*b)*E^{((2*I)*(c + d*x^{(1/3)})}))]/(a + I*b))]/((a^2 + b^2)^2*d^4) \\ &+ (30*b*x*PolyLog[3, -(((a - I*b)*E^{((2*I)*(c + d*x^{(1/3)})}))]/(a + I*b))]/((a - I*b)^2*(a + I*b)*d^3) - ((30*I)*b^2*x*PolyLog[3, -(((a - I*b)*E^{((2*I)*(c + d*x^{(1/3)})}))]/(a + I*b))]/((a^2 + b^2)^2*d^3) \\ &+ ((45*I)*b^2*x^{(1/3)}*PolyLog[4, -(((a - I*b)*E^{((2*I)*(c + d*x^{(1/3)})}))]/(a + I*b))]/((a^2 + b^2)^2*d^5) - (45*b*x^{(2/3)}*PolyLog[4, -(((a - I*b)*E^{((2*I)*(c + d*x^{(1/3)})}))]/(a + I*b))]/((I*a - b)*(a - I*b)^2*d^4) \\ &+ (45*b^2*x^{(2/3)}*PolyLog[4, -(((a - I*b)*E^{((2*I)*(c + d*x^{(1/3)})}))]/(a + I*b))]/((a^2 + b^2)^2*d^4) - (45*b^2*PolyLog[5, -(((a - I*b)*E^{((2*I)*(c + d*x^{(1/3)})}))]/(a + I*b))]/(2*(a^2 + b^2)^2*d^6) \\ &- (45*b*x^{(1/3)}*PolyLog[5, -(((a - I*b)*E^{((2*I)*(c + d*x^{(1/3)})}))]/(a + I*b))]/((a - I*b)^2*(a + I*b)*d^5) + ((45*I)*b^2*x^{(1/3)}*PolyLog[5, -(((a - I*b)*E^{((2*I)*(c + d*x^{(1/3)})}))]/(a + I*b))]/((a^2 + b^2)^2*d^5) \\ &+ (45*b*PolyLog[6, -(((a - I*b)*E^{((2*I)*(c + d*x^{(1/3)})}))]/(a + I*b))]/(2*(I*a - b)*(a - I*b)^2*d^6) - (45*b^2*PolyLog[6, -(((a - I*b)*E^{((2*I)*(c + d*x^{(1/3)})}))]/(a + I*b))]/(2*(a^2 + b^2)^2*d^6) \end{aligned}$$

Rule 2215

Int[(((c_) + (d_)*(x_))^(m_))/((a_) + (b_)*((F_)^((g_)*((e_) + (f_)*(x_))))^(n_)), x_Symbol] := Simp[(c + d*x)^(m + 1)/(a*d*(m + 1)), x] - Dist[b/a, Int[(c + d*x)^m*((F)^(g*(e + f*x)))^n/(a + b*(F)^(g*(e + f*x)))^n], x] /; FreeQ[{F, a, b, c, d, e, f, g, n}, x] && IGtQ[m, 0]

Rule 2216

Int[((a_) + (b_)*((F_)^((g_)*((e_) + (f_)*(x_))))^(n_))^(p_)*((c_) + (d_)*(x_))^(m_), x_Symbol] := Dist[1/a, Int[(c + d*x)^m*(a + b*(F)^(g*(e + f*x)))^n]^(p + 1), x] - Dist[b/a, Int[(c + d*x)^m*(F)^(g*(e + f*x))^n*(a + b*(F)^(g*(e + f*x)))^n]^p, x] /; FreeQ[{F, a, b, c, d, e, f, g, n}, x] && ILtQ[p, 0] && IGtQ[m, 0]

Rule 2221

Int[(((F_)^((g_)*((e_) + (f_)*(x_))))^(n_)*((c_) + (d_)*(x_))^(m_))/((a_) + (b_)*((F_)^((g_)*((e_) + (f_)*(x_))))^(n_)), x_Symbol] := Simp

```

[((c + d*x)^m/(b*f*g*n*Log[F]))*Log[1 + b*((F^(g*(e + f*x)))^n/a)], x] - Dist[d*(m/(b*f*g*n*Log[F])), Int[(c + d*x)^(m - 1)*Log[1 + b*((F^(g*(e + f*x)))^n/a)], x], x] /; FreeQ[{F, a, b, c, d, e, f, g, n}, x] && IGtQ[m, 0]

```

Rule 2222

```

Int[((F_)^((g_)*((e_) + (f_)*(x_))))^(n_)*((a_) + (b_)*((F_)^((g_)*((e_) + (f_)*(x_))))^(n_))^(p_)*((c_) + (d_)*(x_)^(m_)), x_Symbol] :>
Simp[(c + d*x)^m*((a + b*(F^(g*(e + f*x)))^n)^(p + 1)/(b*f*g*n*(p + 1)*Log[F])), x] - Dist[d*(m/(b*f*g*n*(p + 1)*Log[F])), Int[(c + d*x)^(m - 1)*(a + b*(F^(g*(e + f*x)))^n)^(p + 1), x], x] /; FreeQ[{F, a, b, c, d, e, f, g, m, n, p}, x] && NeQ[p, -1]

```

Rule 2320

```

Int[u_, x_Symbol] :> With[{v = FunctionOfExponential[u, x]}, Dist[v/D[v, x], Subst[Int[FunctionOfExponentialFunction[u, x]/x, x], x, v], x] /; FunctionOfExponentialQ[u, x] && !MatchQ[u, (w_)*((a_)*(v_)^(n_))^(m_)] /; FreeQ[{a, m, n}, x] && IntegerQ[m*n] && !MatchQ[u, E^((c_)*((a_) + (b_)*x))*(F_)[v_] /; FreeQ[{a, b, c}, x] && InverseFunctionQ[F[x]]]

```

Rule 2611

```

Int[Log[1 + (e_)*((F_)^((c_)*((a_) + (b_)*(x_))))^(n_)]*((f_) + (g_)*(x_)^(m_)), x_Symbol] :> Simp[(-f + g*x)^m*(PolyLog[2, (-e)*(F^(c*(a + b*x)))^n]/(b*c*n*Log[F])), x] + Dist[g*(m/(b*c*n*Log[F])), Int[(f + g*x)^(m - 1)*PolyLog[2, (-e)*(F^(c*(a + b*x)))^n], x], x] /; FreeQ[{F, a, b, c, e, f, g, n}, x] && GtQ[m, 0]

```

Rule 3815

```

Int[((c_) + (d_)*(x_)^(m_))*((a_) + (b_)*tan[(e_) + (f_)*(x_)])^(n_), x_Symbol] :> Int[ExpandIntegrand[(c + d*x)^m, (1/(a - I*b) - 2*I*(b/(a^2 + b^2 + (a - I*b)^2*E^(2*I*(e + f*x))))^(-n)), x], x] /; FreeQ[{a, b, c, d, e, f}, x] && NeQ[a^2 + b^2, 0] && ILtQ[n, 0] && IGtQ[m, 0]

```

Rule 3832

```

Int[(x_)^(m_)*((a_) + (b_)*Tan[(c_) + (d_)*(x_)^(n_)])^(p_), x_Symbol] :> Dist[1/n, Subst[Int[x^(Simplify[(m + 1)/n] - 1)*(a + b*Tan[c + d*x])^p, x], x, x^n], x] /; FreeQ[{a, b, c, d, m, n, p}, x] && IGtQ[Simplify[(m + 1)/n], 0] && IntegerQ[p]

```

Rule 6724

```

Int[PolyLog[n_, (c_)*((a_) + (b_)*(x_)^(p_)]/((d_) + (e_)*(x_)), x_Symbol] :> Simp[PolyLog[n + 1, c*(a + b*x)^p]/(e*p), x] /; FreeQ[{a, b, c, d}

```


, e, n, p}, x] && EqQ[b*d, a*e]

Rule 6744

Int[((e_.) + (f_.)*(x_))^(m_.)*PolyLog[n_, (d_.)*((F_)^((c_.)*((a_.) + (b_.)*(x_)))^(p_.)], x_Symbol] := Simp[(e + f*x)^m*(PolyLog[n + 1, d*(F^(c*(a + b*x)))^p]/(b*c*p*Log[F])), x] - Dist[f*(m/(b*c*p*Log[F])), Int[(e + f*x)^(m - 1)*PolyLog[n + 1, d*(F^(c*(a + b*x)))^p], x], x] /; FreeQ[{F, a, b, c, d, e, f, n, p}, x] && GtQ[m, 0]

Rubi steps

$$\begin{aligned}
 \text{integral} &= 3\text{Subst}\left(\int \frac{x^5}{(a + b \tan(c + dx))^2} dx, x, \sqrt[3]{x}\right) \\
 &= 3\text{Subst}\left(\int \left(\frac{x^5}{(a - ib)^2} - \frac{4b^2 x^5}{(ia + b)^2 \left(ia \left(1 + \frac{ib}{a}\right) + ia \left(1 - \frac{ib}{a}\right) e^{2ic+2idx}\right)^2} \right. \right. \\
 &\quad \left. \left. + \frac{4bx^5}{(a - ib)^2 \left(ia \left(1 + \frac{ib}{a}\right) + ia \left(1 - \frac{ib}{a}\right) e^{2ic+2idx}\right)}\right) dx, x, \sqrt[3]{x}\right) \\
 &= \frac{x^2}{2(a - ib)^2} + \frac{(12b)\text{Subst}\left(\int \frac{x^5}{ia \left(1 + \frac{ib}{a}\right) + ia \left(1 - \frac{ib}{a}\right) e^{2ic+2idx}} dx, x, \sqrt[3]{x}\right)}{(a - ib)^2} \\
 &\quad - \frac{(12b^2)\text{Subst}\left(\int \frac{x^5}{\left(ia \left(1 + \frac{ib}{a}\right) + ia \left(1 - \frac{ib}{a}\right) e^{2ic+2idx}\right)^2} dx, x, \sqrt[3]{x}\right)}{(ia + b)^2} \\
 &= \frac{x^2}{2(a - ib)^2} + \frac{2bx^2}{(ia - b)(a - ib)^2} + \frac{(12b^2)\text{Subst}\left(\int \frac{x^5}{ia \left(1 + \frac{ib}{a}\right) + ia \left(1 - \frac{ib}{a}\right) e^{2ic+2idx}} dx, x, \sqrt[3]{x}\right)}{(ia - b)(a - ib)^2} \\
 &\quad - \frac{(12b)\text{Subst}\left(\int \frac{e^{2ic+2idx} x^5}{ia \left(1 + \frac{ib}{a}\right) + ia \left(1 - \frac{ib}{a}\right) e^{2ic+2idx}} dx, x, \sqrt[3]{x}\right)}{a^2 + b^2} \\
 &\quad - \frac{(12b^2)\text{Subst}\left(\int \frac{e^{2ic+2idx} x^5}{\left(ia \left(1 + \frac{ib}{a}\right) + ia \left(1 - \frac{ib}{a}\right) e^{2ic+2idx}\right)^2} dx, x, \sqrt[3]{x}\right)}{a^2 + b^2}
 \end{aligned}$$

$$\begin{aligned}
&= -\frac{6b^2x^{5/3}}{(a-ib)^2(a+ib)d\left(ia-b+(ia+b)e^{2i(c+d\sqrt[3]{x}})\right)} + \frac{x^2}{2(a-ib)^2} \\
&+ \frac{2bx^2}{(ia-b)(a-ib)^2} - \frac{2b^2x^2}{(a^2+b^2)^2} + \frac{6bx^{5/3}\log\left(1+\frac{(a-ib)e^{2i(c+d\sqrt[3]{x}})}{a+ib}\right)}{(a-ib)^2(a+ib)d} \\
&- \frac{(12b^2)\text{Subst}\left(\int\frac{e^{2ic+2idx}x^5}{ia\left(1+\frac{ib}{a}\right)+ia\left(1-\frac{ib}{a}\right)e^{2ic+2idx}}dx,x,\sqrt[3]{x}\right)}{(a+ib)^2(ia+b)} \\
&- \frac{(30b)\text{Subst}\left(\int x^4\log\left(1+\frac{\left(1-\frac{ib}{a}\right)e^{2ic+2idx}}{1+\frac{ib}{a}}\right)dx,x,\sqrt[3]{x}\right)}{(a-ib)^2(a+ib)d} \\
&+ \frac{(30b^2)\text{Subst}\left(\int\frac{x^4}{ia\left(1+\frac{ib}{a}\right)+ia\left(1-\frac{ib}{a}\right)e^{2ic+2idx}}dx,x,\sqrt[3]{x}\right)}{(a-ib)^2(a+ib)d} \\
&= -\frac{6ib^2x^{5/3}}{(a^2+b^2)^2d} - \frac{6b^2x^{5/3}}{(a-ib)^2(a+ib)d\left(ia-b+(ia+b)e^{2i(c+d\sqrt[3]{x}})\right)} + \frac{x^2}{2(a-ib)^2} \\
&+ \frac{2bx^2}{(ia-b)(a-ib)^2} - \frac{2b^2x^2}{(a^2+b^2)^2} + \frac{6bx^{5/3}\log\left(1+\frac{(a-ib)e^{2i(c+d\sqrt[3]{x}})}{a+ib}\right)}{(a-ib)^2(a+ib)d} \\
&- \frac{6ib^2x^{5/3}\log\left(1+\frac{(a-ib)e^{2i(c+d\sqrt[3]{x}})}{a+ib}\right)}{(a^2+b^2)^2d} + \frac{15bx^{4/3}\text{PolyLog}\left(2,-\frac{(a-ib)e^{2i(c+d\sqrt[3]{x}})}{a+ib}\right)}{(ia-b)(a-ib)^2d^2} \\
&- \frac{(60b)\text{Subst}\left(\int x^3\text{PolyLog}\left(2,-\frac{\left(1-\frac{ib}{a}\right)e^{2ic+2idx}}{1+\frac{ib}{a}}\right)dx,x,\sqrt[3]{x}\right)}{(ia-b)(a-ib)^2d^2} \\
&- \frac{(30b^2)\text{Subst}\left(\int\frac{e^{2ic+2idx}x^4}{ia\left(1+\frac{ib}{a}\right)+ia\left(1-\frac{ib}{a}\right)e^{2ic+2idx}}dx,x,\sqrt[3]{x}\right)}{(a-ib)(a+ib)^2d} \\
&+ \frac{(30ib^2)\text{Subst}\left(\int x^4\log\left(1+\frac{\left(1-\frac{ib}{a}\right)e^{2ic+2idx}}{1+\frac{ib}{a}}\right)dx,x,\sqrt[3]{x}\right)}{(a^2+b^2)^2d}
\end{aligned}$$

$$\begin{aligned}
&= -\frac{6ib^2x^{5/3}}{(a^2+b^2)^2d} - \frac{6b^2x^{5/3}}{(a-ib)^2(a+ib)d(ia-b+(ia+b)e^{2i(c+d\sqrt[3]{x}})}) \\
&+ \frac{x^2}{2(a-ib)^2} + \frac{2bx^2}{(ia-b)(a-ib)^2} - \frac{2b^2x^2}{(a^2+b^2)^2} \\
&+ \frac{15b^2x^{4/3} \log\left(1 + \frac{(a-ib)e^{2i(c+d\sqrt[3]{x}})}{a+ib}\right)}{(a^2+b^2)^2d^2} + \frac{6bx^{5/3} \log\left(1 + \frac{(a-ib)e^{2i(c+d\sqrt[3]{x}})}{a+ib}\right)}{(a-ib)^2(a+ib)d} \\
&- \frac{6ib^2x^{5/3} \log\left(1 + \frac{(a-ib)e^{2i(c+d\sqrt[3]{x}})}{a+ib}\right)}{(a^2+b^2)^2d} + \frac{15bx^{4/3} \text{PolyLog}\left(2, -\frac{(a-ib)e^{2i(c+d\sqrt[3]{x}})}{a+ib}\right)}{(ia-b)(a-ib)^2d^2} \\
&- \frac{15b^2x^{4/3} \text{PolyLog}\left(2, -\frac{(a-ib)e^{2i(c+d\sqrt[3]{x}})}{a+ib}\right)}{(a^2+b^2)^2d^2} + \frac{30bx \text{PolyLog}\left(3, -\frac{(a-ib)e^{2i(c+d\sqrt[3]{x}})}{a+ib}\right)}{(a-ib)^2(a+ib)d^3} \\
&- \frac{(90b) \text{Subst}\left(\int x^2 \text{PolyLog}\left(3, -\frac{(1-\frac{ib}{a})e^{2ic+2idx}}{1+\frac{ib}{a}}\right) dx, x, \sqrt[3]{x}\right)}{(a-ib)^2(a+ib)d^3} \\
&- \frac{(60b^2) \text{Subst}\left(\int x^3 \log\left(1 + \frac{(1-\frac{ib}{a})e^{2ic+2idx}}{1+\frac{ib}{a}}\right) dx, x, \sqrt[3]{x}\right)}{(a^2+b^2)^2d^2} \\
&+ \frac{(60b^2) \text{Subst}\left(\int x^3 \text{PolyLog}\left(2, -\frac{(1-\frac{ib}{a})e^{2ic+2idx}}{1+\frac{ib}{a}}\right) dx, x, \sqrt[3]{x}\right)}{(a^2+b^2)^2d^2}
\end{aligned}$$

$$\begin{aligned}
&= -\frac{6ib^2x^{5/3}}{(a^2+b^2)^2d} - \frac{6b^2x^{5/3}}{(a-ib)^2(a+ib)d} \frac{e^{2i(c+d\sqrt[3]{x})}}{(ia-b+(a+b)e^{2i(c+d\sqrt[3]{x})})} + \frac{x^2}{2(a-ib)^2} \\
&+ \frac{2bx^2}{(ia-b)(a-ib)^2} - \frac{2b^2x^2}{(a^2+b^2)^2} + \frac{15b^2x^{4/3} \log\left(1 + \frac{(a-ib)e^{2i(c+d\sqrt[3]{x})}}{a+ib}\right)}{(a^2+b^2)^2d^2} \\
&+ \frac{6bx^{5/3} \log\left(1 + \frac{(a-ib)e^{2i(c+d\sqrt[3]{x})}}{a+ib}\right)}{(a-ib)^2(a+ib)d} - \frac{6ib^2x^{5/3} \log\left(1 + \frac{(a-ib)e^{2i(c+d\sqrt[3]{x})}}{a+ib}\right)}{(a^2+b^2)^2d} \\
&- \frac{30ib^2x \operatorname{PolyLog}\left(2, -\frac{(a-ib)e^{2i(c+d\sqrt[3]{x})}}{a+ib}\right)}{(a^2+b^2)^2d^3} + \frac{15bx^{4/3} \operatorname{PolyLog}\left(2, -\frac{(a-ib)e^{2i(c+d\sqrt[3]{x})}}{a+ib}\right)}{(ia-b)(a-ib)^2d^2} \\
&- \frac{15b^2x^{4/3} \operatorname{PolyLog}\left(2, -\frac{(a-ib)e^{2i(c+d\sqrt[3]{x})}}{a+ib}\right)}{(a^2+b^2)^2d^2} + \frac{30bx \operatorname{PolyLog}\left(3, -\frac{(a-ib)e^{2i(c+d\sqrt[3]{x})}}{a+ib}\right)}{(a-ib)^2(a+ib)d^3} \\
&- \frac{30ib^2x \operatorname{PolyLog}\left(3, -\frac{(a-ib)e^{2i(c+d\sqrt[3]{x})}}{a+ib}\right)}{(a^2+b^2)^2d^3} - \frac{45bx^{2/3} \operatorname{PolyLog}\left(4, -\frac{(a-ib)e^{2i(c+d\sqrt[3]{x})}}{a+ib}\right)}{(ia-b)(a-ib)^2d^4} \\
&+ \frac{(90b) \operatorname{Subst}\left(\int x \operatorname{PolyLog}\left(4, -\frac{\left(1-\frac{ib}{a}\right)e^{2ic+2idx}}{1+\frac{ib}{a}}\right) dx, x, \sqrt[3]{x}\right)}{(ia-b)(a-ib)^2d^4} \\
&+ \frac{(90ib^2) \operatorname{Subst}\left(\int x^2 \operatorname{PolyLog}\left(2, -\frac{\left(1-\frac{ib}{a}\right)e^{2ic+2idx}}{1+\frac{ib}{a}}\right) dx, x, \sqrt[3]{x}\right)}{(a^2+b^2)^2d^3} \\
&+ \frac{(90ib^2) \operatorname{Subst}\left(\int x^2 \operatorname{PolyLog}\left(3, -\frac{\left(1-\frac{ib}{a}\right)e^{2ic+2idx}}{1+\frac{ib}{a}}\right) dx, x, \sqrt[3]{x}\right)}{(a^2+b^2)^2d^3}
\end{aligned}$$

$$\begin{aligned}
&= -\frac{6ib^2x^{5/3}}{(a^2+b^2)^2d} - \frac{6b^2x^{5/3}}{(a-ib)^2(a+ib)d} \frac{e^{2i(c+d\sqrt[3]{x})}}{(ia-b+(ia+b)e^{2i(c+d\sqrt[3]{x})})} + \frac{x^2}{2(a-ib)^2} \\
&+ \frac{2bx^2}{(ia-b)(a-ib)^2} - \frac{2b^2x^2}{(a^2+b^2)^2} + \frac{15b^2x^{4/3} \log\left(1 + \frac{(a-ib)e^{2i(c+d\sqrt[3]{x})}}{a+ib}\right)}{(a^2+b^2)^2d^2} \\
&+ \frac{6bx^{5/3} \log\left(1 + \frac{(a-ib)e^{2i(c+d\sqrt[3]{x})}}{a+ib}\right)}{(a-ib)^2(a+ib)d} - \frac{6ib^2x^{5/3} \log\left(1 + \frac{(a-ib)e^{2i(c+d\sqrt[3]{x})}}{a+ib}\right)}{(a^2+b^2)^2d} \\
&- \frac{30ib^2x \operatorname{PolyLog}\left(2, -\frac{(a-ib)e^{2i(c+d\sqrt[3]{x})}}{a+ib}\right)}{(a^2+b^2)^2d^3} + \frac{15bx^{4/3} \operatorname{PolyLog}\left(2, -\frac{(a-ib)e^{2i(c+d\sqrt[3]{x})}}{a+ib}\right)}{(ia-b)(a-ib)^2d^2} \\
&- \frac{15b^2x^{4/3} \operatorname{PolyLog}\left(2, -\frac{(a-ib)e^{2i(c+d\sqrt[3]{x})}}{a+ib}\right)}{(a^2+b^2)^2d^2} \\
&+ \frac{45b^2x^{2/3} \operatorname{PolyLog}\left(3, -\frac{(a-ib)e^{2i(c+d\sqrt[3]{x})}}{a+ib}\right)}{(a^2+b^2)^2d^4} + \frac{30bx \operatorname{PolyLog}\left(3, -\frac{(a-ib)e^{2i(c+d\sqrt[3]{x})}}{a+ib}\right)}{(a-ib)^2(a+ib)d^3} \\
&- \frac{30ib^2x \operatorname{PolyLog}\left(3, -\frac{(a-ib)e^{2i(c+d\sqrt[3]{x})}}{a+ib}\right)}{(a^2+b^2)^2d^3} - \frac{45bx^{2/3} \operatorname{PolyLog}\left(4, -\frac{(a-ib)e^{2i(c+d\sqrt[3]{x})}}{a+ib}\right)}{(ia-b)(a-ib)^2d^4} \\
&+ \frac{45b^2x^{2/3} \operatorname{PolyLog}\left(4, -\frac{(a-ib)e^{2i(c+d\sqrt[3]{x})}}{a+ib}\right)}{(a^2+b^2)^2d^4} \\
&- \frac{45b\sqrt[3]{x} \operatorname{PolyLog}\left(5, -\frac{(a-ib)e^{2i(c+d\sqrt[3]{x})}}{a+ib}\right)}{(a-ib)^2(a+ib)d^5} \\
&+ \frac{(45b) \operatorname{Subst}\left(\int \operatorname{PolyLog}\left(5, -\frac{(1-\frac{ib}{a})e^{2ic+2idx}}{1+\frac{ib}{a}}\right) dx, x, \sqrt[3]{x}\right)}{(a-ib)^2(a+ib)d^5} \\
&- \frac{(90b^2) \operatorname{Subst}\left(\int x \operatorname{PolyLog}\left(3, -\frac{(1-\frac{ib}{a})e^{2ic+2idx}}{1+\frac{ib}{a}}\right) dx, x, \sqrt[3]{x}\right)}{(a^2+b^2)^2d^4} \\
&- \frac{(90b^2) \operatorname{Subst}\left(\int x \operatorname{PolyLog}\left(4, -\frac{(1-\frac{ib}{a})e^{2ic+2idx}}{1+\frac{ib}{a}}\right) dx, x, \sqrt[3]{x}\right)}{(a^2+b^2)^2d^4}
\end{aligned}$$

$$\begin{aligned}
&= -\frac{6ib^2x^{5/3}}{(a^2+b^2)^2d} - \frac{6b^2x^{5/3}}{(a-ib)^2(a+ib)d} \frac{e^{2i(c+d\sqrt[3]{x})}}{(ia-b+(a+b)e^{2i(c+d\sqrt[3]{x})})} + \frac{x^2}{2(a-ib)^2} \\
&+ \frac{2bx^2}{(ia-b)(a-ib)^2} - \frac{2b^2x^2}{(a^2+b^2)^2} + \frac{15b^2x^{4/3} \log\left(1 + \frac{(a-ib)e^{2i(c+d\sqrt[3]{x})}}{a+ib}\right)}{(a^2+b^2)^2d^2} \\
&+ \frac{6bx^{5/3} \log\left(1 + \frac{(a-ib)e^{2i(c+d\sqrt[3]{x})}}{a+ib}\right)}{(a-ib)^2(a+ib)d} - \frac{6ib^2x^{5/3} \log\left(1 + \frac{(a-ib)e^{2i(c+d\sqrt[3]{x})}}{a+ib}\right)}{(a^2+b^2)^2d} \\
&- \frac{30ib^2x \operatorname{PolyLog}\left(2, -\frac{(a-ib)e^{2i(c+d\sqrt[3]{x})}}{a+ib}\right)}{(a^2+b^2)^2d^3} + \frac{15bx^{4/3} \operatorname{PolyLog}\left(2, -\frac{(a-ib)e^{2i(c+d\sqrt[3]{x})}}{a+ib}\right)}{(ia-b)(a-ib)^2d^2} \\
&- \frac{15b^2x^{4/3} \operatorname{PolyLog}\left(2, -\frac{(a-ib)e^{2i(c+d\sqrt[3]{x})}}{a+ib}\right)}{(a^2+b^2)^2d^2} \\
&+ \frac{45b^2x^{2/3} \operatorname{PolyLog}\left(3, -\frac{(a-ib)e^{2i(c+d\sqrt[3]{x})}}{a+ib}\right)}{(a^2+b^2)^2d^4} \\
&+ \frac{30bx \operatorname{PolyLog}\left(3, -\frac{(a-ib)e^{2i(c+d\sqrt[3]{x})}}{a+ib}\right)}{(a-ib)^2(a+ib)d^3} - \frac{30ib^2x \operatorname{PolyLog}\left(3, -\frac{(a-ib)e^{2i(c+d\sqrt[3]{x})}}{a+ib}\right)}{(a^2+b^2)^2d^3} \\
&+ \frac{45ib^2\sqrt[3]{x} \operatorname{PolyLog}\left(4, -\frac{(a-ib)e^{2i(c+d\sqrt[3]{x})}}{a+ib}\right)}{(a^2+b^2)^2d^5} \\
&- \frac{45bx^{2/3} \operatorname{PolyLog}\left(4, -\frac{(a-ib)e^{2i(c+d\sqrt[3]{x})}}{a+ib}\right)}{(ia-b)(a-ib)^2d^4} \\
&+ \frac{45b^2x^{2/3} \operatorname{PolyLog}\left(4, -\frac{(a-ib)e^{2i(c+d\sqrt[3]{x})}}{a+ib}\right)}{(a^2+b^2)^2d^4} \\
&- \frac{45b\sqrt[3]{x} \operatorname{PolyLog}\left(5, -\frac{(a-ib)e^{2i(c+d\sqrt[3]{x})}}{a+ib}\right)}{(a-ib)^2(a+ib)d^5} \\
&+ \frac{45ib^2\sqrt[3]{x} \operatorname{PolyLog}\left(5, -\frac{(a-ib)e^{2i(c+d\sqrt[3]{x})}}{a+ib}\right)}{(a^2+b^2)^2d^5} \\
&+ \frac{(45b) \operatorname{Subst}\left(\int \frac{\operatorname{PolyLog}\left(5, -\frac{(a-ib)x}{a+ib}\right)}{x} dx, x, e^{2i(c+d\sqrt[3]{x})}\right)}{2(ia-b)(a-ib)^2d^6} \\
&- \frac{(45ib^2) \operatorname{Subst}\left(\int \operatorname{PolyLog}\left(4, -\frac{\left(1-\frac{ib}{a}\right)e^{2ic+2idx}}{1+\frac{ib}{a}}\right) dx, x, \sqrt[3]{x}\right)}{(a^2+b^2)^2d^5} \\
&- \frac{(45ib^2) \operatorname{Subst}\left(\int \operatorname{PolyLog}\left(5, -\frac{\left(1-\frac{ib}{a}\right)e^{2ic+2idx}}{1+\frac{ib}{a}}\right) dx, x, \sqrt[3]{x}\right)}{(a^2+b^2)^2d^5}
\end{aligned}$$

$$\begin{aligned}
&= -\frac{6ib^2x^{5/3}}{(a^2+b^2)^2d} - \frac{6b^2x^{5/3}}{(a-ib)^2(a+ib)d} \frac{1}{(ia-b+(ia+b)e^{2i(c+d\sqrt[3]{x}})} + \frac{x^2}{2(a-ib)^2} \\
&+ \frac{2bx^2}{(ia-b)(a-ib)^2} - \frac{2b^2x^2}{(a^2+b^2)^2} + \frac{15b^2x^{4/3} \log\left(1 + \frac{(a-ib)e^{2i(c+d\sqrt[3]{x}})}{a+ib}\right)}{(a^2+b^2)^2d^2} \\
&+ \frac{6bx^{5/3} \log\left(1 + \frac{(a-ib)e^{2i(c+d\sqrt[3]{x}})}{a+ib}\right)}{(a-ib)^2(a+ib)d} - \frac{6ib^2x^{5/3} \log\left(1 + \frac{(a-ib)e^{2i(c+d\sqrt[3]{x}})}{a+ib}\right)}{(a^2+b^2)^2d} \\
&- \frac{30ib^2x \operatorname{PolyLog}\left(2, -\frac{(a-ib)e^{2i(c+d\sqrt[3]{x}})}{a+ib}\right)}{(a^2+b^2)^2d^3} + \frac{15bx^{4/3} \operatorname{PolyLog}\left(2, -\frac{(a-ib)e^{2i(c+d\sqrt[3]{x}})}{a+ib}\right)}{(ia-b)(a-ib)^2d^2} \\
&- \frac{15b^2x^{4/3} \operatorname{PolyLog}\left(2, -\frac{(a-ib)e^{2i(c+d\sqrt[3]{x}})}{a+ib}\right)}{(a^2+b^2)^2d^2} \\
&+ \frac{45b^2x^{2/3} \operatorname{PolyLog}\left(3, -\frac{(a-ib)e^{2i(c+d\sqrt[3]{x}})}{a+ib}\right)}{(a^2+b^2)^2d^4} \\
&+ \frac{30bx \operatorname{PolyLog}\left(3, -\frac{(a-ib)e^{2i(c+d\sqrt[3]{x}})}{a+ib}\right)}{(a-ib)^2(a+ib)d^3} - \frac{30ib^2x \operatorname{PolyLog}\left(3, -\frac{(a-ib)e^{2i(c+d\sqrt[3]{x}})}{a+ib}\right)}{(a^2+b^2)^2d^3} \\
&+ \frac{45ib^2\sqrt[3]{x} \operatorname{PolyLog}\left(4, -\frac{(a-ib)e^{2i(c+d\sqrt[3]{x}})}{a+ib}\right)}{(a^2+b^2)^2d^5} \\
&- \frac{45bx^{2/3} \operatorname{PolyLog}\left(4, -\frac{(a-ib)e^{2i(c+d\sqrt[3]{x}})}{a+ib}\right)}{(ia-b)(a-ib)^2d^4} \\
&+ \frac{45b^2x^{2/3} \operatorname{PolyLog}\left(4, -\frac{(a-ib)e^{2i(c+d\sqrt[3]{x}})}{a+ib}\right)}{(a^2+b^2)^2d^4} \\
&- \frac{45b\sqrt[3]{x} \operatorname{PolyLog}\left(5, -\frac{(a-ib)e^{2i(c+d\sqrt[3]{x}})}{a+ib}\right)}{(a-ib)^2(a+ib)d^5} \\
&+ \frac{45ib^2\sqrt[3]{x} \operatorname{PolyLog}\left(5, -\frac{(a-ib)e^{2i(c+d\sqrt[3]{x}})}{a+ib}\right)}{(a^2+b^2)^2d^5} + \frac{45b \operatorname{PolyLog}\left(6, -\frac{(a-ib)e^{2i(c+d\sqrt[3]{x}})}{a+ib}\right)}{2(ia-b)(a-ib)^2d^6} \\
&- \frac{(45b^2) \operatorname{Subst}\left(\int \frac{\operatorname{PolyLog}\left(4, -\frac{(a-ib)x}{a+ib}\right)}{x} dx, x, e^{2i(c+d\sqrt[3]{x})}\right)}{2(a^2+b^2)^2d^6} \\
&- \frac{(45b^2) \operatorname{Subst}\left(\int \frac{\operatorname{PolyLog}\left(5, -\frac{(a-ib)x}{a+ib}\right)}{x} dx, x, e^{2i(c+d\sqrt[3]{x})}\right)}{2(a^2+b^2)^2d^6}
\end{aligned}$$

$$\begin{aligned}
&= -\frac{6ib^2x^{5/3}}{(a^2+b^2)^2d} - \frac{6b^2x^{5/3}}{(a-ib)^2(a+ib)d} \frac{e^{2i(c+d\sqrt[3]{x})}}{(ia-b+(a+b)e^{2i(c+d\sqrt[3]{x})})} + \frac{x^2}{2(a-ib)^2} \\
&+ \frac{2bx^2}{(ia-b)(a-ib)^2} - \frac{2b^2x^2}{(a^2+b^2)^2} + \frac{15b^2x^{4/3} \log\left(1 + \frac{(a-ib)e^{2i(c+d\sqrt[3]{x})}}{a+ib}\right)}{(a^2+b^2)^2d^2} \\
&+ \frac{6bx^{5/3} \log\left(1 + \frac{(a-ib)e^{2i(c+d\sqrt[3]{x})}}{a+ib}\right)}{(a-ib)^2(a+ib)d} - \frac{6ib^2x^{5/3} \log\left(1 + \frac{(a-ib)e^{2i(c+d\sqrt[3]{x})}}{a+ib}\right)}{(a^2+b^2)^2d} \\
&- \frac{30ib^2x \operatorname{PolyLog}\left(2, -\frac{(a-ib)e^{2i(c+d\sqrt[3]{x})}}{a+ib}\right)}{(a^2+b^2)^2d^3} + \frac{15bx^{4/3} \operatorname{PolyLog}\left(2, -\frac{(a-ib)e^{2i(c+d\sqrt[3]{x})}}{a+ib}\right)}{(ia-b)(a-ib)^2d^2} \\
&- \frac{15b^2x^{4/3} \operatorname{PolyLog}\left(2, -\frac{(a-ib)e^{2i(c+d\sqrt[3]{x})}}{a+ib}\right)}{(a^2+b^2)^2d^2} \\
&+ \frac{45b^2x^{2/3} \operatorname{PolyLog}\left(3, -\frac{(a-ib)e^{2i(c+d\sqrt[3]{x})}}{a+ib}\right)}{(a^2+b^2)^2d^4} \\
&+ \frac{30bx \operatorname{PolyLog}\left(3, -\frac{(a-ib)e^{2i(c+d\sqrt[3]{x})}}{a+ib}\right)}{(a-ib)^2(a+ib)d^3} - \frac{30ib^2x \operatorname{PolyLog}\left(3, -\frac{(a-ib)e^{2i(c+d\sqrt[3]{x})}}{a+ib}\right)}{(a^2+b^2)^2d^3} \\
&+ \frac{45ib^2\sqrt[3]{x} \operatorname{PolyLog}\left(4, -\frac{(a-ib)e^{2i(c+d\sqrt[3]{x})}}{a+ib}\right)}{(a^2+b^2)^2d^5} \\
&- \frac{45bx^{2/3} \operatorname{PolyLog}\left(4, -\frac{(a-ib)e^{2i(c+d\sqrt[3]{x})}}{a+ib}\right)}{(ia-b)(a-ib)^2d^4} \\
&+ \frac{45b^2x^{2/3} \operatorname{PolyLog}\left(4, -\frac{(a-ib)e^{2i(c+d\sqrt[3]{x})}}{a+ib}\right)}{(a^2+b^2)^2d^4} \\
&- \frac{45b^2 \operatorname{PolyLog}\left(5, -\frac{(a-ib)e^{2i(c+d\sqrt[3]{x})}}{a+ib}\right)}{2(a^2+b^2)^2d^6} - \frac{45b\sqrt[3]{x} \operatorname{PolyLog}\left(5, -\frac{(a-ib)e^{2i(c+d\sqrt[3]{x})}}{a+ib}\right)}{(a-ib)^2(a+ib)d^5} \\
&+ \frac{45ib^2\sqrt[3]{x} \operatorname{PolyLog}\left(5, -\frac{(a-ib)e^{2i(c+d\sqrt[3]{x})}}{a+ib}\right)}{(a^2+b^2)^2d^5} \\
&+ \frac{45b \operatorname{PolyLog}\left(6, -\frac{(a-ib)e^{2i(c+d\sqrt[3]{x})}}{a+ib}\right)}{2(ia-b)(a-ib)^2d^6} - \frac{45b^2 \operatorname{PolyLog}\left(6, -\frac{(a-ib)e^{2i(c+d\sqrt[3]{x})}}{a+ib}\right)}{2(a^2+b^2)^2d^6}
\end{aligned}$$

Mathematica [A] (verified)

Time = 3.21 (sec) , antiderivative size = 852, normalized size of antiderivative = 0.74

$$\int \frac{x}{\left(a + b \tan\left(c + d\sqrt[3]{x}\right)\right)^2} dx$$

$$ib \left(12(a+ib)b(ia+b)d^5x^{5/3} + 4a(a+ib)(ia+b)d^6x^2 + 30(a-ib)bd^4(-ib(-1+e^{2ic})+a(1+e^{2ic}))x^{4/3} \log\left(1 + \frac{(a+ib)e^{-2i(c+d\sqrt[3]{x}})}{a-ib}\right) + 12a(a-ib) \right)$$

=

[In] Integrate[x/(a + b*Tan[c + d*x^(1/3)])^2,x]

[Out] (((-I)*b*(12*(a + I*b)*b*(I*a + b)*d^5*x^(5/3) + 4*a*(a + I*b)*(I*a + b)*d^6*x^2 + 30*(a - I*b)*b*d^4*((-I)*b*(-1 + E^((2*I)*c)) + a*(1 + E^((2*I)*c))) *x^(4/3)*Log[1 + (a + I*b)/((a - I*b)*E^((2*I)*(c + d*x^(1/3)))] + 12*a*(a - I*b)*d^5*((-I)*b*(-1 + E^((2*I)*c)) + a*(1 + E^((2*I)*c))) *x^(5/3)*Log[1 + (a + I*b)/((a - I*b)*E^((2*I)*(c + d*x^(1/3)))] + 15*(a - I*b)*b*((-I)*b*(-1 + E^((2*I)*c)) + a*(1 + E^((2*I)*c)))*((4*I)*d^3*x*PolyLog[2, (-a - I*b)/((a - I*b)*E^((2*I)*(c + d*x^(1/3)))] + 6*d^2*x^(2/3)*PolyLog[3, (-a - I*b)/((a - I*b)*E^((2*I)*(c + d*x^(1/3)))] - (6*I)*d*x^(1/3)*PolyLog[4, (-a - I*b)/((a - I*b)*E^((2*I)*(c + d*x^(1/3)))] - 3*PolyLog[5, (-a - I*b)/((a - I*b)*E^((2*I)*(c + d*x^(1/3)))] + 15*a*(a - I*b)*((-I)*b*(-1 + E^((2*I)*c)) + a*(1 + E^((2*I)*c)))*((2*I)*d^4*x^(4/3)*PolyLog[2, (-a - I*b)/((a - I*b)*E^((2*I)*(c + d*x^(1/3)))] + 4*d^3*x*PolyLog[3, (-a - I*b)/((a - I*b)*E^((2*I)*(c + d*x^(1/3)))] - (6*I)*d^2*x^(2/3)*PolyLog[4, (-a - I*b)/((a - I*b)*E^((2*I)*(c + d*x^(1/3)))] - 6*d*x^(1/3)*PolyLog[5, (-a - I*b)/((a - I*b)*E^((2*I)*(c + d*x^(1/3)))] + (3*I)*PolyLog[6, (-a - I*b)/((a - I*b)*E^((2*I)*(c + d*x^(1/3)))])))/(d^6*(b - b*E^((2*I)*c) - I*a*(1 + E^((2*I)*c))) + ((a - I*b)^2*(a + I*b)*x^2*(a*Cos[c] - b*Sin[c]))/(a*Cos[c] + b*Sin[c]) + (6*(a - I*b)^2*(a + I*b)*b^2*x^(5/3)*Sin[d*x^(1/3)]/(d*(a*Cos[c] + b*Sin[c])*(a*Cos[c + d*x^(1/3)] + b*Sin[c + d*x^(1/3)])))/(2*(a - I*b)^3*(a + I*b)^2)

Maple [F]

$$\int \frac{x}{\left(a + b \tan\left(c + dx^{\frac{1}{3}}\right)\right)^2} dx$$

[In] int(x/(a+b*tan(c+d*x^(1/3)))^2,x)**[Out]** int(x/(a+b*tan(c+d*x^(1/3)))^2,x)

Fricas [F]

$$\int \frac{x}{(a + b \tan(c + d\sqrt[3]{x}))^2} dx = \int \frac{x}{(b \tan(dx^{\frac{1}{3}} + c) + a)^2} dx$$

[In] integrate(x/(a+b*tan(c+d*x^(1/3)))^2,x, algorithm="fricas")

[Out] integral(x/(b^2*tan(d*x^(1/3) + c)^2 + 2*a*b*tan(d*x^(1/3) + c) + a^2), x)

Sympy [F]

$$\int \frac{x}{(a + b \tan(c + d\sqrt[3]{x}))^2} dx = \int \frac{x}{(a + b \tan(c + d\sqrt[3]{x}))^2} dx$$

[In] integrate(x/(a+b*tan(c+d*x**(1/3)))**2,x)

[Out] Integral(x/(a + b*tan(c + d*x**(1/3)))**2, x)

Maxima [B] (verification not implemented)

Both result and optimal contain complex but leaf count of result is larger than twice the leaf count of optimal. 4345 vs. 2(928) = 1856.

Time = 1.34 (sec) , antiderivative size = 4345, normalized size of antiderivative = 3.76

$$\int \frac{x}{(a + b \tan(c + d\sqrt[3]{x}))^2} dx = \text{Too large to display}$$

[In] integrate(x/(a+b*tan(c+d*x^(1/3)))^2,x, algorithm="maxima")

[Out]
$$-1/10*(30*(2*a*b*\log(b*\tan(d*x^(1/3) + c) + a)/(a^4 + 2*a^2*b^2 + b^4) - a*b*\log(\tan(d*x^(1/3) + c)^2 + 1)/(a^4 + 2*a^2*b^2 + b^4) + (a^2 - b^2)*(d*x^(1/3) + c)/(a^4 + 2*a^2*b^2 + b^4) - b/(a^3 + a*b^2 + (a^2*b + b^3)*\tan(d*x^(1/3) + c)))*c^5 - (5*(a^3 - I*a^2*b + a*b^2 - I*b^3)*(d*x^(1/3) + c)^6 - 30*(a^3 - I*a^2*b + a*b^2 - I*b^3)*(d*x^(1/3) + c)^5*c + 75*(a^3 - I*a^2*b + a*b^2 - I*b^3)*(d*x^(1/3) + c)^4*c^2 - 100*(a^3 - I*a^2*b + a*b^2 - I*b^3)*(d*x^(1/3) + c)^3*c^3 + 75*(a^3 - I*a^2*b + a*b^2 - I*b^3)*(d*x^(1/3) + c)^2*c^4 - 150*((-I*a*b^2 - b^3)*c^4*\cos(2*d*x^(1/3) + 2*c) + (a*b^2 - I*b^3)*c^4*\sin(2*d*x^(1/3) + 2*c) + (-I*a*b^2 + b^3)*c^4*\arctan2(-b*\cos(2*d*x^(1/3) + 2*c) + a*\sin(2*d*x^(1/3) + 2*c) + b, a*\cos(2*d*x^(1/3) + 2*c) + b*\sin(2*d*x^(1/3) + 2*c) + a) - 4*(48*(I*a^2*b - a*b^2)*(d*x^(1/3) + c)^5 + 75*(I*a*b^2 - b^3 + 2*(-I*a^2*b + a*b^2)*c)*(d*x^(1/3) + c)^4 + 200*(I*a^2*b$$

$$\begin{aligned}
& - a*b^2)*c^2 + (-I*a*b^2 + b^3)*c)*(d*x^(1/3) + c)^3 + 75*(2*(-I*a^2*b + a* \\
& b^2)*c^3 + 3*(I*a*b^2 - b^3)*c^2)*(d*x^(1/3) + c)^2 + 75*((I*a^2*b - a*b^2) \\
& *c^4 + 2*(-I*a*b^2 + b^3)*c^3)*(d*x^(1/3) + c) + (48*(I*a^2*b + a*b^2)*(d*x \\
& ^{(1/3) + c)^5 + 75*(I*a*b^2 + b^3 + 2*(-I*a^2*b - a*b^2)*c)*(d*x^(1/3) + c) \\
& ^4 + 200*((I*a^2*b + a*b^2)*c^2 + (-I*a*b^2 - b^3)*c)*(d*x^(1/3) + c)^3 + 7 \\
& 5*(2*(-I*a^2*b - a*b^2)*c^3 + 3*(I*a*b^2 + b^3)*c^2)*(d*x^(1/3) + c)^2 + 75 \\
& *((I*a^2*b + a*b^2)*c^4 + 2*(-I*a*b^2 - b^3)*c^3)*(d*x^(1/3) + c))*\cos(2*d* \\
& x^(1/3) + 2*c) - (48*(a^2*b - I*a*b^2)*(d*x^(1/3) + c)^5 + 75*(a*b^2 - I*b^ \\
& 3 - 2*(a^2*b - I*a*b^2)*c)*(d*x^(1/3) + c)^4 + 200*((a^2*b - I*a*b^2)*c^2 - \\
& (a*b^2 - I*b^3)*c)*(d*x^(1/3) + c)^3 - 75*(2*(a^2*b - I*a*b^2)*c^3 - 3*(a* \\
& b^2 - I*b^3)*c^2)*(d*x^(1/3) + c)^2 + 75*((a^2*b - I*a*b^2)*c^4 - 2*(a*b^2 \\
& - I*b^3)*c^3)*(d*x^(1/3) + c))*\sin(2*d*x^(1/3) + 2*c))*\arctan2((2*a*b*\cos(2 \\
& *d*x^(1/3) + 2*c) - (a^2 - b^2)*\sin(2*d*x^(1/3) + 2*c))/(a^2 + b^2), (2*a*b \\
& *\sin(2*d*x^(1/3) + 2*c) + a^2 + b^2 + (a^2 - b^2)*\cos(2*d*x^(1/3) + 2*c))/(\\
& a^2 + b^2)) + 5*((a^3 - 3*I*a^2*b - 3*a*b^2 + I*b^3)*(d*x^(1/3) + c)^6 - 6* \\
& (2*I*a*b^2 + 2*b^3 + (a^3 - 3*I*a^2*b - 3*a*b^2 + I*b^3)*c)*(d*x^(1/3) + c) \\
& ^5 - 60*(I*a*b^2 + b^3)*(d*x^(1/3) + c)*c^4 + 15*((a^3 - 3*I*a^2*b - 3*a*b^ \\
& 2 + I*b^3)*c^2 - 4*(-I*a*b^2 - b^3)*c)*(d*x^(1/3) + c)^4 - 20*((a^3 - 3*I*a \\
& ^2*b - 3*a*b^2 + I*b^3)*c^3 + 6*(I*a*b^2 + b^3)*c^2)*(d*x^(1/3) + c)^3 + 15 \\
& *((a^3 - 3*I*a^2*b - 3*a*b^2 + I*b^3)*c^4 - 8*(-I*a*b^2 - b^3)*c^3)*(d*x^(1 \\
& /3) + c)^2)*\cos(2*d*x^(1/3) + 2*c) - 30*(16*(I*a^2*b - a*b^2)*(d*x^(1/3) + \\
& c)^4 + 5*(I*a^2*b - a*b^2)*c^4 + 20*(I*a*b^2 - b^3 + 2*(-I*a^2*b + a*b^2)*c \\
&)*(d*x^(1/3) + c)^3 + 10*(-I*a*b^2 + b^3)*c^3 + 40*((I*a^2*b - a*b^2)*c^2 + \\
& (-I*a*b^2 + b^3)*c)*(d*x^(1/3) + c)^2 + 10*(2*(-I*a^2*b + a*b^2)*c^3 + 3*(\\
& I*a*b^2 - b^3)*c^2)*(d*x^(1/3) + c) + (16*(I*a^2*b + a*b^2)*(d*x^(1/3) + c) \\
& ^4 + 5*(I*a^2*b + a*b^2)*c^4 + 20*(I*a*b^2 + b^3 + 2*(-I*a^2*b - a*b^2)*c)* \\
& (d*x^(1/3) + c)^3 + 10*(-I*a*b^2 - b^3)*c^3 + 40*((I*a^2*b + a*b^2)*c^2 + (\\
& -I*a*b^2 - b^3)*c)*(d*x^(1/3) + c)^2 + 10*(2*(-I*a^2*b - a*b^2)*c^3 + 3*(I* \\
& a*b^2 + b^3)*c^2)*(d*x^(1/3) + c))*\cos(2*d*x^(1/3) + 2*c) - (16*(a^2*b - I* \\
& a*b^2)*(d*x^(1/3) + c)^4 + 5*(a^2*b - I*a*b^2)*c^4 + 20*(a*b^2 - I*b^3 - 2* \\
& (a^2*b - I*a*b^2)*c)*(d*x^(1/3) + c)^3 - 10*(a*b^2 - I*b^3)*c^3 + 40*((a^2* \\
& b - I*a*b^2)*c^2 - (a*b^2 - I*b^3)*c)*(d*x^(1/3) + c)^2 - 10*(2*(a^2*b - I* \\
& a*b^2)*c^3 - 3*(a*b^2 - I*b^3)*c^2)*(d*x^(1/3) + c))*\sin(2*d*x^(1/3) + 2*c) \\
&)*\operatorname{dilog}((I*a + b)*e^{(2*I*d*x^(1/3) + 2*I*c)/(-I*a + b)}) + 75*((a*b^2 - I*b^ \\
& 3)*c^4*\cos(2*d*x^(1/3) + 2*c) - (-I*a*b^2 - b^3)*c^4*\sin(2*d*x^(1/3) + 2*c) \\
& + (a*b^2 + I*b^3)*c^4)*\log((a^2 + b^2)*\cos(2*d*x^(1/3) + 2*c)^2 + 4*a*b*\si \\
& n(2*d*x^(1/3) + 2*c) + (a^2 + b^2)*\sin(2*d*x^(1/3) + 2*c)^2 + a^2 + b^2 + 2 \\
& *(a^2 - b^2)*\cos(2*d*x^(1/3) + 2*c)) + 2*(48*(a^2*b + I*a*b^2)*(d*x^(1/3) + \\
& c)^5 + 75*(a*b^2 + I*b^3 - 2*(a^2*b + I*a*b^2)*c)*(d*x^(1/3) + c)^4 + 200* \\
& ((a^2*b + I*a*b^2)*c^2 - (a*b^2 + I*b^3)*c)*(d*x^(1/3) + c)^3 - 75*(2*(a^2* \\
& b + I*a*b^2)*c^3 - 3*(a*b^2 + I*b^3)*c^2)*(d*x^(1/3) + c)^2 + 75*((a^2*b + \\
& I*a*b^2)*c^4 - 2*(a*b^2 + I*b^3)*c^3)*(d*x^(1/3) + c) + (48*(a^2*b - I*a*b^ \\
& 2)*(d*x^(1/3) + c)^5 + 75*(a*b^2 - I*b^3 - 2*(a^2*b - I*a*b^2)*c)*(d*x^(1/3) \\
&) + c)^4 + 200*((a^2*b - I*a*b^2)*c^2 - (a*b^2 - I*b^3)*c)*(d*x^(1/3) + c)^ \\
& 3 - 75*(2*(a^2*b - I*a*b^2)*c^3 - 3*(a*b^2 - I*b^3)*c^2)*(d*x^(1/3) + c)^2
\end{aligned}$$

$$\begin{aligned}
& + 75*((a^2*b - I*a*b^2)*c^4 - 2*(a*b^2 - I*b^3)*c^3)*(d*x^{(1/3)} + c))*\cos(2 \\
& *d*x^{(1/3)} + 2*c) - (48*(-I*a^2*b - a*b^2)*(d*x^{(1/3)} + c)^5 + 75*(-I*a*b^2 \\
& - b^3 + 2*(I*a^2*b + a*b^2)*c)*(d*x^{(1/3)} + c)^4 + 200*((-I*a^2*b - a*b^2) \\
& *c^2 + (I*a*b^2 + b^3)*c)*(d*x^{(1/3)} + c)^3 + 75*(2*(I*a^2*b + a*b^2)*c^3 + \\
& 3*(-I*a*b^2 - b^3)*c^2)*(d*x^{(1/3)} + c)^2 + 75*((-I*a^2*b - a*b^2)*c^4 + 2 \\
& *(I*a*b^2 + b^3)*c^3)*(d*x^{(1/3)} + c))*\sin(2*d*x^{(1/3)} + 2*c))*\log(((a^2 + \\
& b^2)*\cos(2*d*x^{(1/3)} + 2*c))^2 + 4*a*b*\sin(2*d*x^{(1/3)} + 2*c) + (a^2 + b^2)* \\
& \sin(2*d*x^{(1/3)} + 2*c))^2 + a^2 + b^2 + 2*(a^2 - b^2)*\cos(2*d*x^{(1/3)} + 2*c) \\
&))/(a^2 + b^2)) - 720*(I*a^2*b - a*b^2 + (I*a^2*b + a*b^2)*\cos(2*d*x^{(1/3)} + \\
& 2*c) - (a^2*b - I*a*b^2)*\sin(2*d*x^{(1/3)} + 2*c))*\text{polylog}(6, (I*a + b)*e^{(2 \\
& *I*d*x^{(1/3)} + 2*I*c)/(-I*a + b)} - 90*(5*a*b^2 + 5*I*b^3 + 16*(a^2*b + I*a \\
& *b^2)*(d*x^{(1/3)} + c) - 10*(a^2*b + I*a*b^2)*c + (5*a*b^2 - 5*I*b^3 + 16*(a \\
& ^2*b - I*a*b^2)*(d*x^{(1/3)} + c) - 10*(a^2*b - I*a*b^2)*c)*\cos(2*d*x^{(1/3)} + \\
& 2*c) + (5*I*a*b^2 + 5*b^3 + 16*(I*a^2*b + a*b^2)*(d*x^{(1/3)} + c) + 10*(-I* \\
& a^2*b - a*b^2)*c)*\sin(2*d*x^{(1/3)} + 2*c))*\text{polylog}(5, (I*a + b)*e^{(2*I*d*x^{(1/3)} + \\
& 2*I*c)/(-I*a + b)} - 60*(24*(-I*a^2*b + a*b^2)*(d*x^{(1/3)} + c)^2 + 1 \\
& 0*(-I*a^2*b + a*b^2)*c^2 + 15*(-I*a*b^2 + b^3 + 2*(I*a^2*b - a*b^2)*c)*(d*x^{(1/3)} + c) + 10*(I*a*b^2 - b^3)*c + (24*(-I*a^2*b - a*b^2)*(d*x^{(1/3)} + c) \\
& ^2 + 10*(-I*a^2*b - a*b^2)*c^2 + 15*(-I*a*b^2 - b^3 + 2*(I*a^2*b + a*b^2)*c) \\
&)*(d*x^{(1/3)} + c) + 10*(I*a*b^2 + b^3)*c)*\cos(2*d*x^{(1/3)} + 2*c) + (24*(a^2 \\
& *b - I*a*b^2)*(d*x^{(1/3)} + c)^2 + 10*(a^2*b - I*a*b^2)*c^2 + 15*(a*b^2 - I* \\
& b^3 - 2*(a^2*b - I*a*b^2)*c)*(d*x^{(1/3)} + c) - 10*(a*b^2 - I*b^3)*c)*\sin(2* \\
& d*x^{(1/3)} + 2*c))*\text{polylog}(4, (I*a + b)*e^{(2*I*d*x^{(1/3)} + 2*I*c)/(-I*a + b)} \\
&) + 30*(32*(a^2*b + I*a*b^2)*(d*x^{(1/3)} + c)^3 - 10*(a^2*b + I*a*b^2)*c^3 + \\
& 30*(a*b^2 + I*b^3 - 2*(a^2*b + I*a*b^2)*c)*(d*x^{(1/3)} + c)^2 + 15*(a*b^2 + \\
& I*b^3)*c^2 + 40*((a^2*b + I*a*b^2)*c^2 - (a*b^2 + I*b^3)*c)*(d*x^{(1/3)} + c) \\
&) + (32*(a^2*b - I*a*b^2)*(d*x^{(1/3)} + c)^3 - 10*(a^2*b - I*a*b^2)*c^3 + 30 \\
& *(a*b^2 - I*b^3 - 2*(a^2*b - I*a*b^2)*c)*(d*x^{(1/3)} + c)^2 + 15*(a*b^2 - I* \\
& b^3)*c^2 + 40*((a^2*b - I*a*b^2)*c^2 - (a*b^2 - I*b^3)*c)*(d*x^{(1/3)} + c))* \\
& \cos(2*d*x^{(1/3)} + 2*c) - (32*(-I*a^2*b - a*b^2)*(d*x^{(1/3)} + c)^3 + 10*(I*a \\
& ^2*b + a*b^2)*c^3 + 30*(-I*a*b^2 - b^3 + 2*(I*a^2*b + a*b^2)*c)*(d*x^{(1/3)} \\
& + c)^2 + 15*(-I*a*b^2 - b^3)*c^2 + 40*((-I*a^2*b - a*b^2)*c^2 + (I*a*b^2 + \\
& b^3)*c)*(d*x^{(1/3)} + c))*\sin(2*d*x^{(1/3)} + 2*c))*\text{polylog}(3, (I*a + b)*e^{(2* \\
& I*d*x^{(1/3)} + 2*I*c)/(-I*a + b)} - 5*((-I*a^3 - 3*a^2*b + 3*I*a*b^2 + b^3)* \\
& (d*x^{(1/3)} + c)^6 - 6*(2*a*b^2 - 2*I*b^3 - (I*a^3 + 3*a^2*b - 3*I*a*b^2 - b \\
& ^3)*c)*(d*x^{(1/3)} + c)^5 - 60*(a*b^2 - I*b^3)*(d*x^{(1/3)} + c)*c^4 + 15*((-I \\
& *a^3 - 3*a^2*b + 3*I*a*b^2 + b^3)*c^2 + 4*(a*b^2 - I*b^3)*c)*(d*x^{(1/3)} + c) \\
&)^4 + 20*((I*a^3 + 3*a^2*b - 3*I*a*b^2 - b^3)*c^3 - 6*(a*b^2 - I*b^3)*c^2)* \\
& (d*x^{(1/3)} + c)^3 + 15*((-I*a^3 - 3*a^2*b + 3*I*a*b^2 + b^3)*c^4 + 8*(a*b^2 \\
& - I*b^3)*c^3)*(d*x^{(1/3)} + c)^2*\sin(2*d*x^{(1/3)} + 2*c))/(a^5 + I*a^4*b + \\
& 2*a^3*b^2 + 2*I*a^2*b^3 + a*b^4 + I*b^5 + (a^5 - I*a^4*b + 2*a^3*b^2 - 2*I* \\
& a^2*b^3 + a*b^4 - I*b^5)*\cos(2*d*x^{(1/3)} + 2*c) - (-I*a^5 - a^4*b - 2*I*a^3 \\
& *b^2 - 2*a^2*b^3 - I*a*b^4 - b^5)*\sin(2*d*x^{(1/3)} + 2*c)))/d^6
\end{aligned}$$

Giac [F]

$$\int \frac{x}{(a + b \tan(c + d\sqrt[3]{x}))^2} dx = \int \frac{x}{(b \tan(dx^{\frac{1}{3}} + c) + a)^2} dx$$

[In] integrate(x/(a+b*tan(c+d*x^(1/3)))^2,x, algorithm="giac")

[Out] integrate(x/(b*tan(d*x^(1/3) + c) + a)^2, x)

Mupad [F(-1)]

Timed out.

$$\int \frac{x}{(a + b \tan(c + d\sqrt[3]{x}))^2} dx = \int \frac{x}{(a + b \tan(c + dx^{1/3}))^2} dx$$

[In] int(x/(a + b*tan(c + d*x^(1/3)))^2,x)

[Out] int(x/(a + b*tan(c + d*x^(1/3)))^2, x)

3.64
$$\int \frac{1}{\left(a+b \tan \left(c+d \sqrt[3]{x}\right)\right)^2} dx$$

Optimal result	439
Rubi [A] (verified)	440
Mathematica [A] (verified)	447
Maple [F]	447
Fricas [B] (verification not implemented)	448
Sympy [F]	449
Maxima [B] (verification not implemented)	449
Giac [F]	450
Mupad [F(-1)]	450

Optimal result

Integrand size = 16, antiderivative size = 610

$$\begin{aligned}
 \int \frac{1}{(a + b \tan(c + d\sqrt[3]{x}))^2} dx &= -\frac{6ib^2x^{2/3}}{(a^2 + b^2)^2 d} \\
 &+ \frac{6b^2x^{2/3}}{(a + ib)(ia + b)^2 d (ia - b + (ia + b)e^{2i(c+d\sqrt[3]{x})})} \\
 &+ \frac{x}{(a - ib)^2} + \frac{4bx}{(ia - b)(a - ib)^2} - \frac{4b^2x}{(a^2 + b^2)^2} \\
 &+ \frac{6b^2\sqrt[3]{x} \log\left(1 + \frac{(a-ib)e^{2i(c+d\sqrt[3]{x})}}{a+ib}\right)}{(a^2 + b^2)^2 d^2} \\
 &+ \frac{6bx^{2/3} \log\left(1 + \frac{(a-ib)e^{2i(c+d\sqrt[3]{x})}}{a+ib}\right)}{(a - ib)^2(a + ib)d} \\
 &- \frac{6ib^2x^{2/3} \log\left(1 + \frac{(a-ib)e^{2i(c+d\sqrt[3]{x})}}{a+ib}\right)}{(a^2 + b^2)^2 d} \\
 &- \frac{3ib^2 \text{PolyLog}\left(2, -\frac{(a-ib)e^{2i(c+d\sqrt[3]{x})}}{a+ib}\right)}{(a^2 + b^2)^2 d^3} \\
 &+ \frac{6b\sqrt[3]{x} \text{PolyLog}\left(2, -\frac{(a-ib)e^{2i(c+d\sqrt[3]{x})}}{a+ib}\right)}{(ia - b)(a - ib)^2 d^2} \\
 &- \frac{6b^2\sqrt[3]{x} \text{PolyLog}\left(2, -\frac{(a-ib)e^{2i(c+d\sqrt[3]{x})}}{a+ib}\right)}{(a^2 + b^2)^2 d^2} \\
 &+ \frac{3b \text{PolyLog}\left(3, -\frac{(a-ib)e^{2i(c+d\sqrt[3]{x})}}{a+ib}\right)}{(a - ib)^2(a + ib)d^3} \\
 &- \frac{3ib^2 \text{PolyLog}\left(3, -\frac{(a-ib)e^{2i(c+d\sqrt[3]{x})}}{a+ib}\right)}{(a^2 + b^2)^2 d^3}
 \end{aligned}$$

[Out] $-6*I*b^2*x^{(2/3)}/(a^2+b^2)^2/d+6*b^2*x^{(2/3)}/(a+I*b)/(I*a+b)^2/d/(I*a-b+(I*a+b)*\exp(2*I*(c+d*x^{(1/3)})))+x/(a-I*b)^2+4*b*x/(I*a-b)/(a-I*b)^2-4*b^2*x/(a^2+b^2)^2/d^2+6*b*x^{(2/3)}*\ln(1+(a-I*b)*\exp(2*I*(c+d*x^{(1/3)})))/(a+I*b)/(a^2+b^2)^2/d^2+6*b*x^{(2/3)}*\ln(1+(a-I*b)*\exp(2*I*(c+d*x^{(1/3)})))/(a+I*b)/(a-I*b)^2/(a+I*b)/d-6*I*b^2*x^{(2/3)}*\ln(1+(a-I*b)*\exp(2*I*(c+d*x^{(1/3)})))/(a+I*b)/(a^2+b^2)^2/d-3*I*b^2*polylog(2,-(a-I*b)*\exp(2*I*(c+d*x^{(1/3)})))/(a+I*b)/(a^2$

$$\begin{aligned}
& +b^2)^2/d^3+6*b*x^{(1/3)*polylog(2,-(a-I*b)*exp(2*I*(c+d*x^{(1/3)}))/(a+I*b))/} \\
& (I*a-b)/(a-I*b)^2/d^2-6*b^2*x^{(1/3)*polylog(2,-(a-I*b)*exp(2*I*(c+d*x^{(1/3)}))} \\
&)/(a+I*b))/(a^2+b^2)^2/d^2+3*b*polylog(3,-(a-I*b)*exp(2*I*(c+d*x^{(1/3)}))/(} \\
& a+I*b))/(a-I*b)^2/(a+I*b)/d^3-3*I*b^2*polylog(3,-(a-I*b)*exp(2*I*(c+d*x^{(1/} \\
& 3)))/(a+I*b))/(a^2+b^2)^2/d^3
\end{aligned}$$

Rubi [A] (verified)

Time = 1.59 (sec) , antiderivative size = 610, normalized size of antiderivative = 1.00, number of steps used = 19, number of rules used = 11, $\frac{\text{number of rules}}{\text{integrand size}} = 0.688$, Rules

used = {3824, 3815, 2216, 2215, 2221, 2611, 2320, 6724, 2222, 2317, 2438}

$$\int \frac{1}{(a + b \tan(c + d\sqrt[3]{x}))^2} dx = -\frac{3ib^2 \operatorname{PolyLog}\left(2, -\frac{(a-ib)e^{2i(c+d\sqrt[3]{x})}}{a+ib}\right)}{d^3(a^2+b^2)^2}$$

$$-\frac{3ib^2 \operatorname{PolyLog}\left(3, -\frac{(a-ib)e^{2i(c+d\sqrt[3]{x})}}{a+ib}\right)}{d^3(a^2+b^2)^2}$$

$$-\frac{6b^2\sqrt[3]{x} \operatorname{PolyLog}\left(2, -\frac{(a-ib)e^{2i(c+d\sqrt[3]{x})}}{a+ib}\right)}{d^2(a^2+b^2)^2}$$

$$+\frac{6b^2\sqrt[3]{x} \log\left(1 + \frac{(a-ib)e^{2i(c+d\sqrt[3]{x})}}{a+ib}\right)}{d^2(a^2+b^2)^2}$$

$$-\frac{6ib^2x^{2/3} \log\left(1 + \frac{(a-ib)e^{2i(c+d\sqrt[3]{x})}}{a+ib}\right)}{d(a^2+b^2)^2}$$

$$-\frac{6ib^2x^{2/3}}{d(a^2+b^2)^2} - \frac{4b^2x}{(a^2+b^2)^2}$$

$$+\frac{6b^2x^{2/3}}{d(a+ib)(b+ia)^2((b+ia)e^{2i(c+d\sqrt[3]{x})} + ia - b)}$$

$$+\frac{3b \operatorname{PolyLog}\left(3, -\frac{(a-ib)e^{2i(c+d\sqrt[3]{x})}}{a+ib}\right)}{d^3(a-ib)^2(a+ib)}$$

$$+\frac{6b\sqrt[3]{x} \operatorname{PolyLog}\left(2, -\frac{(a-ib)e^{2i(c+d\sqrt[3]{x})}}{a+ib}\right)}{d^2(-b+ia)(a-ib)^2}$$

$$+\frac{6bx^{2/3} \log\left(1 + \frac{(a-ib)e^{2i(c+d\sqrt[3]{x})}}{a+ib}\right)}{d(a-ib)^2(a+ib)}$$

$$+\frac{4bx}{(-b+ia)(a-ib)^2} + \frac{x}{(a-ib)^2}$$

[In] Int[(a + b*Tan[c + d*x^(1/3)])^(-2), x]

[Out] ((-6*I)*b^2*x^(2/3))/((a^2 + b^2)^2*d) + (6*b^2*x^(2/3))/((a + I*b)*(I*a + b)^2*d*(I*a - b + (I*a + b)*E^((2*I)*(c + d*x^(1/3)))) + x/(a - I*b)^2 + (4*b*x)/((I*a - b)*(a - I*b)^2) - (4*b^2*x)/(a^2 + b^2)^2 + (6*b^2*x^(1/3)*Log[1 + ((a - I*b)*E^((2*I)*(c + d*x^(1/3))))/(a + I*b)])/((a^2 + b^2)^2*d^2) + (6*b*x^(2/3)*Log[1 + ((a - I*b)*E^((2*I)*(c + d*x^(1/3))))/(a + I*b)])/((a - I*b)^2*(a + I*b)*d) - ((6*I)*b^2*x^(2/3)*Log[1 + ((a - I*b)*E^((2*I)*(c + d*x^(1/3))))/(a + I*b)])/((a^2 + b^2)^2*d) - ((3*I)*b^2*PolyLog[2, -((

$$\frac{(a - I*b)*E^{((2*I)*(c + d*x^{(1/3)}))}/(a + I*b)}}{(a^2 + b^2)^2*d^3} + (6*b*x^{(1/3)}*PolyLog[2, -(((a - I*b)*E^{((2*I)*(c + d*x^{(1/3)}))}/(a + I*b)))]/(I*a - b)*(a - I*b)^2*d^2 - (6*b^2*x^{(1/3)}*PolyLog[2, -(((a - I*b)*E^{((2*I)*(c + d*x^{(1/3)}))}/(a + I*b)))]/(a^2 + b^2)^2*d^2) + (3*b*PolyLog[3, -(((a - I*b)*E^{((2*I)*(c + d*x^{(1/3)}))}/(a + I*b)))]/(a - I*b)^2*(a + I*b)*d^3) - ((3*I)*b^2*PolyLog[3, -(((a - I*b)*E^{((2*I)*(c + d*x^{(1/3)}))}/(a + I*b)))]/(a^2 + b^2)^2*d^3)$$

Rule 2215

```
Int[((c_.) + (d_.)*(x_))^(m_.)/((a_) + (b_.)*((F_)^((g_.)*((e_.) + (f_.)*(x_))))^(n_.)), x_Symbol] := Simp[(c + d*x)^(m + 1)/(a*d*(m + 1)), x] - Dist[b/a, Int[(c + d*x)^m*((F^(g*(e + f*x)))^n/(a + b*(F^(g*(e + f*x)))^n)), x], x] /; FreeQ[{F, a, b, c, d, e, f, g, n}, x] && IGtQ[m, 0]
```

Rule 2216

```
Int[((a_) + (b_.)*((F_)^((g_.)*((e_.) + (f_.)*(x_))))^(n_.))^p*((c_.) + (d_.)*(x_))^(m_.), x_Symbol] := Dist[1/a, Int[(c + d*x)^m*(a + b*(F^(g*(e + f*x)))^n)^(p + 1), x], x] - Dist[b/a, Int[(c + d*x)^m*(F^(g*(e + f*x)))^n*(a + b*(F^(g*(e + f*x)))^n)^p, x], x] /; FreeQ[{F, a, b, c, d, e, f, g, n}, x] && ILtQ[p, 0] && IGtQ[m, 0]
```

Rule 2221

```
Int[((F_)^((g_.)*((e_.) + (f_.)*(x_))))^(n_.)*((c_.) + (d_.)*(x_))^(m_.)/((a_) + (b_.)*((F_)^((g_.)*((e_.) + (f_.)*(x_))))^(n_.)), x_Symbol] := Simp[((c + d*x)^m/(b*f*g*n*Log[F]))*Log[1 + b*((F^(g*(e + f*x)))^n/a)], x] - Dist[d*(m/(b*f*g*n*Log[F])), Int[(c + d*x)^(m - 1)*Log[1 + b*((F^(g*(e + f*x)))^n/a)], x], x] /; FreeQ[{F, a, b, c, d, e, f, g, n}, x] && IGtQ[m, 0]
```

Rule 2222

```
Int[((F_)^((g_.)*((e_.) + (f_.)*(x_))))^(n_.)*((a_.) + (b_.)*((F_)^((g_.)*((e_.) + (f_.)*(x_))))^(n_.))^p*((c_.) + (d_.)*(x_))^(m_.), x_Symbol] := Simp[(c + d*x)^m*((a + b*(F^(g*(e + f*x)))^n)^(p + 1)/(b*f*g*n*(p + 1)*Log[F])), x] - Dist[d*(m/(b*f*g*n*(p + 1)*Log[F])), Int[(c + d*x)^(m - 1)*(a + b*(F^(g*(e + f*x)))^n)^(p + 1), x], x] /; FreeQ[{F, a, b, c, d, e, f, g, m, n, p}, x] && NeQ[p, -1]
```

Rule 2317

```
Int[Log[(a_) + (b_.)*((F_)^((e_.)*((c_.) + (d_.)*(x_))))^(n_.)], x_Symbol] := Dist[1/(d*e*n*Log[F]), Subst[Int[Log[a + b*x]/x, x], x, (F^(e*(c + d*x)))^n], x] /; FreeQ[{F, a, b, c, d, e, n}, x] && GtQ[a, 0]
```

Rule 2320

```
Int[u_, x_Symbol] := With[{v = FunctionOfExponential[u, x]}, Dist[v/D[v, x]
, Subst[Int[FunctionOfExponentialFunction[u, x]/x, x], x, v], x] /; Functi
onOfExponentialQ[u, x] && !MatchQ[u, (w_)*((a_)*(v_)^(n_))^(m_)] /; FreeQ[
{a, m, n}, x] && IntegerQ[m*n] && !MatchQ[u, E^((c_)*((a_) + (b_)*x))*
(F_) [v_] /; FreeQ[{a, b, c}, x] && InverseFunctionQ[F[x]]]
```

Rule 2438

```
Int[Log[(c_)*((d_) + (e_)*(x_)^(n_))]/(x_), x_Symbol] := Simp[-PolyLog[2
, (-c)*e*x^n]/n, x] /; FreeQ[{c, d, e, n}, x] && EqQ[c*d, 1]
```

Rule 2611

```
Int[Log[1 + (e_)*((F_)^((c_)*((a_) + (b_)*(x_))))^(n_)]*((f_) + (g_)
*(x_)^(m_), x_Symbol] := Simp[(-f + g*x)^m*(PolyLog[2, (-e)*(F^(c*(a +
b*x)))^n]/(b*c*n*Log[F])), x] + Dist[g*(m/(b*c*n*Log[F])), Int[(f + g*x)^(m
- 1)*PolyLog[2, (-e)*(F^(c*(a + b*x)))^n], x], x] /; FreeQ[{F, a, b, c, e,
f, g, n}, x] && GtQ[m, 0]
```

Rule 3815

```
Int[((c_) + (d_)*(x_))^(m_)*((a_) + (b_)*tan[(e_) + (f_)*(x_)])^(n_),
x_Symbol] := Int[ExpandIntegrand[(c + d*x)^m, (1/(a - I*b) - 2*I*(b/(a^2 +
b^2 + (a - I*b)^2*E^(2*I*(e + f*x))))^(-n), x], x] /; FreeQ[{a, b, c, d,
e, f}, x] && NeQ[a^2 + b^2, 0] && ILtQ[n, 0] && IGtQ[m, 0]
```

Rule 3824

```
Int[((a_) + (b_)*Tan[(c_) + (d_)*(x_)^(n_)])^(p_), x_Symbol] := Dist[1
/n, Subst[Int[x^(1/n - 1)*(a + b*Tan[c + d*x])^p, x], x, x^n], x] /; FreeQ[
{a, b, c, d, p}, x] && IGtQ[1/n, 0] && IntegerQ[p]
```

Rule 6724

```
Int[PolyLog[n_, (c_)*((a_) + (b_)*(x_))^(p_)]/((d_) + (e_)*(x_)), x_S
ymbol] := Simp[PolyLog[n + 1, c*(a + b*x)^p]/(e*p), x] /; FreeQ[{a, b, c, d
, e, n, p}, x] && EqQ[b*d, a*e]
```

Rubi steps

$$\text{integral} = 3 \text{Subst} \left(\int \frac{x^2}{(a + b \tan(c + dx))^2} dx, x, \sqrt[3]{x} \right)$$

$$\begin{aligned}
&= 3\text{Subst} \left(\int \left(\frac{x^2}{(a-ib)^2} - \frac{4b^2x^2}{(ia+b)^2 (ia(1+\frac{ib}{a}) + ia(1-\frac{ib}{a})e^{2ic+2idx})^2} \right. \right. \\
&\quad \left. \left. + \frac{4bx^2}{(a-ib)^2 (ia(1+\frac{ib}{a}) + ia(1-\frac{ib}{a})e^{2ic+2idx})} \right) dx, x, \sqrt[3]{x} \right) \\
&= \frac{x}{(a-ib)^2} + \frac{(12b)\text{Subst} \left(\int \frac{x^2}{ia(1+\frac{ib}{a}) + ia(1-\frac{ib}{a})e^{2ic+2idx}} dx, x, \sqrt[3]{x} \right)}{(a-ib)^2} \\
&\quad - \frac{(12b^2)\text{Subst} \left(\int \frac{x^2}{(ia(1+\frac{ib}{a}) + ia(1-\frac{ib}{a})e^{2ic+2idx})^2} dx, x, \sqrt[3]{x} \right)}{(ia+b)^2} \\
&= \frac{x}{(a-ib)^2} + \frac{4bx}{(ia-b)(a-ib)^2} + \frac{(12b^2)\text{Subst} \left(\int \frac{x^2}{ia(1+\frac{ib}{a}) + ia(1-\frac{ib}{a})e^{2ic+2idx}} dx, x, \sqrt[3]{x} \right)}{(ia-b)(a-ib)^2} \\
&\quad - \frac{(12b)\text{Subst} \left(\int \frac{e^{2ic+2idx}x^2}{ia(1+\frac{ib}{a}) + ia(1-\frac{ib}{a})e^{2ic+2idx}} dx, x, \sqrt[3]{x} \right)}{a^2+b^2} \\
&\quad - \frac{(12b^2)\text{Subst} \left(\int \frac{e^{2ic+2idx}x^2}{(ia(1+\frac{ib}{a}) + ia(1-\frac{ib}{a})e^{2ic+2idx})^2} dx, x, \sqrt[3]{x} \right)}{a^2+b^2} \\
&= -\frac{6b^2x^{2/3}}{(a-ib)^2(a+ib)d(ia-b+(ia+b)e^{2i(c+d\sqrt[3]{x}})} + \frac{x}{(a-ib)^2} \\
&\quad + \frac{4bx}{(ia-b)(a-ib)^2} - \frac{4b^2x}{(a^2+b^2)^2} + \frac{6bx^{2/3} \log \left(1 + \frac{(a-ib)e^{2i(c+d\sqrt[3]{x}})}{a+ib} \right)}{(a-ib)^2(a+ib)d} \\
&\quad - \frac{(12b^2)\text{Subst} \left(\int \frac{e^{2ic+2idx}x^2}{ia(1+\frac{ib}{a}) + ia(1-\frac{ib}{a})e^{2ic+2idx}} dx, x, \sqrt[3]{x} \right)}{(a+ib)^2(ia+b)} \\
&\quad - \frac{(12b)\text{Subst} \left(\int x \log \left(1 + \frac{(1-\frac{ib}{a})e^{2ic+2idx}}{1+\frac{ib}{a}} \right) dx, x, \sqrt[3]{x} \right)}{(a-ib)^2(a+ib)d} \\
&\quad + \frac{(12b^2)\text{Subst} \left(\int \frac{x}{ia(1+\frac{ib}{a}) + ia(1-\frac{ib}{a})e^{2ic+2idx}} dx, x, \sqrt[3]{x} \right)}{(a-ib)^2(a+ib)d}
\end{aligned}$$

$$\begin{aligned}
&= -\frac{6ib^2x^{2/3}}{(a^2+b^2)^2d} - \frac{6b^2x^{2/3}}{(a-ib)^2(a+ib)d} \frac{e^{2i(c+d\sqrt[3]{x})}}{(ia-b+(ia+b)e^{2i(c+d\sqrt[3]{x})})} + \frac{x}{(a-ib)^2} \\
&+ \frac{4bx}{(ia-b)(a-ib)^2} - \frac{4b^2x}{(a^2+b^2)^2} + \frac{6bx^{2/3} \log\left(1 + \frac{(a-ib)e^{2i(c+d\sqrt[3]{x})}}{a+ib}\right)}{(a-ib)^2(a+ib)d} \\
&- \frac{6ib^2x^{2/3} \log\left(1 + \frac{(a-ib)e^{2i(c+d\sqrt[3]{x})}}{a+ib}\right)}{(a^2+b^2)^2d} + \frac{6b\sqrt[3]{x} \operatorname{PolyLog}\left(2, -\frac{(a-ib)e^{2i(c+d\sqrt[3]{x})}}{a+ib}\right)}{(ia-b)(a-ib)^2d^2} \\
&- \frac{(6b) \operatorname{Subst}\left(\int \operatorname{PolyLog}\left(2, -\frac{(1-\frac{ib}{a})e^{2ic+2idx}}{1+\frac{ib}{a}}\right) dx, x, \sqrt[3]{x}\right)}{(ia-b)(a-ib)^2d^2} \\
&- \frac{(12b^2) \operatorname{Subst}\left(\int \frac{e^{2ic+2idx}x}{ia(1+\frac{ib}{a})+ia(1-\frac{ib}{a})e^{2ic+2idx}} dx, x, \sqrt[3]{x}\right)}{(a-ib)(a+ib)^2d} \\
&+ \frac{(12ib^2) \operatorname{Subst}\left(\int x \log\left(1 + \frac{(1-\frac{ib}{a})e^{2ic+2idx}}{1+\frac{ib}{a}}\right) dx, x, \sqrt[3]{x}\right)}{(a^2+b^2)^2d} \\
&= -\frac{6ib^2x^{2/3}}{(a^2+b^2)^2d} - \frac{6b^2x^{2/3}}{(a-ib)^2(a+ib)d} \frac{e^{2i(c+d\sqrt[3]{x})}}{(ia-b+(ia+b)e^{2i(c+d\sqrt[3]{x})})} + \frac{x}{(a-ib)^2} \\
&+ \frac{4bx}{(ia-b)(a-ib)^2} - \frac{4b^2x}{(a^2+b^2)^2} + \frac{6b^2\sqrt[3]{x} \log\left(1 + \frac{(a-ib)e^{2i(c+d\sqrt[3]{x})}}{a+ib}\right)}{(a^2+b^2)^2d^2} \\
&+ \frac{6bx^{2/3} \log\left(1 + \frac{(a-ib)e^{2i(c+d\sqrt[3]{x})}}{a+ib}\right)}{(a-ib)^2(a+ib)d} - \frac{6ib^2x^{2/3} \log\left(1 + \frac{(a-ib)e^{2i(c+d\sqrt[3]{x})}}{a+ib}\right)}{(a^2+b^2)^2d} \\
&+ \frac{6b\sqrt[3]{x} \operatorname{PolyLog}\left(2, -\frac{(a-ib)e^{2i(c+d\sqrt[3]{x})}}{a+ib}\right)}{(ia-b)(a-ib)^2d^2} - \frac{6b^2\sqrt[3]{x} \operatorname{PolyLog}\left(2, -\frac{(a-ib)e^{2i(c+d\sqrt[3]{x})}}{a+ib}\right)}{(a^2+b^2)^2d^2} \\
&+ \frac{(3b) \operatorname{Subst}\left(\int \frac{\operatorname{PolyLog}\left(2, -\frac{(a-ib)x}{a+ib}\right)}{x} dx, x, e^{2i(c+d\sqrt[3]{x})}\right)}{(a-ib)^2(a+ib)d^3} \\
&- \frac{(6b^2) \operatorname{Subst}\left(\int \log\left(1 + \frac{(1-\frac{ib}{a})e^{2ic+2idx}}{1+\frac{ib}{a}}\right) dx, x, \sqrt[3]{x}\right)}{(a^2+b^2)^2d^2} \\
&+ \frac{(6b^2) \operatorname{Subst}\left(\int \operatorname{PolyLog}\left(2, -\frac{(1-\frac{ib}{a})e^{2ic+2idx}}{1+\frac{ib}{a}}\right) dx, x, \sqrt[3]{x}\right)}{(a^2+b^2)^2d^2}
\end{aligned}$$

$$\begin{aligned}
&= -\frac{6ib^2x^{2/3}}{(a^2+b^2)^2d} - \frac{6b^2x^{2/3}}{(a-ib)^2(a+ib)d} \frac{ia-b+(ia+b)e^{2i(c+d\sqrt[3]{x}})}{(a-ib)^2(a+ib)d} \\
&+ \frac{x}{(a-ib)^2} + \frac{4bx}{(ia-b)(a-ib)^2} - \frac{4b^2x}{(a^2+b^2)^2} \\
&+ \frac{6b^2\sqrt[3]{x} \log\left(1 + \frac{(a-ib)e^{2i(c+d\sqrt[3]{x}})}{a+ib}\right)}{(a^2+b^2)^2d^2} + \frac{6bx^{2/3} \log\left(1 + \frac{(a-ib)e^{2i(c+d\sqrt[3]{x}})}{a+ib}\right)}{(a-ib)^2(a+ib)d} \\
&- \frac{6ib^2x^{2/3} \log\left(1 + \frac{(a-ib)e^{2i(c+d\sqrt[3]{x}})}{a+ib}\right)}{(a^2+b^2)^2d} + \frac{6b\sqrt[3]{x} \text{PolyLog}\left(2, -\frac{(a-ib)e^{2i(c+d\sqrt[3]{x}})}{a+ib}\right)}{(ia-b)(a-ib)^2d^2} \\
&- \frac{6b^2\sqrt[3]{x} \text{PolyLog}\left(2, -\frac{(a-ib)e^{2i(c+d\sqrt[3]{x}})}{a+ib}\right)}{(a^2+b^2)^2d^2} + \frac{3b \text{PolyLog}\left(3, -\frac{(a-ib)e^{2i(c+d\sqrt[3]{x}})}{a+ib}\right)}{(a-ib)^2(a+ib)d^3} \\
&+ \frac{(3ib^2) \text{Subst}\left(\int \frac{\log\left(1 + \frac{(1-\frac{ib}{a})x}{1+\frac{ib}{a}}\right)}{x} dx, x, e^{2i(c+d\sqrt[3]{x})}\right)}{(a^2+b^2)^2d^3} \\
&- \frac{(3ib^2) \text{Subst}\left(\int \frac{\text{PolyLog}\left(2, -\frac{(a-ib)x}{a+ib}\right)}{x} dx, x, e^{2i(c+d\sqrt[3]{x})}\right)}{(a^2+b^2)^2d^3} \\
&= -\frac{6ib^2x^{2/3}}{(a^2+b^2)^2d} - \frac{6b^2x^{2/3}}{(a-ib)^2(a+ib)d} \frac{ia-b+(ia+b)e^{2i(c+d\sqrt[3]{x}})}{(a-ib)^2(a+ib)d} \\
&+ \frac{x}{(a-ib)^2} + \frac{4bx}{(ia-b)(a-ib)^2} - \frac{4b^2x}{(a^2+b^2)^2} \\
&+ \frac{6b^2\sqrt[3]{x} \log\left(1 + \frac{(a-ib)e^{2i(c+d\sqrt[3]{x}})}{a+ib}\right)}{(a^2+b^2)^2d^2} + \frac{6bx^{2/3} \log\left(1 + \frac{(a-ib)e^{2i(c+d\sqrt[3]{x}})}{a+ib}\right)}{(a-ib)^2(a+ib)d} \\
&- \frac{6ib^2x^{2/3} \log\left(1 + \frac{(a-ib)e^{2i(c+d\sqrt[3]{x}})}{a+ib}\right)}{(a^2+b^2)^2d} - \frac{3ib^2 \text{PolyLog}\left(2, -\frac{(a-ib)e^{2i(c+d\sqrt[3]{x}})}{a+ib}\right)}{(a^2+b^2)^2d^3} \\
&+ \frac{6b\sqrt[3]{x} \text{PolyLog}\left(2, -\frac{(a-ib)e^{2i(c+d\sqrt[3]{x}})}{a+ib}\right)}{(ia-b)(a-ib)^2d^2} - \frac{6b^2\sqrt[3]{x} \text{PolyLog}\left(2, -\frac{(a-ib)e^{2i(c+d\sqrt[3]{x}})}{a+ib}\right)}{(a^2+b^2)^2d^2} \\
&+ \frac{3b \text{PolyLog}\left(3, -\frac{(a-ib)e^{2i(c+d\sqrt[3]{x}})}{a+ib}\right)}{(a-ib)^2(a+ib)d^3} - \frac{3ib^2 \text{PolyLog}\left(3, -\frac{(a-ib)e^{2i(c+d\sqrt[3]{x}})}{a+ib}\right)}{(a^2+b^2)^2d^3}
\end{aligned}$$

Mathematica [A] (verified)

Time = 2.91 (sec) , antiderivative size = 538, normalized size of antiderivative = 0.88

$$\int \frac{1}{(a + b \tan(c + d\sqrt[3]{x}))^2} dx$$

$$b \left(\frac{\frac{6bx^{2/3}}{a-ib} + \frac{4adx}{a-ib}}{a-ib} + \frac{6b(-ib(-1+e^{2ic})+a(1+e^{2ic}))\sqrt[3]{x} \log\left(1 + \frac{(a+ib)e^{-2i(c+d\sqrt[3]{x})}}{a-ib}\right)}{(a+ib)(ia+b)d} \right) + \frac{6a(-ib(-1+e^{2ic})+a(1+e^{2ic}))x^{2/3} \log\left(1 + \frac{(a+ib)e^{-2i(c+d\sqrt[3]{x})}}{a-ib}\right)}{(a+ib)(ia+b)}$$

=

`[In] Integrate[(a + b*Tan[c + d*x^(1/3)])^(-2), x]`

```
[Out] ((b*((6*b*x^(2/3))/(a - I*b) + (4*a*d*x)/(a - I*b) + (6*b*((-I)*b*(-1 + E^((2*I)*c)) + a*(1 + E^((2*I)*c))))*x^(1/3)*Log[1 + (a + I*b)/((a - I*b)*E^((2*I)*(c + d*x^(1/3)))]])/((a + I*b)*(I*a + b)*d) + (6*a*((-I)*b*(-1 + E^((2*I)*c)) + a*(1 + E^((2*I)*c)))*x^(2/3)*Log[1 + (a + I*b)/((a - I*b)*E^((2*I)*(c + d*x^(1/3)))]])/((a + I*b)*(I*a + b)) + (3*b*((-I)*b*(-1 + E^((2*I)*c)) + a*(1 + E^((2*I)*c)))*PolyLog[2, (-a - I*b)/((a - I*b)*E^((2*I)*(c + d*x^(1/3)))]])/((a^2 + b^2)*d^2) + (3*a*((-I)*b*(-1 + E^((2*I)*c)) + a*(1 + E^((2*I)*c)))*(2*d*x^(1/3)*PolyLog[2, (-a - I*b)/((a - I*b)*E^((2*I)*(c + d*x^(1/3)))]]) - I*PolyLog[3, (-a - I*b)/((a - I*b)*E^((2*I)*(c + d*x^(1/3)))]])/((a^2 + b^2)*d^2))/((d*(b - b*E^((2*I)*c) - I*a*(1 + E^((2*I)*c)))) + (x*(a*Cos[c] - b*Sin[c]))/(a*Cos[c] + b*Sin[c]) + (3*b^2*x^(2/3)*Sin[d*x^(1/3)])/((d*(a*Cos[c] + b*Sin[c])*(a*Cos[c + d*x^(1/3)] + b*Sin[c + d*x^(1/3)])))/(a^2 + b^2)
```

Maple [F]

$$\int \frac{1}{\left(a + b \tan\left(c + d x^{\frac{1}{3}}\right)\right)^2} dx$$

`[In] int(1/(a+b*tan(c+d*x^(1/3)))^2,x)``[Out] int(1/(a+b*tan(c+d*x^(1/3)))^2,x)`

Fricas [B] (verification not implemented)

Both result and optimal contain complex but leaf count of result is larger than twice the leaf count of optimal. 1187 vs. $2(491) = 982$.

Time = 0.27 (sec) , antiderivative size = 1187, normalized size of antiderivative = 1.95

$$\int \frac{1}{(a + b \tan(c + d\sqrt[3]{x}))^2} dx = \text{Too large to display}$$

[In] integrate(1/(a+b*tan(c+d*x^(1/3)))^2,x, algorithm="fricas")

[Out]
$$\begin{aligned} & -1/2*(6*b^3*d^2*x^{2/3} - 2*(a^3 - a*b^2)*d^3*x + 2*(a^3 - a*b^2)*d^3 + 3*(\\ & -2*I*a^2*b*d*x^{1/3} - I*a*b^2 + (-2*I*a*b^2*d*x^{1/3} - I*b^3)*\tan(d*x^{1/3} \\ & + c))*\operatorname{dilog}(2*((I*a*b - b^2)*\tan(d*x^{1/3} + c)^2 - a^2 - I*a*b + (I*a^2 \\ & - 2*a*b - I*b^2)*\tan(d*x^{1/3} + c)))/((a^2 + b^2)*\tan(d*x^{1/3} + c)^2 + a \\ & ^2 + b^2) + 1) + 3*(2*I*a^2*b*d*x^{1/3} + I*a*b^2 + (2*I*a*b^2*d*x^{1/3} + \\ & I*b^3)*\tan(d*x^{1/3} + c))*\operatorname{dilog}(2*((-I*a*b - b^2)*\tan(d*x^{1/3} + c)^2 - a \\ & ^2 + I*a*b + (-I*a^2 - 2*a*b + I*b^2)*\tan(d*x^{1/3} + c)))/((a^2 + b^2)*\tan(\\ & d*x^{1/3} + c)^2 + a^2 + b^2) + 1) - 6*(a^2*b*d^2*x^{2/3} - a^2*b*c^2 + a*b \\ & ^2*d*x^{1/3} + a*b^2*c + (a*b^2*d^2*x^{2/3} - a*b^2*c^2 + b^3*d*x^{1/3} + b \\ & ^3*c)*\tan(d*x^{1/3} + c))*\log(-2*((I*a*b - b^2)*\tan(d*x^{1/3} + c)^2 - a^2 \\ & - I*a*b + (I*a^2 - 2*a*b - I*b^2)*\tan(d*x^{1/3} + c)))/((a^2 + b^2)*\tan(d*x^{1/3} \\ & + c)^2 + a^2 + b^2)) - 6*(a^2*b*d^2*x^{2/3} - a^2*b*c^2 + a*b^2*d*x^{1/3} \\ & + a*b^2*c + (a*b^2*d^2*x^{2/3} - a*b^2*c^2 + b^3*d*x^{1/3} + b^3*c)*\tan \\ & (d*x^{1/3} + c))*\log(-2*((-I*a*b - b^2)*\tan(d*x^{1/3} + c)^2 - a^2 + I*a*b \\ & + (-I*a^2 - 2*a*b + I*b^2)*\tan(d*x^{1/3} + c)))/((a^2 + b^2)*\tan(d*x^{1/3} \\ & + c)^2 + a^2 + b^2)) - 6*(a^2*b*c^2 - a*b^2*c + (a*b^2*c^2 - b^3*c)*\tan(d*x \\ & ^{1/3} + c))*\log(((I*a*b + b^2)*\tan(d*x^{1/3} + c)^2 - a^2 + I*a*b + (I*a^2 \\ & + I*b^2)*\tan(d*x^{1/3} + c)))/(\tan(d*x^{1/3} + c)^2 + 1)) - 6*(a^2*b*c^2 - \\ & a*b^2*c + (a*b^2*c^2 - b^3*c)*\tan(d*x^{1/3} + c))*\log(((I*a*b - b^2)*\tan(d* \\ & x^{1/3} + c)^2 + a^2 + I*a*b + (I*a^2 + I*b^2)*\tan(d*x^{1/3} + c)))/(\tan(d*x \\ & ^{1/3} + c)^2 + 1)) - 3*(a*b^2*\tan(d*x^{1/3} + c) + a^2*b)*\operatorname{polylog}(3, ((a^2 \\ & + 2*I*a*b - b^2)*\tan(d*x^{1/3} + c)^2 - a^2 - 2*I*a*b + b^2 - 2*(-I*a^2 + \\ & 2*a*b + I*b^2)*\tan(d*x^{1/3} + c)))/((a^2 + b^2)*\tan(d*x^{1/3} + c)^2 + a^2 \\ & + b^2)) - 3*(a*b^2*\tan(d*x^{1/3} + c) + a^2*b)*\operatorname{polylog}(3, ((a^2 - 2*I*a*b - \\ & b^2)*\tan(d*x^{1/3} + c)^2 - a^2 + 2*I*a*b + b^2 - 2*(I*a^2 + 2*a*b - I*b^2 \\ &)*\tan(d*x^{1/3} + c)))/((a^2 + b^2)*\tan(d*x^{1/3} + c)^2 + a^2 + b^2)) - 2*(\\ & 3*a*b^2*d^2*x^{2/3} + (a^2*b - b^3)*d^3*x - (a^2*b - b^3)*d^3)*\tan(d*x^{1/3} \\ & + c))/((a^4*b + 2*a^2*b^3 + b^5)*d^3*\tan(d*x^{1/3} + c) + (a^5 + 2*a^3*b^ \\ & 2 + a*b^4)*d^3) \end{aligned}$$

SymPy [F]

$$\int \frac{1}{(a + b \tan(c + d\sqrt[3]{x}))^2} dx = \int \frac{1}{(a + b \tan(c + d\sqrt[3]{x}))^2} dx$$

```
[In] integrate(1/(a+b*tan(c+d*x**(1/3)))**2,x)
```

```
[Out] Integral((a + b*tan(c + d*x**(1/3)))**(-2), x)
```

Maxima [B] (verification not implemented)

Both result and optimal contain complex but leaf count of result is larger than twice the leaf count of optimal. 1732 vs. 2(491) = 982.

Time = 0.70 (sec) , antiderivative size = 1732, normalized size of antiderivative = 2.84

$$\int \frac{1}{(a + b \tan(c + d\sqrt[3]{x}))^2} dx = \text{Too large to display}$$

```
[In] integrate(1/(a+b*tan(c+d*x^(1/3)))^2,x, algorithm="maxima")
```

```
[Out] (3*(2*a*b*log(b*tan(d*x^(1/3) + c) + a)/(a^4 + 2*a^2*b^2 + b^4) - a*b*log(tan(d*x^(1/3) + c)^2 + 1)/(a^4 + 2*a^2*b^2 + b^4) + (a^2 - b^2)*(d*x^(1/3) + c)/(a^4 + 2*a^2*b^2 + b^4) - b/(a^3 + a*b^2 + (a^2*b + b^3)*tan(d*x^(1/3) + c)))*c^2 + ((a^3 - I*a^2*b + a*b^2 - I*b^3)*(d*x^(1/3) + c)^3 - 3*(a^3 - I*a^2*b + a*b^2 - I*b^3)*(d*x^(1/3) + c)^2*c - 6*((I*a*b^2 + b^3)*c*cos(2*d*x^(1/3) + 2*c) - (a*b^2 - I*b^3)*c*sin(2*d*x^(1/3) + 2*c) + (I*a*b^2 - b^3)*c)*arctan2(-b*cos(2*d*x^(1/3) + 2*c) + a*sin(2*d*x^(1/3) + 2*c) + b, a*cos(2*d*x^(1/3) + 2*c) + b*sin(2*d*x^(1/3) + 2*c) + a) - 6*((I*a^2*b - a*b^2)*(d*x^(1/3) + c)^2 + (I*a*b^2 - b^3 + 2*(-I*a^2*b + a*b^2)*c)*(d*x^(1/3) + c) + ((I*a^2*b + a*b^2)*(d*x^(1/3) + c)^2 + (I*a*b^2 + b^3 + 2*(-I*a^2*b - a*b^2)*c)*(d*x^(1/3) + c))*cos(2*d*x^(1/3) + 2*c) - ((a^2*b - I*a*b^2)*(d*x^(1/3) + c)^2 + (a*b^2 - I*b^3 - 2*(a^2*b - I*a*b^2)*c)*(d*x^(1/3) + c))*sin(2*d*x^(1/3) + 2*c))*arctan2((2*a*b*cos(2*d*x^(1/3) + 2*c) - (a^2 - b^2)*sin(2*d*x^(1/3) + 2*c))/(a^2 + b^2), (2*a*b*sin(2*d*x^(1/3) + 2*c) + a^2 + b^2 + (a^2 - b^2)*cos(2*d*x^(1/3) + 2*c))/(a^2 + b^2)) + ((a^3 - 3*I*a^2*b - 3*a*b^2 + I*b^3)*(d*x^(1/3) + c)^3 - 3*(2*I*a*b^2 + 2*b^3 + (a^3 - 3*I*a^2*b - 3*a*b^2 + I*b^3)*c)*(d*x^(1/3) + c)^2 - 12*(-I*a*b^2 - b^3)*(d*x^(1/3) + c)*c*cos(2*d*x^(1/3) + 2*c) - 3*(I*a*b^2 - b^3 + 2*(I*a^2*b - a*b^2)*(d*x^(1/3) + c) + 2*(-I*a^2*b + a*b^2)*c + (I*a*b^2 + b^3 + 2*(I*a^2*b + a*b^2)*(d*x^(1/3) + c) + 2*(-I*a^2*b - a*b^2)*c)*cos(2*d*x^(1/3) + 2*c) - (a*b^2 - I*b^3 + 2*(a^2*b - I*a*b^2)*(d*x^(1/3) + c) - 2*(a^2*b - I*a*b^2)*c)*sin(2*d*x^(1/3) + 2*c))*dilog((I*a + b)*e^(2*I*d*x^(1/3) + 2*I*c)/(-I*a + b)) - 3*((a*b^2 - I*b^3)*c*cos(2*d*x^(1/3) + 2*c) + (I*a*b^2 + b^3)*c*sin(2*d*
```

$$\begin{aligned}
& x^{1/3} + 2c) + (a^2 b^2 + I b^3) c) \log((a^2 + b^2) \cos(2 d x^{1/3} + 2c)^2 + 4 a b \sin(2 d x^{1/3} + 2c) + (a^2 + b^2) \sin(2 d x^{1/3} + 2c)^2 + a^2 + b^2 + 2(a^2 - b^2) \cos(2 d x^{1/3} + 2c)) + 3((a^2 b + I a b^2) (d x^{1/3} + c)^2 + (a^2 b^2 + I b^3 - 2(a^2 b + I a b^2) c) (d x^{1/3} + c) + ((a^2 b - I a b^2) (d x^{1/3} + c)^2 + (a^2 b^2 - I b^3 - 2(a^2 b - I a b^2) c) (d x^{1/3} + c)) \cos(2 d x^{1/3} + 2c) - ((-I a^2 b - a b^2) (d x^{1/3} + c)^2 + (-I a b^2 - b^3 + 2(I a^2 b + a b^2) c) (d x^{1/3} + c)) \sin(2 d x^{1/3} + 2c)) \log(((a^2 + b^2) \cos(2 d x^{1/3} + 2c)^2 + 4 a b \sin(2 d x^{1/3} + 2c) + (a^2 + b^2) \sin(2 d x^{1/3} + 2c)^2 + a^2 + b^2 + 2(a^2 - b^2) \cos(2 d x^{1/3} + 2c)) / (a^2 + b^2)) + 3(a^2 b + I a b^2 + (a^2 b - I a b^2) \cos(2 d x^{1/3} + 2c) - (-I a^2 b - a b^2) \sin(2 d x^{1/3} + 2c)) \operatorname{polylog}(3, (I a + b) e^{(2 I d x^{1/3} + 2 I c) / (-I a + b)}) + ((I a^3 + 3 a^2 b - 3 I a b^2 - b^3) (d x^{1/3} + c)^3 + 3(2 a b^2 - 2 I b^3 - (I a^3 + 3 a^2 b - 3 I a b^2 - b^3) c) (d x^{1/3} + c)^2 - 12(a b^2 - I b^3) (d x^{1/3} + c) c) \sin(2 d x^{1/3} + 2c) / (a^5 + I a^4 b + 2 a^3 b^2 + 2 I a^2 b^3 + a b^4 + I b^5 + (a^5 - I a^4 b + 2 a^3 b^2 - 2 I a^2 b^3 + a b^4 - I b^5) \cos(2 d x^{1/3} + 2c) - (-I a^5 - a^4 b - 2 I a^3 b^2 - 2 a^2 b^3 - I a b^4 - b^5) \sin(2 d x^{1/3} + 2c))) / d^3
\end{aligned}$$

Giac [F]

$$\int \frac{1}{(a + b \tan(c + d \sqrt[3]{x}))^2} dx = \int \frac{1}{(b \tan(dx^{1/3} + c) + a)^2} dx$$

[In] integrate(1/(a+b*tan(c+d*x^(1/3)))^2,x, algorithm="giac")

[Out] integrate((b*tan(d*x^(1/3) + c) + a)^(-2), x)

Mupad [F(-1)]

Timed out.

$$\int \frac{1}{(a + b \tan(c + d \sqrt[3]{x}))^2} dx = \int \frac{1}{(a + b \tan(c + d x^{1/3}))^2} dx$$

[In] int(1/(a + b*tan(c + d*x^(1/3)))^2,x)

[Out] int(1/(a + b*tan(c + d*x^(1/3)))^2, x)

$$3.65 \quad \int \frac{1}{x \left(a + b \tan \left(c + d \sqrt[3]{x} \right) \right)^2} dx$$

Optimal result	451
Rubi [N/A]	451
Mathematica [N/A]	452
Maple [N/A] (verified)	452
Fricas [N/A]	452
Sympy [N/A]	453
Maxima [N/A]	453
Giac [N/A]	455
Mupad [N/A]	455

Optimal result

Integrand size = 20, antiderivative size = 20

$$\int \frac{1}{x \left(a + b \tan \left(c + d \sqrt[3]{x} \right) \right)^2} dx = \text{Int} \left(\frac{1}{x \left(a + b \tan \left(c + d \sqrt[3]{x} \right) \right)^2}, x \right)$$

[Out] Unintegrable(1/x/(a+b*tan(c+d*x^(1/3)))^2,x)

Rubi [N/A]

Not integrable

Time = 0.03 (sec) , antiderivative size = 20, normalized size of antiderivative = 1.00, number of steps used = 0, number of rules used = 0, $\frac{\text{number of rules}}{\text{integrand size}} = 0.000$, Rules used = {}

$$\int \frac{1}{x \left(a + b \tan \left(c + d \sqrt[3]{x} \right) \right)^2} dx = \int \frac{1}{x \left(a + b \tan \left(c + d \sqrt[3]{x} \right) \right)^2} dx$$

[In] Int[1/(x*(a + b*Tan[c + d*x^(1/3)])^2),x]

[Out] Defer[Int][1/(x*(a + b*Tan[c + d*x^(1/3)])^2), x]

Rubi steps

$$\text{integral} = \int \frac{1}{x \left(a + b \tan \left(c + d \sqrt[3]{x} \right) \right)^2} dx$$

Mathematica [N/A]

Not integrable

Time = 165.45 (sec) , antiderivative size = 22, normalized size of antiderivative = 1.10

$$\int \frac{1}{x (a + b \tan (c + d \sqrt[3]{x}))^2} dx = \int \frac{1}{x (a + b \tan (c + d \sqrt[3]{x}))^2} dx$$

[In] Integrate[1/(x*(a + b*Tan[c + d*x^(1/3)]))^2,x]

[Out] Integrate[1/(x*(a + b*Tan[c + d*x^(1/3)]))^2, x]

Maple [N/A] (verified)

Not integrable

Time = 0.64 (sec) , antiderivative size = 18, normalized size of antiderivative = 0.90

$$\int \frac{1}{x \left(a + b \tan \left(c + dx^{\frac{1}{3}} \right) \right)^2} dx$$

[In] int(1/x/(a+b*tan(c+d*x^(1/3)))^2,x)

[Out] int(1/x/(a+b*tan(c+d*x^(1/3)))^2,x)

Fricas [N/A]

Not integrable

Time = 0.24 (sec) , antiderivative size = 38, normalized size of antiderivative = 1.90

$$\int \frac{1}{x (a + b \tan (c + d \sqrt[3]{x}))^2} dx = \int \frac{1}{\left(b \tan \left(dx^{\frac{1}{3}} + c \right) + a \right)^2 x} dx$$

[In] integrate(1/x/(a+b*tan(c+d*x^(1/3)))^2,x, algorithm="fricas")

[Out] integral(1/(b^2*x*tan(d*x^(1/3) + c)^2 + 2*a*b*x*tan(d*x^(1/3) + c) + a^2*x), x)

Sympy [N/A]

Not integrable

Time = 3.81 (sec) , antiderivative size = 19, normalized size of antiderivative = 0.95

$$\int \frac{1}{x (a + b \tan (c + d \sqrt[3]{x}))^2} dx = \int \frac{1}{x (a + b \tan (c + d \sqrt[3]{x}))^2} dx$$

`[In] integrate(1/x/(a+b*tan(c+d*x**(1/3)))**2,x)``[Out] Integral(1/(x*(a + b*tan(c + d*x**(1/3)))**2), x)`**Maxima [N/A]**

Not integrable

Time = 3.56 (sec) , antiderivative size = 3514, normalized size of antiderivative = 175.70

$$\int \frac{1}{x (a + b \tan (c + d \sqrt[3]{x}))^2} dx = \int \frac{1}{(b \tan (dx^{\frac{1}{3}} + c) + a)^2} dx$$

`[In] integrate(1/x/(a+b*tan(c+d*x^(1/3)))^2,x, algorithm="maxima")`

```
[Out] (((((4*a^10*b^2 + 16*a^8*b^4 + 24*a^6*b^6 + 17*a^4*b^8 + 6*a^2*b^10 + b^12)*
cos(2*c)^2 + (4*a^10*b^2 + 16*a^8*b^4 + 24*a^6*b^6 + 17*a^4*b^8 + 6*a^2*b^10
+ b^12)*sin(2*c)^2)*d*cos(2*d*x^(1/3))^2 + (a^12 + 2*a^10*b^2 + a^8*b^4)*
d*cos(2*d*x^(1/3) + 2*c)^2 + ((4*a^10*b^2 + 16*a^8*b^4 + 24*a^6*b^6 + 17*a^
4*b^8 + 6*a^2*b^10 + b^12)*cos(2*c)^2 + (4*a^10*b^2 + 16*a^8*b^4 + 24*a^6*b
^6 + 17*a^4*b^8 + 6*a^2*b^10 + b^12)*sin(2*c)^2)*d*sin(2*d*x^(1/3))^2 + (a^
12 + 2*a^10*b^2 + a^8*b^4)*d*sin(2*d*x^(1/3) + 2*c)^2 - 2*((a^8*b^4 + 4*a^6
*b^6 + 6*a^4*b^8 + 4*a^2*b^10 + b^12)*cos(2*c) - 2*(a^11*b + 5*a^9*b^3 + 10
*a^7*b^5 + 10*a^5*b^7 + 5*a^3*b^9 + a*b^11)*sin(2*c))*d*cos(2*d*x^(1/3)) +
2*(2*(a^11*b + 5*a^9*b^3 + 10*a^7*b^5 + 10*a^5*b^7 + 5*a^3*b^9 + a*b^11)*co
s(2*c) + (a^8*b^4 + 4*a^6*b^6 + 6*a^4*b^8 + 4*a^2*b^10 + b^12)*sin(2*c))*d*
sin(2*d*x^(1/3)) + (a^12 + 6*a^10*b^2 + 15*a^8*b^4 + 20*a^6*b^6 + 15*a^4*b^
8 + 6*a^2*b^10 + b^12)*d - 2*((a^8*b^4 + 2*a^6*b^6 + a^4*b^8)*cos(2*c) - 2
*(a^11*b + 3*a^9*b^3 + 3*a^7*b^5 + a^5*b^7)*sin(2*c))*d*cos(2*d*x^(1/3)) -
(2*(a^11*b + 3*a^9*b^3 + 3*a^7*b^5 + a^5*b^7)*cos(2*c) + (a^8*b^4 + 2*a^6*b
^6 + a^4*b^8)*sin(2*c))*d*sin(2*d*x^(1/3)) - (a^12 + 4*a^10*b^2 + 6*a^8*b^4
+ 4*a^6*b^6 + a^4*b^8)*d*cos(2*d*x^(1/3) + 2*c) - 2*((2*(a^11*b + 3*a^9*b
^3 + 3*a^7*b^5 + a^5*b^7)*cos(2*c) + (a^8*b^4 + 2*a^6*b^6 + a^4*b^8)*sin(2*
c))*d*cos(2*d*x^(1/3)) + ((a^8*b^4 + 2*a^6*b^6 + a^4*b^8)*cos(2*c) - 2*(a^1
1*b + 3*a^9*b^3 + 3*a^7*b^5 + a^5*b^7)*sin(2*c))*d*sin(2*d*x^(1/3)))*sin(2*
d*x^(1/3) + 2*c))*x*integrate(-2*(2*(a^5*b*d*sin(2*d*x^(1/3) + 2*c) - (a*b^
```

$$\begin{aligned}
& 5*\sin(2*c) + 2*(a^4*b^2 + a^2*b^4)*\cos(2*c))*d*\cos(2*d*x^(1/3)) - (a*b^5*\cos(2*c) - 2*(a^4*b^2 + a^2*b^4)*\sin(2*c))*d*\sin(2*d*x^(1/3))*x - (a^4*b^2*\sin(2*d*x^(1/3) + 2*c) - (b^6*\sin(2*c) + 2*(a^3*b^3 + a*b^5)*\cos(2*c))*\cos(2*d*x^(1/3)) - (b^6*\cos(2*c) - 2*(a^3*b^3 + a*b^5)*\sin(2*c))*\sin(2*d*x^(1/3)))*x^(2/3))/((a^8*d*\cos(2*d*x^(1/3) + 2*c)^2 + a^8*d*\sin(2*d*x^(1/3) + 2*c)^2 + ((4*a^6*b^2 + 8*a^4*b^4 + 4*a^2*b^6 + b^8)*\cos(2*c)^2 + (4*a^6*b^2 + 8*a^4*b^4 + 4*a^2*b^6 + b^8)*\sin(2*c)^2)*d*\cos(2*d*x^(1/3))^2 + ((4*a^6*b^2 + 8*a^4*b^4 + 4*a^2*b^6 + b^8)*\cos(2*c)^2 + (4*a^6*b^2 + 8*a^4*b^4 + 4*a^2*b^6 + b^8)*\sin(2*c)^2)*d*\sin(2*d*x^(1/3))^2 - 2*((a^4*b^4 + 2*a^2*b^6 + b^8)*\cos(2*c) - 2*(a^7*b + 3*a^5*b^3 + 3*a^3*b^5 + a*b^7)*\sin(2*c))*d*\cos(2*d*x^(1/3)) + 2*(2*(a^7*b + 3*a^5*b^3 + 3*a^3*b^5 + a*b^7)*\cos(2*c) + (a^4*b^4 + 2*a^2*b^6 + b^8)*\sin(2*c))*d*\sin(2*d*x^(1/3)) + (a^8 + 4*a^6*b^2 + 6*a^4*b^4 + 4*a^2*b^6 + b^8)*d - 2*((a^4*b^4*\cos(2*c) - 2*(a^7*b + a^5*b^3)*\sin(2*c))*d*\cos(2*d*x^(1/3)) - (a^4*b^4*\sin(2*c) + 2*(a^7*b + a^5*b^3)*\cos(2*c))*d*\sin(2*d*x^(1/3)) - (a^8 + 2*a^6*b^2 + a^4*b^4)*d)*\cos(2*d*x^(1/3) + 2*c) - 2*((a^4*b^4*\sin(2*c) + 2*(a^7*b + a^5*b^3)*\cos(2*c))*d*\cos(2*d*x^(1/3)) + (a^4*b^4*\cos(2*c) - 2*(a^7*b + a^5*b^3)*\sin(2*c))*d*\sin(2*d*x^(1/3)))*\sin(2*d*x^(1/3) + 2*c))*x^2, x) + (((4*a^8*b^2 + 4*a^6*b^4 - 4*a^4*b^6 - 3*a^2*b^8 - b^10)*\cos(2*c)^2 + (4*a^8*b^2 + 4*a^6*b^4 - 4*a^4*b^6 - 3*a^2*b^8 - b^10)*\sin(2*c)^2)*d*\cos(2*d*x^(1/3))^2 + (a^10 - a^8*b^2)*d*\cos(2*d*x^(1/3) + 2*c)^2 + ((4*a^8*b^2 + 4*a^6*b^4 - 4*a^4*b^6 - 3*a^2*b^8 - b^10)*\cos(2*c)^2 + (4*a^8*b^2 + 4*a^6*b^4 - 4*a^4*b^6 - 3*a^2*b^8 - b^10)*\sin(2*c)^2)*d*\sin(2*d*x^(1/3))^2 + (a^10 - a^8*b^2)*d*\sin(2*d*x^(1/3) + 2*c)^2 - 2*((a^6*b^4 + a^4*b^6 - a^2*b^8 - b^10)*\cos(2*c) - 2*(a^9*b + 2*a^7*b^3 - 2*a^3*b^7 - a*b^9)*\sin(2*c))*d*\cos(2*d*x^(1/3)) + 2*(2*(a^9*b + 2*a^7*b^3 - 2*a^3*b^7 - a*b^9)*\cos(2*c) + (a^6*b^4 + a^4*b^6 - a^2*b^8 - b^10)*\sin(2*c))*d*\sin(2*d*x^(1/3)) + (a^10 + 3*a^8*b^2 + 2*a^6*b^4 - 2*a^4*b^6 - 3*a^2*b^8 - b^10)*d - 2*((a^6*b^4 - a^4*b^6)*\cos(2*c) - 2*(a^9*b - a^5*b^5)*\sin(2*c))*d*\cos(2*d*x^(1/3)) - (2*(a^9*b - a^5*b^5)*\cos(2*c) + (a^6*b^4 - a^4*b^6)*\sin(2*c))*d*\sin(2*d*x^(1/3)) - (a^10 + a^8*b^2 - a^6*b^4 - a^4*b^6)*d)*\cos(2*d*x^(1/3) + 2*c) - 2*((2*(a^9*b - a^5*b^5)*\cos(2*c) + (a^6*b^4 - a^4*b^6)*\sin(2*c))*d*\cos(2*d*x^(1/3)) + ((a^6*b^4 - a^4*b^6)*\cos(2*c) - 2*(a^9*b - a^5*b^5)*\sin(2*c))*d*\sin(2*d*x^(1/3)))*\sin(2*d*x^(1/3) + 2*c))*x*log(x) - 6*((2*(a^7*b^3 + 3*a^5*b^5 + 3*a^3*b^7 + a*b^9)*\cos(2*c) + (a^4*b^6 + 2*a^2*b^8 + b^10)*\sin(2*c))*\cos(2*d*x^(1/3)) + ((a^4*b^6 + 2*a^2*b^8 + b^10)*\cos(2*c) - 2*(a^7*b^3 + 3*a^5*b^5 + 3*a^3*b^7 + a*b^9)*\sin(2*c))*\sin(2*d*x^(1/3)) - (a^8*b^2 + 2*a^6*b^4 + a^4*b^6)*\sin(2*d*x^(1/3) + 2*c))*x^(2/3))/((((4*a^10*b^2 + 16*a^8*b^4 + 24*a^6*b^6 + 17*a^4*b^8 + 6*a^2*b^10 + b^12)*\cos(2*c)^2 + (4*a^10*b^2 + 16*a^8*b^4 + 24*a^6*b^6 + 17*a^4*b^8 + 6*a^2*b^10 + b^12)*\sin(2*c)^2)*d*\cos(2*d*x^(1/3))^2 + (a^12 + 2*a^10*b^2 + a^8*b^4)*d*\cos(2*d*x^(1/3) + 2*c)^2 + ((4*a^10*b^2 + 16*a^8*b^4 + 24*a^6*b^6 + 17*a^4*b^8 + 6*a^2*b^10 + b^12)*\cos(2*c)^2 + (4*a^10*b^2 + 16*a^8*b^4 + 24*a^6*b^6 + 17*a^4*b^8 + 6*a^2*b^10 + b^12)*\sin(2*c)^2)*d*\sin(2*d*x^(1/3))^2 + (a^12 + 2*a^10*b^2 + a^8*b^4)*d*\sin(2*d*x^(1/3) + 2*c)^2 - 2*((a^8*b^4 + 4*a^6*b^6 + 6*a^4*b^8 + 4*a^2*b^10 + b^12)*\cos(2*c) - 2*(a^11*b + 5*a^9*b^3 + 10*a^7*b^5
\end{aligned}$$

+ 10*a^5*b^7 + 5*a^3*b^9 + a*b^11)*sin(2*c))*d*cos(2*d*x^(1/3)) + 2*(2*(a^11*b + 5*a^9*b^3 + 10*a^7*b^5 + 10*a^5*b^7 + 5*a^3*b^9 + a*b^11)*cos(2*c) + (a^8*b^4 + 4*a^6*b^6 + 6*a^4*b^8 + 4*a^2*b^10 + b^12)*sin(2*c))*d*sin(2*d*x^(1/3)) + (a^12 + 6*a^10*b^2 + 15*a^8*b^4 + 20*a^6*b^6 + 15*a^4*b^8 + 6*a^2*b^10 + b^12)*d - 2*((a^8*b^4 + 2*a^6*b^6 + a^4*b^8)*cos(2*c) - 2*(a^11*b + 3*a^9*b^3 + 3*a^7*b^5 + a^5*b^7)*sin(2*c))*d*cos(2*d*x^(1/3)) - (2*(a^11*b + 3*a^9*b^3 + 3*a^7*b^5 + a^5*b^7)*cos(2*c) + (a^8*b^4 + 2*a^6*b^6 + a^4*b^8)*sin(2*c))*d*sin(2*d*x^(1/3)) - (a^12 + 4*a^10*b^2 + 6*a^8*b^4 + 4*a^6*b^6 + a^4*b^8)*d*cos(2*d*x^(1/3) + 2*c) - 2*((2*(a^11*b + 3*a^9*b^3 + 3*a^7*b^5 + a^5*b^7)*cos(2*c) + (a^8*b^4 + 2*a^6*b^6 + a^4*b^8)*sin(2*c))*d*cos(2*d*x^(1/3)) + ((a^8*b^4 + 2*a^6*b^6 + a^4*b^8)*cos(2*c) - 2*(a^11*b + 3*a^9*b^3 + 3*a^7*b^5 + a^5*b^7)*sin(2*c))*d*sin(2*d*x^(1/3)))*sin(2*d*x^(1/3) + 2*c))*x)

Giac [N/A]

Not integrable

Time = 1.06 (sec) , antiderivative size = 20, normalized size of antiderivative = 1.00

$$\int \frac{1}{x (a + b \tan (c + d \sqrt[3]{x}))^2} dx = \int \frac{1}{(b \tan (dx^{\frac{1}{3}} + c) + a)^2 x} dx$$

[In] integrate(1/x/(a+b*tan(c+d*x^(1/3)))^2,x, algorithm="giac")

[Out] integrate(1/((b*tan(dx^(1/3) + c) + a)^2*x), x)

Mupad [N/A]

Not integrable

Time = 4.58 (sec) , antiderivative size = 20, normalized size of antiderivative = 1.00

$$\int \frac{1}{x (a + b \tan (c + d \sqrt[3]{x}))^2} dx = \int \frac{1}{x (a + b \tan (c + d x^{1/3}))^2} dx$$

[In] int(1/(x*(a + b*tan(c + d*x^(1/3)))^2),x)

[Out] int(1/(x*(a + b*tan(c + d*x^(1/3)))^2), x)

$$3.66 \quad \int \frac{1}{x^2 (a + b \tan(c + d \sqrt[3]{x}))^2} dx$$

Optimal result	456
Rubi [N/A]	456
Mathematica [N/A]	457
Maple [N/A] (verified)	457
Fricas [N/A]	457
Sympy [F(-1)]	458
Maxima [N/A]	458
Giac [N/A]	459
Mupad [N/A]	460

Optimal result

Integrand size = 20, antiderivative size = 20

$$\int \frac{1}{x^2 (a + b \tan(c + d \sqrt[3]{x}))^2} dx = \text{Int}\left(\frac{1}{x^2 (a + b \tan(c + d \sqrt[3]{x}))^2}, x\right)$$

[Out] Unintegrable(1/x^2/(a+b*tan(c+d*x^(1/3)))^2,x)

Rubi [N/A]

Not integrable

Time = 0.03 (sec) , antiderivative size = 20, normalized size of antiderivative = 1.00, number of steps used = 0, number of rules used = 0, $\frac{\text{number of rules}}{\text{integrand size}} = 0.000$, Rules used = {}

$$\int \frac{1}{x^2 (a + b \tan(c + d \sqrt[3]{x}))^2} dx = \int \frac{1}{x^2 (a + b \tan(c + d \sqrt[3]{x}))^2} dx$$

[In] Int[1/(x^2*(a + b*Tan[c + d*x^(1/3)])^2),x]

[Out] Defer[Int][1/(x^2*(a + b*Tan[c + d*x^(1/3)])^2), x]

Rubi steps

$$\text{integral} = \int \frac{1}{x^2 (a + b \tan(c + d \sqrt[3]{x}))^2} dx$$

Mathematica [N/A]

Not integrable

Time = 119.96 (sec) , antiderivative size = 22, normalized size of antiderivative = 1.10

$$\int \frac{1}{x^2 (a + b \tan (c + d \sqrt[3]{x}))^2} dx = \int \frac{1}{x^2 (a + b \tan (c + d \sqrt[3]{x}))^2} dx$$

[In] Integrate[1/(x^2*(a + b*Tan[c + d*x^(1/3)]))^2, x]

[Out] Integrate[1/(x^2*(a + b*Tan[c + d*x^(1/3)]))^2, x]

Maple [N/A] (verified)

Not integrable

Time = 0.67 (sec) , antiderivative size = 18, normalized size of antiderivative = 0.90

$$\int \frac{1}{x^2 \left(a + b \tan \left(c + d x^{\frac{1}{3}} \right) \right)^2} dx$$

[In] int(1/x^2/(a+b*tan(c+d*x^(1/3)))^2,x)

[Out] int(1/x^2/(a+b*tan(c+d*x^(1/3)))^2,x)

Fricas [N/A]

Not integrable

Time = 0.24 (sec) , antiderivative size = 44, normalized size of antiderivative = 2.20

$$\int \frac{1}{x^2 (a + b \tan (c + d \sqrt[3]{x}))^2} dx = \int \frac{1}{\left(b \tan \left(d x^{\frac{1}{3}} + c \right) + a \right)^2 x^2} dx$$

[In] integrate(1/x^2/(a+b*tan(c+d*x^(1/3)))^2,x, algorithm="fricas")

[Out] integral(1/(b^2*x^2*tan(d*x^(1/3) + c)^2 + 2*a*b*x^2*tan(d*x^(1/3) + c) + a^2*x^2), x)

Sympy [F(-1)]

Timed out.

$$\int \frac{1}{x^2 (a + b \tan(c + d\sqrt[3]{x}))^2} dx = \text{Timed out}$$

```
[In] integrate(1/x**2/(a+b*tan(c+d*x**(1/3)))**2,x)
```

```
[Out] Timed out
```

Maxima [N/A]

Not integrable

Time = 15.40 (sec) , antiderivative size = 2524, normalized size of antiderivative = 126.20

$$\int \frac{1}{x^2 (a + b \tan(c + d\sqrt[3]{x}))^2} dx = \int \frac{1}{(b \tan(dx^{\frac{1}{3}} + c) + a)^2 x^2} dx$$

```
[In] integrate(1/x^2/(a+b*tan(c+d*x^(1/3)))^2,x, algorithm="maxima")
```

```
[Out] ((a^8*d*cos(2*d*x^(1/3) + 2*c)^2 + a^8*d*sin(2*d*x^(1/3) + 2*c)^2 + ((4*a^6
*b^2 + 8*a^4*b^4 + 4*a^2*b^6 + b^8)*cos(2*c)^2 + (4*a^6*b^2 + 8*a^4*b^4 + 4
*a^2*b^6 + b^8)*sin(2*c)^2)*d*cos(2*d*x^(1/3))^2 + ((4*a^6*b^2 + 8*a^4*b^4
+ 4*a^2*b^6 + b^8)*cos(2*c)^2 + (4*a^6*b^2 + 8*a^4*b^4 + 4*a^2*b^6 + b^8)*s
in(2*c)^2)*d*sin(2*d*x^(1/3))^2 - 2*((a^4*b^4 + 2*a^2*b^6 + b^8)*cos(2*c) -
2*(a^7*b + 3*a^5*b^3 + 3*a^3*b^5 + a*b^7)*sin(2*c))*d*cos(2*d*x^(1/3)) + 2
*((a^7*b + 3*a^5*b^3 + 3*a^3*b^5 + a*b^7)*cos(2*c) + (a^4*b^4 + 2*a^2*b^6
+ b^8)*sin(2*c))*d*sin(2*d*x^(1/3)) + (a^8 + 4*a^6*b^2 + 6*a^4*b^4 + 4*a^2
*b^6 + b^8)*d - 2*((a^4*b^4*cos(2*c) - 2*(a^7*b + a^5*b^3)*sin(2*c))*d*cos(
2*d*x^(1/3)) - (a^4*b^4*sin(2*c) + 2*(a^7*b + a^5*b^3)*cos(2*c))*d*sin(2*d*
x^(1/3)) - (a^8 + 2*a^6*b^2 + a^4*b^4)*d*cos(2*d*x^(1/3) + 2*c) - 2*((a^4*
b^4*sin(2*c) + 2*(a^7*b + a^5*b^3)*cos(2*c))*d*cos(2*d*x^(1/3)) + (a^4*b^4*
cos(2*c) - 2*(a^7*b + a^5*b^3)*sin(2*c))*d*sin(2*d*x^(1/3)))*sin(2*d*x^(1/3
) + 2*c))*x^2*integrate(-4*((a^5*b*d*sin(2*d*x^(1/3) + 2*c) - (a*b^5*sin(2*
c) + 2*(a^4*b^2 + a^2*b^4)*cos(2*c))*d*cos(2*d*x^(1/3)) - (a*b^5*cos(2*c) -
2*(a^4*b^2 + a^2*b^4)*sin(2*c))*d*sin(2*d*x^(1/3)))*x - 2*(a^4*b^2*sin(2*d
*x^(1/3) + 2*c) - (b^6*sin(2*c) + 2*(a^3*b^3 + a*b^5)*cos(2*c))*cos(2*d*x^(
1/3)) - (b^6*cos(2*c) - 2*(a^3*b^3 + a*b^5)*sin(2*c))*sin(2*d*x^(1/3)))*x^(
2/3))/((a^8*d*cos(2*d*x^(1/3) + 2*c)^2 + a^8*d*sin(2*d*x^(1/3) + 2*c)^2 + (
4*a^6*b^2 + 8*a^4*b^4 + 4*a^2*b^6 + b^8)*cos(2*c)^2 + (4*a^6*b^2 + 8*a^4*b
^4 + 4*a^2*b^6 + b^8)*sin(2*c)^2)*d*cos(2*d*x^(1/3))^2 + ((4*a^6*b^2 + 8*a^
4*b^4 + 4*a^2*b^6 + b^8)*cos(2*c)^2 + (4*a^6*b^2 + 8*a^4*b^4 + 4*a^2*b^6 +
b^8)*sin(2*c)^2)*d*sin(2*d*x^(1/3))^2 - 2*((a^4*b^4 + 2*a^2*b^6 + b^8)*cos(
2*c) - 2*(a^7*b + 3*a^5*b^3 + 3*a^3*b^5 + a*b^7)*sin(2*c))*d*cos(2*d*x^(1/3
```

$$\begin{aligned}
&)) + 2*(2*(a^7*b + 3*a^5*b^3 + 3*a^3*b^5 + a*b^7)*\cos(2*c) + (a^4*b^4 + 2*a^2*b^6 + b^8)*\sin(2*c))*d*\sin(2*d*x^{(1/3)}) + (a^8 + 4*a^6*b^2 + 6*a^4*b^4 + 4*a^2*b^6 + b^8)*d - 2*((a^4*b^4*\cos(2*c) - 2*(a^7*b + a^5*b^3)*\sin(2*c))*d*\cos(2*d*x^{(1/3)}) - (a^4*b^4*\sin(2*c) + 2*(a^7*b + a^5*b^3)*\cos(2*c))*d*\sin(2*d*x^{(1/3)}) - (a^8 + 2*a^6*b^2 + a^4*b^4)*d)*\cos(2*d*x^{(1/3)} + 2*c) - 2*((a^4*b^4*\sin(2*c) + 2*(a^7*b + a^5*b^3)*\cos(2*c))*d*\cos(2*d*x^{(1/3)}) + (a^4*b^4*\cos(2*c) - 2*(a^7*b + a^5*b^3)*\sin(2*c))*d*\sin(2*d*x^{(1/3)}))*\sin(2*d*x^{(1/3)} + 2*c))*x^3, x) - ((a^6 + a^4*b^2)*d*\cos(2*d*x^{(1/3)} + 2*c)^2 + (a^6 + a^4*b^2)*d*\sin(2*d*x^{(1/3)} + 2*c)^2 - ((4*a^4*b^2 + 5*a^2*b^4 - b^6)*\cos(2*c) - 2*(a^5*b - 2*a*b^5)*\sin(2*c))*d*\cos(2*d*x^{(1/3)}) + (2*(a^5*b - 2*a*b^5)*\cos(2*c) + (4*a^4*b^2 + 5*a^2*b^4 - b^6)*\sin(2*c))*d*\sin(2*d*x^{(1/3)}) + (a^6 + a^4*b^2 - a^2*b^4 - b^6)*d - (((a^2*b^4 + b^6)*\cos(2*c) - 2*(a^5*b + 2*a^3*b^3 + a*b^5)*\sin(2*c))*d*\cos(2*d*x^{(1/3)}) - (2*(a^5*b + 2*a^3*b^3 + a*b^5)*\cos(2*c) + (a^2*b^4 + b^6)*\sin(2*c))*d*\sin(2*d*x^{(1/3)}) - (2*a^6 + 2*a^4*b^2 + 3*a^2*b^4 + b^6)*d)*\cos(2*d*x^{(1/3)} + 2*c) + (2*a^5*b*d - (2*(a^5*b + 2*a^3*b^3 + a*b^5)*\cos(2*c) + (a^2*b^4 + b^6)*\sin(2*c))*d*\cos(2*d*x^{(1/3)}) - ((a^2*b^4 + b^6)*\cos(2*c) - 2*(a^5*b + 2*a^3*b^3 + a*b^5)*\sin(2*c))*d*\sin(2*d*x^{(1/3)}))*\sin(2*d*x^{(1/3)} + 2*c))*x + 6*(a^4*b^2*\sin(2*d*x^{(1/3)} + 2*c) - (b^6*\sin(2*c) + 2*(a^3*b^3 + a*b^5)*\cos(2*c))*\cos(2*d*x^{(1/3)} + 2*c) - (b^6*\cos(2*c) - 2*(a^3*b^3 + a*b^5)*\sin(2*c))*\sin(2*d*x^{(1/3)} + 2*c))*x^2/3) / ((a^8*d*\cos(2*d*x^{(1/3)} + 2*c)^2 + a^8*d*\sin(2*d*x^{(1/3)} + 2*c)^2 + ((4*a^6*b^2 + 8*a^4*b^4 + 4*a^2*b^6 + b^8)*\cos(2*c)^2 + (4*a^6*b^2 + 8*a^4*b^4 + 4*a^2*b^6 + b^8)*\sin(2*c)^2)*d*\cos(2*d*x^{(1/3)})^2 + ((4*a^6*b^2 + 8*a^4*b^4 + 4*a^2*b^6 + b^8)*\cos(2*c)^2 + (4*a^6*b^2 + 8*a^4*b^4 + 4*a^2*b^6 + b^8)*\sin(2*c)^2)*d*\sin(2*d*x^{(1/3)})^2 - 2*((a^4*b^4 + 2*a^2*b^6 + b^8)*\cos(2*c) - 2*(a^7*b + 3*a^5*b^3 + 3*a^3*b^5 + a*b^7)*\sin(2*c))*d*\cos(2*d*x^{(1/3)}) + 2*(2*(a^7*b + 3*a^5*b^3 + 3*a^3*b^5 + a*b^7)*\cos(2*c) + (a^4*b^4 + 2*a^2*b^6 + b^8)*\sin(2*c))*d*\sin(2*d*x^{(1/3)}) + (a^8 + 4*a^6*b^2 + 6*a^4*b^4 + 4*a^2*b^6 + b^8)*d - 2*((a^4*b^4*\cos(2*c) - 2*(a^7*b + a^5*b^3)*\sin(2*c))*d*\cos(2*d*x^{(1/3)}) - (a^4*b^4*\sin(2*c) + 2*(a^7*b + a^5*b^3)*\cos(2*c))*d*\sin(2*d*x^{(1/3)}) - (a^8 + 2*a^6*b^2 + a^4*b^4)*d)*\cos(2*d*x^{(1/3)} + 2*c) - 2*((a^4*b^4*\sin(2*c) + 2*(a^7*b + a^5*b^3)*\cos(2*c))*d*\cos(2*d*x^{(1/3)}) + (a^4*b^4*\cos(2*c) - 2*(a^7*b + a^5*b^3)*\sin(2*c))*d*\sin(2*d*x^{(1/3)}))*\sin(2*d*x^{(1/3)} + 2*c))*x^2)
\end{aligned}$$

Giac [N/A]

Not integrable

Time = 1.13 (sec) , antiderivative size = 20, normalized size of antiderivative = 1.00

$$\int \frac{1}{x^2 (a + b \tan(c + d\sqrt[3]{x}))^2} dx = \int \frac{1}{(b \tan(dx^{\frac{1}{3}} + c) + a)^2 x^2} dx$$

[In] integrate(1/x^2/(a+b*tan(c+d*x^(1/3)))^2,x, algorithm="giac")

[Out] integrate(1/((b*tan(d*x^(1/3) + c) + a)^2*x^2), x)

Mupad [N/A]

Not integrable

Time = 4.29 (sec) , antiderivative size = 20, normalized size of antiderivative = 1.00

$$\int \frac{1}{x^2 (a + b \tan(c + d\sqrt[3]{x}))^2} dx = \int \frac{1}{x^2 (a + b \tan(c + dx^{1/3}))^2} dx$$

[In] int(1/(x^2*(a + b*tan(c + d*x^(1/3)))^2),x)

[Out] int(1/(x^2*(a + b*tan(c + d*x^(1/3)))^2), x)

CHAPTER 4

APPENDIX

4.1 Listing of Grading functions 461

4.1 Listing of Grading functions

The following are the current version of the grading functions used for grading the quality of the antiderivative with reference to the optimal antiderivative included in the test suite.

There is a version for Maple and for Mathematica/Rubi. There is a version for grading Sympy and version for use with Sagemath.

The following are links to the current source code.

The following are the listings of source code of the grading functions.

Mathematica and Rubi grading function

```
(* Original version thanks to Albert Rich emailed on 03/21/2017 *)
(* ::Package:: *)

(* Nasser: April 7,2022. add second output which gives reason for the grade *)
(*      Small rewrite of logic in main function to make it*)
(*      match Maple's logic. No change in functionality otherwise*)

(* ::Subsection:: *)
(*GradeAntiderivative[result,optimal]*)

(* ::Text:: *)
(*If result and optimal are mathematical expressions, *)
```

```

(*      GradeAntiderivative[result,optimal] returns*)
(* "F" if the result fails to integrate an expression that*)
(*   is integrable*)
(* "C" if result involves higher level functions than necessary*)
(* "B" if result is more than twice the size of the optimal*)
(*   antiderivative*)
(* "A" if result can be considered optimal*)

GradeAntiderivative[result_,optimal_] := Module[{expnResult,expnOptimal,leafCountResult,leafCo
  expnResult = ExpnType[result];
  expnOptimal = ExpnType[optimal];
  leafCountResult = LeafCount[result];
  leafCountOptimal = LeafCount[optimal];

  (*Print["expnResult=",expnResult," expnOptimal=",expnOptimal];*)
  If[expnResult<=expnOptimal,
    If[Not[FreeQ[result,Complex]], (*result contains complex*)
      If[Not[FreeQ[optimal,Complex]], (*optimal contains complex*)
        If[leafCountResult<=2*leafCountOptimal,
          finalresult={"A",""}
          , (*ELSE*)
          finalresult={"B","Both result and optimal contain complex but leaf count is
        ]
      , (*ELSE*)
      finalresult={"C","Result contains complex when optimal does not."}
    ]
    , (*ELSE*) (*result does not contains complex*)
    If[leafCountResult<=2*leafCountOptimal,
      finalresult={"A",""}
      , (*ELSE*)
      finalresult={"B","Leaf count is larger than twice the leaf count of optimal. $"
    ]
  ]
  , (*ELSE*) (*expnResult>expnOptimal*)
  If[FreeQ[result,Integrate] && FreeQ[result,Int],
    finalresult={"C","Result contains higher order function than in optimal. Order "<>
    ,
    finalresult={"F","Contains unresolved integral."}
  ]
];

  finalresult
]

(* ::Text:: *)
(*The following summarizes the type number assigned an *)

```

```

(*expression based on the functions it involves*)
(*1 = rational function*)
(*2 = algebraic function*)
(*3 = elementary function*)
(*4 = special function*)
(*5 = hyperpergeometric function*)
(*6 = appell function*)
(*7 = rootsum function*)
(*8 = integrate function*)
(*9 = unknown function*)

```

```

ExpnType[expn_] :=
  If[AtomQ[expn],
    1,
    If[ListQ[expn],
      Max[Map[ExpnType, expn]],
      If[Head[expn]===Power,
        If[IntegerQ[expn[[2]]],
          ExpnType[expn[[1]]],
          If[Head[expn[[2]]]===Rational,
            If[IntegerQ[expn[[1]]] || Head[expn[[1]]]===Rational,
              1,
              Max[ExpnType[expn[[1]], 2]],
            Max[ExpnType[expn[[1]], ExpnType[expn[[2]], 3]]],
          If[Head[expn]===Plus || Head[expn]===Times,
            Max[ExpnType[First[expn]], ExpnType[Rest[expn]]],
            If[ElementaryFunctionQ[Head[expn]],
              Max[3, ExpnType[expn[[1]]],
            If[SpecialFunctionQ[Head[expn]],
              Apply[Max, Append[Map[ExpnType, Apply[List, expn]], 4]],
            If[HypergeometricFunctionQ[Head[expn]],
              Apply[Max, Append[Map[ExpnType, Apply[List, expn]], 5]],
            If[AppellFunctionQ[Head[expn]],
              Apply[Max, Append[Map[ExpnType, Apply[List, expn]], 6]],
            If[Head[expn]===RootSum,
              Apply[Max, Append[Map[ExpnType, Apply[List, expn]], 7]],
            If[Head[expn]===Integrate || Head[expn]===Int,
              Apply[Max, Append[Map[ExpnType, Apply[List, expn]], 8]],
            9]]]]]]]]]]

```

```

ElementaryFunctionQ[func_] :=
  MemberQ[{
    Exp, Log,
    Sin, Cos, Tan, Cot, Sec, Csc,
    ArcSin, ArcCos, ArcTan, ArcCot, ArcSec, ArcCsc,

```

```

    Sinh, Cosh, Tanh, Coth, Sech, Csch,
    ArcSinh, ArcCosh, ArcTanh, ArcCoth, ArcSech, ArcCsch
  }, func]

SpecialFunctionQ[func_] :=
  MemberQ[{
    Erf, Erfc, Erfi,
    FresnelS, FresnelC,
    ExpIntegralE, ExpIntegralEi, LogIntegral,
    SinIntegral, CosIntegral, SinhIntegral, CoshIntegral,
    Gamma, LogGamma, PolyGamma,
    Zeta, PolyLog, ProductLog,
    EllipticF, EllipticE, EllipticPi
  }, func]

HypergeometricFunctionQ[func_] :=
  MemberQ[{Hypergeometric1F1, Hypergeometric2F1, HypergeometricPFQ}, func]

AppellFunctionQ[func_] :=
  MemberQ[{AppellF1}, func]

```

Maple grading function

```

# File: GradeAntiderivative.mpl
# Original version thanks to Albert Rich emailed on 03/21/2017

#Nasser 03/22/2017 Use Maple leaf count instead since buildin
#Nasser 03/23/2017 missing 'ln' for ElementaryFunctionQ added
#Nasser 03/24/2017 corrected the check for complex result
#Nasser 10/27/2017 check for leafsize and do not call ExpnType()
#
# if leaf size is "too large". Set at 500,000
#Nasser 12/22/2019 Added debug flag, added 'dilog' to special functions
#
# see problem 156, file Apostol_Problems
#Nasser 4/07/2022 add second output which gives reason for the grade

GradeAntiderivative := proc(result, optimal)
local leaf_count_result,
      leaf_count_optimal,
      ExpnType_result,
      ExpnType_optimal,
      debug:=false;

      leaf_count_result:=leafcount(result);

```



```

#do NOT call ExpnType() if leaf size is too large. Recursion problem
if leaf_count_result > 500000 then
    return "B","result has leaf size over 500,000. Avoiding possible recursion issues
fi;

leaf_count_optimal := leafcount(optimal);
ExpnType_result := ExpnType(result);
ExpnType_optimal := ExpnType(optimal);

if debug then
    print("ExpnType_result",ExpnType_result," ExpnType_optimal=",ExpnType_optimal);
fi;

# If result and optimal are mathematical expressions,
# GradeAntiderivative[result,optimal] returns
# "F" if the result fails to integrate an expression that
# is integrable
# "C" if result involves higher level functions than necessary
# "B" if result is more than twice the size of the optimal
# antiderivative
# "A" if result can be considered optimal

#This check below actually is not needed, since I only
#call this grading only for passed integrals. i.e. I check
#for "F" before calling this. But no harm of keeping it here.
#just in case.

if not type(result,freeof('int')) then
    return "F","Result contains unresolved integral";
fi;

if ExpnType_result<=ExpnType_optimal then
    if debug then
        print("ExpnType_result<=ExpnType_optimal");
    fi;
    if is_contains_complex(result) then
        if is_contains_complex(optimal) then
            if debug then
                print("both result and optimal complex");
            fi;
            if leaf_count_result<=2*leaf_count_optimal then
                return "A"," ";
            else
                return "B",cat("Both result and optimal contain complex but leaf count of
                                convert(leaf_count_result,string)," vs. $2 ("
```

```

                                convert(leaf_count_optimal,string)," ) = ",convert(2*leaf_c
    end if
  else #result contains complex but optimal is not
    if debug then
      print("result contains complex but optimal is not");
    fi;
    return "C","Result contains complex when optimal does not.";
  fi;
else # result do not contain complex
  # this assumes optimal do not as well. No check is needed here.
  if debug then
    print("result do not contain complex, this assumes optimal do not as well");
  fi;
  if leaf_count_result<=2*leaf_count_optimal then
    if debug then
      print("leaf_count_result<=2*leaf_count_optimal");
    fi;
    return "A"," ";
  else
    if debug then
      print("leaf_count_result>2*leaf_count_optimal");
    fi;
    return "B",cat("Leaf count of result is larger than twice the leaf count of opt
                                convert(leaf_count_result,string)," $ vs. $2(",
                                convert(leaf_count_optimal,string)," )=",convert(2*leaf_count
    fi;
  fi;
else #ExpnType(result) > ExpnType(optimal)
  if debug then
    print("ExpnType(result) > ExpnType(optimal)");
  fi;
  return "C",cat("Result contains higher order function than in optimal. Order ",
                convert(ExpnType_result,string)," vs. order ",
                convert(ExpnType_optimal,string),".");
fi;

end proc:

#
# is_contains_complex(result)
# takes expressions and returns true if it contains "I" else false
#
#Nasser 032417
is_contains_complex:= proc(expression)
  return (has(expression,I));
end proc:

```

```

# The following summarizes the type number assigned an expression
# based on the functions it involves
# 1 = rational function
# 2 = algebraic function
# 3 = elementary function
# 4 = special function
# 5 = hyperpergeometric function
# 6 = appell function
# 7 = rootsum function
# 8 = integrate function
# 9 = unknown function

ExpnType := proc(expn)
  if type(expn,'atomic') then
    1
  elif type(expn,'list') then
    apply(max,map(ExpnType,expn))
  elif type(expn,'sqrt') then
    if type(op(1,expn),'rational') then
      1
    else
      max(2,ExpnType(op(1,expn)))
    end if
  elif type(expn,'^^') then
    if type(op(2,expn),'integer') then
      ExpnType(op(1,expn))
    elif type(op(2,expn),'rational') then
      if type(op(1,expn),'rational') then
        1
      else
        max(2,ExpnType(op(1,expn)))
      end if
    else
      max(3,ExpnType(op(1,expn)),ExpnType(op(2,expn)))
    end if
  elif type(expn,'+`) or type(expn,'*`) then
    max(ExpnType(op(1,expn)),max(ExpnType(rest(expn))))
  elif ElementaryFunctionQ(op(0,expn)) then
    max(3,ExpnType(op(1,expn)))
  elif SpecialFunctionQ(op(0,expn)) then
    max(4,apply(max,map(ExpnType,[op(expn)])))
  elif HypergeometricFunctionQ(op(0,expn)) then
    max(5,apply(max,map(ExpnType,[op(expn)])))
  elif AppellFunctionQ(op(0,expn)) then
    max(6,apply(max,map(ExpnType,[op(expn)])))
  elif op(0,expn)='int' then
    max(8,apply(max,map(ExpnType,[op(expn)]))) else

```

```

9
end if
end proc:

ElementaryFunctionQ := proc(func)
  member(func, [
    exp, log, ln,
    sin, cos, tan, cot, sec, csc,
    arcsin, arccos, arctan, arccot, arcsec, arccsc,
    sinh, cosh, tanh, coth, sech, csch,
    arcsinh, arccosh, arctanh, arccoth, arcsech, arccsch])
end proc:

SpecialFunctionQ := proc(func)
  member(func, [
    erf, erfc, erfi,
    FresnelS, FresnelC,
    Ei, Ei, Li, Si, Ci, Shi, Chi,
    GAMMA, lnGAMMA, Psi, Zeta, polylog, dilog, LambertW,
    EllipticF, EllipticE, EllipticPi])
end proc:

HypergeometricFunctionQ := proc(func)
  member(func, [Hypergeometric1F1, hypergeom, HypergeometricPFQ])
end proc:

AppellFunctionQ := proc(func)
  member(func, [AppellF1])
end proc:

# u is a sum or product. rest(u) returns all but the
# first term or factor of u.
rest := proc(u) local v;
  if nops(u)=2 then
    op(2,u)
  else
    apply(op(0,u), op(2..nops(u), u))
  end if
end proc:

#leafcount(u) returns the number of nodes in u.
#Nasser 3/23/17 Replaced by build-in leafCount from package in Maple
leafcount := proc(u)
  MmaTranslator[Mma][LeafCount](u);
end proc:

```

Sympy grading function

```

#Dec 24, 2019. Nasser M. Abbasi:
#      Port of original Maple grading function by
#      Albert Rich to use with Sympy/Python
#Dec 27, 2019 Nasser. Added `RootSum`. See problem 177, Timofeev file
#      added 'exp_polar'
from sympy import *

def leaf_count(expr):
    #sympy do not have leaf count function. This is approximation
    return round(1.7*count_ops(expr))

def is_sqrt(expr):
    if isinstance(expr,Pow):
        if expr.args[1] == Rational(1,2):
            return True
        else:
            return False
    else:
        return False

def is_elementary_function(func):
    return func in [exp,log,ln,sin,cos,tan,cot,sec,csc,
        asin,acos,atan,acot,asec,acsc,sinh,cosh,tanh,coth,sech,csch,
        asinh,acosh,atanh,acoth,asech,acsch
    ]

def is_special_function(func):
    return func in [ erf,erfc,erfi,
        fresnels,fresnelc,Ei,Ei,Li,Si,Ci,Shi,Chi,
        gamma,loggamma,digamma,zeta,polylog,LambertW,
        elliptic_f,elliptic_e,elliptic_pi,exp_polar
    ]

def is_hypergeometric_function(func):
    return func in [hyper]

def is_appell_function(func):
    return func in [appellf1]

def is_atom(expn):
    try:
        if expn.isAtom or isinstance(expn,int) or isinstance(expn,float):
            return True
        else:
            return False

```

```

except AttributeError as error:
    return False

def expnType(expn):
    debug=False
    if debug:
        print("expn=",expn,"type(expn)=",type(expn))

    if is_atom(expn):
        return 1
    elif isinstance(expn,list):
        return max(map(expnType, expn)) #apply(max,map(ExpnType,expn))
    elif is_sqrt(expn):
        if isinstance(expn.args[0],Rational): #type(op(1,expn),'rational')
            return 1
        else:
            return max(2,expnType(expn.args[0])) #max(2,ExpnType(op(1,expn)))
    elif isinstance(expn,Pow): #type(expn,'^')
        if isinstance(expn.args[1],Integer): #type(op(2,expn),'integer')
            return expnType(expn.args[0]) #ExpnType(op(1,expn))
        elif isinstance(expn.args[1],Rational): #type(op(2,expn),'rational')
            if isinstance(expn.args[0],Rational): #type(op(1,expn),'rational')
                return 1
            else:
                return max(2,expnType(expn.args[0])) #max(2,ExpnType(op(1,expn)))
        else:
            return max(3,expnType(expn.args[0]),expnType(expn.args[1])) #max(3,ExpnType(op(1,expn)),ExpnTy
    elif isinstance(expn,Add) or isinstance(expn,Mul): #type(expn,'+') or type(expn,'*')
        m1 = expnType(expn.args[0])
        m2 = expnType(list(expn.args[1:]))
        return max(m1,m2) #max(ExpnType(op(1,expn)),max(ExpnType(rest(expn))))
    elif is_elementary_function(expn.func): #ElementaryFunctionQ(op(0,expn))
        return max(3,expnType(expn.args[0])) #max(3,ExpnType(op(1,expn)))
    elif is_special_function(expn.func): #SpecialFunctionQ(op(0,expn))
        m1 = max(map(expnType, list(expn.args)))
        return max(4,m1) #max(4,apply(max,map(ExpnType,[op(expn)])))
    elif is_hypergeometric_function(expn.func): #HypergeometricFunctionQ(op(0,expn))
        m1 = max(map(expnType, list(expn.args)))
        return max(5,m1) #max(5,apply(max,map(ExpnType,[op(expn)])))
    elif is_appell_function(expn.func):
        m1 = max(map(expnType, list(expn.args)))
        return max(6,m1) #max(5,apply(max,map(ExpnType,[op(expn)])))
    elif isinstance(expn,RootSum):
        m1 = max(map(expnType, list(expn.args))) #Apply[Max,Append[Map[ExpnType,Apply[List,expn]],7]],
        return max(7,m1)
    elif str(expn).find("Integral") != -1:

```

```

    m1 = max(map(expnType, list(expn.args)))
    return max(8,m1)  #max(5,apply(max,map(ExpnType,[op(expn)])))
else:
    return 9

#main function
def grade_antiderivative(result,optimal):

    #print ("Enter grade_antiderivative for sagemath")
    #print("Enter grade_antiderivative, result=",result," optimal=",optimal)

    leaf_count_result = leaf_count(result)
    leaf_count_optimal = leaf_count(optimal)

    #print("leaf_count_result=",leaf_count_result)
    #print("leaf_count_optimal=",leaf_count_optimal)

    expnType_result = expnType(result)
    expnType_optimal = expnType(optimal)

    if str(result).find("Integral") != -1:
        grade = "F"
        grade_annotation = ""
    else:
        if expnType_result <= expnType_optimal:
            if result.has(I):
                if optimal.has(I): #both result and optimal complex
                    if leaf_count_result <= 2*leaf_count_optimal:
                        grade = "A"
                        grade_annotation = ""
                    else:
                        grade = "B"
                        grade_annotation = "Both result and optimal contain complex but leaf count of result is large"
                else: #result contains complex but optimal is not
                    grade = "C"
                    grade_annotation = "Result contains complex when optimal does not."
            else: # result do not contain complex, this assumes optimal do not as well
                if leaf_count_result <= 2*leaf_count_optimal:
                    grade = "A"
                    grade_annotation = ""
                else:
                    grade = "B"
                    grade_annotation = "Leaf count of result is larger than twice the leaf count of optimal. "+str(leaf_count_result)
            else:
                grade = "C"
                grade_annotation = "Result contains higher order function than in optimal. Order "+str(ExpnType_result)

```

```

#print("Before returning. grade=",grade, " grade_annotation=",grade_annotation)

return grade, grade_annotation

```

SageMath grading function

```

#Dec 24, 2019. Nasser: Ported original Maple grading function by
#    Albert Rich to use with Sagemath. This is used to
#    grade Fricas, Giac and Maxima results.
#Dec 24, 2019. Nasser: Added 'exp_integral_e' and 'sng', 'sin_integral'
#    'arctan2', 'floor', 'abs', 'log_integral'
#June 4, 2022 Made default grade_annotation "none" instead of "" due
#    issue later when reading the file.
#July 14, 2022. Added ellipticF. This is until they fix sagemath, then remove it.

from sage.all import *
from sage.symbolic.operators import add_vararg, mul_vararg

debug=False;

def tree_size(expr):
    r"""
    Return the tree size of this expression.
    """
    #print("Enter tree_size, expr is ",expr)

    if expr not in SR:
        # deal with lists, tuples, vectors
        return 1 + sum(tree_size(a) for a in expr)
    expr = SR(expr)
    x, aa = expr.operator(), expr.operands()
    if x is None:
        return 1
    else:
        return 1 + sum(tree_size(a) for a in aa)

def is_sqrt(expr):
    if expr.operator() == operator.pow: #isinstance(expr, Pow):
        if expr.operands()[1]==1/2: #expr.args[1] == Rational(1,2):
            if debug: print ("expr is sqrt")
            return True
        else:
            return False
    else:
        return False

```



```

def is_elementary_function(func):
    #debug=False
    m = func.name() in ['exp','log','ln',
        'sin','cos','tan','cot','sec','csc',
        'arcsin','arccos','arctan','arccot','arcsec','arccsc',
        'sinh','cosh','tanh','coth','sech','csch',
        'arcsinh','arccosh','arctanh','arccoth','arcsech','arccsch','sgn',
        'arctan2','floor','abs'
    ]
    if debug:
        if m:
            print ("func ", func , " is elementary_function")
        else:
            print ("func ", func , " is NOT elementary_function")

    return m

def is_special_function(func):
    #debug=False
    if debug:
        print ("type(func)=", type(func))

    m= func.name() in ['erf','erfc','erfi','fresnel_sin','fresnel_cos','Ei',
        'Ei','Li','Si','sin_integral','Ci','cos_integral','Shi','sinh_integral',
        'Chi','cosh_integral','gamma','log_gamma','psi,zeta',
        'polylog','lambert_w','elliptic_f','elliptic_e','ellipticF',
        'elliptic_pi','exp_integral_e','log_integral']

    if debug:
        print ("m=",m)
        if m:
            print ("func ", func , " is special_function")
        else:
            print ("func ", func , " is NOT special_function")

    return m

def is_hypergeometric_function(func):
    return func.name() in ['hypergeometric','hypergeometric_M','hypergeometric_U']

def is_appell_function(func):
    return func.name() in ['hypergeometric']    #[appellf1] can't find this in sagemath

```

```

def is_atom(expn):

    #debug=False
    if debug:
        print ("Enter is_atom, expn=",expn)

    if not hasattr(expn, 'parent'):
        return False

    #thanks to answer at https://ask.sagemath.org/question/49179/what-is-sagemath-equivalent-to-atomic-type
    try:
        if expn.parent() is SR:
            return expn.operator() is None
        if expn.parent() in (ZZ, QQ, AA, QQbar):
            return expn in expn.parent() # Should always return True
        if hasattr(expn.parent(), "base_ring") and hasattr(expn.parent(), "gens"):
            return expn in expn.parent().base_ring() or expn in expn.parent().gens()

        return False

    except AttributeError as error:
        print("Exception,AttributeError in is_atom")
        print ("caught exception" , type(error).__name__ )
        return False

def expnType(expn):

    if debug:
        print (">>>>>Enter expnType, expn=", expn)
        print (">>>>>is_atom(expn)=", is_atom(expn))

    if is_atom(expn):
        return 1
    elif type(expn)==list: #isinstance(expn,list):
        return max(map(expnType, expn)) #apply(max,map(ExpnType,expn))
    elif is_sqrt(expn):
        if type(expn.operands()[0])==Rational: #type(isinstance(expn.args[0],Rational):
            return 1
        else:
            return max(2,expnType(expn.operands()[0])) #max(2,expnType(expn.args[0]))
    elif expn.operator() == operator.pow: #isinstance(expn,Pow)
        if type(expn.operands()[1])==Integer: #isinstance(expn.args[1],Integer)
            return expnType(expn.operands()[0]) #expnType(expn.args[0])
        elif type(expn.operands()[1])==Rational: #isinstance(expn.args[1],Rational)
            if type(expn.operands()[0])==Rational: #isinstance(expn.args[0],Rational)

```

```

        return 1
    else:
        return max(2,expnType(expn.operands()[0])) #max(2,expnType(expn.args[0]))
    else:
        return max(3,expnType(expn.operands()[0]),expnType(expn.operands()[1])) #max(3,expnType(expn.
elif expn.operator() == add_vararg or expn.operator() == mul_vararg: #isinstance(expn,Add) or isinst
    m1 = expnType(expn.operands()[0]) #expnType(expn.args[0])
    m2 = expnType(expn.operands()[1:]) #expnType(list(expn.args[1:]))
    return max(m1,m2) #max(ExpnType(op(1,expn)),max(ExpnType(rest(expn))))
elif is_elementary_function(expn.operator()): #is_elementary_function(expn.func)
    return max(3,expnType(expn.operands()[0]))
elif is_special_function(expn.operator()): #is_special_function(expn.func)
    m1 = max(map(expnType, expn.operands())) #max(map(expnType, list(expn.args)))
    return max(4,m1) #max(4,m1)
elif is_hypergeometric_function(expn.operator()): #is_hypergeometric_function(expn.func)
    m1 = max(map(expnType, expn.operands())) #max(map(expnType, list(expn.args)))
    return max(5,m1) #max(5,m1)
elif is_appell_function(expn.operator()):
    m1 = max(map(expnType, expn.operands())) #max(map(expnType, list(expn.args)))
    return max(6,m1) #max(6,m1)
elif str(expn).find("Integral") != -1: #this will never happen, since it
    #is checked before calling the grading function that is passed.
    #but kept it here.
    m1 = max(map(expnType, expn.operands())) #max(map(expnType, list(expn.args)))
    return max(8,m1) #max(5,apply(max,map(ExpnType,[op(expn)])))
else:
    return 9

#main function
def grade_antiderivative(result,optimal):

    if debug:
        print ("Enter grade_antiderivative for sagemath")
        print("Enter grade_antiderivative, result=",result)
        print("Enter grade_antiderivative, optimal=",optimal)
        print("type(anti)=",type(result))
        print("type(optimal)=",type(optimal))

    leaf_count_result = tree_size(result) #leaf_count(result)
    leaf_count_optimal = tree_size(optimal) #leaf_count(optimal)

    #if debug: print ("leaf_count_result=", leaf_count_result, "leaf_count_optimal=",leaf_count_optimal)

    expnType_result = expnType(result)
    expnType_optimal = expnType(optimal)

```

```

if debug: print ("expnType_result=", expnType_result, "expnType_optimal=",expnType_optimal)

if expnType_result <= expnType_optimal:
    if result.has(I):
        if optimal.has(I): #both result and optimal complex
            if leaf_count_result <= 2*leaf_count_optimal:
                grade = "A"
                grade_annotation = "none"
            else:
                grade = "B"
                grade_annotation = "Both result and optimal contain complex but leaf count of result is larger than"
        else: #result contains complex but optimal is not
            grade = "C"
            grade_annotation = "Result contains complex when optimal does not."
    else: # result do not contain complex, this assumes optimal do not as well
        if leaf_count_result <= 2*leaf_count_optimal:
            grade = "A"
            grade_annotation = "none"
        else:
            grade = "B"
            grade_annotation = "Leaf count of result is larger than twice the leaf count of optimal. " + str(leaf_c

else:
    grade = "C"
    grade_annotation = "Result contains higher order function than in optimal. Order " + str(expnType_result

print("Before returning. grade=",grade, " grade_annotation=",grade_annotation)

return grade, grade_annotation

```